

Article

Design of a Biaxial Laminar Shear Box for 1g Shaking Table Tests

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Abstract: In this paper, the design of a new laminar shear box at the Laboratory of Earthquake Engineering and Dynamic Analysis (L.E.D.A.) of the University of Enna “Kore” (Sicily, Italy), is presented. The laminar box has been developed to investigate the liquefaction phenomenon and to validate advanced numerical models and/or the numerical approaches assessed to simulate and prevent related effects. The first part of the paper describes in detail the types of soil containers that have been used in the last three decades around the world. Particular attention is paid to laminar shear box and liquefaction studies. Moreover, the most important factors that affect the performance of a laminar shear box are reported. The last part of the paper describes components, properties, and design advantages of the new laminar shear box for 1g shaking table tests at L.E.D.A. The new laminar box has a rectangular cross section and consists of 16 layers. Each layer is composed of two frames: an inner frame and an outer frame. The inner frame has an internal dimension of 2570 mm by 2310 mm, while the outer frame has an internal dimension of 2700 mm by 2770 mm. Between the layers, there is a 20 mm gap, making the total height 1600 mm.

Keywords: liquefaction; 1g shaking table test; laminar shear box



Citation: Castelli, F.; Grasso, S.; Lentini, V.; Sammito, M.S.V. Design of a Biaxial Laminar Shear Box for 1g Shaking Table Tests. *Geotechnics* **2022**, *2*, 467–487. <https://doi.org/10.3390/geotechnics2020023>

Academic Editors: Qi Wang, Bei Jiang, Xuezheng Wu and Hongke Gao

Received: 26 April 2022

Accepted: 10 June 2022

Published: 16 June 2022

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1. Introduction

Liquefaction is one of the major reasons for damage during an earthquake [1]. The phenomenon occurs as a result of build-up of pore pressure and hence a reduction of soil strength [2]. A better understanding of this phenomenon is of relevant interest in geotechnical earthquake engineering.

Liquefaction studies involve several approaches and procedures: laboratory cyclic triaxial tests [3–5], stress-based simplified procedures [6–12], numerical models [1,13–15], dynamic element tests [16,17], reduced-scale model tests [18–20], and full-scale field tests [21–23].

Reduced-scale model tests are advantageous for seismic studies thanks to the ability to provide economic and realistic information about the ground amplification, change in water pressure, and soil non-linearity [18,24].

This paper presents the design of a biaxial laminar shear box for reduced-scale model tests. The laminar shear box can be used in liquefaction studies, especially to validate numerical models and/or the numerical approaches assessed to prevent related effects.

The numerical simulation of soil lab tests is relevant to qualitatively understand the behavior of the “artificial soil” and should therefore be considered in the validation process.

2. Background

Geotechnical scaled seismic model tests can be divided into two categories: shaking table test at 1g and centrifuge test at n -g [1,24–27]. Shaking table tests have the advantages of well controlled large amplitude, and easier experimental measurements than centrifuge

tests. However, high gravitational stresses cannot be produced to faithfully simulate field conditions [18,20,25,26,28–30].

Most studies of seismic soil behaviours were for one-dimensional shaking [24,26,27,31–35]. However, real earthquake excitations are multiaxial [36]. Ng et al. [37] performed biaxial shaking centrifuge tests to investigate the response of saturated embankments. Ueng et al. [38] developed a large flexible laminar shear box for the study of the behaviour of saturated sand under two-dimensional earthquake shaking. Zeghal et al. [36] investigated the dynamic response and liquefaction of saturated sand deposits subjected to biaxial shaking.

A variety of model container configurations have been used in the last three decades. Six types of soil container can be identified: rigid, rigid with flexible boundaries, rigid with hinged end-wall, equivalent shear beam (EBS), laminar, and active boundary container [29].

The simplest method for geotechnical modelling is to use a rigid box. In this design, the shear stiffness of the end wall is much higher than the stiffness of the layers of soil contained in it [29]. Sadrekarimi & Ghalandarzadeh [2] performed 1g shaking table tests using a transparent plexiglas container to study liquefaction mitigation methods.

Motamed & Towhata [39] used a rigid container with transparent side walls to study the seismic performance of pile groups behind quay walls subjected to liquefaction (Figure 1). Özener et al. [40] investigated the liquefaction behaviour of layered sands using a cylindrical Plexiglas container (Figure 2).

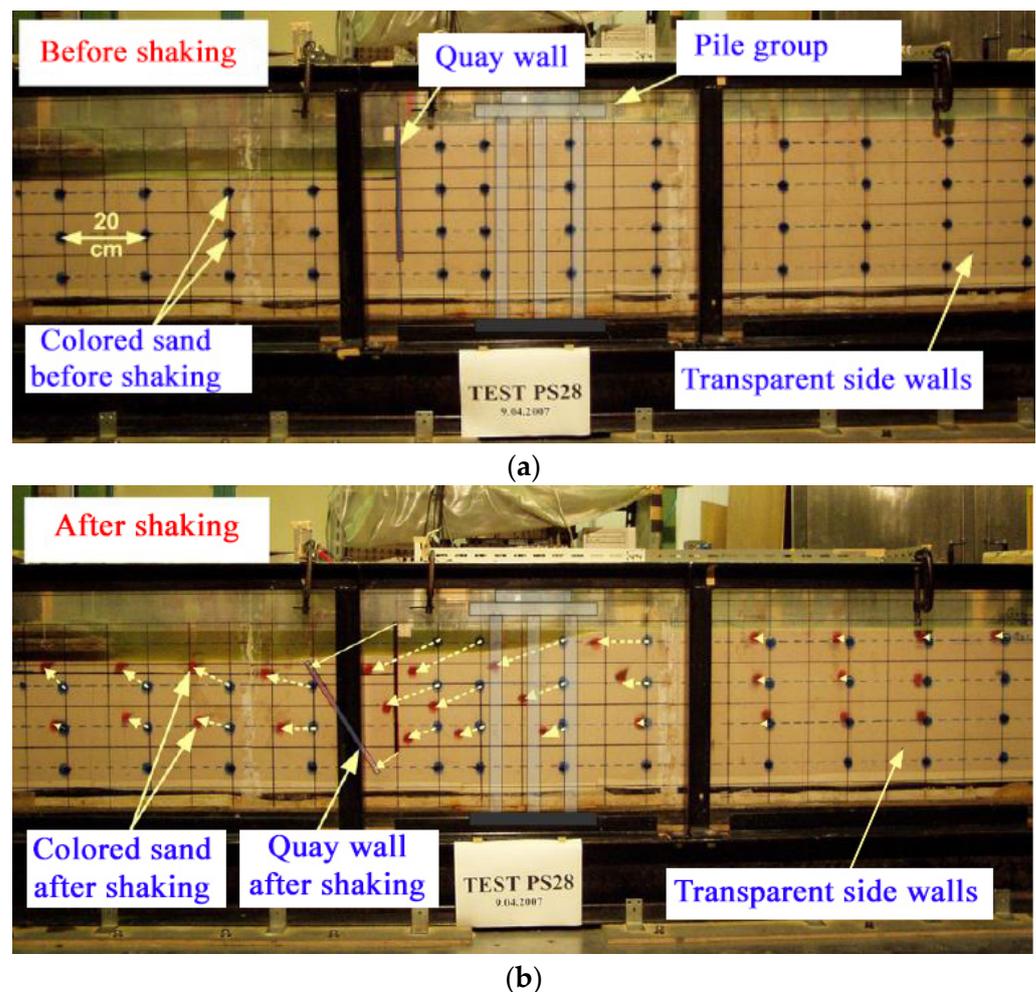


Figure 1. View of the model: (a) before shaking, (b) after shaking (From [39]; modified).

