Article

Radial Kick in High-Efficiency Output Structures

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Abstract: We have developed an analytical approach that predicts radial oscillation near the aperture of a pillbox cavity. In addition, it provides natural criteria for the design of a tapered guiding magnetic field in the output section of a relativistic klystron amplifier, as well as that of a travelling wave tube, in a method that is self-consistent with the dynamics of the electrons.

1. Introduction

Periodic structures play an important role in the interactions of electrons with waves, since they support harmonics of phase-velocity that are smaller than c, and with an adequate design, this velocity can be set to be equal to the average velocity of the electrons. In particular, in extraction structures, as the electrons interact with the wave and lose energy, they slip out of phase and consequently, the interaction is degraded. In order to avoid this situation, the phase velocity of the wave has to be adjusted, and the geometry change that is associated with this process should be designed for minimum reflections, otherwise the system oscillates. In a similar way, in photo-injectors, electron bunches are accelerated from zero velocity to virtually the speed of light in a relatively short distance (typically 2.5–5.5 periods) and therefore, the design needs to account for the accelerating bunch, such that the latter experiences the maximum radio frequency (rf) electric field.

At a given frequency and in single-mode operation, the electromagnetic wave is characterized by a single wave-number k, and quantities such as phase velocity, group velocity, and interaction impedance are well-defined. In principle, if the structure is no longer periodic, the field cannot be represented by a single wave-number, except when the variations are adiabatic, in which case, these characteristics are assumed to be determined by the geometry of the local cell. Adiabatic perturbations in the geometry may improve the efficiency from the level of few percent in uniform structures, to a level of 30%. However, one cannot expect to achieve 60–80% efficiency by moderate variation of the structure, bearing in mind that in contrast to accelerators where these changes occur over many wavelengths, in traveling-wave extraction structures, these changes should occur within a few wavelengths.

An abrupt change of geometry dictates a wide spatial spectrum, in which case the formulation of the interaction in terms of a single wave with a varying amplitude and phase is inadequate. In fact, the electromagnetic field cannot be expressed in a simple (analytic) form if substantial geometric variations occur from one cell to another. To be more specific: in a uniform or weakly tapered disk-loaded waveguide, as an example, the beam–wave interaction is analyzed, assuming that the general functional form of the electromagnetic wave is known; e.g., $A(z)\cos[\omega t - kz - \phi(z)]$, and the beam affects the amplitude $A(z)$ and the phase, $\phi(z)$. Furthermore, it is assumed that the variation due to the interaction is small, being on the scale of one wavelength of radiation. Both assumptions are not acceptable in the case of a structure that is designed for high-efficiency interaction. To emphasize

this difficulty even further, we recall that a non-adiabatic local perturbation of geometry affects global electromagnetic characteristics; this is to say that a change in a given cell affects the interaction impedance or the group velocity several cells before and after the point where the geometry was altered.

To overcome these difficulties, an analytical technique has been developed in order to design and analyze quasi-periodic metallic structures. The method relies on a model consisting of a cylindrical waveguide, to which a number of pill-box cavities and radial arms are attached. In principle, the number of cavities and arms is arbitrary. The boundary condition problem is formulated in terms of the amplitudes of the electromagnetic field in the cavities. The elements of the matrix, which relates these amplitudes with the source term, are analytic functions, and no a-priori knowledge of the functional behavior of the electromagnetic field is necessary.

The study regarding travelling wave tube (TWT) output structures was triggered by research conducted at Cornell University by Nation et al. [1–40] during the 1970s, 1980s, and 1990s; the references are listed chronologically, and thus, in order of development. Order power levels in excess of 200 MW were generated at the X-band in a 50 MHz bandwidth. These power levels were accompanied by gradients that are larger than 200 MV/m, and no rf breakdown was observed experimentally—the pulse duration was less than 100 ns. However, for further increases in the power levels, it was necessary to increase the volume of the last two or three cells, in order to minimize the electric field on the metallic surface. The system then becomes quasi-periodic. To envision the process in a clearer way, let us assume that 80% efficiency is required from our source. If the initial beam is not highly relativistic, which is the case in most systems, such an efficiency implies a dramatic change in the geometry of the structure over a short distance. Specifically, for a 500 keV beam, the initial velocity is $v_0 \sim 0.86c$, and an 80% efficiency would imply a phase velocity of $0.55c$ at the output. This corresponds to a 36% change in the phase velocity, and a similar change will be required in the geometry, which is by no means an adiabatic change when it occurs in one period of the wave.

