

Article

The Evaluation of Non-Destructive Tests for the Strength and Physical Properties of Granite, Marble, and Sandstone: A Case Study from North Pakistan

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Abstract: Nondestructive tests, commonly employed in rock mechanics, estimate mechanical parameters without affecting the rocks in situ properties. This study evaluates non-destructive tests (ultrasonic pulse velocity and Schmidt hammer) for forecasting the strength and physical properties of commonly used rocks. Weathering grades and moisture content are provided as variables that produce variances in both non-destructive tests. The coefficient of determination (R^2) and subsequent empirical equations for the best-fit trend line are calculated using a simple regression method. The ultrasonic pulse velocity is found to be more efficient in estimating most of the physical properties (specific gravity, porosity, water absorption, and dry density) of granite, marble, and sandstone, with high correlation coefficients. Whereas the Schmidt hammer is found to be more reproducible in determining the strength (compressive and tensile) of granite, marble, and sandstone. The student's *t*-test proved the sensitivity and correctness of the acquired equations from the suggested correlations, and agreement was established between measured and estimated plots of strength and physical properties. Although the student's *t*-test confirms that the performance of all empirical models established in this study are significant, any non-destructive test with a low R^2 value should be used with caution when estimating the studied properties.

Keywords: non-destructive testing; Schmidt hammer; ultrasonic pulse velocity; strength and physical properties

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1. Introduction

Destructive and non-destructive tests are used to measure the strength and physical characteristics of rocks, which are critical factors in engineering design [1–3]. Non-destructive testing (NDT) does not include any intrusion of the rock specimen for specimen preparation, while destructive testing (DT) does [4]. For physico-mechanical characteristics, direct destructive testing is expensive, time-consuming, and requires a significant understanding of specimen preparation and high-tech equipment. These drawbacks have been addressed by the scientific community through the introduction of inexpensive, fast, reliable, and indirect non-destructive techniques that require little or no sample preparation and only minimal operating expertise [2,5,6]. UPV (ultrasonic pulse velocity) and SH (Schmidt hammer) are two examples that may be utilized in the field or laboratory [7–10]. Table 1 shows a description of the abbreviations and acronyms used.

Table 1. List of abbreviations and acronyms used in this article.

Abbreviation	Explanation
NDTs	Non-destructive testings
DT	Destructive testing
NDTs-dry	Non-destructive testings in the dry state
UPVdry	Ultrasonic pulse velocity in the dry state
UPVsat	Ultrasonic pulse velocity in the saturated state
R _{dry} -value	Schmidt hammer rebound-value in the dry state
R _{sat} -value	Schmidt hammer rebound-value in the saturated state
UCS	Unconfined compressive strength
UTS	Unconfined tensile strength
SH	Schmidt hammer
PPAIP	Peshawar plain alkaline igneous province
AGC	Ambela granitic complex
MG	Malakand granite
UGA	Utla granite A
UGB	Utla granite B
NFA	Nowshera formation A
NFB	Nowshera formation B
MFA	Murree formation A
MFB	Murree formation B
MFC	Murree formation C
n	Porosity
WA	Water absorption
WG	Weathering grade

When determining an object's ultrasonic pulse velocity, P-waves of various pulse durations are sent, propagated, and received in the medium [11–16]. The sample length divided by the time it takes for the P-wave (primary wave measurement) to go through the rock sample gives the velocity. Whereas the spring-loaded mass and electronic or sliding pointer and plunger make up the Schmidt hammer. The rock rebound (R-value) is recorded when the hammer hits the rocks surface [17,18]. Rock texture (grain size and form), weathering grade, moisture content, density, porosity, anisotropy, confining pressure, and bedding planes all impact the UPV and R-value fluctuation. A positive correlation exists between the P-wave velocity and R-value and the strength and dry density, and the opposite is true for porosity and water absorption. Higher UPV and R-values are typically obtained in stronger materials, making them more desirable in engineering applications. Several studies have found a reasonable correlation between the strength and physical properties of various rocks and NTDs [19–22]. As density and moisture content rise, so do porosity and microfracture, and vice versa [7,23–25]. However, even when the weathering grade is high, this technique may have opposite results for rocks with water-filled pores; thus, it must be used with caution. According to Karaman and Kesimal [26] uniaxial compressive strength (UCS) and UPV have a non-linear connection. The UPV decreases with increasing fracture roughness and vice versa, according to statistical models constructed by Aşçı et al. [27]. Shear strength, indirect tensile strength, compressive strength, modulus of elasticity, Poisson's ratio, and density of rock specimens comprising coal-bearing strata were all studied by Khandelwal [28] using regression analysis to produce empirical equations. There was a substantial correlation and coefficient of determination in the developed equations. Regression analysis was used on 64 sedimentary rock samples to get the best-fit equation by Moradian and Behnia [29]. To estimate the specified parameter, the resulting equation was both accurate and usable. A similar approach has been used to estimate the unconfined compressive strength, Young's modulus, and dry density of

Schmidt hammers by comparing the R-values of the Schmidt hammer [18,30]. The efficiency of R-values in predicting the strength of different rock types has also been examined in several studies [30]. The equations that were generated could predict a wide range of mechanical characteristics. Based on statistical analyses, equations are also established between the physical and strength characteristics of rocks to estimate the abrasion wear resistance. The findings demonstrate that these equations can be used to predict the abrasion wear resistance of natural building stone [31–33].

Preliminary investigations on the geotechnical properties of North-Pakistani rocks concentrated on the relation between strength and petrographic features; however, their association with NDT was missing, demanding more study. Similarly, elsewhere, the NDTs have been studied extensively, but little attention has been dedicated to comparing them. In this study, non-destructive testing (NDT) techniques such as ultrasonic pulse velocity and Schmidt hammer testing are used to determine the strength and physical properties of the selected rocks. Granite, marble, and sandstone were studied as examples of common rock types. The investigation also improved our knowledge of the NDTs' dependability. Following a petrographic analysis, the strength and physical properties of the material are assessed. Additionally, the effect of moisture content on NDTs is examined. Results are then linked with strength and physical attributes to define an efficient NDT.

2. Geology of the Study Area

In the research area, located in the Peshawar Plain Alkaline Igneous Province (PPAIP) and the Peshawar basin, a range of igneous, metamorphic, and sedimentary rocks are well exposed [34,35] (Figure 1). This study focuses on granite (Igneous rock) from Malakand and Utlā, marble (Metamorphic rock) from Nowshera Formation, and sandstone (Sedimentary rock) from Murree Formation to establish their physical and strength characteristics using NDTs. A brief description of the selected rock units is given in this section.