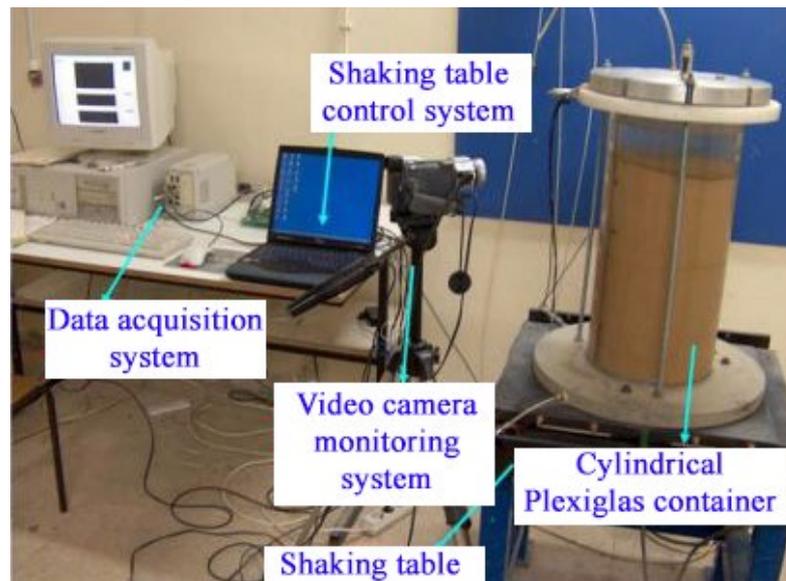


Figure 2. General view of the experimental test (From [40]; modified).

However, the rigid box is often not suitable because the waves reach the rigid walls and reflect back to the soil. To reduce the reflection of the waves and the lateral stiffness of the walls, boundary conditions can be modified by the use of soft materials, as for example duxseal or sponge [29].

Madabhushi et al. [41] performed centrifuge tests using a rigid box with absorbent boundaries constituted of a 5-inch thick duxseal layer with a thin sand sheet. Saha et al. [42] studied the effect of soil-structure interaction using a rigid box with absorbent boundaries. They were simulated by fixing up 50 mm thickness of sponge at both end walls (Figure 3).

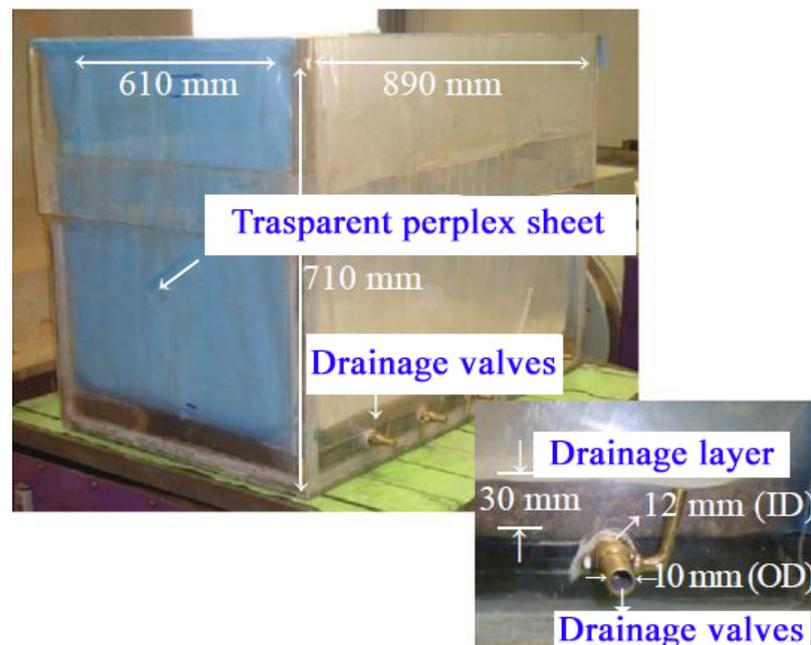


Figure 3. Rigid box with absorbent boundaries (From [42]; modified).

In a rigid container with a hinged end-wall, the walls can rotate about the base due to the hinged connection [29] (Figure 4). Fishman et al. [43] designed a rigid container with a hinged end-wall to replicate the free-field seismic response of a soil layer overlying a rigid base.

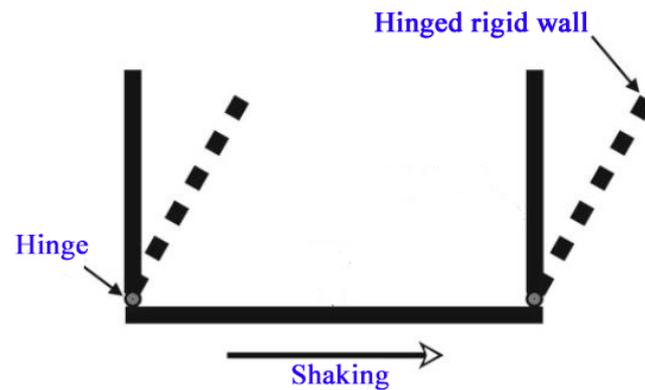


Figure 4. Schematic diagram of rigid container with hinged end-walls (from [29]; modified).

For increasing the flexibility of the box wall, equivalent shear beam (ESB) containers [44] or laminar box soil containers [45] can be used.

The ESB container consists of an alternating stack of aluminium alloy and rubber rings for flexibility [31,44,46–48].

In this last design, the stiffness of the end walls of the container is designed to match the shear stiffness of the soil contained in it at a particular strain level [29].

Massimino et al. [49] and Biondi et al. [50] carried out shaking table tests at the Earthquake Engineering Research Centre (EERC-University of Bristol) in order to investigate some aspects of the dynamic soil-structure interaction (DSSI). The Bristol University ESB (5.0 m × 1.0 m × 1.2 m) was designed by Crewe et al. [51]. It is formed of a series of rectangular aluminium rings, each of which is linked to the upper and lower rings with neoprene blocks (Figure 5). Aldaikh et al. [52] conducted a series of shaking table tests at Earthquake and Large Structures Laboratory (EQUALS—University of Bristol) to examine the effects of soil-structure-soil interaction on the response of a model building when bordered by up to two other model buildings under dynamic excitation. Penna et al. [53] studied the dynamic response of cantilever retaining walls under seismic actions by means of a 1g shaking table at EQUALS.

