

# Supporting Information

## **Evaluation on Thermal Behavior, Synergistic Catalysis, and Pollutant Emissions during the Co-combustion of Sewage Sludge and Coal Gasification Fine Slag Residual Carbon**

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**Table S1.** Kinetic mechanism functions.

Kinetic mechanism functions	$g(\alpha)$
O1, Chemical reaction, First-order	$-\ln(1 - \alpha)$
O2, Chemical reaction, Second-order	$(1 - \alpha)^{-1}$
O3, Chemical reaction, Third-order	$(1 - \alpha)^{-2}$
D1, One-dimensional diffusion	$\alpha^2$
D2, Two-dimensional diffusion	$(1 - \alpha) \ln(1 - \alpha) + \alpha$
D3, Three-dimensional diffusion, Spherical model	$[1 - (1 - \alpha)^{1/3}]^2$
D4, Three-dimensional diffusion, Outside of a spherical model	$1 - 2\alpha/3 - (1 - \alpha)^{2/3}$

**Table S2.** Kinetic parameters of various samples at different combustion stage.

Samples	Combustion stage	Kinetic mechanism functions	Coats-Redfern method	
			Kinetic equation	$R^2$
SS	Stage 1	O1	<b><math>Y=-2286.5X-9.3</math></b>	<b>0.9812</b>
		O2	$Y=3324.6X-6.2$	0.8986
		O3	$Y=-7952.7X+2.6$	0.9211
		D1	$Y=-2555.1X-10.1$	0.7503
		D2	$Y=-3312.5X-9.2$	0.8404
		D3	$Y=-4488.7X-8.4$	0.9282
		D4	$Y=-3688.3X-10.0$	0.8761
RC	Stage 2	O1	<b><math>Y=-12711.1X+18.4</math></b>	<b>0.9789</b>
		O2	$Y=-50289.5X+48.2$	0.8949
		O3	$Y=-102686.4X+111.9$	0.8980

20SS80RC	Stage 1	D1	$Y=-22390.0X+12.1$	0.7160
		D2	$Y=-28645.5X+19.2$	0.7657
		D3	$Y=-40197.6X+31.9$	0.8371
		D4	$Y=-32203.3X+22.1$	0.7930
		O1	<b><math>Y=-4051.0X+20.1</math></b>	<b>0.9714</b>
		O2	$Y=-4236.7X+23.2$	0.9512
		O3	$Y=-4409.15X+27.5$	0.9043
		D1	$Y=-3956.6X-11.0$	0.9286
	Stage 2	D2	$Y=-4050.3X-11.4$	0.9318
		D3	$Y=-4641.8X-12.7$	0.9350
		D4	$Y=-4082.5X-12.9$	0.9329
		O1	<b><math>Y=-6644.2X+18.0</math></b>	<b>0.9844</b>
		O2	$Y=-7058.0X+21.3$	0.8085
		O3	$Y=-5768.5X+15.2$	0.8174
		D1	$Y=-6479.1X+14.4$	0.8871
		D2	$Y=-7417.0X+16.5$	0.9013
40SS60RC	Stage 1	D3	$Y=-8751.1X+21.7$	0.8989
		D4	$Y=-8432.2X+19.9$	0.9233
		O1	<b><math>Y=-3633.6X-11.1</math></b>	<b>0.9691</b>
		O2	$Y=-3815.0X-13.2$	0.9235
		O3	$Y=-4947.2X-20.5$	0.9107
		D1	$Y=-4575.0X-8.7$	0.9244
		D2	$Y=-4779.0X-9.0$	0.9310
		D3	$Y=-4995.2X-10.1$	0.9375
	Stage 2	D4	$Y=-4851.1X-10.4$	0.9333
		O1	<b><math>Y=-6181.1X+3.3</math></b>	<b>0.9573</b>

