

Supplementary Materials:

Table S1. Fitting results of the E_{dd2} and E_{dd1} spectra in Figure 3 obtained by using Eq. (1).

$E_{dd1} \ (e_{1g} \rightarrow a_{1g})$

Temp. (K)	E_1 (eV)	E_2 (eV)	E_{const} (eV)	τ_1 (fs)	τ_2 (ps)
35	$-0.2547 \pm 4.1E-02$	$-0.0819 \pm 1.4E-02$	$2.3198 \pm 7.8E-05$	$266.80 \pm 1.4E+01$	$1.52 \pm 8.0E-01$
40	$-0.2547 \pm 1.3E-05$	$-0.0736 \pm 2.0E-05$	$2.3139 \pm 9.5E-07$	$283.10 \pm 4.4E-02$	$1.98 \pm 5.2E-04$
45	$-0.2340 \pm 5.9E-03$	$-0.0932 \pm 2.9E-03$	$2.3171 \pm 1.3E-03$	$358.85 \pm 1.5E+01$	$1.51 \pm 2.4E-01$
50	$-0.2285 \pm 2.1E-05$	$-0.0831 \pm 2.2E-05$	$2.3097 \pm 5.5E-07$	$353.18 \pm 3.9E-02$	$1.72 \pm 3.5E-04$
55	$-0.2719 \pm 3.9E-02$	$-0.0802 \pm 3.9E-02$	$2.3328 \pm 9.1E-03$	$381.88 \pm 9.4E+01$	$2.31 \pm 1.0E-02$
60	$-0.2500 \pm 4.2E-02$	$-0.0980 \pm 4.2E-02$	$2.3219 \pm 2.0E-03$	$263.22 \pm 4.2E+01$	$2.40 \pm 1.1E+00$
65	$-0.2320 \pm 6.3E-02$	$-0.0936 \pm 6.0E-02$	$2.3148 \pm 1.3E-03$	$514.70 \pm 2.4E+02$	$2.55 \pm 9.2E-01$
70	$-0.1457 \pm 5.3E-02$	$-0.1645 \pm 6.6E-02$	$2.2984 \pm 1.8E-03$	$319.07 \pm 1.8E+02$	$1.63 \pm 4.3E-01$
75	$-0.1415 \pm 2.9E-02$	$-0.1703 \pm 3.3E-02$	$2.3041 \pm 4.8E-03$	$328.97 \pm 1.1E+01$	$2.01 \pm 3.1E-01$
80	-	$-0.3128 \pm 7.7E-03$	$2.2980 \pm 3.9E-03$	-	$1.38 \pm 1.4E-01$
100	-	$-0.3116 \pm 3.2E-03$	$2.2918 \pm 1.7E-02$	-	$1.82 \pm 5.0E-01$
120	-	$-0.2878 \pm 5.6E-03$	$2.2675 \pm 3.9E-03$	-	$1.26 \pm 2.5E-01$
130	-	$-0.2723 \pm 6.8E-03$	$2.2764 \pm 7.5E-03$	-	$2.33 \pm 9.8E-02$
140	-	$-0.2753 \pm 3.6E-03$	$2.2365 \pm 7.7E-04$	-	$2.20 \pm 1.6E-01$
150	-	$-0.2468 \pm 1.4E-02$	$2.2305 \pm 1.0E-02$	-	$3.42 \pm 3.2E-01$

$E_{dd2} \ (e_{2g} \rightarrow a_{1g})$

Temp. (K)	E_1 (eV)	E_2 (eV)	E_{const} (eV)	τ_1 (fs)	τ_2 (ps)
35	$-0.0301 \pm 1.8E-03$	$-0.0322 \pm 3.6E-04$	$1.7704 \pm 3.5E-04$	$346.520 \pm 7.0E+01$	$2.12 \pm 3.5E-02$
40	$-0.0248 \pm 6.4E-03$	$-0.0363 \pm 2.5E-03$	$1.7684 \pm 2.8E-04$	$275.392 \pm 4.7E+01$	$1.95 \pm 7.3E-02$
45	$-0.0262 \pm 4.4E-03$	$-0.0281 \pm 2.8E-03$	$1.7642 \pm 6.4E-04$	$485.113 \pm 1.2E+02$	$2.32 \pm 1.4E-01$
50	$-0.0257 \pm 5.1E-03$	$-0.0302 \pm 3.6E-04$	$1.7612 \pm 3.9E-04$	$354.641 \pm 1.0E+02$	$2.52 \pm 8.9E-02$
55	$-0.0346 \pm 9.6E-03$	$-0.0308 \pm 4.4E-03$	$1.7681 \pm 2.1E-04$	$455.891 \pm 1.6E+02$	$2.35 \pm 1.9E-01$
60	$-0.0383 \pm 7.2E-03$	$-0.0364 \pm 3.3E-03$	$1.7629 \pm 4.0E-04$	$308.325 \pm 5.3E-01$	$2.13 \pm 1.7E-02$
65	$-0.0170 \pm 1.9E-03$	$-0.0268 \pm 6.9E-04$	$1.7515 \pm 4.1E-04$	$342.099 \pm 4.7E+01$	$2.98 \pm 1.6E-02$
70	$-0.0185 \pm 1.3E-03$	$-0.0266 \pm 2.1E-03$	$1.7465 \pm 7.9E-05$	$475.203 \pm 3.9E+01$	$3.05 \pm 3.2E-01$
75	$-0.0231 \pm 4.5E-03$	$-0.0132 \pm 1.1E-03$	$1.7477 \pm 4.3E-03$	$1519.961 \pm 2.2E+02$	$16.16 \pm 1.6E+01$
80	$-0.0218 \pm 1.1E-02$	$-0.0184 \pm 1.1E-02$	$1.7441 \pm 1.8E-03$	$1156.294 \pm 8.0E+02$	$5.77 \pm 3.6E+00$
100	$-0.0145 \pm 3.2E-03$	$-0.0132 \pm 9.9E-03$	$1.7288 \pm 1.0E-03$	$1315.512 \pm 1.6E+03$	$5.52 \pm 1.9E+00$
130	$-0.0171 \pm 7.7E-03$	$-0.0130 \pm 2.8E-03$	$1.7166 \pm 4.5E-03$	$576.011 \pm 7.3E+01$	$6.82 \pm 3.5E+00$
150	$-0.0101 \pm 2.1E-05$	$-0.0117 \pm 4.0E-03$	$1.7127 \pm 2.5E-03$	$471.907 \pm 1.7E+02$	$5.33 \pm 1.1E+00$