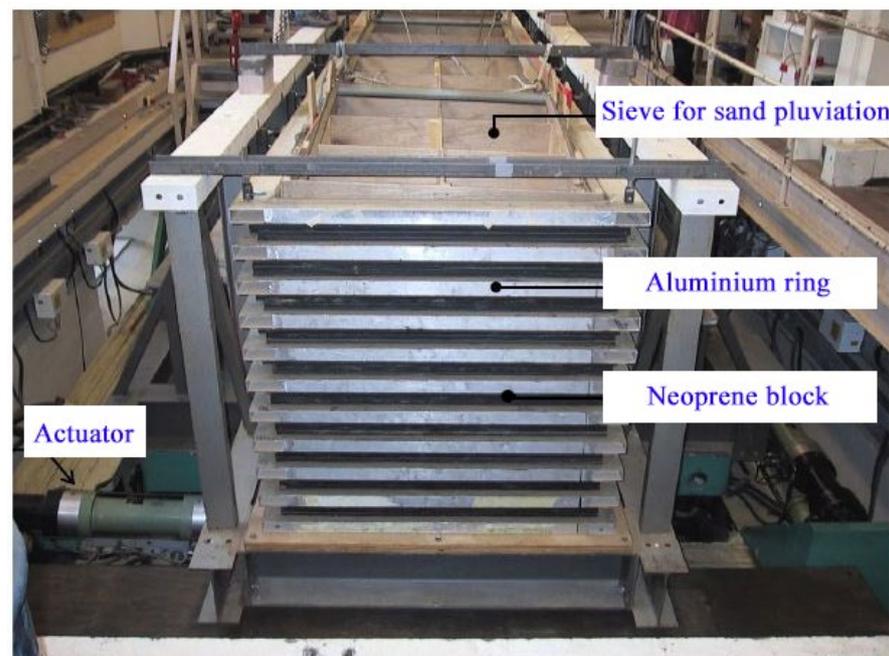


Figure 5. General view of the shear stack (From [5]; modified).

Chidichimo et al. [54] investigated the effect of soil inhomogeneity and material nonlinearity on kinematic soil-pile interaction by means of 1g shaking table tests using an equivalent shear beam container. The ESB consists of eight rectangular aluminium rings, stacked alternately with rubber sections. Durante et al. [55] illustrated a simplified analytical procedure for determining the shear wave velocity profile (V_s) in a single or bi-layer deposit. The proposed method was compared to experimental data. The tests were performed using the equivalent shear beam (ESB) container at the Bristol Laboratory for advanced Dynamics Engineering (BLADE—University of Bristol). Fiorentino et al. [56] investigated the benefits of adding compressible inclusions (CIs) between the abutment and the backfill, with an emphasis on SSI. A flexible shear stack was employed to minimize the effects of physical boundaries on the dynamic response of the soil.

The laminar box soil container consists of a stack of stiff rings (or layers) supported by ball bearings, linear bearings, or rollers. Moreover, during shaking, an internal rubber membrane is placed inside the container to protect the layers from soil penetration. The design principle of a laminar box is to minimize the lateral stiffness of the container in order to ensure that soil governs the response of the soil-box system. The active boundaries container is very similar to the laminar container, but external actuators are connected to each lamina (Figure 6) [29].

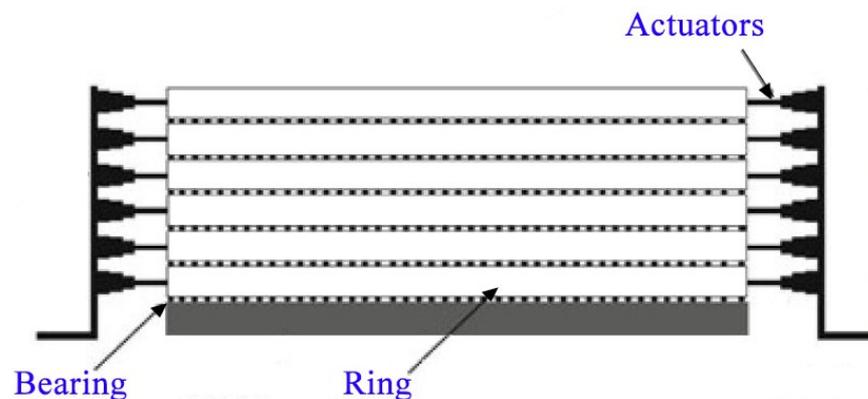


Figure 6. Active boundaries container (From [29]; modified).

A laminar box soil container is often used to model liquefaction [18–20,25,36,38,57–59].

Alaie & Chenari [28] designed a laminar shear box at University of Guilan in the province of Guilan, Northern Iran. The box consists of fifteen rectangular layers separated by ball bearings; four roller columns were installed to prevent the frames from moving perpendicular to the shaking direction (Figure 7).

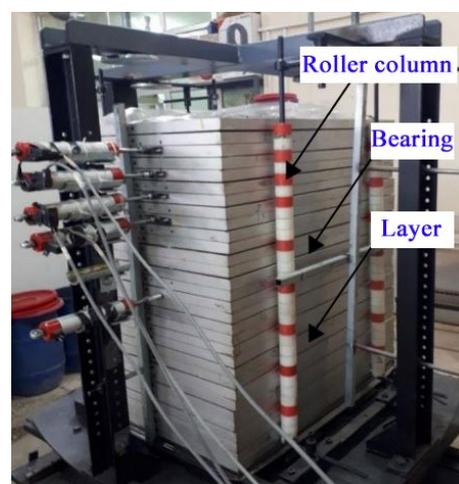


Figure 7. General view of the laminar box (From [28]; modified).

Ecemis [25] carried out 1D shaking table tests in order to simulate the liquefaction of loose to medium dense saturated sands. The laminar box was composed of 24 rings made of aluminium I-beams. In order to reduce the friction between the layer, rings were separated and supported by eight rollers (Figure 8).

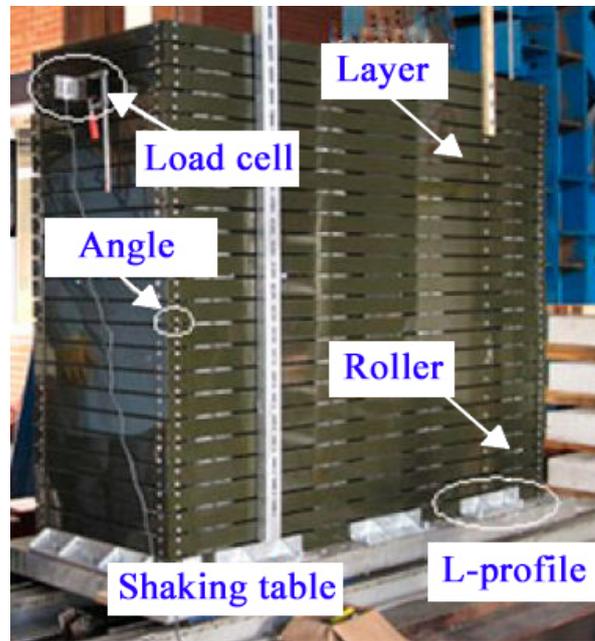


Figure 8. General view of the laminar box (From [25]; modified).

Zayed et al. [27] designed a laminar container at the University of California, San Diego. The container consists of laminates supported by a cantilevered bearing connected to an external frame (Figure 9). This design has the advantage of avoiding a cumulative vertical load.

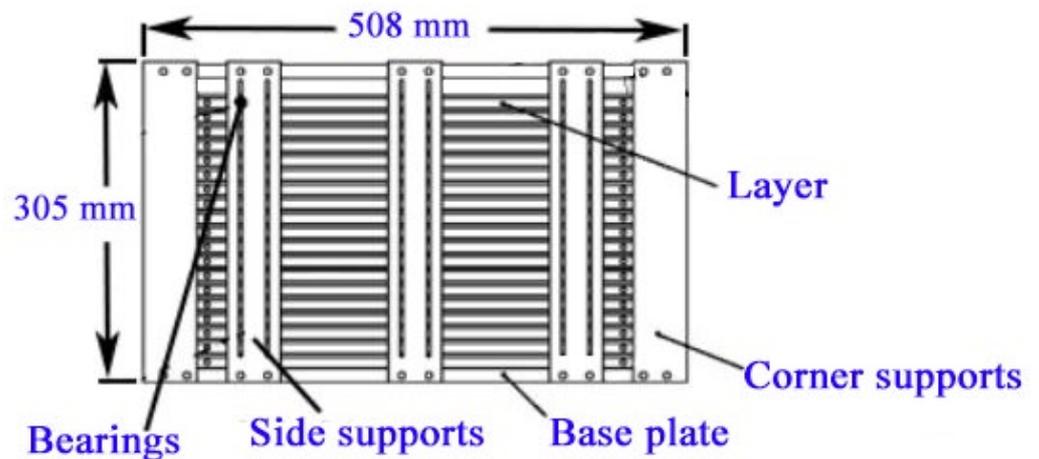


Figure 9. General view of the laminar box (From [27]; modified).

