

# Supplementary Materials

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## Crystal Structure and Theoretical Analysis of $\text{Cs}_2\text{Ca}_3(\text{SO}_4)_4$

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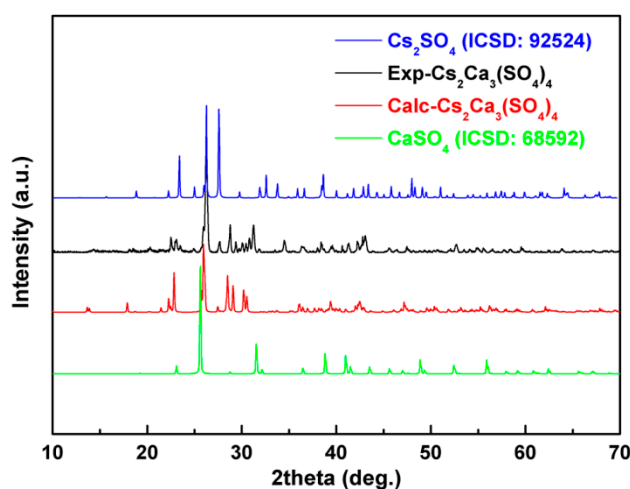
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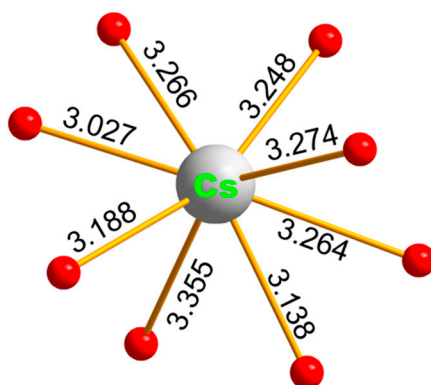
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Calculation Setting

The kinetic energy absorption, empty bands, k-point sampling, and pseudopotential used for calculating the birefringence were 310 eV, 12,  $1 \times 1 \times 1$ , and ultrasoft for  $\text{Cs}_2\text{Ca}_3(\text{SO}_4)_4$ , 310 eV,  $2 \times 2 \times 1$ , and ultrasoft for  $\text{Cs}_2\text{Mg}_3(\text{SO}_4)_4$ , 310 eV, 12,  $1 \times 1 \times 1$ , and ultrasoft for  $\text{Rb}_2\text{Mg}_3(\text{SO}_4)_4$ , respectively.



**Figure S1.** The comparison of XRD patterns with raw reagents of  $\text{Cs}_2\text{SO}_4$  and  $\text{CaSO}_4$ .  $\text{Cs}_2\text{SO}_4$ -(ICSD: 92524) represents the calculated XRD pattern of  $\text{Cs}_2\text{SO}_4$  with the Inorganic Crystal Structure Database (ICSD) number of 92524.  $\text{CaSO}_4$ -(ICSD: 68592) represents the calculated XRD pattern of  $\text{Cs}_2\text{SO}_4$  with the ICSD number of 68592.



**Figure S2.** The ball-and-stick representation of a  $\text{CsO}_8$  polyhedron in  $\text{Cs}_2\text{Ca}_3(\text{SO}_4)_4$ .

**Table S1.** Crystal data and structure refinement for Cs<sub>2</sub>Ca<sub>3</sub>(SO<sub>4</sub>)<sub>4</sub>.

Formula sum	Cs <sub>2</sub> Ca <sub>3</sub> (SO <sub>4</sub> ) <sub>4</sub>
Formula weight	770.30
Crystal system	Monoclinic
Space group	<i>P</i> 2 <sub>1</sub> / <i>c</i> (no. 14)
<i>a</i> (Å)	9.9153(8)
<i>b</i> (Å)	9.3760(6)
<i>c</i> (Å)	9.8044(9)
$\beta$	118.365(3)
<i>V</i> (Å <sup>3</sup> )	802.04(11)
<i>Z</i>	2
D <sub>calcd</sub> (g cm <sup>-3</sup> )	3.190
Temperature (K)	299(2)
$\lambda$ (Å)	0.71073
<i>F</i> (000)	724
Crystal size	0.08 × 0.06 × 0.06 mm <sup>3</sup>
Data/restraints/parameters	1635/0/115
$\mu$ (mm <sup>-1</sup> )	6.104
GOF ( <i>F</i> <sup>2</sup> )	1.246
<i>R</i> (int)	0.0506
<i>R</i> <sub>1</sub> / <i>wR</i> <sub>2</sub> ( <i>I</i> > 2σ( <i>I</i> )) <sup>a</sup>	0.0438/0.0832
<i>R</i> <sub>1</sub> / <i>wR</i> <sub>2</sub> (all data)	0.0521/0.0864

$$^a) R_1 = \sum ||F_0| - |F_c|| / \sum |F_0| \text{ and } wR_2 = [\sum [w(F_0^2 - F_c^2)^2] / \sum [w(F_0^2)^2]]^{1/2} \text{ for } F_0^2 > 2\sigma(F_c^2)$$

**Table S2.** Atom coordinates and equivalent isotropic displacement parameters for Cs<sub>2</sub>Ca<sub>3</sub>(SO<sub>4</sub>)<sub>4</sub>.