Relying on our experience, there are several difficulties that are associated with an extraction section based on a quasi-periodic traveling-wave structure: (i) reduction of the reflections primarily at the output end of the structure, in order to maintain a clean spectrum and to avoid oscillations; (ii) Tapering of the output section to avoid breakdown; (iii) Compensation for the decrease in the velocity of the electrons when maintaining a resonance condition; (iv) Adaptation of the guiding magnetic field to the variation in current density of the electron beam; (v) Accounting for the transverse oscillation of the electrons, in order to circumvent them from impinging upon the metallic structure. While the first three items were investigated in Chapter 6 of Reference [41], it is our goal in this study to consider the last two analytically—see also [28,31,32]. They were triggered by a new relativistic klystron amplifier (RKA) design by the first author (HH). The S-band device is driven by an 850 keV electron annular-beam (8 kA, radius 2.8 cm, and thickness 3 mm). The guiding magnetic field has a typical intensity of 1 T. In Figure 1, the top frame shows (not up to scale) the schematic of the configuration, and subsequently, we will need the cavity parameters: the drift tube radius is 3 cm, the gap width is 2.1 cm; the electric field in the gap of the output cavity is of the order of 20 MV/m. Originally, the RKA was developed over more than two decades by Moshe Friedman at the Naval Research Laboratory [42–82], and renewed interest was triggered by the possibility of designing a high-efficiency device; note that the references are presented in chronological order.
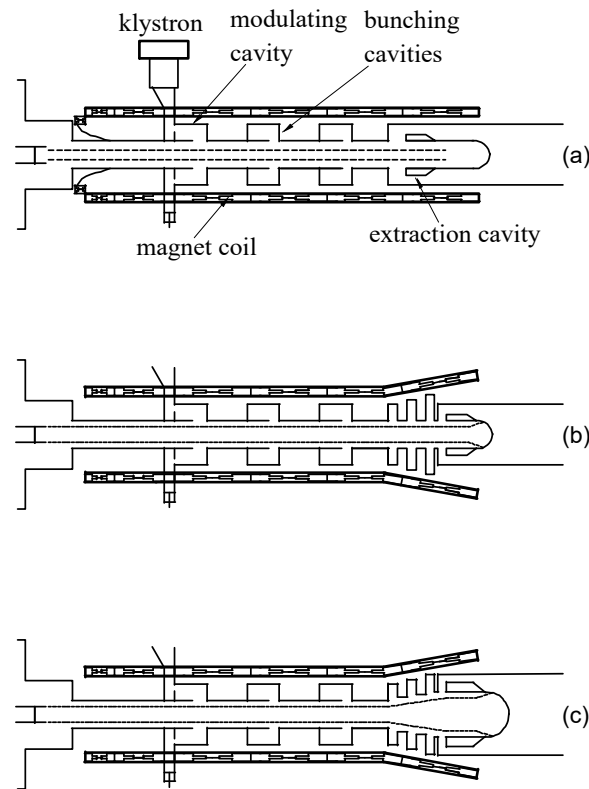
Figure 1. (**a**) Schematic description (not up to scale) of the relativistic klystron amplifier designed by one of us (HH). A single-output cavity is employed. (**b**) The radii of the drift tube and beam are kept uniform; the intensity of the guiding field is tapered. (**c**) Both the beam, the cavity, and the guiding field are varied.