Mohsan et al. [20] designed a laminar soil box for studying the behaviour of saturated soils, especially liquefaction. A set of seventeen laminae were placed on top of each other in a skeleton by linear bearings (Figure 10). The movement is allowed in one direction.

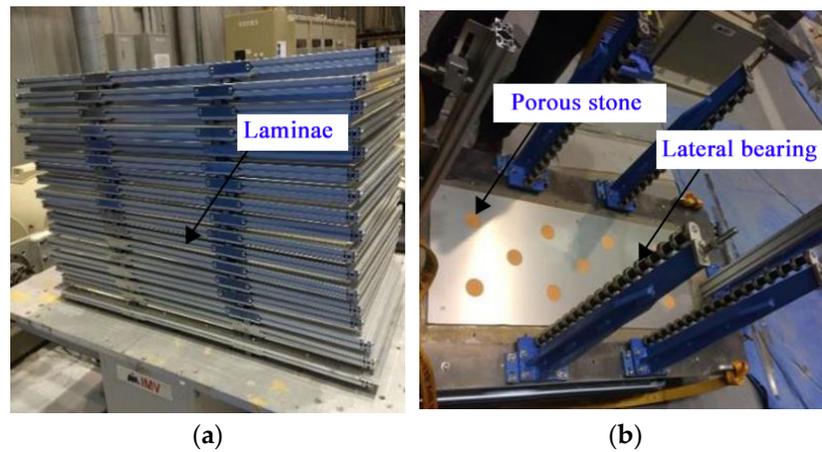


Figure 10. (a) Laminae (b) skeleton for laminae (From [20]; modified).

Thevanayagam et al. [57] studied the effects of liquefaction and lateral spreading using a 2D laminar box system. The laminar box consists of 24 octagon-shaped aluminium laminates made of I-beams. The rings were separated by high-capacity ball bearings placed between the laminates. Figure 11 shows the laminar box system. Zeghal et al. [36] performed a number of centrifuge model tests using a 2D laminar container. This consists of twelve-sided rings separated from the ones above and below by roller bearings. A view of the laminar container is reported in Figure 12.

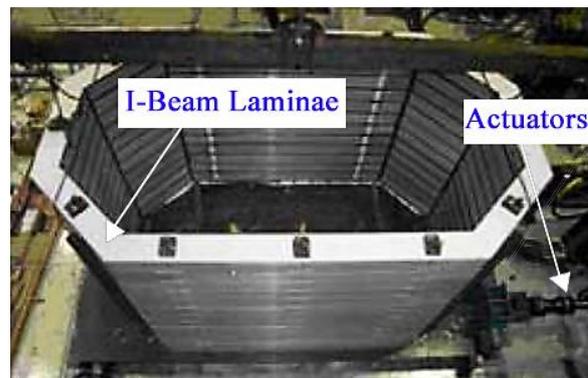


Figure 11. Laminar box system (From Thevanayagam et al. [57]; modified).

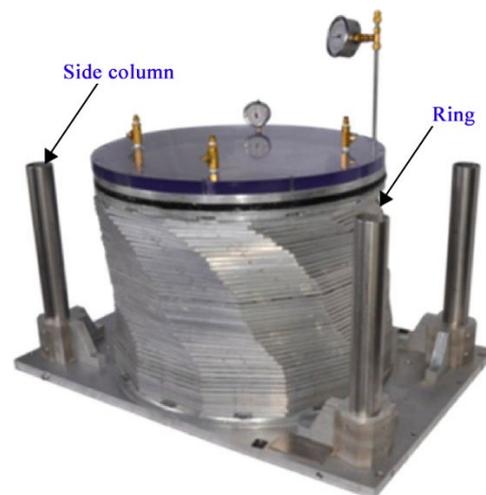


Figure 12. General view of the laminar container (From [36]; modified).

Jafarzadeh [30] designed a 2D laminar box for the shaking table of the Earthquake Research Centre of Sharif University of Technology (SUT). The system was composed of 24 layers separated by transfer ball bearings. In the four sides of the box, four steel columns were installed to prevent oversized deformations (Figure 13).

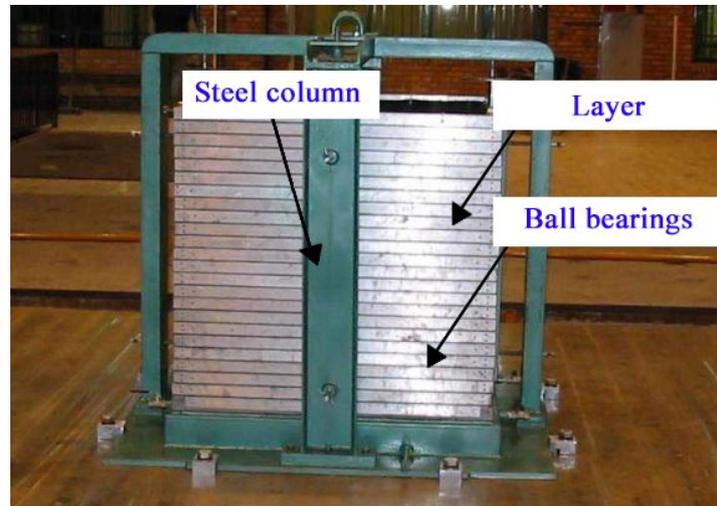


Figure 13. General view of the laminar container (From Jafarzadeh [30]; modified).

A 2D laminar shear box was designed by Ueng et al. [38] at the National Centre for Research on Earthquake Engineering (NCREE) in Taiwan for the study of liquefaction and soil-structure interaction. To allow biaxial motion and to ensure non-torsional motion, a special mechanism design was adopted.

The laminar box is composed of 15 layers supported on the surrounding rigid steel walls. Each layer consists of two nested frames, an inner frame with inside dimensions of 1880 mm by 1880 mm and an outer frame with inside dimensions of 1940 mm by 2340 mm.

Schematic drawings of the biaxial laminar box are reported in Figure 14, while in Table 1 several examples of laminar shear boxes have been summarized.