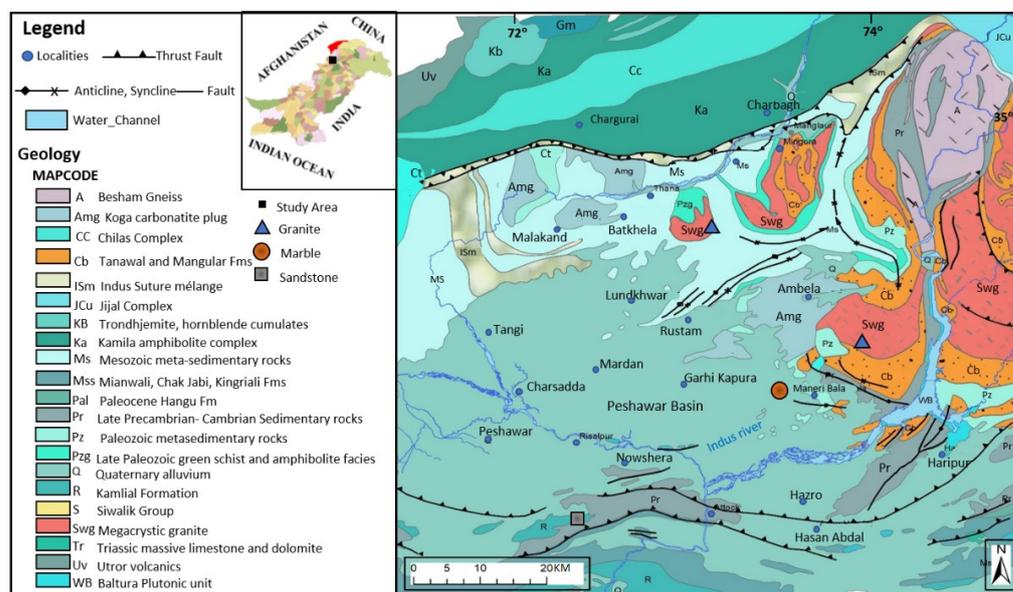


Figure 1. Geological map of the study area showing the locations of the selected samples.

2.1. Malakand Granite

According to Chaudhry et al. [36], it is still debatable whether Malakand granite is a component of PPAIP, despite being chemically identical to Ambela, Shewa-Shahbazgarhi, and Warsak granite. Malakand granite is a small, oval-shaped pluton covering about 40 km² with fine-grained chill zones at its contact and a cross-cut interaction with the country rocks [37,38]. According to Khattak et al. [39] and Le Bas et al. [40], alkaline magmatism

occurred in two phases: (i) Permian and (ii) Paleogene (Oligocene). The emplacement of Malakand granite is attributed to the second phase.

2.2. Utlā Granite

Khan and Hammad [41] investigated the petrography of Utlā granite and concluded that it is related to the Ambela granitic complex (AGC), which encompasses 900 km² and is the primary associate of the PPAIP. The Utlā granites to the east of the Ambela granitic complex appear to be in spatial continuity and hence may constitute the AGC's eastward expansion [42]. Later studies, on the other hand, grouped the Utlā granites with the Mansehra and Swat granites [43–46]. Sajid et al. [47] attributed an early palaeozoic emplacement date to the Utlā granite, which is statistically synchronous to the Mansehra granites based on U-Pb zircon geochronological analysis.

2.3. Nowshera Formation

Stauffer [48] gives the fossiliferous carbonates under Misri Banda Quartzite the name Nowshera Formation. Pogue and Hussain [49] later added calcareous and dolomitic quartzite, labelled Misri Banda Quartzite by Stauffer [48], to the Nowshera Formation. The type locality is along the Nowshera-Risalpur road to the north of Nowshera and is classified as a reef complex due to its extremely fossiliferous nature [50,51]. It is comprised of dolomitic and calcareous quartzite, sandy dolomite, fossiliferous limestone, and subordinate argillite. It includes calcite-rich marble near Maneri village in the district of Swabi. According to Talent and Mawson [52], the formation dates from the Early to Late Devonian.

2.4. Murree Formation

The stratigraphic committee of Pakistan named the Murree Formation after the Murree Hills in Rawalpindi District. The type locality is in Attock District, to the north of Dhok Maiki [53–55]. It stretches from Darra Adamkhel in the southwest to the southernmost point of the Peshawar Basin, where it spreads on the northwestern edge of the Attock-Cherat ranges [56]. Sandstone, siltstone, and shale make up the formation. The sandstone content is significant, and its colour ranges from greyish brown to greenish grey and purple in parts [57]. The Murree Formation is Early Miocene in age and has lower confirmable contact with the Patala Formation [58].

3. Materials and Methods

Table 2 shows the three granite samples (MG, UGA, and UGB), two marble samples (NFA and NFB), and three sandstone samples obtained in the field (MFA, MFB, and MFC). Selected samples were homogeneous in terms of their fundamental properties, such as texture and weathering grade. Weathering grades (WG) were assigned following the study of Borrelli et al. (2007). Figure 2 shows the flow chart of the research methodology. For NDT, strength, and physical testing, samples were taken to the Geotechnical Engineering Laboratory at the National Centre for Excellence in Geology (NCEG) in Pakistan. Three NX-size (54.75 mm) core specimens were obtained from each sample. A polarized microscope (Microscope Model Eclipse LV100ND of Nikon, Tokyo, Japan) was used for petrographic investigation. To get an idea of what minerals were present in the sample, the mineral composition and grain size were visually analyzed according to BS EN 12407 (British National Standards) [59].

