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TABLE S1. Singlet-triplet energy gap  $E_{\text{ST}}$  (in kcal/mol) of GNP[ $m,n$ ] ( $m = 1\text{--}4$ ), calculated using spin-unrestricted TAO-LDA.

| $n$ | $E_{\text{ST}}$ (GNP[1, $n$ ]) | $E_{\text{ST}}$ (GNP[2, $n$ ]) | $E_{\text{ST}}$ (GNP[3, $n$ ]) | $E_{\text{ST}}$ (GNP[4, $n$ ]) |
|-----|--------------------------------|--------------------------------|--------------------------------|--------------------------------|
| 2   | 64.77                          | 50.08                          | 33.96                          | 22.24                          |
| 3   | 43.21                          | 33.97                          | 23.50                          | 15.38                          |
| 4   | 29.01                          | 22.25                          | 15.38                          | 10.16                          |
| 5   | 19.60                          | 14.64                          | 10.13                          | 6.82                           |
| 6   | 13.55                          | 10.07                          | 7.01                           | 4.84                           |
| 7   | 9.91                           | 7.38                           | 5.17                           | 3.67                           |
| 8   | 7.84                           | 5.71                           | 4.02                           | 2.94                           |
| 9   | 6.66                           | 4.59                           | 3.26                           | 2.45                           |
| 10  | 5.90                           | 3.79                           | 2.75                           | 2.11                           |
| 11  | 5.32                           | 3.22                           | 2.37                           | 1.85                           |
| 12  | 4.82                           | 2.81                           | 2.09                           | 1.65                           |
| 13  | 4.38                           | 2.50                           | 1.86                           | 1.49                           |
| 14  | 3.98                           | 2.26                           | 1.69                           | 1.35                           |
| 15  | 3.65                           | 2.06                           | 1.54                           | 1.25                           |
| 16  | 3.37                           | 1.90                           | 1.42                           | 1.15                           |
| 17  | 3.14                           | 1.76                           | 1.31                           | 1.07                           |
| 18  | 2.94                           | 1.64                           | 1.22                           | 1.00                           |
| 19  | 2.77                           | 1.53                           | 1.14                           | 0.94                           |
| 20  | 2.62                           | 1.44                           | 1.08                           | 0.89                           |
| 21  | 2.49                           | 1.36                           | 1.02                           | 0.84                           |
| 22  | 2.37                           | 1.28                           | 0.96                           | 0.80                           |
| 23  | 2.25                           | 1.22                           | 0.91                           | 0.76                           |
| 24  | 2.15                           | 1.16                           | 0.87                           | 0.73                           |
| 25  | 2.06                           | 1.11                           | 0.83                           | 0.69                           |

|    |      |      |      |      |
|----|------|------|------|------|
| 26 | 1.98 | 1.06 | 0.79 | 0.66 |
| 27 | 1.90 | 1.01 | 0.76 | 0.64 |
| 28 | 1.83 | 0.97 | 0.73 | 0.61 |
| 29 | 1.76 | 0.93 | 0.70 | 0.59 |
| 30 | 1.70 | 0.90 | 0.68 | 0.57 |

TABLE S2. Vertical ionization potential  $\text{IP}_v$  (in eV), vertical electron affinity  $\text{EA}_v$  (in eV), fundamental gap  $E_g$  (in eV), and symmetrized von Neumann entropy  $S_{\text{vN}}$  for the ground state of  $\text{GNP}[1,n]$ , calculated using spin-unrestricted TAO-LDA.

| $n$ | $\text{IP}_v$ | $\text{EA}_v$ | $E_g$ | $S_{\text{vN}}$ |
|-----|---------------|---------------|-------|-----------------|
| 2   | 7.81          | -0.62         | 8.43  | 0.00            |
| 3   | 7.00          | 0.28          | 6.73  | 0.03            |
| 4   | 6.46          | 0.90          | 5.56  | 0.15            |
| 5   | 6.07          | 1.34          | 4.73  | 0.40            |
| 6   | 5.79          | 1.66          | 4.13  | 0.75            |
| 7   | 5.59          | 1.89          | 3.69  | 1.08            |
| 8   | 5.44          | 2.06          | 3.38  | 1.34            |
| 9   | 5.33          | 2.19          | 3.13  | 1.52            |
| 10  | 5.23          | 2.30          | 2.93  | 1.67            |
| 11  | 5.15          | 2.39          | 2.76  | 1.82            |
| 12  | 5.08          | 2.48          | 2.60  | 1.98            |
| 13  | 5.01          | 2.55          | 2.46  | 2.16            |
| 14  | 4.96          | 2.61          | 2.34  | 2.36            |
| 15  | 4.91          | 2.67          | 2.23  | 2.55            |
| 16  | 4.86          | 2.72          | 2.13  | 2.75            |
| 17  | 4.82          | 2.77          | 2.05  | 2.94            |
| 18  | 4.78          | 2.81          | 1.97  | 3.13            |
| 19  | 4.75          | 2.85          | 1.89  | 3.31            |
| 20  | 4.71          | 2.89          | 1.83  | 3.50            |
| 21  | 4.68          | 2.92          | 1.76  | 3.69            |