2. Formulation of the Model

Our goal is to examine the radial motion of the electrons in the vicinity of a cavity, and in the presence of a guiding magnetic field $\left(B_0 \right)$—the geometric parameters of the cavity and the beam are revealed in Figure 2, which illustrates the output from CHIPIC [83].
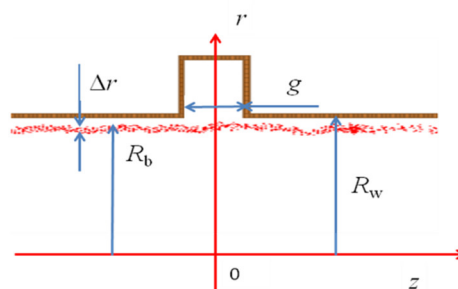

Figure 2. Schematic description (not up to scale) of a pillbox cavity attached to a waveguide. R_w is the radius of the waveguide; R_b is the annular-beam average radius, and Δ_r represents its thickness; g is the gap. The system is assumed to be azimuthally symmetric. Not shown is the guiding magnetic field of intensity B_0 along the z-direction.

In the gap of the cavity, we assume the existence of a uniform in space, steady-state $\left(\exp j\omega t \right)$ in time-longitudinal electric fields of complex amplitude $\bar{E}_0$; thus

$E_z\left(r = R_w, |z| < \mathrm{g}/2, t\right) = \mathrm{Re}\left[\bar{E}_0 \exp\left(j\omega t\right)\right]$. Explicitly, in the cylindrical waveguide $\left(r \le R_w\right)$, the magnetic vector potential is:

$$A_z\left(r, z, \omega\right) = \int_{-\infty}^{\infty} dk A\left(k\right) I_0\left(\Gamma r\right) \exp\left(-jkz\right) \tag{1}$$

wherein $\Gamma^2 = k^2 - \omega^2/c^2$, $I_0\left(u\right)$ is the zero-order-modified Bessel function of the first kind, and the amplitude $A\left(k\right)$ is set by the field in the gap of the cavity $\left(r = R_w\right)$:

$$E_z\left(z\right) = \int_{-\infty}^{\infty} dk\, \frac{c^2 \Gamma^2}{-j\omega} A\left(k\right) I_0\left(\Gamma R_w\right) \exp\left(-jkz\right) = \begin{cases} \bar{E}_0, & |z| < g/2 \\ 0, & \text{otherwise} \end{cases} \tag{2}$$

or explicitly:

$$A\left(k, \omega\right) = \bar{E}_0 \frac{-j\omega}{c^2 \Gamma^2} \frac{1}{I_0\left(\Gamma R_w\right)} \frac{1}{2\pi} \int_{-g/2}^{g/2} dz \exp\left(jkz\right) \tag{3}$$

Thus, the field components in the entire volume $\left(r \le R_w, |z| < \infty\right)$ of the waveguide are given by:

$$\begin{bmatrix} E_z \\ E_r \\ H_\phi \end{bmatrix} = \mathrm{Re}\left\{ \bar{E}_0 \exp\left(j\omega t\right) \int_{-g/2}^{g/2} dz' \frac{1}{2\pi} \int_{-\infty}^{\infty} dk \begin{bmatrix} I_0\left(\Gamma r\right) \\ \left(jk/\Gamma\right) I_1\left(\Gamma r\right) \\ \left(j\omega/c\Gamma\eta_0\right) I_1\left(\Gamma r\right) \end{bmatrix} \frac{\exp\left[-jk\left(z - z'\right)\right]}{I_0\left(\Gamma R_w\right)} \right\} \tag{4}$$

For completeness in the pillbox cavity $\left(R_w < r < R_{\text{ext}}\right)$, the dominant field components are:

$$E_z\left(r\right) = \bar{E}_0 \left[J_0\left(\frac{\omega}{c} r\right) Y_0\left(\frac{\omega}{c} R_{\text{ext}}\right) - Y_0\left(\frac{\omega}{c} r\right) J_0\left(\frac{\omega}{c} R_{\text{ext}}\right) \right]$$
$$H_\phi\left(r\right) = \frac{j}{\eta_0} \bar{E}_0 \left[J_1\left(\frac{\omega}{c} r\right) Y_0\left(\frac{\omega}{c} R_{\text{ext}}\right) - Y_1\left(\frac{\omega}{c} r\right) J_0\left(\frac{\omega}{c} R_{\text{ext}}\right) \right] \tag{5}$$

with $\eta_0 = \sqrt{\mu_0/\varepsilon_0}$ representing the vacuum wave impedance, R_{ext} is the external wall of the pillbox cavity, and $J_\nu\left(u\right), Y_\nu\left(u\right), \nu = 0,1$ are the νth-order Bessel functions of the first and second kind, correspondingly