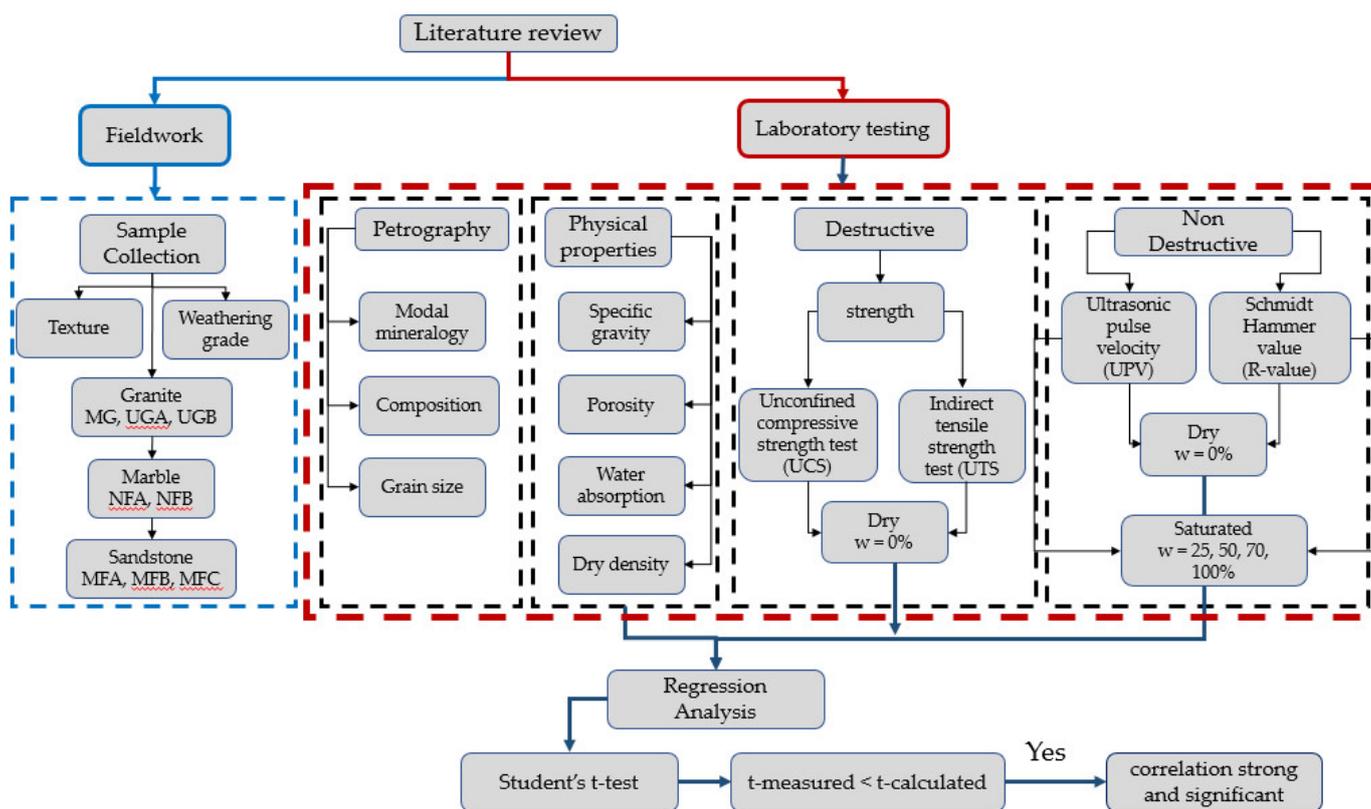


Figure 2. Flow chart of the research methodology.

By producing core samples at different moisture levels, including 0, 25, 50, 75, and 100%, the impact of moisture content on both NDTs was investigated, as proposed by Bozkurt and Yazicioglu [60] and Chen et al. [61]. The moisture content was regulated to the required percentage by adjusting the mass of pores and water in the specimen by periodic weighing while drying in air at room temperature.

$$Sr = \frac{M_{pw} - M_{od}}{M_{sat} - M_{od}} \times 100\% \tag{1}$$

Where,

M_{pw} = Mass of the specimen with pore water

M_{sat} = Mass of saturated specimen

M_{od} = Oven dry mass

Table 2. List of abbreviations and acronyms used in this article.

Rock Type	Origin	Sample	Specimen	WG *
Granite	Utla	UGB	UGB1	I
			UGB2	
			UGB3	
	Malakand	MG	MG1	II
			MG2	
			MG3	
	Utla	UGA	UGA1	III
			UGA2	
			UGA3	
Marble	Manerai	NFA	NFA1	I
			NFA2	

			NFA3	
			NFB1	
		NFB	NFB2	II
			NFB3	
			MFA1	
		MFA	MFA2	I
			MFA3	
			MFB1	
Sandstone	Jenakor	MFB	MFB2	II
			MFB3	
			MFC1	
		MFC	MFC2	III
			MFC3	

*Weathering Grade

A UPV tester was used to evaluate the ultrasonic pulse velocity (UPV) of dry and saturated samples (i.e., 0, 25, 50, 75, and 100%) (Model 58-E4800 UPV MS Controls Italy). The researchers employed a pitch-catch technique, which uses a pair of transducers (transmitter and receiver) [62]. With a pulse rate of 2 s⁻¹ and a natural resonance frequency of 54 kHz, piezoelectric transducers (probes) were used. Both probes were positioned on opposite sides of the cylindrical specimen in a direct-transmission manner. To reduce the impact of pores and improve the signal-to-noise ratio between the probes and the specimen, a coupling agent was used. An average of three transit time values was collected for each specimen in the dry condition. After measuring the length of the route, Equation (2) calculated the ultrasonic pulse velocities.

$$UPV = \frac{L}{t} \tag{2}$$

Where,

L = length of the path

t = transit time

The rebound hardness test was performed according to ASTM D 5873–14 using an N-type Schmidt hammer with an impact energy of 2.207 Nm (MS Controls Italy Model D5873-14). To show the effect on rebound values, the approach was applied to dry and saturated samples (i.e., 0, 25, 50, 75, and 100%) (R_{dry}-value and R_{sat}-value).

The ASTM C 170M-17 (C170M-17) and ASTM D 3967-16 (D3967-16) standards were used to measure unconfined compressive strength (using core samples with 110 mm length and 55 mm diameter) and indirect tensile strength (using disc samples with 55 mm diameter and 28 mm thickness). The ASTM (C97M-18) was used to assess physical parameters such as specific gravity and water absorption, while the saturation and buoyancy technique was used to estimate porosity and dry density [63].