|    |      |      |      |      |
|----|------|------|------|------|
| 22 | 4.66 | 2.95 | 1.71 | 3.88 |
| 23 | 4.63 | 2.98 | 1.65 | 4.07 |
| 24 | 4.61 | 3.00 | 1.60 | 4.26 |
| 25 | 4.59 | 3.03 | 1.56 | 4.44 |
| 26 | 4.57 | 3.05 | 1.52 | 4.63 |
| 27 | 4.55 | 3.07 | 1.47 | 4.82 |
| 28 | 4.53 | 3.09 | 1.44 | 5.01 |
| 29 | 4.51 | 3.11 | 1.40 | 5.20 |
| 30 | 4.50 | 3.13 | 1.37 | 5.39 |

TABLE S3. Vertical ionization potential  $\text{IP}_v$  (in eV), vertical electron affinity  $\text{EA}_v$  (in eV), fundamental gap  $E_g$  (in eV), and symmetrized von Neumann entropy  $S_{\text{vN}}$  for the ground state of  $\text{GNP}[2,n]$ , calculated using spin-unrestricted TAO-LDA.

| $n$ | $\text{IP}_v$ | $\text{EA}_v$ | $E_g$ | $S_{\text{vN}}$ |
|-----|---------------|---------------|-------|-----------------|
| 2   | 7.05          | 0.19          | 6.86  | 0.02            |
| 3   | 6.45          | 0.89          | 5.57  | 0.09            |
| 4   | 6.02          | 1.40          | 4.62  | 0.32            |
| 5   | 5.72          | 1.76          | 3.96  | 0.67            |
| 6   | 5.51          | 2.01          | 3.50  | 1.04            |
| 7   | 5.37          | 2.19          | 3.17  | 1.36            |
| 8   | 5.25          | 2.33          | 2.92  | 1.64            |
| 9   | 5.16          | 2.45          | 2.71  | 1.93            |
| 10  | 5.08          | 2.54          | 2.53  | 2.23            |
| 11  | 5.01          | 2.62          | 2.38  | 2.53            |
| 12  | 4.95          | 2.69          | 2.26  | 2.82            |
| 13  | 4.90          | 2.76          | 2.14  | 3.10            |
| 14  | 4.85          | 2.81          | 2.04  | 3.38            |
| 15  | 4.81          | 2.86          | 1.95  | 3.67            |
| 16  | 4.78          | 2.90          | 1.87  | 3.95            |
| 17  | 4.74          | 2.94          | 1.80  | 4.23            |

|    |      |      |      |      |
|----|------|------|------|------|
| 18 | 4.71 | 2.98 | 1.73 | 4.52 |
| 19 | 4.69 | 3.01 | 1.67 | 4.80 |
| 20 | 4.66 | 3.04 | 1.62 | 5.09 |
| 21 | 4.64 | 3.07 | 1.56 | 5.37 |
| 22 | 4.61 | 3.10 | 1.52 | 5.65 |
| 23 | 4.59 | 3.12 | 1.47 | 5.94 |
| 24 | 4.57 | 3.14 | 1.43 | 6.22 |
| 25 | 4.56 | 3.17 | 1.39 | 6.51 |
| 26 | 4.54 | 3.19 | 1.35 | 6.79 |
| 27 | 4.52 | 3.20 | 1.32 | 7.07 |
| 28 | 4.51 | 3.22 | 1.29 | 7.36 |
| 29 | 4.49 | 3.24 | 1.25 | 7.64 |
| 30 | 4.48 | 3.25 | 1.23 | 7.93 |

TABLE S4. Vertical ionization potential  $\text{IP}_v$  (in eV), vertical electron affinity  $\text{EA}_v$  (in eV), fundamental gap  $E_g$  (in eV), and symmetrized von Neumann entropy  $S_{\text{vN}}$  for the ground state of GNP[3, $n$ ], calculated using spin-unrestricted TAO-LDA.

