

Supplementary Materials:

S1: Numerical model setup for anisotropic medium:

Considering a linear elastic material, the constitutive equations can be expressed in terms of generalized Hooke's law as follows:

$$\sigma_{ij} = C_{ijkl} \varepsilon_{kl} \quad i, j, k, l = 1, 2, 3 \quad (1)$$

where σ_{ij} and ε_{kl} are the components of the stress and strain tensors and C_{ijkl} are the elements of the fourth-order elastic tensor which has 81 components; in the case of isotropic materials, this number is reduced to 2 and the elastic tensor can be expressed as:

$$C_{ijkl} = \lambda \delta_{ij} \delta_{kl} + \mu (\delta_{ik} \delta_{jl} + \delta_{il} \delta_{jk}) \quad (2)$$

where μ and λ are the Lamé's constants and δ_{ij} is the Kronecker's delta. Using Voigt notation, the elastic tensor can be expressed as a 6×6 matrix (e.g., Mavko et al., 2020):

$$[C] = \begin{bmatrix} 2\mu + \lambda & \lambda & \lambda & 0 & 0 & 0 \\ \lambda & 2\mu + \lambda & \lambda & 0 & 0 & 0 \\ \lambda & \lambda & 2\mu + \lambda & 0 & 0 & 0 \\ 0 & 0 & 0 & \mu & 0 & 0 \\ 0 & 0 & 0 & 0 & \mu & 0 \\ 0 & 0 & 0 & 0 & 0 & \mu \end{bmatrix} \quad (3)$$

The components of this matrix are stiffness components in which $2\mu + \lambda$ is $C_{11} = C_{22} = C_{33}$, λ is $C_{12} = C_{23} = C_{31}$ and μ is $C_{44} = C_{55} = C_{66}$ for isotropic material, and these values are related to the speed of pressure and shear waves in the domain as follows:

$$V_p = \sqrt{\frac{C_{11}}{\rho}} \quad (4)$$

$$V_s = \sqrt{\frac{C_{44}}{\rho}} \quad (5)$$

where V_p and V_s are the speeds of pressure and shear waves. Such a model can be used for numerically model dynamic wave propagation in anisotropic materials with 1) extrinsic source of anisotropy such as existing poly materials and micro-cracks and 2) intrinsic source of anisotropy such as crystallographic preferred orientations. A numerical tool has been developed on COMSOL multi-physics, which provides a concrete framework to implement the above formulation by the finite element method. For this purpose, "solid mechanics" or "wave propagation" modules of the software can be employed.