3.1. Regression Analysis

Simple regression analysis was used to develop prediction models for dependent variables, such as physical parameters (specific gravity, porosity, water absorption, and dry density), strength parameters (unconfined compressive strength and indirect tensile strength), and independent variables, i.e., NDTs (UPV and Schmidt Hammer). The XY scatter chart in the Microsoft Excel software suite was used to depict the data from the responder and regressor/predictor variables. Several trend line functions, including both linear and nonlinear functions, were used to examine the relationships (exponential, logarithmic, polynomial, and power) based on the lowest fit of errors criteria. Each of these functions produces a correlation coefficient and an equation (R²). The R² calculates the

variability of one variable by dividing it by the variability (deviation) of the other [64]. During the regression analysis, the response variables were estimated using the equation with the best R² value.

A student's *t*-test with a 95% confidence level was used to investigate the significance of the R² values produced from the established associations (i.e., NDT_{dry} versus UCS and UTS) (3).

$$t = \frac{\bar{X}A - \bar{X}B}{\sqrt{\left(\frac{\text{Var}A}{nA} + \frac{\text{Var}B}{nB}\right)}} \quad (3)$$

Where,

$\bar{X}A - \bar{X}B$ = Actual difference between the means of two variables

$\sqrt{\left(\frac{\text{Var}A}{nA} + \frac{\text{Var}B}{nB}\right)}$ = the variation or dispersion in the data

The calculated and tabulated *t*-values are compared in this test. The value of the *t*-tabulated, also known as the *t*-critical, must be smaller than the calculated *t*-value derived from the regression to declare a strong and significant correlation [65].

4. Results

4.1. Petrographic Observation

This section gives a quick overview of the rocks that were studied. The modal mineralogy and mean grain size are reported in Table 3, and selected microphotographs of the rock samples are shown in Figure 3.

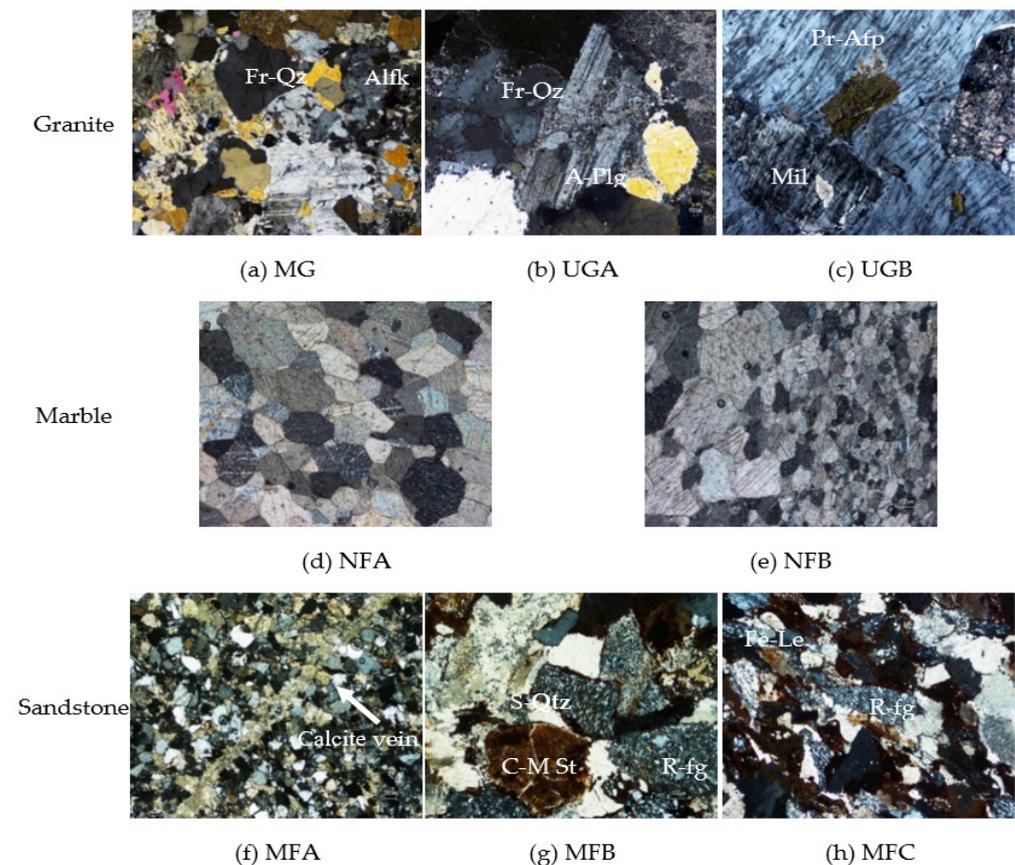


Figure 3. Photomicrographs of investigated granite, marble, and sandstone (a-c) One set of cleavages are observed in UGA and UGB samples, Fr-Qz: fractured quartz, Alfk: alkali feldspar, A-Plg: altered plagioclase, Pr-Afp: perthite alkali feldspar, Mil: microcline (d-e) calcite-rich marble in NFA

and NF B (f-h) fractures are seen in MFA and MFC samples, C-M St: clay rich mudstone, R-fg: volcanic rock fragments, Fe-Le: iron leaching.

Table 3. Modal mineralogy and mean grain size of the investigated rocks.

Rock Type	Sample	Qtz	Alkf	Plg	Ms	Bt	Ep	Mnz	Apt	Mc	Cal	RF	Chl	IO	Opq	Q:F	Cal:Opq	C/M	MGS
Granite	MG	26.60	38.97	19.43	4.53	1.63	1.47	0.47	0.27	1.95	--	--	--	--	1.00	0.45	--	--	1.05
	UGA	24.30	44.63	17.97	1.40	3.40	3.57	--	1.63	--	--	--	--	--	0.73	0.39	--	--	3.86
	UGB	29.27	36.47	17.67	1.73	6.27	--	0.73	0.60	2.70	--	--	--	--	2.83	0.52	--	--	0.96
Marble	NFA	2.10	--	--	--	--	--	--	--	--	96.97	--	--	--	2.33	--	41.63	--	0.10
	NFB	2.10	--	--	--	--	--	--	--	--	96.97	--	--	--	2.33	--	41.63	--	0.10
Sandstone	MFA	26.97	13.40	--	0.47	--	--	0.37	--	--	--	3.93	0.47	12.50	--	2.07	--	41.53	0.08
	MFB	16.77	9.73	--	0.13	--	--	0.33	--	--	--	16.73	0.20	5.37	--	1.73	--	50.47	0.24
	MFC	13.17	9.30	--	0.63	--	--	0.50	--	--	--	29.97	0.10	5.67	--	1.43	--	40.03	0.28

Alkf = alkali feldspar, Apt = apatite, Bt = biotite, Cal = calcite, Cal:OM = calcite to opaque mineral ratio, Chl = chlorite, C/M = cement to matrix ratio, Ep = epidote, IO = iron oxides, Mc = microcline, MGS = mean grain size, Ms = muscovite, Mnz = monazite, Opq = opaque minerals, Plg = plagioclase, Qtz = quartz, RF = rock fragments, Q: F = quartz-to-feldspar ratio.