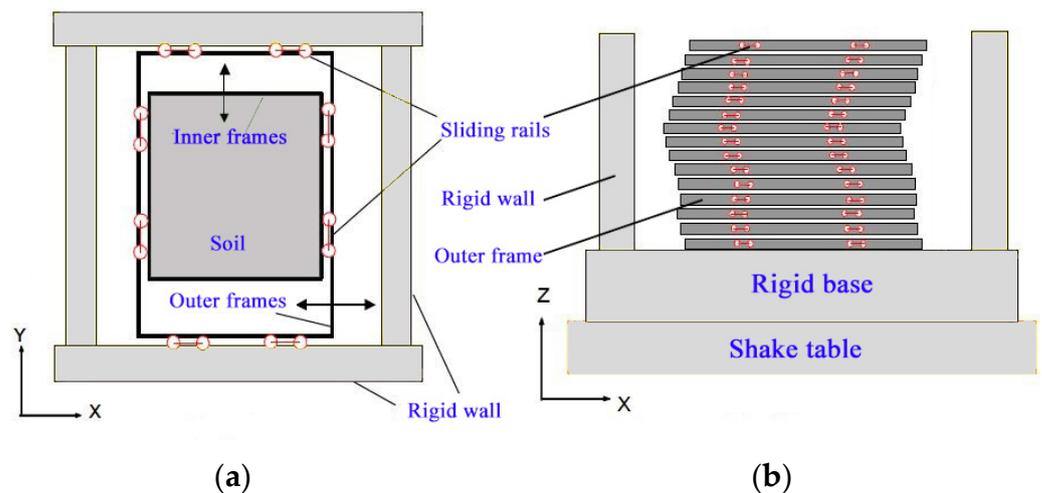


Figure 14. Schematic drawings of the biaxial laminar box (From [60]; modified): (a) top view and (b) side view.

Table 1. Examples of laminar shear boxes.

Reference	1g/n-g	Direction	Design
Alaie & Chenari [28]	1g	1D	Layers supported by ball bearings
Ecemis [25]	1g	1D	Layers supported by rollers
Zayed et al. [27]	n-g	1D	Layers supported by bearings connected to an external frame
Mohsan et al. [20]	n-g	1D	Layers placed in a skeleton supported by linear bearing
Thevanayagam et al. [57]	n-g	2D	Layers supported by ball bearings
Zeghal et al. [36]	n-g	2D	Layers supported by roller bearings
Jafarzadeh [30]	1g	2D	Layers supported by ball bearings
Ueng et al. [38]	1g	2D	Layers of frames supported on the surrounding rigid steel walls

3. Performance and Requirements of a Laminar Box

Before shaking the soil is assumed to be in a k_0 condition, while during shaking, the normal stresses remain constant and the shear stresses increase [29]. The soil at different depths could move differently on horizontal and vertical planes [38]. For this reason, the design principle of a laminar box is to minimize the lateral stiffness of the container in order to ensure that the soil governs the response of the soil-box system [29].

Important factors that affect the performance of the laminar box are the wall effect, the membrane effect, the effect of friction between the layers and the effect of inertia induced by the mass of the box walls [25,26,30,38].

In a laminar box the stiffness of the walls is limited to the friction between the layers and the influence of the rubber membrane [25,61]. Prasad et al. [26] performed several tests, with membrane and without membrane, demonstrating that the membrane effect was localized near the edge and did not affect the performance of the soil.

To reduce the friction between layers ball bearings, linear bearings or roller bearings are placed between the layers. The remaining friction force can be measured by static pull out tests [25,26,30].

Due to the inertia effect, the measured acceleration in the model is less than the real value. To account for this effect, the measured acceleration needs to be corrected by the following equation:

$$a_s = \left(\frac{m_1 + m_2}{m_1} \right) a \quad (1)$$

being a_s = acceleration of the soil without the influence of the box; a = measured acceleration; m_1 = mass of soil within the layer; m_2 = mass of the corresponding layer [25,26,30].

Moreover, Bhattacharya et al. [29] defined the following criteria that a model container has to satisfy:

- Maintenance of stress similarity in the model as in the prototype—The stress field is not affected by the boundaries at a considerably distance from the end walls. It has to be adequately evaluated by experimental or numerical analysis;
- Maintenance of strain similarity between the model and the prototype—The displacement at a particular depth has to be constant. In other words, the horizontal cross section must remain horizontal;
- Reduction of the wave reflections on the sidewalls;
- Propagation of the shaking to the soil layer. This can be accomplished by the use of a rough base;
- Water tightness for saturated soil tests.

4. New Laminar Shear Box at L.E.D.A.

Based on the large flexible laminar shear box developed by Ueng et al. [38], a new laminar shear box has been designed at the Laboratory of Earthquake engineering and

Dynamic Analysis (L.E.D.A.) of “Kore” University, Enna (Sicily, Italy), for 1g shaking table tests.

The most important facility of the laboratory is an array of two identical 6-DOF 4.0 m × 4.0 m shaking tables. It is possible to use the tables both separately and simultaneously in order to simulate the effects of earthquakes [62].

The 2D laminar box has been developed to monitor liquefaction under two dimensional shaking on a shaking table at L.E.D.A. Figure 15 shows the external and internal views of L.E.D.A. building. Figures 16 and 17 report some views of the shaking tables system, while the features for the configuration of single table are summarized in Table 2. For increasing the flexibility of the box wall, a laminar system has been applied.



(a)



(b)

Figure 15. Laboratory of Earthquake Engineering and Dynamic Analysis (L.E.D.A.) of “Kore” University of Enna (Sicily, Italy): (a) external view; (b) internal view (From [62]).

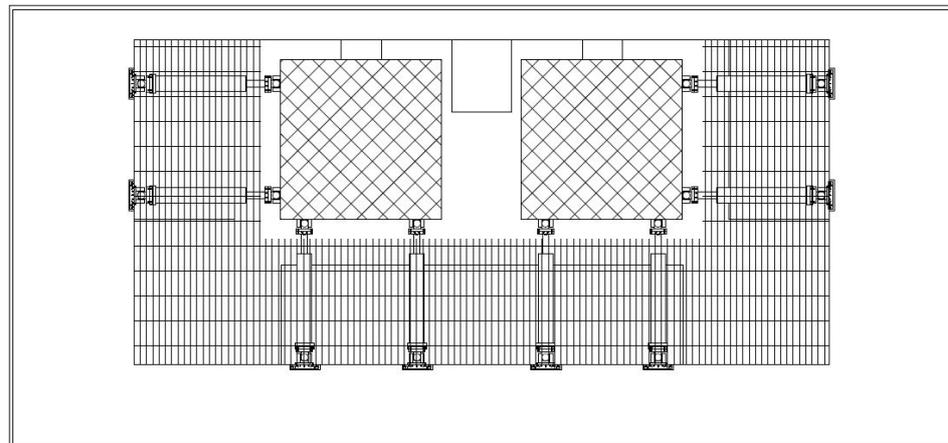


Figure 16. Plan view of the shaking tables system (From [62]).



Figure 17. Photographic view of the shaking tables system (From [62]).

Table 2. Features of LEDA shaking tables (From [62]).

Feature	Single Table
Dimensions [m]	4.0 × 4.0
DOF	6
Payload [t]	60
Max Frequency [Hz]	60
Stroke (horizontal axes) [mm]	±400
Stroke (vertical axis) [mm]	±250
Velocity (horizontal axes) [mm/s]	±2200
Velocity (vertical axis) [mm/s]	±1500
Acceleration (horizontal axes) [g]	±1.50
Acceleration (vert. axis) [g]	±1.00

The laminar box is rectangular in cross section and consists of 16 layers. Each layer is composed of two frames: An inner frame and an outer frame. The inner frame has an internal dimension of 2570 mm by 2310 mm, while the outer frame has an internal dimension of 2744 mm by 2770 mm. Each frame is made from hollow aluminium profiles with (30 × 80) mm² section and 2 mm thickness. The frames provide the lateral confinement

of the soil in order to reproduce the k_0 conditions. Indeed, aluminium is chosen for its strength to provide unyielding boundaries and for its light to reduce the inertial effect of the frame on the soil during shaking [63]. The inertia effect induced by the mass of the layers can lead to damping. Due to the inertia effect, the measured acceleration in the model is less than the real value. Considering the box filled of saturated sand, the correction factor (Equation (1)) is equal to 0.998. The isometric view of the inner and outer frames is shown in Figure 18.

