

Joule Heating Effect of Thin Films with Carbon-Based Nanomaterials

Usha Kiran Sanivada ^{1,2,3*}, Dina Esteves ^{1,3}, Luisa M. Arruda ^{1,3}, Carla Silva ⁴, Inês P. Moreira ^{1,3} and Raul Fangueiro ^{1,3}

¹ Fibrenamics – Institute of Innovation in Fiber-Based Materials and Composites, Azurém Campus, 4800-058, Guimarães, Portugal

² Mechanical Engineering and Resources Sustainability Centre (MEtRICS), University of Minho, Azurém Campus, 4800-058, Guimarães, Portugal

³ Centre for Textile Science and Technology (2C2T), University of Minho, Azurém Campus, 4800-058, Guimarães, Portugal

⁴ Simoldes Plastics, Research & Innovation, Rua Comendador António da Silva Rodrigues 165, Oliveira de Azeméis, Portugal

* Correspondence: ushakiran.sanivada@gmail.com (U.K.S); rfangueiro@dem.uminho.pt (R.F.)

Table S1. Technical data of the materials

Material	Technical Specifications	Supplier Details
Edolan CM	Aqueous aliphatic polycarbonate polyether polyurethane dispersion	Tanatex Chemicals, Netherlands
	Viscosity at 20°C ≤ 90 s (ISO 2431, flow cup 4 mm)	
	Density: 1.1 g/cm ³	
	Ionicity: Anionic	
	White	
Tanapur EP 3061	Aqueous preparation of an aliphatic polyether polyurethane	Tanatex Chemicals, Netherlands
	Density: 1.0-1.1 g/cm ³	
	Ionicity: Slightly cationic	
	Light Yellow, Yellow clear liquid	
Thickener A 02	Polyurethane preparation	Tanatex Chemicals, Netherlands
	Viscosity at 23°C: 5000-10000 mPa.s	
	Density: 1.19 g/cm ³	
	Ionicity: Nonionic	
	Yellowish liquid	
GNPs	Thickness: 3 and 10 nm	Graphenest, Portugal
	Planar size: 0.5 to 0.2 µm	
	Surface Area: 150 m ² /g	
CNTs	Multi-Walled Carbon Nanotubes	Iolitec Ionic Technologies, Germany
	Length: ~1.5 µm	
	90% C Purity Industrial Grade	
Cotton Fabric	Weft density = 26/cm ² , Warp density = 33/cm ²	Lameirinho, Portugal
	GSM= 119.68 g/m ²	

Table S2. Electrical resistivity of various samples coated with GNPs

GNPs % (w/v)	Electrical Resistivity (Ωm)		
	1 Layer	2 Layers	3 Layers
0	$8.80\text{E}+07 \pm 0.00\text{E}+00$	$8.80\text{E}+07 \pm 0.00\text{E}+00$	$8.80\text{E}+07 \pm 0.00\text{E}+00$
2	$2.24\text{E}+05 \pm 9.80\text{E}+03$	$2.40\text{E}+05 \pm 0.00\text{E}+00$	$2.40\text{E}+05 \pm 0.00\text{E}+00$
3	$1.12\text{E}+03 \pm 1.50\text{E}+02$	$1.40\text{E}+04 \pm 0.00\text{E}+00$	$8.00\text{E}+04 \pm 0.00\text{E}+00$
5	$3.11\text{E}+00 \pm 1.85\text{E}-02$	$3.94\text{E}+00 \pm 1.39\text{E}-01$	$4.97\text{E}+00 \pm 2.18\text{E}-01$
7	$9.62\text{E}-01 \pm 8.21\text{E}-02$	$1.06\text{E}+00 \pm 4.64\text{E}-02$	$2.04\text{E}+00 \pm 2.36\text{E}-01$
10	$1.45\text{E}-01 \pm 4.39\text{E}-03$	$1.53\text{E}-01 \pm 7.65\text{E}-03$	$2.09\text{E}-01 \pm 8.33\text{E}-03$
12	$1.07\text{E}-01 \pm 1.09\text{E}-03$	$1.11\text{E}-01 \pm 1.83\text{E}-03$	$1.67\text{E}-01 \pm 3.03\text{E}-03$

Table S3. Conductivity of various samples coated with GNPs

GNPs % (w/v)	Electrical Conductivity (S/m)		
	1 Layer	2 Layers	3 Layers
0	$1.14\text{E}-08 \pm 0.00\text{E}+00$	$1.14\text{E}-08 \pm 0.00\text{E}+00$	$1.14\text{E}-08 \pm 0.00\text{E}+00$
2	$4.56\text{E}-06 \pm 2.04\text{E}-07$	$4.17\text{E}-06 \pm 0.00\text{E}+00$	$4.17\text{E}-06 \pm 0.00\text{E}+00$
3	$9.58\text{E}-04 \pm 1.25\text{E}-04$	$7.14\text{E}-05 \pm 0.00\text{E}+00$	$1.25\text{E}-05 \pm 0.00\text{E}+00$
5	$3.22\text{E}-01 \pm 1.91\text{E}-03$	$2.55\text{E}-01 \pm 9.31\text{E}-03$	$2.03\text{E}-01 \pm 8.31\text{E}-03$
7	$1.06\text{E}+00 \pm 7.16\text{E}-02$	$9.48\text{E}-01 \pm 3.81\text{E}-02$	$5.08\text{E}-01 \pm 4.29\text{E}-02$
10	$6.92\text{E}+00 \pm 1.99\text{E}-01$	$6.57\text{E}+00 \pm 2.90\text{E}-01$	$4.82\text{E}+00 \pm 1.79\text{E}-01$
12	$9.39\text{E}+00 \pm 1.28\text{E}-01$	$9.04\text{E}+00 \pm 1.35\text{E}-01$	$6.01\text{E}+00 \pm 1.13\text{E}-01$

Table S4. Electrical resistivity and conductivity of various samples coated with GNPs + CNTs (50:50)

GNPs % (w/v)	Electrical Resistivity (Ωm)	Electrical Conductivity (S/m)
	1 Layer	1 Layer
0	$8.80\text{E}+07 \pm 0.00\text{E}+00$	$1.14\text{E}-08 \pm 0.00\text{E}+00$
3	$4.23\text{E}-01 \pm 4.02\text{E}-03$	$2.37\text{E}+00 \pm 2.05\text{E}-02$
5	$1.11\text{E}-01 \pm 9.46\text{E}-04$	$9.02\text{E}+00 \pm 6.62\text{E}-02$
7	$2.11\text{E}-01 \pm 1.12\text{E}-03$	$4.73\text{E}+00 \pm 3.07\text{E}-02$
10	$3.96\text{E}-01 \pm 6.80\text{E}-03$	$2.52\text{E}+00 \pm 5.00\text{E}-02$