

## Supplementary material

**Figure S1** Structure of (a) methylene blue and (b) kaolinite DD3.

**Figure S2** Adsorption tests for the removal of MB on acid activated prepared materials, ( $C_0$  (MB) = 250 mg/L,  $m/V$  = 1 g/L, contact time 24 h,  $T = 25 \pm 3$  °C, and unadjusted pH).

**Figure S3** Point of zero charge (pH<sub>pzc</sub>) of DD3 and Treated-DD3.

**Figure S4** Plots showing the variation in the amount of MB adsorbed on DD3 and Treated-DD3 in the time range 0–60 min for the PSO model ( $m/V$  = 1 g/L,  $T = 25 \pm 3$  °C, and unadjusted pH), as a nonlinear expression.

**Figure S5** Multicollinearity test

**Figure S6** Residuals relating to the model established by the different techniques according to the estimated values: (a) Relationship between experimental data and the predicted data of samples, (b) Residue of errors, and (c) Instances distribution of errors, and (d) Frequency distribution of errors.

**Figure S7** MATLAB Interface: prediction of the adsorption quantity with GPR-PSO model.

**Table S1.** Maximum adsorption capacity (Q<sub>max</sub> (mg/g) of MB by various adsorbents in other reports.

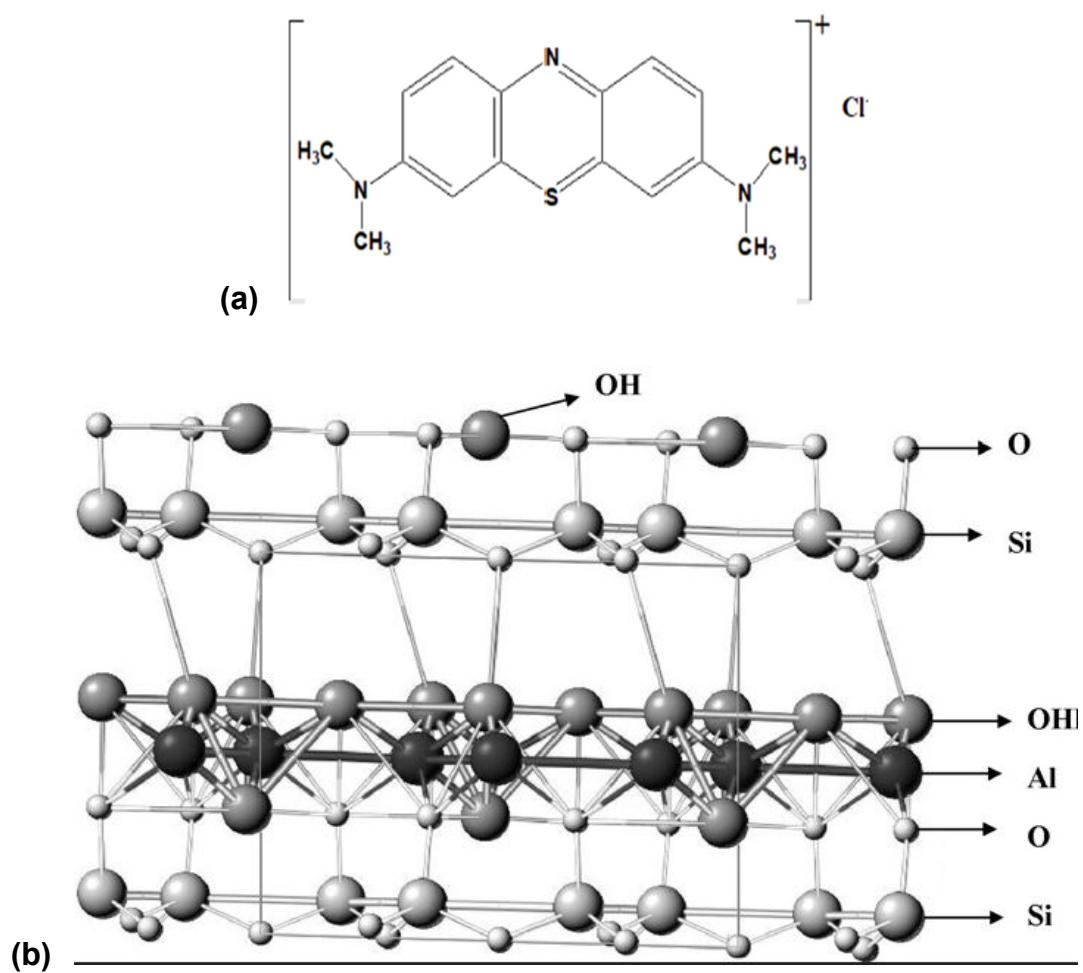
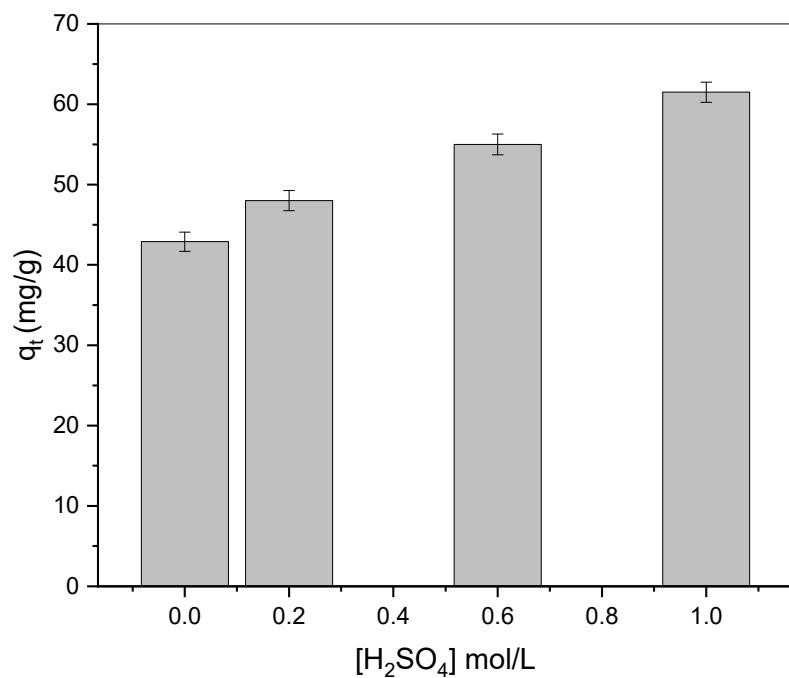
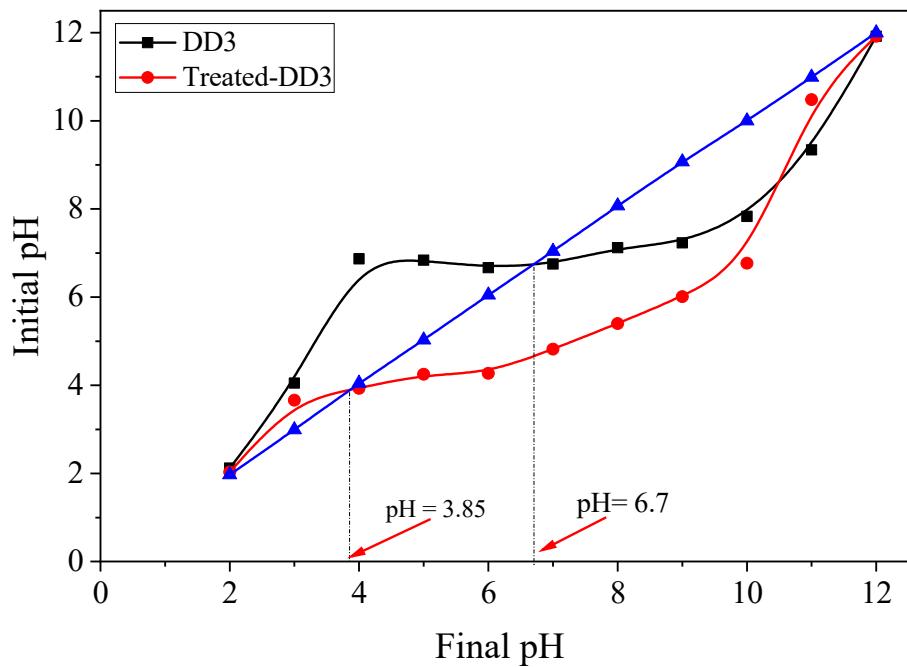