Atom	Wyck.	Symmetry	<i>x/a</i>	<i>y/b</i>	<i>z/c</i>	<i>U</i> <sub>eq</sub> (Å <sup>2</sup> ) <sup>a</sup>
Cs1	4e	1	0.66389(5)	0.82800(5)	0.55989(5)	0.0297(2)
Ca1	4e	1	0.24601(14)	0.62804(12)	0.24129(15)	0.0123(3)
Ca2	2a	−1	0	0	0	0.0166(4)
S1	4e	1	0.39243(16)	0.93806(15)	0.14757(18)	0.0107(3)
S2	4e	1	−0.02522(16)	0.34085(15)	0.16829(17)	0.0102(3)
O1	4e	1	0.5390(5)	1.0101(5)	0.2385(6)	0.0259(11)
O2	4e	1	0.3795(5)	0.8283(5)	0.2465(5)	0.0235(11)
O3	4e	1	0.2670(5)	1.0420(5)	0.1031(6)	0.0223(11)
O4	4e	1	0.3848(6)	0.8735(5)	0.0089(6)	0.0274(11)
O5	4e	1	0.1202(6)	0.4159(6)	0.2309(6)	0.0351(14)
O6	4e	1	−0.0740(6)	0.3377(6)	0.2892(6)	0.0331(13)
O7	4e	1	−0.0043(7)	0.1920(5)	0.1399(7)	0.0472(17)
O8	4e	1	−0.1423(6)	0.4069(5)	0.0277(5)	0.0263(12)

<sup>a</sup>) *U*<sub>eq</sub> is defined as one-third of the trace of the orthogonalized *U*<sub>ij</sub> tensor.

**Table S3.** Selected bond distances and angles for Cs<sub>2</sub>Ca<sub>3</sub>(SO<sub>4</sub>)<sub>4</sub>.

Bonds	Bond distances (Å)	Bonds	Bond angles (°)	Bonds	Bond angles (°)
Cs(1)-O(2)	3.026(5)	O(1)#5-Ca(1)-O(8)#7	85.63(17)	O(7)-Ca(2)-O(6)#10	86.1(2)
Cs(1)-O(1)	3.266(5)	O(1)#5-Ca(1)-O(6)#1	157.01(19)	O(7)#6-Ca(2)-O(3)#8	93.0(2)
Cs(1)-O(3)#4	3.275(5)	O(2)-Ca(1)-O(6)#11	73.39(18)	O(7)-Ca(2)-O(3)#8	87.0(2)
Cs(1)-O(3)#5	3.354(5)	O(2)-Ca(1)-O(4)#2	87.34(17)	O(7)#6-Ca(2)-O(6)#9	86.1(2)
Cs(1)-O(4)#2	3.188(5)	O(2)-Ca(1)-O(1)#5	83.74(18)	O(7)-Ca(2)-O(6)#9	93.9(2)
Cs(1)-O(5)#1	3.138(5)	O(2)-Ca(1)-O(5)	176.3(2)	O(7)#6-Ca(2)-O(7)	180.0
Cs(1)-O(7)#1	3.263(6)	O(2)-Ca(1)-O(8)#7	94.56(17)	O(7)#6-Ca(2)-O(3)#7	87.0(2)
Cs(1)-O(8)#3	3.248(5)	O(4)#2-Ca(1)-O(5)	93.56(19)	O(7)-Ca(2)-O(3)#7	93.0(2)
Ca(1)-O(1)#5	2.325(4)	O(4)#2-Ca(1)-O(8)#7	167.92(18)	O(6)#9-Ca(2)-O(6)#10	180.0(2)
Ca(1)-O(2)	2.284(5)	O(4)#2-Ca(1)-O(1)#5	82.71(18)	O(1)-S(1)-O(2)	107.2(3)
Ca(1)-O(4)#2	2.312(5)	O(4)#2-Ca(1)-O(6)#1	98.25(18)	O(1)-S(1)-O(3)	109.3(3)
Ca(1)-O(5)	2.324(5)	O(5)-Ca(1)-O(1)#5	92.8(2)	O(2)-S(1)-O(3)	109.5(3)
Ca(1)-O(6)#11	2.526(5)	O(5)-Ca(1)-O(8)#7	83.82(19)	O(4)-S(1)-O(1)	110.9(3)
Ca(1)-O(8)#7	2.354(5)	O(5)-Ca(1)-O(6)#11	110.04(19)	O(4)-S(1)-O(2)	110.2(3)
Ca(2)-O(3)#7	2.376(5)	O(8)#7-Ca(1)-O(6)#1	93.72(17)	O(4)-S(1)-O(3)	109.6(3)
Ca(2)-O(3)#8	2.376(5)	O(3)#7-Ca(2)-O(6)#1	85.15(17)	O(5)-S(2)-O(6)	107.9(3)
Ca(2)-O(6)#9	2.384(5)	O(3)#8-Ca(2)-O(6)#1	94.85(17)	O(5)-S(2)-O(7)	110.0(4)
Ca(2)-O(6)#10	2.384(5)	O(3)#7-Ca(2)-O(6)#9	94.85(17)	O(7)-S(2)-O(6)	105.4(4)
Ca(2)-O(7)#6	2.276(5)	O(3)#8-Ca(2)-O(6)#9	85.15(17)	O(8)-S(2)-O(5)	112.3(3)
Ca(2)-O(7)	2.276(5)	O(3)#7-Ca(2)-O(3)#8	180.0	O(8)-S(2)-O(6)	110.5(3)
S(1)-O(1)	1.461(4)	O(7)#6-Ca(2)-O(6)#1	93.9(2)	O(8)-S(2)-O(7)	110.4(3)
S(1)-O(2)	1.461(5)				
S(1)-O(3)	1.474(4)				
S(1)-O(4)	1.457(5)				
S(2)-O(5)	1.453(5)				
S(2)-O(6)	1.478(5)				
S(2)-O(7)	1.457(5)				
S(2)-O(8)	1.453(5)				