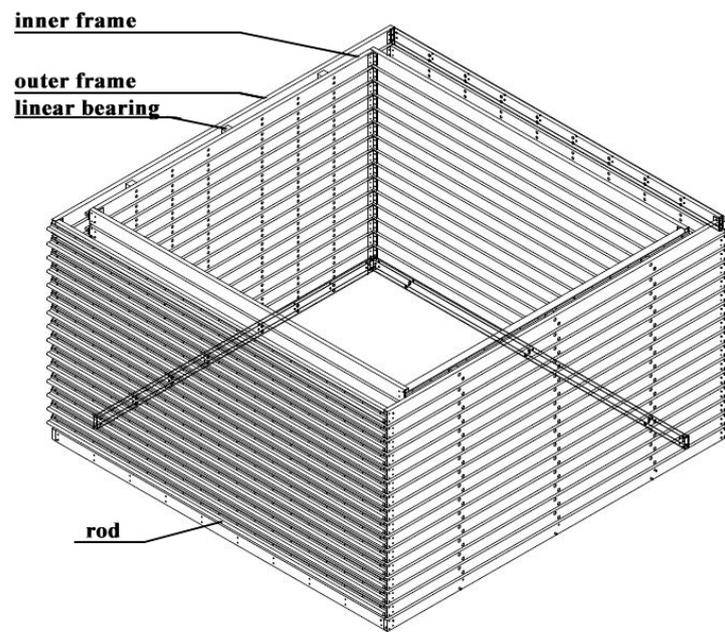


Figure 18. Isometric view of the inner and outer frames.

Each internal frame is supported independently by means of rods on a series of linear bearings connected to the external frame, while each external frame is supported independently by means of rods on a series of linear bearings connected to the surrounding rigid steel walls. The isometric view of the rigid steel walls is shown in Figure 19.

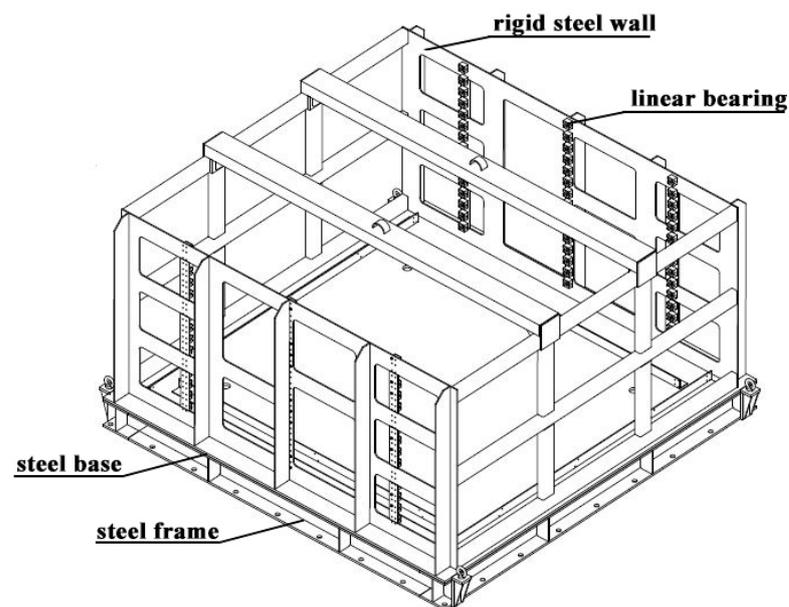


Figure 19. Isometric view of the rigid steel walls.

Linear bearings allow a maximum displacement of ± 150 mm in the two horizontal directions with almost negligible friction. Thanks to this arrangement, the external frames can move in the x direction and, at the same time, the internal frames can move in the y direction. This design has several advantages: the weight of each frame is transferred to the surrounding rigid steel walls; the effects of inertia and friction do not accumulate along the depth; each frame can move independently without torsion; the horizontal cross section remains horizontal (strain similarity).

Between the layers, there is a 20 mm gap making the total height 1600 mm. The lowest layer is fixed on a steel base of dimensions 3274 mm \times 3276 mm \times 20 mm. To reinforce the base, a steel frame is installed between the base and the shaking table. A drainage system is added on a steel base. It consists of water tubes and four valves. The plan view of the steel frame is shown in Figure 20.

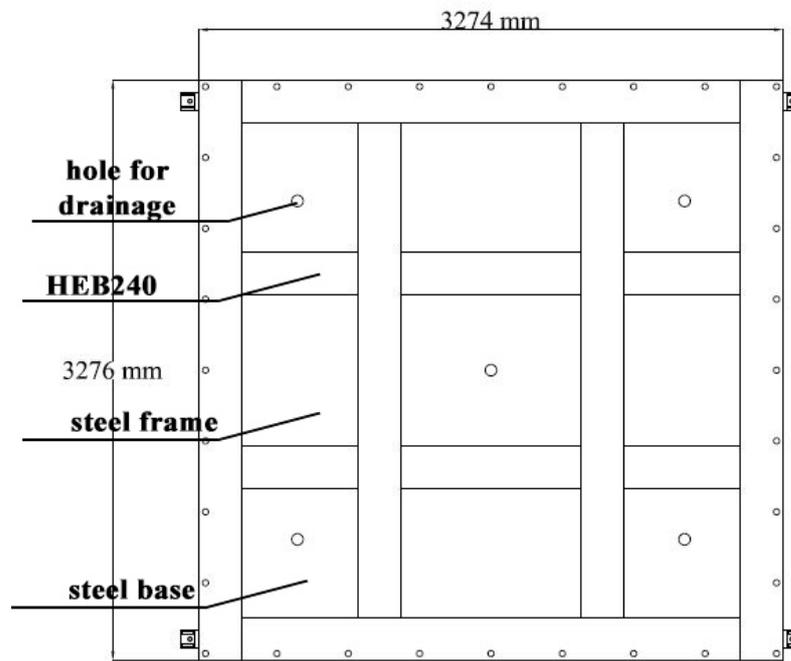


Figure 20. Plan view of the steel frame.

During shaking, to improve the shear stress transition from the steel base to the soil, a thin layer of gravels is placed on the base. Moreover, a 2 mm thick rubber membrane with high elasticity is installed inside the box to provide water tightness and protect the external mechanism from soil penetration. The main components of the laminar shear box are reported in Table 3.

Table 3. Components of the laminar shear box.

Component	Property	Value
Inner frame	Mass	12.07 kg
	Internal Dimensions	(2570 \times 2310) mm ²
	Number	16
	Height	80 mm
Outer frame	Mass	12.53 kg
	Internal Dimensions	(2744 \times 2770) mm ²
	Number	16
	Height	80 mm
Rod (inner frame)	Length	2370 mm
	Diameter	19 mm
	Number	30

Table 3. *Cont.*

Component	Property	Value
Rod (outer frame)	Length	2804 mm
	Diameter	19 mm
	Number	30
Linear bearing	Number	180
Gap between frames	Dimension	20 mm
Steel base	Mass	1682.89 kg
	Dimensions	(3274 × 3276) mm ²
	Height	20 mm
Steel walls	Total mass	592.94 kg
Steel frame	Total mass	1359.83 kg
Total mass of the laminar box		4033.27 kg

The plan and profile views of the laminar box are shown in Figures 21 and 22, respectively.