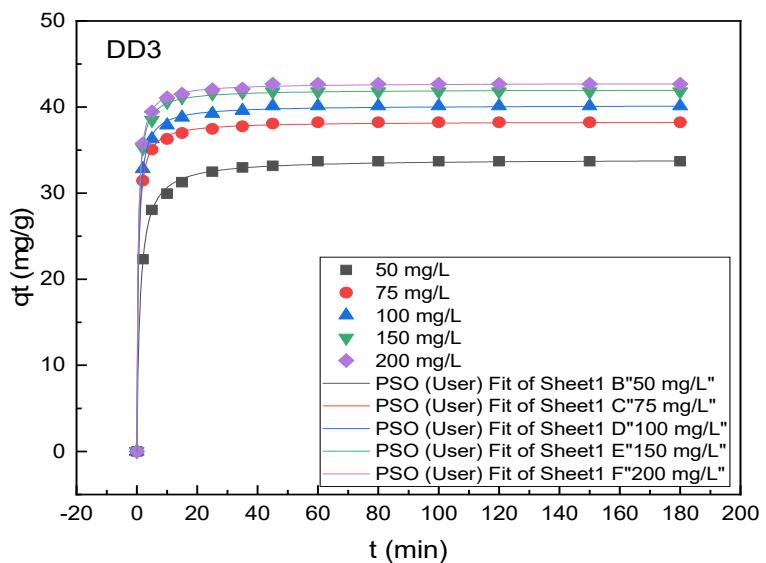
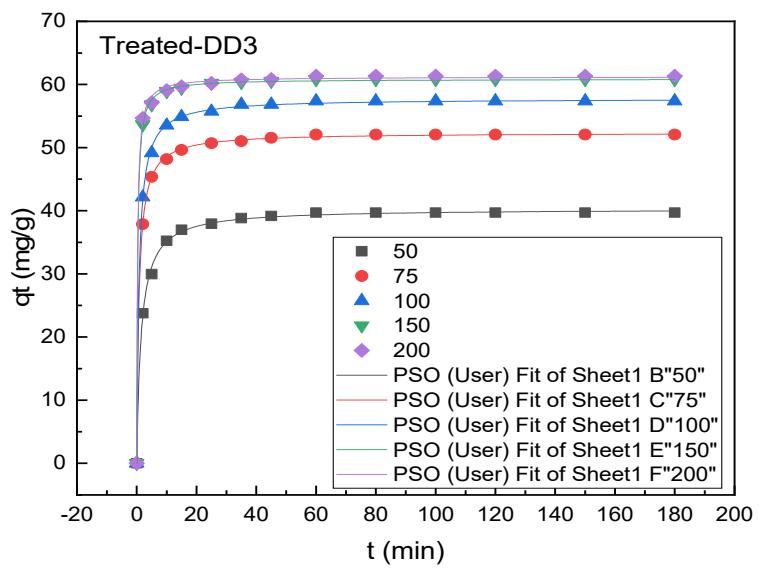
Figure S1