Symmetry transformations used to generate equivalent atoms: (#1) 1-x, 1-y, 1-z; (#2) x, 1.5-y, 0.5+z; (#3) 1+x, 1.5-y, 0.5+z; (#4) 1-x, 2-y, 1-z; (#5) 1-x, -0.5+y, 0.5-z; (#6) -x, -y, -z; (#7) -x, 1-y, -z; (#8) x, -1+y, z; (#9) -x, -0.5+y, 0.5-z; (#10) x, 0.5-y, -0.5+z; (#11) -x, 0.5+y, 0.5-z.

**Table S4.** Anisotropic displacement parameters for Cs<sub>2</sub>Ca<sub>3</sub>(SO<sub>4</sub>)<sub>4</sub>.

Atom	$U_{11}$ (Å <sup>2</sup> )	$U_{22}$ (Å <sup>2</sup> )	$U_{33}$ (Å <sup>2</sup> )	$U_{23}$ (Å <sup>2</sup> )	$U_{13}$ (Å <sup>2</sup> )	$U_{12}$ (Å <sup>2</sup> )
Cs1	0.0245(3)	0.0295(3)	0.0202(3)	0.00058(19)	−0.00149(19)	0.00301(19)
Ca1	0.0092(6)	0.0104(6)	0.0132(7)	−0.0012(4)	0.0018(5)	0.0022(5)
Ca2	0.0136(9)	0.0124(8)	0.0155(10)	0.0046(7)	0.0001(7)	−0.0053(7)
S1	0.0098(7)	0.0116(7)	0.0100(7)	−0.0023(5)	0.0042(6)	−0.0005(6)
S2	0.0105(7)	0.0105(7)	0.0094(7)	−0.0017(5)	0.0046(6)	−0.0018(6)
O1	0.014(2)	0.037(3)	0.022(3)	−0.015(2)	0.005(2)	−0.003(2)
O2	0.023(2)	0.025(2)	0.016(3)	−0.008(2)	0.005(2)	0.007(2)
O3	0.019(2)	0.022(2)	0.025(3)	0.0101(19)	0.009(2)	0.005(2)
O4	0.026(3)	0.043(3)	0.014(3)	−0.001(2)	0.010(2)	−0.011(2)
O5	0.020(3)	0.039(3)	0.031(3)	−0.021(2)	0.000(2)	0.012(2)
O6	0.029(3)	0.057(4)	0.022(3)	−0.010(3)	0.019(2)	−0.003(3)
O7	0.056(4)	0.025(3)	0.036(3)	0.015(3)	0.001(3)	−0.021(3)
O8	0.027(3)	0.027(3)	0.012(3)	0.004(2)	−0.001(2)	0.004(2)