4.1.1. Granite

The key minerals in MG were anhedral alkali feldspar, plagioclase, and quartz. MG was medium- to fine-grained. With the addition of apatite, zircon, and clinozoisite, quartz displayed undulose extinction and intra-granular fractures. Muscovite, biotite, tourmaline, opaque minerals, epidote, microcline, and monazite were among the other accessory minerals found.

UGA was composed of subhedral to anhedral alkali feldspar, quartz, and plagioclase and was coarse- to medium-grained. At the boundaries, both alkali feldspar and plagioclase displayed strong sericitization and dissolution. In the quartz grains, there was an intense intra-granular discontinuity as well as the presence of andalusite, apatite, and zircon. Biotite, muscovite, tourmaline, epidote, and opaque minerals are examples of accessory minerals.

UGB had a porphyritic texture and was fine-grained. Subhedral to anhedral alkali feldspar, plagioclase, quartz, and microcline made up the phenocryst. Because sericite is the alteration result of feldspar and plagioclase, the alteration process is largely sericitization. Perthite grains were found in abundance in all the types studied. Quartz, feldspar, plagioclase, microcline, biotite, muscovite, tourmaline, and opaque minerals made up the groundmass.

4.1.2. Marble

NFA ranged from fine-grained to very fine-grained. Calcite had a sub-idioblastic to xenoblastic shape and was undeformed. The grain boundaries were predominantly granoblastic interlobate, although the triple junction also had a granoblastic polygonal shape. Quartz and opaque minerals were also present in trace concentrations.

NFB is fine-grained homoblastic marble. Calcite is the primary component of these variations with idioblastic to subidioblastic shapes, according to the modal composition. With a triple junction, calcite grains have flawless orthorhombic twinning and polygonal boundaries. There was no intra-granular fracture, and the contact between the calcite

grains was longitudinal. A small quantity of quartz and opaque minerals were also investigated.

4.1.3. Sandstone

MFA included calcite cement and was exceedingly fine-grained (carbonate cement). Quartz was primarily monocrystalline and included monazite and apatite inclusions among the framework grains. Partially sericitized orthoclase feldspar. The rock fragments were sedimentary in nature (chert and shale). Calcite veins were found among iron oxides (magnetite and hematite). Muscovite, chlorite, and rutile were among the accessory minerals.

Carbonaceous cement and ferruginous matrix were found in MFB, which was medium- to fine-grained. Apatite, monazite, and zircon were found as inclusions in quartz (which was largely monocrystalline). Polysynthetic twinning was seen in plagioclase. Shale, sandstone, chert, quartzite, clay-rich mudstone, schistose quartz, and some igneous fragments were among the rock fragments found. Muscovite and chlorite are two more trace minerals.

Compared to the other two varieties, MFC was medium-grained and had a higher amount of rock fragments (chert, shale, clay-rich mudstone, and volcanic rocks). The size of the clay matrix (ferruginous) was restricted. The calcitic cementing material filled the pore spaces. The second most common framework grain was quartz (rarely polycrystalline). The bigger monocrystalline grains were shattered, and calcite cement was used to fill them. Orthoclase feldspar saw a lot of changes. Small calcite veins and iron leaching were also found.

4.2. Physical and Strength Properties

The weathering grades and average findings of the physical and strength attributes of the studied rocks are shown in Table 4. The specific gravity of the samples varied from 2.65 (sample MG) to 2.76 (sample MFC), while porosity and water absorption were 0.23 to 2.45% and 0.09 and 0.91%, respectively. Similarly, the strength values of the investigated samples fall into three groups, according to the international association of engineering geologists: moderately strong (15–50 MPa, samples NFA, NFB, and UGB); strong (50–120 MPa, sample MFC); and very strong (>120 MPa, samples MG, UGB, MFA, and MFB) [66]. The findings reveal that samples with relatively high strength and weathering grade have low porosity and water absorption values, and vice versa, for each rock type. The previous study on granite [67], marble [68], and sandstone [67] showed similar results.

Table 4. Weathering grades and calculated average values of strength and physical properties of the studied rocks.

Rock Type	Sample	WG	Specific Gravity	Porosity (%)	Water Absorption (%)	Dry Density (g/cm ³)	UCS (MPa)	UTS (MPa)
Granite	UGB	I	2.69	0.89	0.33	2.66	131.20	8.47
	MG	II	2.65	1.25	0.47	2.62	122.78	4.99
	UGA	III	2.67	2.00	0.76	2.61	40.69	3.66
Marble	NFA	I	2.72	0.23	0.09	2.71	38.38	3.02
	NFB	II	2.72	0.42	0.15	2.70	34.29	2.67
Sandstone	MFA	I	2.72	1.09	0.41	2.69	141.33	18.07
	MFB	II	2.73	2.10	0.78	2.68	132.48	15.63
	MFC	III	2.76	2.45	0.91	2.69	61.94	11.80

5. Discussion

5.1. Factors Affecting NDTs

5.1.1. Weathering Grade

The relationship between NDTs in dry states (UPV_{dry} and R_{dry} -value) and weathering grades is shown in Figure 4. Both NDTs dropped as weathering grades increased for all the rocks studied. Weathering weakens rock-forming minerals and stiffens grain boundaries, as well as causing dissolution and leaching of mineral phases, resulting in high porosity. The propagation of UPV_{dry} is slowed when there are more pores and micro-fissures [67]. Similarly, increasing porosity affects the rock's hardness and strength, resulting in lower R_{dry} values [69]. Granite, basalt, and quartzite all have equivalent UPV and R -values, according to Gupta and Rao [70] and Gupta et al. [5].