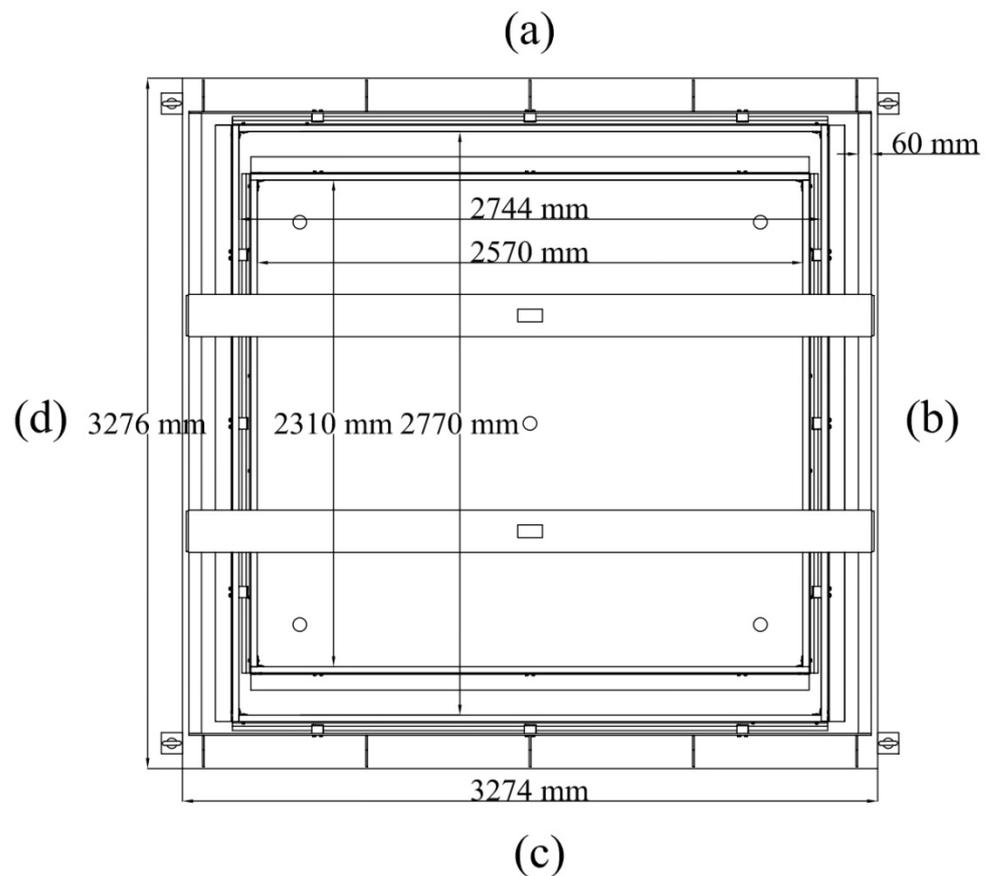


Figure 21. Plan view of the laminar shear box: (a) back view; (b) right view; (c) front view; (d) left view.

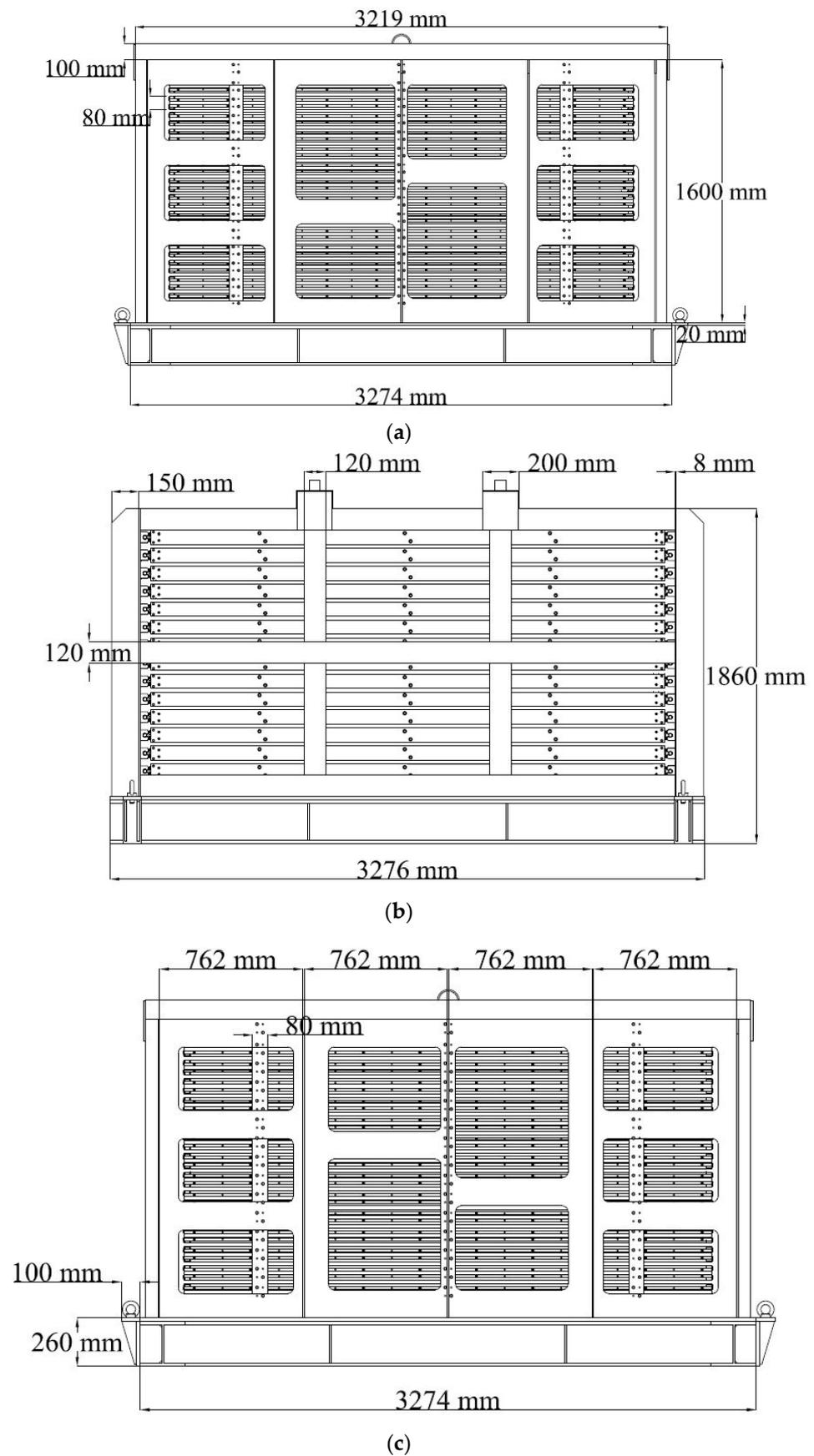


Figure 22. Cont.