Now that we have determined the rf field, we focus on the dc field, ignoring the metallic wall. Assuming a thin annular-beam carrying a current I with a velocity $\mathrm{v}_z = c\beta$, the effective electric field $\left(E_r - \mathrm{v}_z B_\phi\right)$ at the beam location is:

$$E_r^{(SC)}\left(r \simeq R_b\right) \simeq -\frac{\eta_0 I}{\beta\gamma^2} \frac{1}{2\pi R_b} \tag{6}$$

and $\gamma = 1/\sqrt{1 - \beta^2}$ —note that these are average values. Here, we ignored the effects of the metallic wall on the static field components. With the dc and the rf components established, the radial equation of motion, ignoring the energy exchange due to the longitudinal oscillation, reads:

$$\frac{\mathrm{d}}{\mathrm{d}t} \mathrm{v}_r - \frac{1}{r} \mathrm{v}_\phi^2 = -\frac{e}{m} \frac{1}{\gamma} \left(E_r^{(RF)} + E_r^{(SC)} + v_\phi B_0 \right). \tag{7}$$

wherein e and m are the charge and rest mass of the electron, and:

$$E_{r,i}^{(RF)}(t) = \left[E_r - v_z B_\phi\right]_{\substack{r=R_b \\ z=z_i+c\beta t}}$$

$$= \mathrm{Re}\left\{\bar{E}_0 \exp(j\omega t) \int\limits_{-g/2}^{g/2} dz' \frac{1}{2\pi} \int\limits_{-\infty}^{\infty} dk \left[\frac{jk}{\Gamma} - \beta \frac{j\omega}{c\Gamma}\right] I_1(\Gamma r) \frac{\exp\left[-jk(z-z')\right]}{I_0(\Gamma R_w)}\right\}_{\substack{r=R_b \\ z=z_i+c\beta t}} \quad (8)$$

Due to the azimuthal symmetry of the problem, the canonical angular momentum is a constant of motion. Further, since the guiding magnetic field is uniform, the azimuthal component of the static magnetic vector potential is $A_\phi = rB_0 / 2$; $\Omega_c = eB_0 / m$ will represent in what follows, the non-relativistic cyclotron frequency. The conservation of the canonical angular momentum implies $rp_\phi = r\left(m\gamma v_\phi - eA_\phi\right) = rm\left(\gamma v_\phi - \Omega_c r / 2\right) = \mathrm{const.}$, thus assuming that the *i*th electron has an initially zero azimuthal velocity:

$$v_{\phi,i} = \frac{1}{2r_i\gamma_i} \Omega_c \left(r_i^2 - r_{i,0}^2\right) \quad (9)$$

and denoting by $h(u)$ the Heaviside step function, we get:

$$\frac{d^2 r_i}{dt^2} - \frac{\Omega_c^2}{4r_i^3\gamma_i^2}\left(r_i^2 - r_{i,0}^2\right)^2 = -\frac{e}{m}\frac{1}{\gamma_i}E_{r,i}^{(RF)} + \frac{e}{m}\frac{\eta_0 I}{\beta_i\gamma_i^3}\frac{h(r_i - R_b)}{2\pi r_i} - \frac{\Omega_c^2}{2r_i\gamma_i^2}\left(r_i^2 - r_{i,0}^2\right) \quad (10)$$

It should be emphasized that the effect of the image-charge, due to the wall presence, was tacitly neglected, since it is well-known that it tends to reduce the (effective) plasma frequency and in the framework of this analytic study, we consider only the main processes involved.