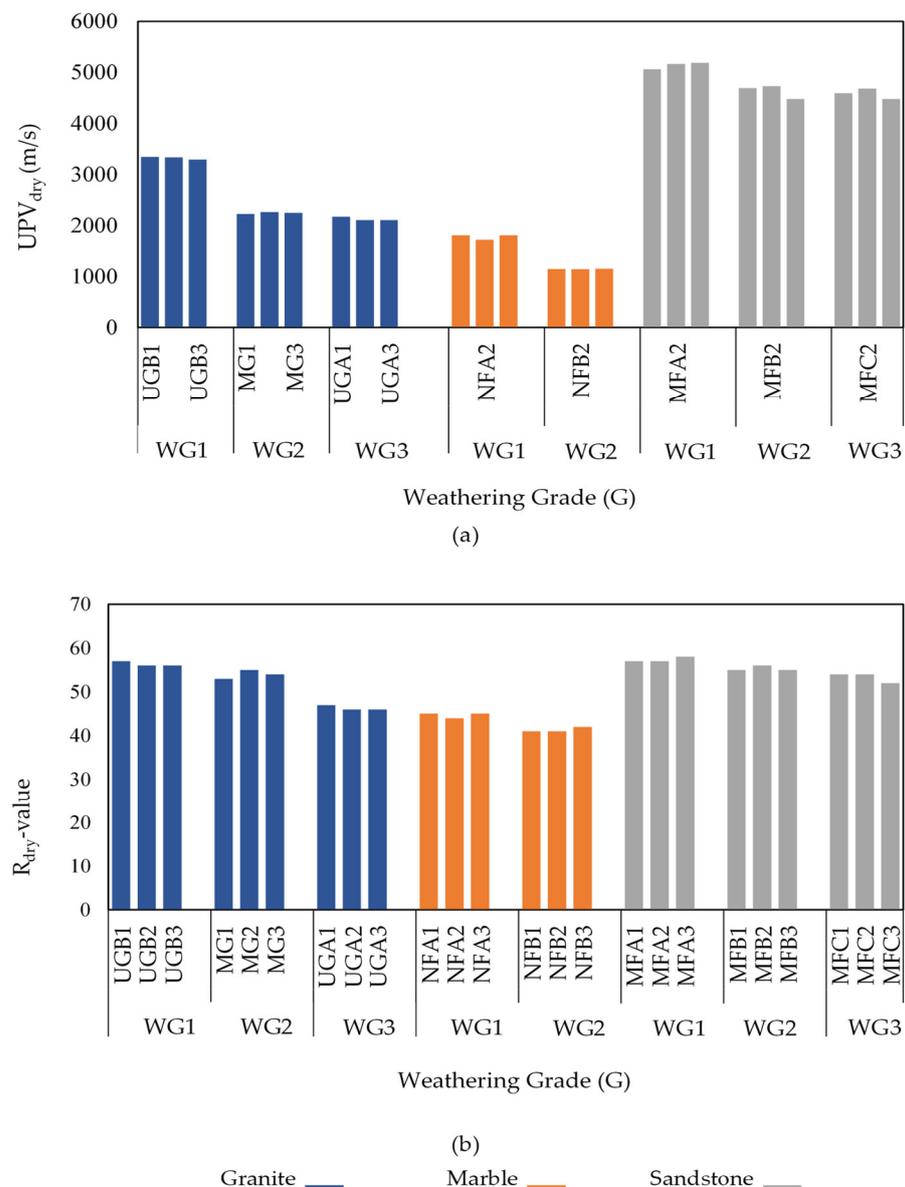


Figure 4. Variation of weathering grade (a) with UPV_{dry} (b) with R_{dry} -value

5.1.2. Moisture Content and Porosity

The influence of moisture content on NDTs is seen in Figure 5. The average values of the NDTs are shown in Figure 5a,b at different moisture levels (i.e., 0, 25, 50, 75, and 100%),

ranging from dry to saturated specimens. As the moisture content varies, the data demonstrate a steady shift in NDTs [71]. In general, UPV propagation increased when moisture content rose in all the rocks investigated; however, this shift was less pronounced in sandstone (MFA, MFB, and MFC in Figure 5a).

