

Supplementary Materials

S1. The estimation of fine resolution surface water map based on the MRF

X can be formulated by applying the maximum a posteriori rule in Bayesian framework by solving the maximization problem:

$$\{P^{\text{posterior}}(X|Y)\} = \text{argmax} \left\{ \frac{1}{Z} \exp[-U^{\text{posterior}}(X|Y)] \right\} \quad (\text{S1})$$

where $U^{\text{posterior}}(X|Y)$ is the posterior energy function of X given Y , and Z is a normalization constant. The optimal X can be estimated by minimizing the energy function $U^{\text{posterior}}(X|Y)$:

$$U^{\text{posterior}}(X|Y) = \lambda \cdot U^{\text{spatial}}(X) + U^{\text{fraction}}(Y|X) \quad (\text{S2})$$

where $U^{\text{spatial}}(X)$ is the spatial constraint function and $U^{\text{fraction}}(Y|X)$ is the surface water fraction constraint function that represents the inconsistency between Y and X . λ is a balance parameter.

The spatial constraint function is used to maximize the spatial dependence for the water class and land class. For each 2 m resolution pixel, the spatial dependence for the water (or land) pixel is calculated by a weighted sum of all water (or land) pixels within a local window using the target pixel as the window center. The spatial constraint function is calculated according to the spatial dependences of all the 2 m pixels as:

$$U^{\text{spatial}}(X) = \sum_{i=1}^I \sum_{j=1}^J \sum_{k=1}^{s^2} \left(-1 \times \sum_{l \in N(a_{ijk})} \delta(c(a_{ijk}), c(a_l)) / d(a_{ijk}, a_l) \right) \quad (\text{S3})$$

where I and J are the number of Sentinel-2 pixels, a_{ijk} is a target 2 m resolution pixel, $N(a_{ijk})$ is a $w \times w$ sized window with which a_{ijk} is its center, a_l is its neighborhood pixel $N(a_{ijk})$, $d(a_{ijk}, a_l)$ is the geometric distance between a_{ijk} and a_l , $c(a_{ijk})$ and $c(a_l)$ are the class labels of the pixels a_{ijk} and a_l , and $\delta(c(a_{ijk}), c(a_l))$ is the Kronecker delta function that equals 1 if $c(a_{ijk})$ and $c(a_l)$ are the same or 0 otherwise.

The water fraction constraint function is used to minimize the surface water fractions between the unmixed Sentinel-2 pixels and the predicted 2 m surface water map as:

$$U^{\text{fraction}}(Y|X) = \sum_{i=1}^I \sum_{j=1}^J (F_{ij}^{\text{unmix}} - F_{ij}^{\text{predict}})^2 \quad (\text{S4})$$

where F_{ij}^{unmix} and F_{ij}^{predict} are the surface water fractions within the 10 m Sentinel-2 pixel

(i,j) . F_{ij}^{predict} is calculated by dividing the total number of 2 m resolution water pixels within

the Sentinel-2 pixel (i,j) by s^2 , and the value of F_{ij}^{predict} is iteratively updated.