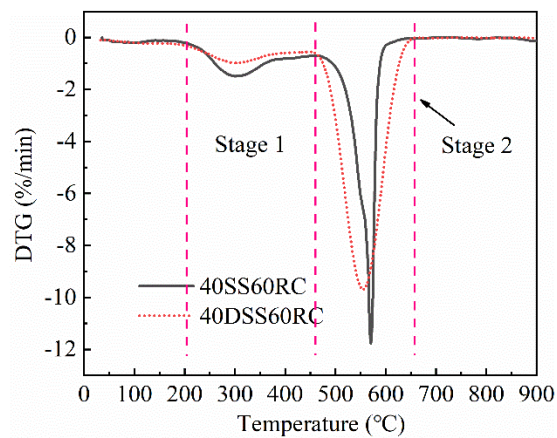
60SS40RC	Stage 1	O2	$Y=-6658.3X+5.2$	0.9102
		O3	$Y=-6947.2X+7.5$	0.8876
		D1	$Y=-5145.0X+24.4$	0.9213
		D2	$Y=-6107.0X+22.5$	0.9009
		D3	$Y=-6751.1X+21.7$	0.9227
		D4	$Y=-6832.2X+20.9$	0.9235
		O1	<b><math>Y=-4308.4X-10.4</math></b>	<b>0.9828</b>
		O2	$Y=-5315.0X-12.6$	0.9012
	Stage 2	O3	$Y=-5947.2X-13.4$	0.9680
		D1	$Y=-4437.2X-8.14$	0.9093
		D2	$Y=-4757.8X-8.2$	0.9215
		D3	$Y=-5110.8X-9.0$	0.9333
		D4	$Y=-4875.2X-9.4$	0.9257
		O1	$Y=-8135.8X-3.1$	0.9002
		O2	$Y=-8459.8X-5.2$	0.8863
		O3	$Y=-9147.2X-7.5$	0.8971
80SS20RC	Stage 1	D1	$Y=-5658.2X-7.2$	0.9187
		D2	$Y=-7124.2X-4.5$	0.9432
		D3	<b><math>Y=-7836.2X-2.2</math></b>	<b>0.9806</b>
		D4	$Y=-7639.4X-1.9$	0.9567
		O1	<b><math>Y=-4759.4X-9.8</math></b>	<b>0.9803</b>
		O2	$Y=-5315.0X-11.2$	0.9234
		O3	$Y=-5947.2X-17.5$	0.9416
		D1	$Y=-4853.0X-4.4$	0.8946
		D2	$Y=-4107.0X-2.5$	0.9025
		D3	$Y=-5751.1X-5.7$	0.9198

40DSS60RC	Stage 2	D4	$Y=-6074.3X-9.2$	0.8909
		O1	$Y=-9174.8X-9.9$	0.9104
		O2	$Y=-10315.0X-13.2$	0.9325
		O3	$Y=-9947.2X-10.5$	0.9057
		D1	$Y=-8198.7X-14.4$	0.8924
		D2	$Y=-8207.0X-12.2$	0.8819
		D3	$Y=-8375.1X-11.7$	0.9361
		D4	<b><math>Y=-8421.9X-10.9</math></b>	<b>0.9660</b>
		O1	<b><math>Y=-3835.70X-12.4</math></b>	<b>0.9844</b>
		O2	$Y=-4705.6X-9.2$	0.9304
	Stage 1	O3	$Y=-5122.3X-7.8$	0.9128
		D1	$Y=-5068.9X-16.0$	0.8656
		D2	$Y=-5397.1X-14.4$	0.8874
		D3	$Y=-5308.2X-13.0$	0.8512
		D4	$Y=-5742.3X-8.6$	0.8975
		O1	<b><math>Y=-8204.2X+15.9</math></b>	<b>0.9787</b>
		O2	$Y=-9021.6X+18.2$	0.9501
	Stage 2	O3	$Y=-9877.4X+21.5$	0.9534
		D1	$Y=-9107.8X+24.3$	0.9011
		D2	$Y=-9589.1X+29.2$	0.9226
		D3	$Y=-11021.3X+19.7$	0.8998
		D4	$Y=-9698.2X+9.8$	0.9115

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Table S3. The kinetic parameters of 40SS60RC and 40DSS60RC.

Samples	Stage 1			Stage 2		
	$E_a$ (kJ/mol)	Model	$R^2$	$E_a$ (kJ/mol)	Model	$R^2$
40SS60RC	30.21	O1	0.9691	51.39	O1	0.9573
40DSS60RC	31.89	O1	0.9844	68.21	O1	0.9678



**Figure S1.** Comparison of the DTG results of 40SS60RC and 40DSS60RC.