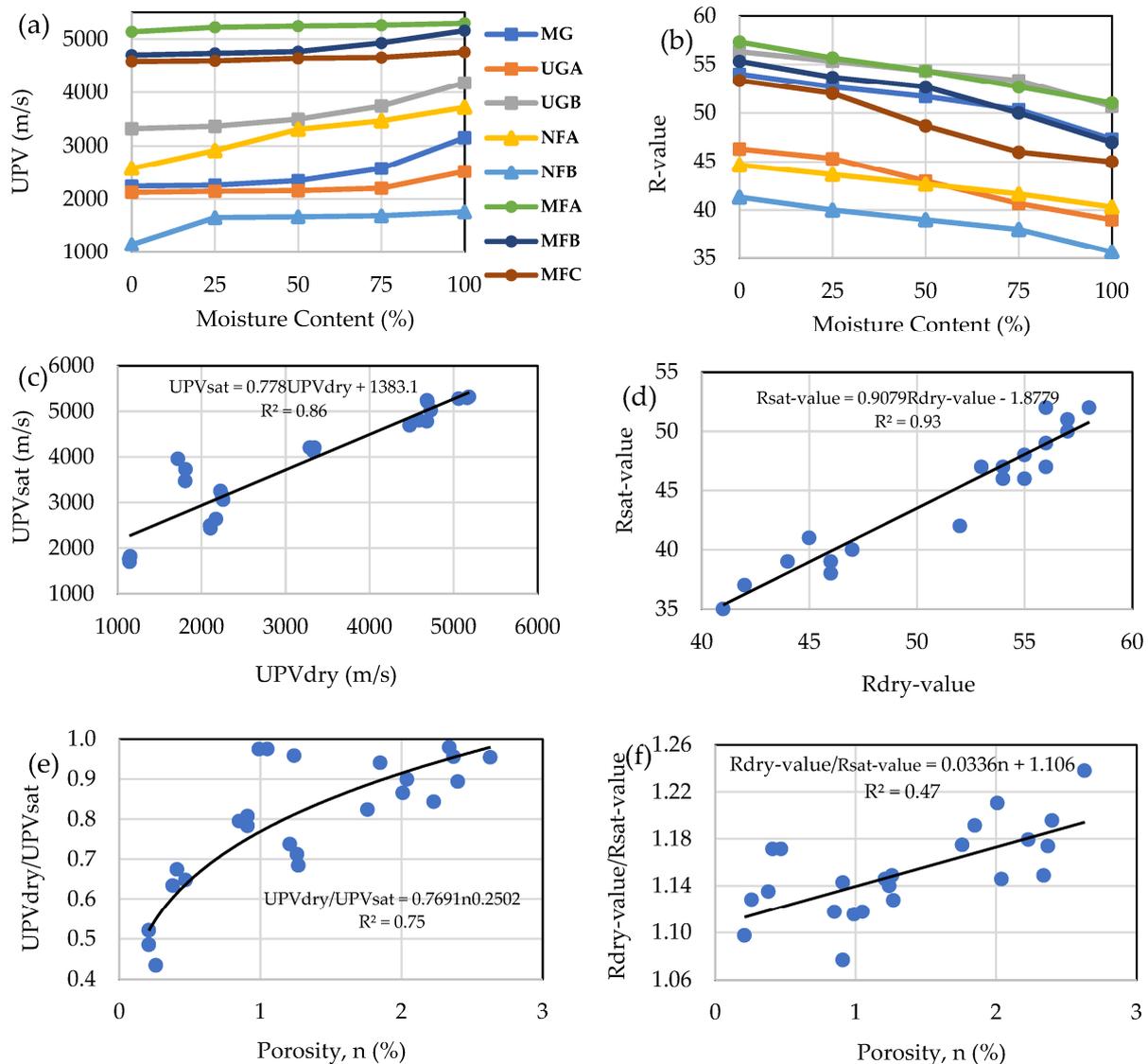


Figure 5. Variation of UPV_{dry} and R_{dry} (a;b) with moisture content (c) UPV_{sat} vs UPV_{dry} (d) R_{sat} -value vs R_{dry} value (e) UPV_{dry}/UPV_{sat} vs Porosity (f) R_{dry} -value/ R_{sat} -value vs Porosity (g) Cal:OM vs UPV_{dry} (h) Cal:OM vs R_{dry} value.

The R-values (Figure 5b) show a consistent negative trend with moisture content, with a decrease of 10 to 15% from dry to completely saturated. Grain softening and skeletal connections decrease when water content rises, resulting in inter-grain sliding and a decline in R-value [14,69,72]. Figure 5c,d show the NDT values in dry and saturated conditions, demonstrating that the UPV sat and R-sat-values can be estimated with excellent accuracy from the values obtained in a dry specimen ($R^2 = 0.86$ and 0.93 , respectively). The dry to saturated ratio of NDTs vs porosity is shown in Figure 5e,f to highlight how porosity affects NDTs. The UPV rises with porosity, and above 1%, the UPV_{dry} varies from 0.70 to 0.98% of the UPV sat, with only the marble sample having lower values. This is in contrast to the results of Vasconcelos et al. [67], who reported similar ranges for low-porosity granite samples (0.6%). The difference in R-value between the two moisture conditions (Figure 5f) demonstrates a considerable scatter with no relation to porosity. Figure 5g,h

plots the relationship between mineralogy (quartz to feldspar ratio, Q:F for granite and sandstone; and calcite to opaque mineral ratio, Cal:OM for marble) and NDTs (UPV_{dry} and R_{dry}). With the increase in the quartz-to-feldspar ratio in granite and sandstone, NDTs increased. Compared to sandstone, the NDTs of granite are more sensitive to changes in quartz content. Sousa [73] and Yusof and Zabidi [74] have reported similar relationships for the quartz-rich rocks. Likewise, with an increase in the calcite to opaque mineral ratio in marble, both NDTs decreased. These results suggest that ultrasonic pulse velocity and rebound values are higher in physically strong minerals such as quartz and opaque minerals.

5.1.3. Correlation Between NDTs and Physical Properties

Figures 6–7 and Table 5 show the results of NDTs (dry) based on experimental data derived from the physical properties of the analyzed rock type studied by simple regression. Physical factors such as specific gravity, porosity, water absorption, and dry density were evaluated. The statistical connections between UPV and R-value in dry specimens with physical parameters are shown in Table 5. Figure 6a illustrates the UPV_{dry} and specific gravity of granite and sandstone with logarithmic connections that are quite substantial ($R^2 = 0.67$ and 0.71 , respectively). Marble, on the other hand, showed no correlation since the specific gravity remained constant while the UPV_{dry} fluctuated. Figure 6b shows that power relations exist for granite and marble ($R^2 = 0.75$ and 0.96 , respectively), whereas a polynomial exists for sandstone ($R^2 = 0.95$). UPV_{dry} has a significant power connection for granite, an exponential relationship for marble, and a logarithmic relationship for sandstone when it comes to water absorption (Figure 6c) (0.76 , 0.95 , and 0.94 , respectively). Finally, logarithmic connections exist between dry density and UPV_{dry} (Figure 6d) for granite and marble ($R^2 = 0.98$ and 0.51 , respectively), but not for sandstone.