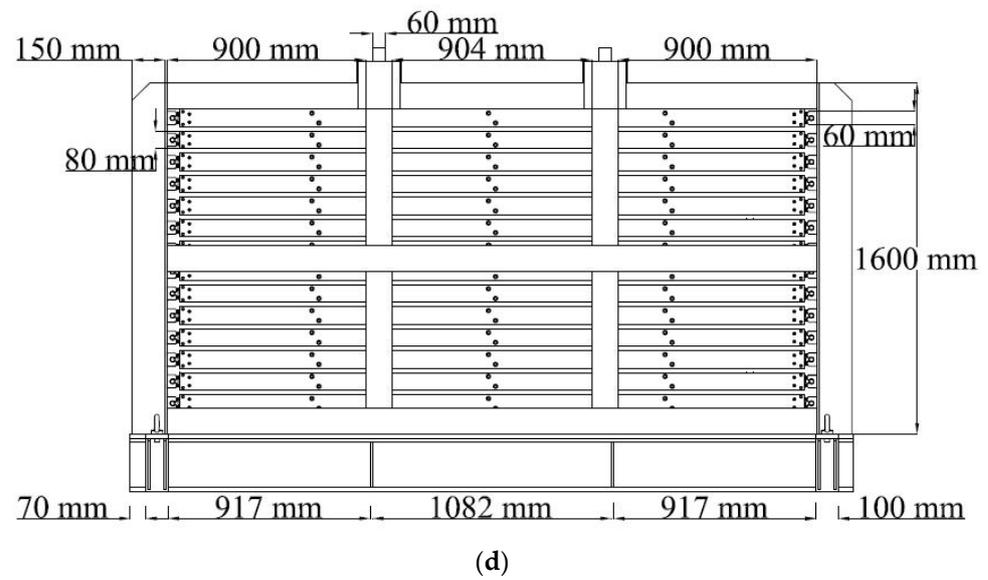


Figure 22. Profile views of the laminar shear box: (a) back view; (b) right view; (c) front view; (d) left view.

The isometric and 3D views are illustrated in Figure 23. The built laminar shear box is shown in Figure 24.

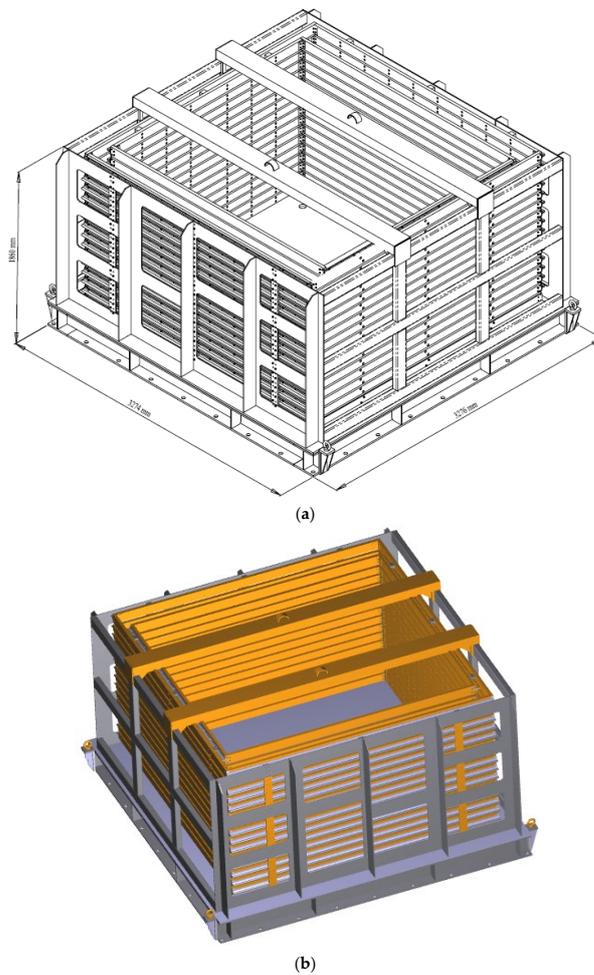


Figure 23. (a) The isometric and (b) 3D views of the laminar shear box.



(a)



(b)

Figure 24. Laminar shear box at the Laboratory of Earthquake engineering and Dynamic Analysis (L.E.D.A.).

5. Conclusions

Liquefaction damage during earthquakes can be prevented if the performance of liquefiable soils and its interaction with structures can be accurately predicted [64]. Therefore, for a better understanding and to provide the data for verification of the analyses and modelling of soil responses under earthquake loading, a new large-scale shear box on a shaking table has been developed.

In this paper, the design process of the laminar box system at L.E.D.A. of “Kore” University (Sicily, Italy) has been presented. It has been described along with its various components, properties, and design advantages. The box is designed for biaxial shaking on a 6-DOF large shaking table, that is rare in the world. In fact, most experimental studies in literature were for one-dimensional shaking. Moreover, each layer is composed of two frames: an outer frame that can move in the x direction and an inner frame that can move in the y direction by imposing constraints on movements. Thanks to this arrangement, torsion, that occurs during biaxial shaking in laminar containers composed of one frame per layer, is not allowed. Furthermore, ball bearings or roller bearings could be placed between the layers. However, in this design, the effects of inertia and friction accumulate along the depth. This is prevented in the laminar box under consideration. Indeed, each internal frame is supported independently by means of rods on a series of linear bearings connected to the external frame, while each external frame is supported independently by means of rods on a series of linear bearings connected to the surrounding rigid steel walls. Therefore, the weight of each layer is transferred externally.

The new laminar shear box will be placed on a 4.0 m × 4.0 m shaking table in order to study the dynamic soil-structure interaction (DSSI) on liquefiable soils. Seismic-induced soil liquefaction is a major cause of damage and loss of human lives during earthquakes. Thus, the evaluation of the susceptibility of a site to liquefaction and the assessment of its effect on structures are important topics in seismic geotechnical engineering. Several studies have been carried out in the last decades to assess soil liquefaction. However, it is still a challenging task. The main issues are the uncertainties associated to soil behaviour and the large number of variables related to the interaction between soil and water.

The numerical simulations and the use of constitutive models are a valuable help in these complex problems. However, liquefaction is difficult to achieve in the constitutive models and requires a large number of input parameters. Instead, shaking table tests are favourable thanks to the ability to provide realistic and economic results in terms of excess pore-pressure generation.

The new laminar box has been designed and assembled at L.E.D.A. The next research steps consist in conducting experimental studies by the laminar shear box and to analyse the gap areas of the numerical modelling to be incorporated in the future simulations to exactly capture the liquefaction phenomenon. Shaking table tests will be carried out on saturated sandy soil in the new laminar box. Then, the measured data inside the soil will be compared with those obtained by means of numerical analysis in order to validate advanced numerical models.

Author Contributions: Data curation, F.C.; Funding acquisition, F.C.; Investigation, V.L.; Methodology, S.G. and M.S.V.S.; Supervision, V.L.; Writing—original draft, S.G. and M.S.V.S.; Writing—review & editing, S.G. and M.S.V.S. All authors have read and agreed to the published version of the manuscript.

Funding: This research work was funded by the MIUR (Ministry of Education, Universities and Research [Italy]) through the project entitled “eWAS: an early WARNING System for cultural-heritage” (Project code: ARS01_00926/CUP J66C18000390005).

Acknowledgments: The authors acknowledge the financial support received from the MIUR (Ministry of Education, Universities and Research [Italy]) through the project entitled “eWAS: an early WARNING System for cultural-heritage” (Project code: ARS01_00926/CUP J66C18000390005), financed with the PNR 2015-2020 (National Research Program). The authors authorize the MIUR to reproduce and distribute reprints for Governmental purposes, notwithstanding any copyright notations thereon. Any opinions, findings, and conclusions or recommendations expressed in this material are those of the authors and do not necessarily reflect the views of the MIUR.

Conflicts of Interest: The authors declare no conflict of interest.

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