**Figure S2**



**Figure S3**



**Figure S4**

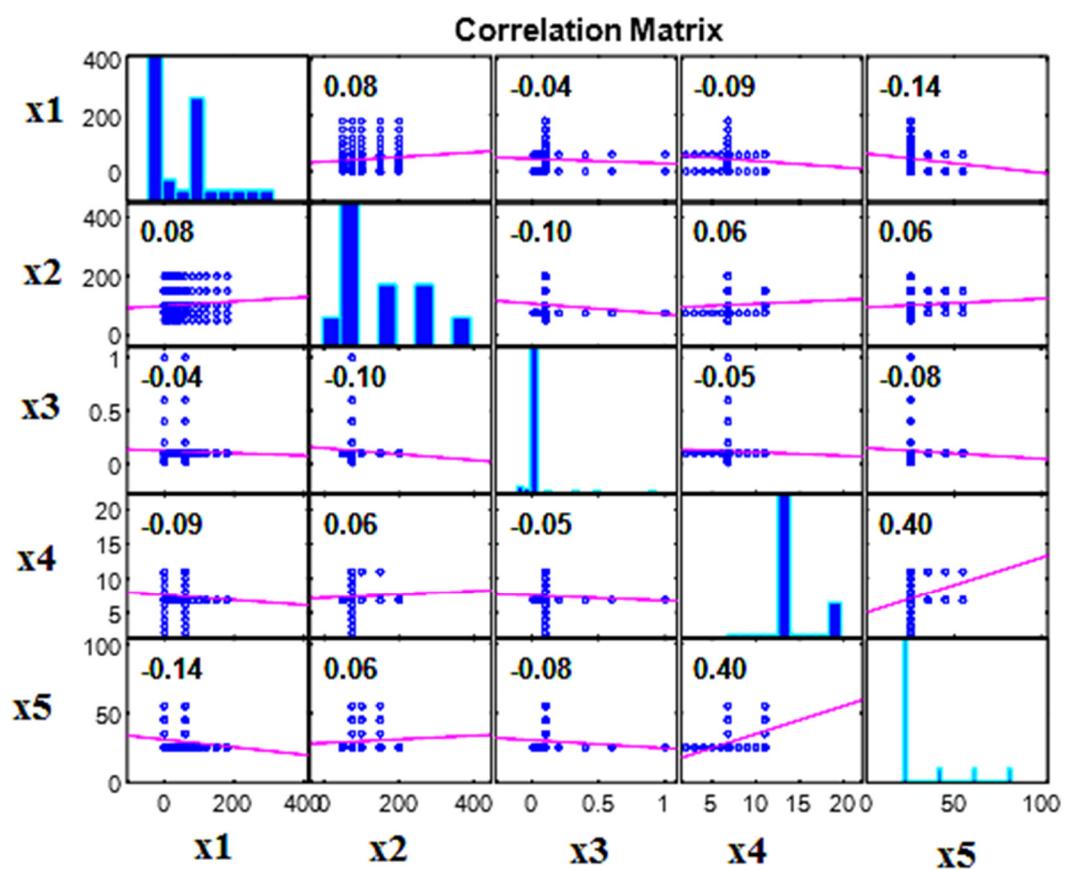