Next, we assess the equilibrium $\left(r_{eq} \simeq R_b\right)$ in the absence of the rf, and we assume that the oscillation is small relative to the beam's radius $r_i \simeq R_b + \delta r_i$, $r_{i,0} \simeq R_b$. Further defining the current and the plasma frequency $I = enc\beta\left(2\pi R_b\right)\Delta_r$, $\Omega_p^2 = e^2 n / m\varepsilon_0$, the radial equation of motion for the *i*th electron is:

$$\left(\gamma_i \frac{d^2}{dt^2} + \frac{\Omega_c^2}{\gamma_i} - \frac{\Omega_p^2}{\gamma_i^2}\right)\delta r_i \simeq -\frac{e}{m}E_{r,i}^{(RF)} \quad (11)$$

Note that the dc space charge force (expressed in terms of the plasma frequency) is taken for the worst case scenario, namely all electrons are concentrated in an extremely thin layer, and the radial (image-charge) force between this layer and the waveguide's wall is neglected. This can be readily corrected by replacing the plasma frequency with the effective plasma frequency, which accounts for the plasma frequency reduction, due to the ground metallic wall.

3. Effective Radial Force

Our goal in this section is to simplify the expression for the radial force $F_r(t) = -eE_{r,i}^{(RF)}$, and for this purpose, we employ the Cauchy residue theorem for the evaluation of the integral on k in Equation (8); thus:

$$G(z,z') \equiv \frac{1}{2\pi} \int_{-\infty}^{\infty} dk \frac{I_1\left[R_w\sqrt{k^2 - (\omega/c)^2}\right]\exp\left[-jk(z-z')\right]}{R_w\sqrt{k^2 - (\omega/c)^2}\, I_0\left[R_w\sqrt{k^2 - (\omega/c)^2}\right]} = \frac{1}{R_w^2}\sum_{s=1}^{\infty} \frac{\exp\left[-\Gamma_s|z-z'|\right]}{\Gamma_s} \quad (12)$$

wherein p_s are the zeroes of the Bessel function of the first kind, $J_0(p_s) = 0$, and $\Gamma_s \equiv \sqrt{(p_s/R_w)^2 - (\omega/c)^2}$. With this definition, the radial force consists of an infinite manifold of evanescent waves, thus keeping in mind that from $\overline{E}_0 = E_0\exp(j\psi)$, we get:

$$\frac{F_r^{(RF)}}{-eE_0} = \frac{g}{R_w}\sum_{s=1}^{\infty} G_s(z)J_1\left(p_s\frac{r}{R_w}\right)J_1^{-1}(p_s)\left[\cos(\omega t + \psi) + \beta\frac{\omega}{c\Gamma_s}\sin(\omega t + \psi)\right] \quad (13)$$

and here, $G_s(z) \equiv \frac{1}{g}\int_{-g/2}^{g/2} dz'\exp\left[-\Gamma_s|z-z'|\right]$. At this stage, we consider the transverse kick experienced by the electron. In general, momentarily ignoring all of the force components except rf, the normalized transverse kick associated with the radial rfforce is given by:

$$mc\frac{d\gamma\beta_r}{dt} = F_r(R_b, z = c\beta t, t) \Rightarrow \Delta_{\gamma\beta_r} \equiv \frac{1}{mc}\int_{-\infty}^{\infty} dt F_r(R_b, z = c\beta t, t) \quad (14)$$

or explicitly, in the framework of our model:

$$\frac{\Delta_{\gamma\beta_r}}{-eE_0 g/mc^2} = \frac{1}{g}\int_{-\infty}^{\infty} dtc\frac{g}{R_w}\sum_{s=1}^{\infty} G_s(c\beta t)J_1\left(p_s\frac{R_b}{R_w}\right)J_1^{-1}(p_s)\left[\cos(\omega t + \psi) + \beta\frac{\omega}{c\Gamma_s}\sin(\omega t + \psi)\right] \quad (15)$$