| $n$ | $\text{IP}_v$ | $\text{EA}_v$ | $E_g$ | $S_{\text{vN}}$ |
|-----|---------------|---------------|-------|-----------------|
| 2   | 6.45          | 0.89          | 5.57  | 0.09            |
| 3   | 6.01          | 1.40          | 4.60  | 0.28            |
| 4   | 5.68          | 1.80          | 3.88  | 0.62            |
| 5   | 5.46          | 2.07          | 3.38  | 1.03            |
| 6   | 5.30          | 2.27          | 3.03  | 1.41            |
| 7   | 5.19          | 2.42          | 2.77  | 1.77            |
| 8   | 5.10          | 2.54          | 2.56  | 2.12            |
| 9   | 5.02          | 2.63          | 2.39  | 2.47            |
| 10  | 4.96          | 2.71          | 2.25  | 2.82            |
| 11  | 4.91          | 2.78          | 2.13  | 3.16            |
| 12  | 4.86          | 2.84          | 2.02  | 3.50            |
| 13  | 4.82          | 2.89          | 1.93  | 3.84            |

|    |      |      |      |      |
|----|------|------|------|------|
| 14 | 4.78 | 2.94 | 1.84 | 4.18 |
| 15 | 4.75 | 2.98 | 1.77 | 4.52 |
| 16 | 4.72 | 3.02 | 1.70 | 4.86 |
| 17 | 4.69 | 3.05 | 1.63 | 5.20 |
| 18 | 4.66 | 3.09 | 1.58 | 5.54 |
| 19 | 4.64 | 3.12 | 1.52 | 5.88 |
| 20 | 4.62 | 3.14 | 1.48 | 6.22 |
| 21 | 4.60 | 3.17 | 1.43 | 6.55 |
| 22 | 4.58 | 3.19 | 1.39 | 6.89 |
| 23 | 4.56 | 3.21 | 1.35 | 7.23 |
| 24 | 4.54 | 3.23 | 1.31 | 7.57 |
| 25 | 4.53 | 3.25 | 1.28 | 7.91 |
| 26 | 4.51 | 3.27 | 1.24 | 8.25 |
| 27 | 4.50 | 3.29 | 1.21 | 8.58 |
| 28 | 4.49 | 3.30 | 1.18 | 8.92 |
| 29 | 4.48 | 3.32 | 1.16 | 9.26 |
| 30 | 4.46 | 3.33 | 1.13 | 9.60 |

TABLE S5. Vertical ionization potential  $\text{IP}_v$  (in eV), vertical electron affinity  $\text{EA}_v$  (in eV), fundamental gap  $E_g$  (in eV), and symmetrized von Neumann entropy  $S_{\text{vN}}$  for the ground state of GNP[4, $n$ ], calculated using spin-unrestricted TAO-LDA.

| $n$ | $\text{IP}_v$ | $\text{EA}_v$ | $E_g$ | $S_{\text{vN}}$ |
|-----|---------------|---------------|-------|-----------------|
| 2   | 6.02          | 1.40          | 4.62  | 0.32            |
| 3   | 5.68          | 1.80          | 3.88  | 0.62            |
| 4   | 5.44          | 2.10          | 3.34  | 1.03            |
| 5   | 5.27          | 2.31          | 2.96  | 1.46            |
| 6   | 5.15          | 2.47          | 2.69  | 1.88            |
| 7   | 5.06          | 2.59          | 2.48  | 2.28            |
| 8   | 4.99          | 2.68          | 2.31  | 2.68            |
| 9   | 4.93          | 2.76          | 2.17  | 3.06            |

|    |      |      |      |       |
|----|------|------|------|-------|
| 10 | 4.88 | 2.83 | 2.05 | 3.44  |
| 11 | 4.83 | 2.89 | 1.94 | 3.82  |
| 12 | 4.79 | 2.95 | 1.85 | 4.20  |
| 13 | 4.76 | 2.99 | 1.77 | 4.58  |
| 14 | 4.73 | 3.03 | 1.69 | 4.96  |
| 15 | 4.70 | 3.07 | 1.63 | 5.33  |
| 16 | 4.67 | 3.11 | 1.57 | 5.71  |
| 17 | 4.65 | 3.14 | 1.51 | 6.09  |
| 18 | 4.63 | 3.17 | 1.46 | 6.46  |
| 19 | 4.61 | 3.19 | 1.41 | 6.84  |
| 20 | 4.59 | 3.22 | 1.37 | 7.21  |
| 21 | 4.57 | 3.24 | 1.33 | 7.59  |
| 22 | 4.55 | 3.26 | 1.29 | 7.96  |
| 23 | 4.54 | 3.28 | 1.26 | 8.34  |
| 24 | 4.52 | 3.30 | 1.22 | 8.72  |
| 25 | 4.51 | 3.32 | 1.19 | 9.09  |
| 26 | 4.50 | 3.33 | 1.16 | 9.47  |
| 27 | 4.48 | 3.35 | 1.13 | 9.84  |
| 28 | 4.47 | 3.36 | 1.11 | 10.22 |
| 29 | 4.46 | 3.38 | 1.08 | 10.59 |
| 30 | 4.45 | 3.39 | 1.06 | 10.97 |