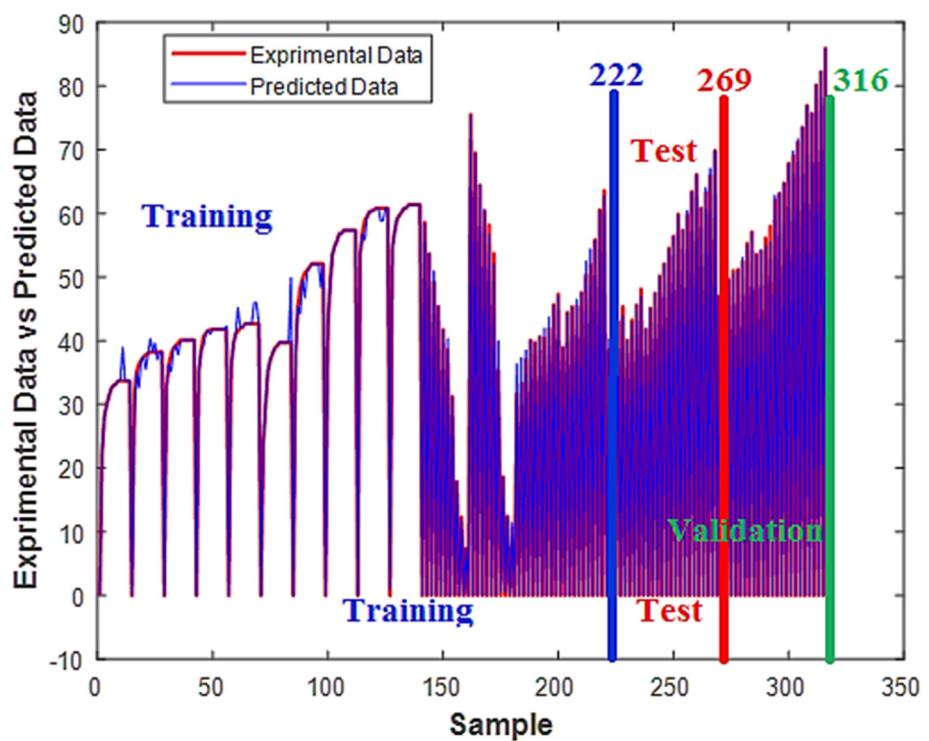
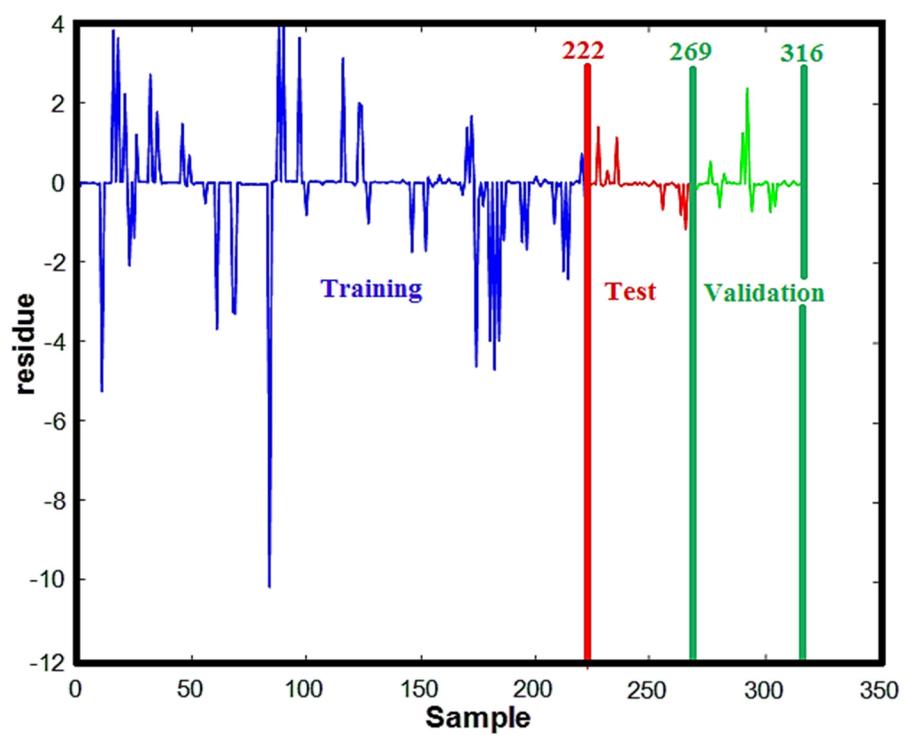