At $r = R_b$ the normalized transverse kick within an excellent approximation and for the specified parameters, is given by $1.293\cos(\psi - \pi/6)$. Now, we replace the exact rf force with the kick multiplied by the Delta function, such that the momentum transferred in the process is preserved, but its profile may differ quite significantly. Explicitly, the momentum transfer is given by:

$$\frac{d\gamma\beta_r}{dt} = \Delta_{\gamma\beta_r}\delta(t) \quad (16)$$

or in our particular case, for the specified set of geometric parameters:

$$\Delta_{\gamma\beta_r} = -1.293\frac{eE_0 g}{mc^2}\cos\left(\psi - \frac{\pi}{6}\right) \quad (17)$$

and thus, after reinstating the other force components, we get:

$$\left(\frac{d^2}{dt^2} + \frac{\Omega_c^2}{\gamma_i^2} - \frac{\Omega_p^2}{\gamma_i^3}\right)\delta r_i \simeq \Delta_{\gamma\beta_r}\frac{c}{\gamma_i}\delta(t) \quad (18)$$

This equation may be readily solved, keeping in mind that the Green's function of:

$$\left(\frac{d^2}{dt^2} + \Omega^2\right)G_0(t,t') = \delta(t-t') \quad (19)$$

is subject to the zero initial conditions: $G_0(t = t', t') = 0$, and $\left[dG_0(t,t')/dt\right]_{t=t'} = 0$ is given by:

$$G_o\left(t,t'\right) = \frac{1}{\Omega}\sin\left[\Omega\left(t-t'\right)\right]h\left(t-t'\right) \tag{20}$$

Thus:

$$\delta r_i\left(t\right) \simeq \Delta_{\gamma\beta_r} \frac{c}{\sqrt{\Omega_c^2 - \Omega_p^2\gamma_i^{-1}}}\sin\left(\sqrt{\Omega_c^2\gamma_i^{-2} - \Omega_p^2\gamma_i^{-3}}\,t\right)h\left(t\right) \tag{21}$$

This is the main analytical result of this study.

4. Discussion

Several features are evident from the present formulation:

1. For beam stability, it is required that the relativistic cyclotron frequency is significantly larger than the relativistic plasma frequency $\Omega_c^2\gamma^{-2} \geq \Omega_p^2\gamma^{-3}$. In all of the expressions so far, we considered the average beam density, but we need to keep in mind that high-efficiency energy conversion is facilitated by a highly bunched beam; thus local density may exceed the averaged value by a factor of $\alpha = 10$ or even higher. Consequently, it will be more realistic to adopt a more stringent constraint on the magnetic field $\Omega_c^2 \geq \alpha\Omega_p^2\gamma^{-1}$.

2. The radial transverse kick, $\Delta_{\gamma\beta_r}$, is proportional to the amplitude of the radial oscillation.

3. In case of a quasi-periodic structure whereby electrons lose a significant fraction of their energy $\gamma_i\left(z\right)$, the magnetic field is tapered $\Omega_c\left(z\right)$, the bunch density varies $\Omega_p\left(z\right)$, and assuming that there are no reflected electrons, then on the first order, we may assume that the radial oscillation as a function of the location is:

$$\begin{aligned}\delta r_i\left(z\right) &\simeq \frac{c\Delta_{\gamma\beta_r}h\left(z\right)}{\sqrt{\Omega_c^2\left(z\right) - \Omega_p^2\left(z\right)\gamma_i^{-1}\left(z\right)}}\sin\left(\frac{1}{c}\int_0^z dz'\sqrt{\frac{\Omega_c^2\left(z'\right) - \Omega_p^2\left(z'\right)\gamma_i^{-1}\left(z'\right)}{\gamma_i^2\left(z'\right) - 1}}\right)\\ &\simeq \frac{c\Delta_{\gamma\beta_r}h\left(z\right)}{\Omega_c\left(z\right)}\sin\left(\int_0^z dz'\frac{\Omega_c\left(z'\right)}{c\sqrt{\gamma_i^2\left(z'\right) - 1}}\right)\end{aligned} \tag{22}$$

4. According to the last result, there are several possibilities to taper the structure. Two are the most plausible: (i) Keeping the radius of the waveguide constant, but varying the guiding magnetic field and the external radius of the cavities (see in Figure 1b), such that the phase of the radial oscillation is preserved:

$$\frac{\Omega_c\left(z\right)}{c\sqrt{\left\langle\gamma_i^2\left(z\right)\right\rangle - 1}} = \text{const.} \tag{23}$$

(ii) Varying the waveguide radius, and thus the volume of the constraint on the guiding field may be weakened:

$$\frac{\Omega_c^2\left(z\right) - \Omega_p^2\left(z\right)\left\langle\gamma_i\left(z\right)\right\rangle^{-1}}{\left\langle\gamma_i^2\left(z\right)\right\rangle - 1} = \text{const.} \tag{24}$$

See the bottom frame in Figure 1. However, the tapering in the latter case may be accompanied by a coupling to high-order modes (hybrid modes), which may lead to beam break-up.

In order to obtain a flavor regarding the maximum radial displacement, $\delta r_{\max} \simeq 1.293\left(eE_0 g / mc^2\right)\left(c / \Omega_c\right) \simeq 1.7[\text{mm}] / B_0\left[T\right]$, that the electron beam is experiencing as it traverses the gap, we illustrate the following results of several particle in cell (PIC) simulations. The

left frame of Figure 3 shows the configuration-space, and the latter reveals the radial oscillation very vividly. In the right frame, we show the beam transport over the cavity gap. The red curve shows the upstream current. Blue, green, and magenta represent the downstream currents for $B_0 = 0.6, 0.7, 1.0 T$. For the weaker magnetic field, the radial kick is larger; as a result, more electrons are intercepted by the structure, and thus, the transported current is lower.
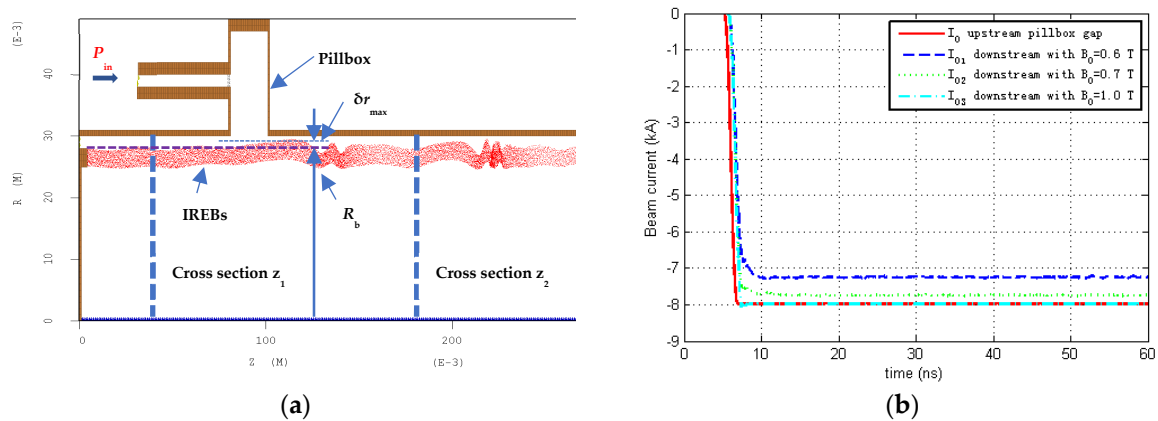

(**a**)   (**b**)

Figure 3. Left frame: PIC simulation—see [83] for details—revealing the transverse kick exerted on the electrons by the rf field in the cavity. Right frame: Beam transport over the cavity gap. The red curve shows the upstream current. Blue, green, and magenta represent the downstream currents for $B_0 = 0.6, 0.7, 1.0 T$. For the weaker magnetic field the radial kick is larger, and as a result, more electrons are intercepted by the structure, and thus the transported current is lower.

In conclusion, we have developed an analytical approach that on one hand, may predict the radial oscillation near the aperture of a pillbox cavity, and on the other hand, it provides us with the natural criteria for the design of the tapered magnetic field in the output sections of a relativistic klystron amplifier, as well as the travelling wave tube.

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