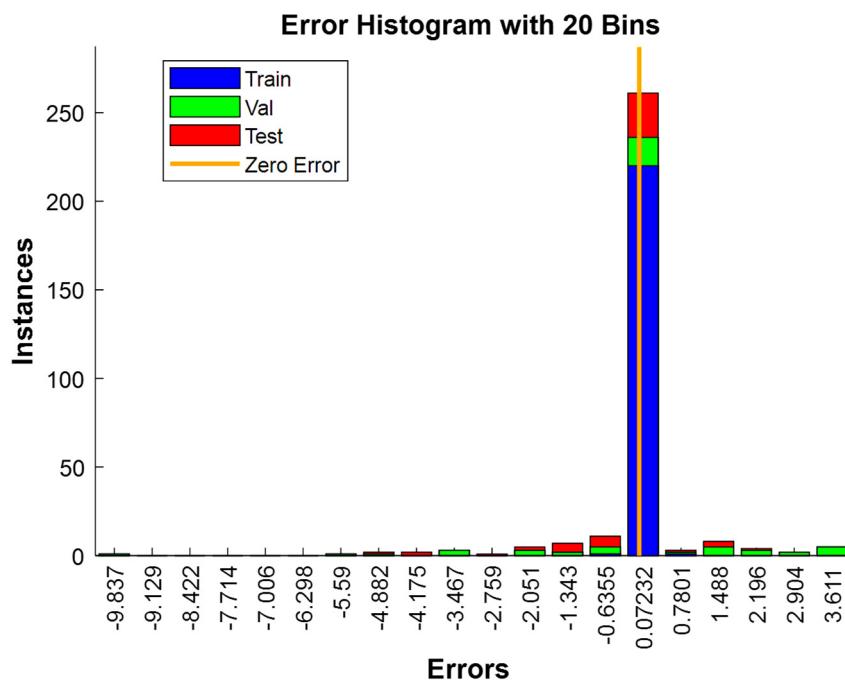
Figure 5



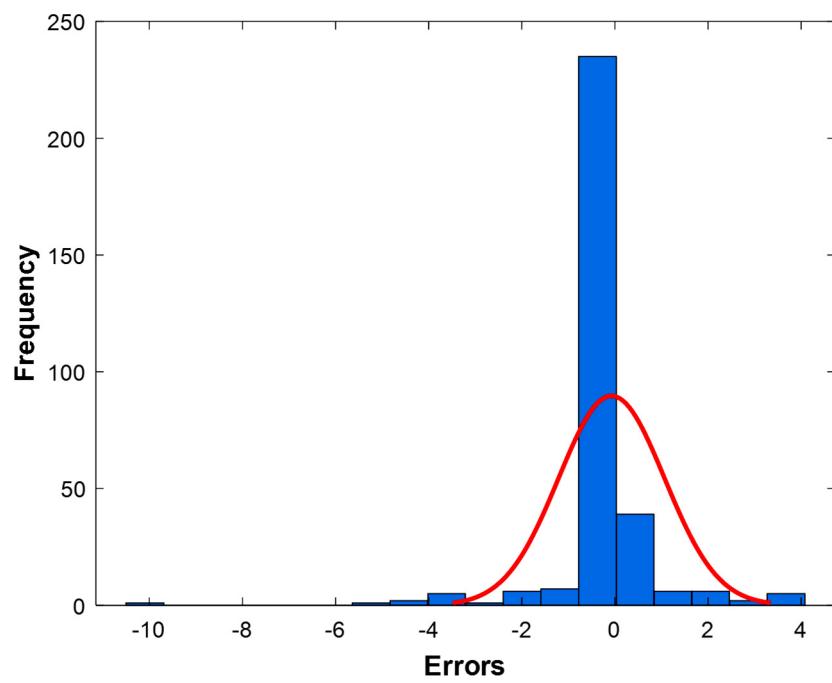
(a)



(b)

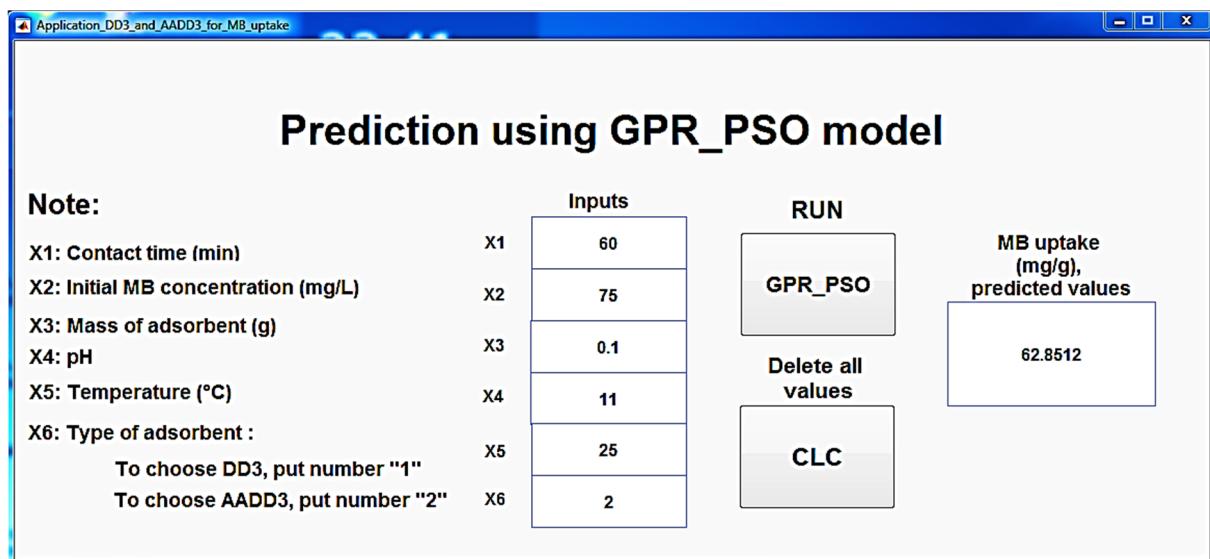


(c)



(d)

**Figure S6**



**Figure S7**

**Table S1**

Adsorbents	Qmax (mg/g)	References
Kaolin KAFE-7	42.3	Fei, F et al. (2020)
Kaolin KT3B	52.76	Mouni, L et al. (2018)
Zeolite 4AZW	9.95	Imessaoudene A. et al (2022)
Persian Kaolin	29.85	Tehrani-Bagha, A.R. et al (2011)
Geopolymer	39.52	Candamano, S. et al (2023)
Zeolite	22.00	Rida, K. et al. (2013)
10% GK	28.02	Kai, He et al. (2018)
Treated-DD3	64.58	In this study