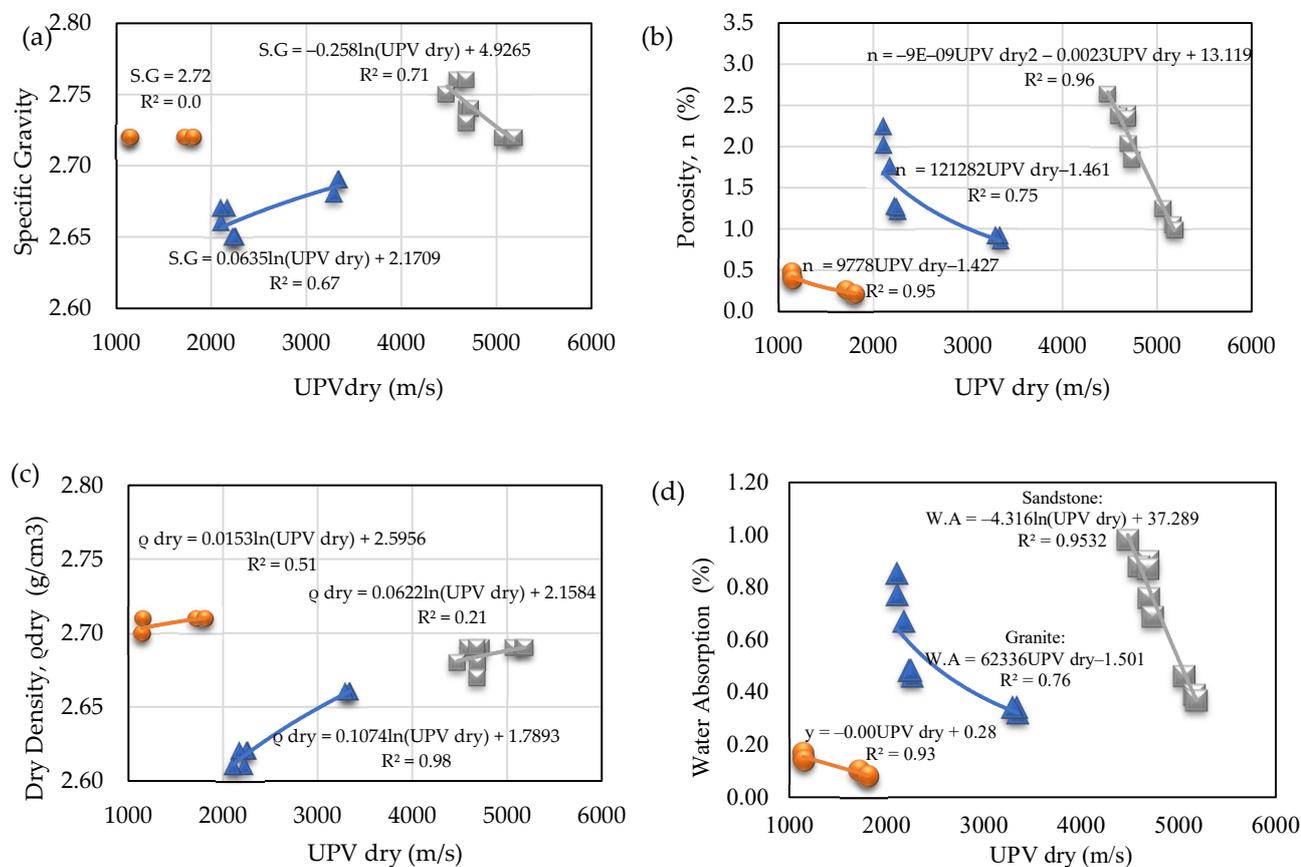


Figure 6. Correlation of UPV_{dry} against (a) specific gravity, (b) porosity, (c) dry density and (d) water absorption for granite, marble, and sandstone. Granite — Marble — Sandstone —.

Except for dry density, which exhibits an exponential best fit curve, the scatter plots of R_{dry} -value vs physical characteristics in Figure 7 show logarithmic correlations. Since specific gravity remained constant with R_{dry} -value, there was no link between R_{dry} -value and specific gravity (Figure 7a). The R^2 value is strong in all other associations except for granite ($R^2 = 0.07$) in the R_{dry} -value vs specific gravity plot and sandstone ($R^2 = 0.16$) in the R_{dry} -value vs. dry density chart.

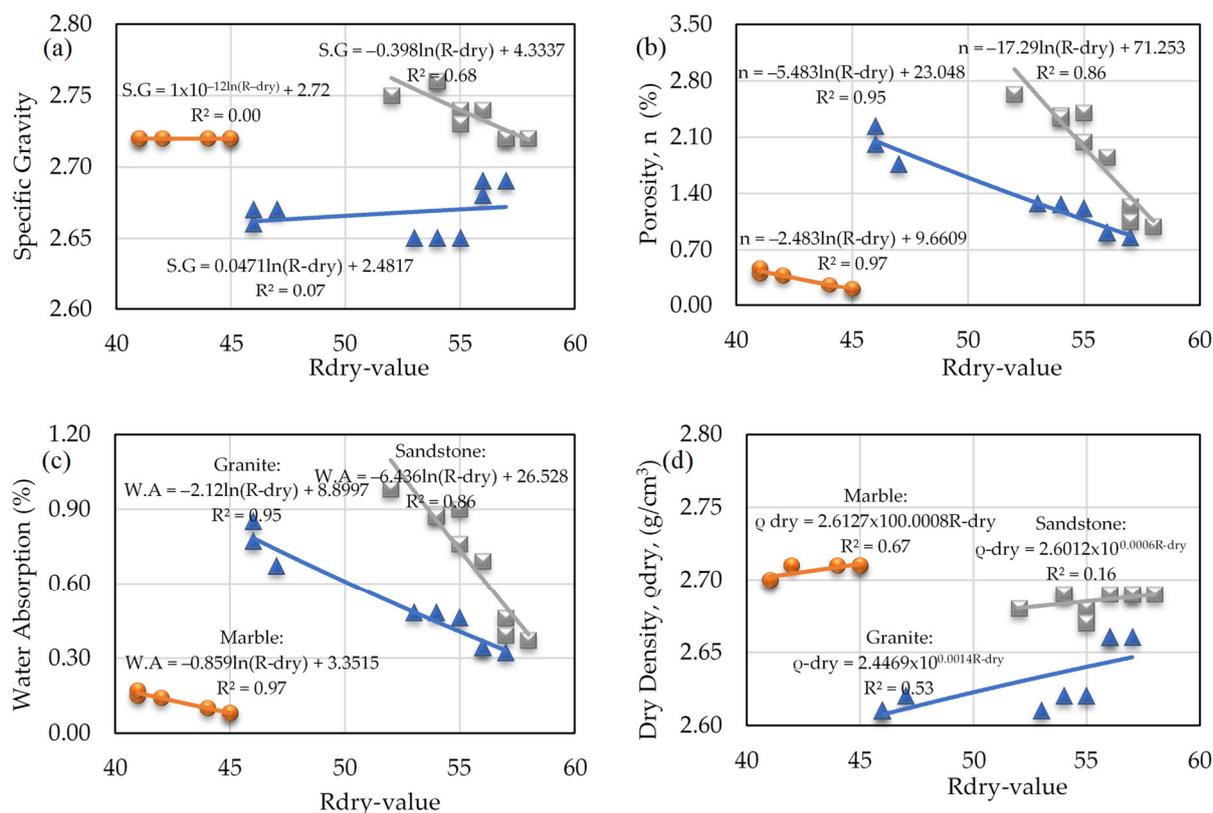


Figure 7. Correlation of R_{dry} -value against (a) Specific gravity, (b) Porosity, (c) Water absorption and (d) dry density for granite, marble and sandstone

Table 5. Statistical relations of NDTs-dry with physical properties.

Physical Property	Rock Type	Ultrasonic Pulse Velocity, UPV_{dry}		Rebound-Value, R_{dry} -Value	
		Equations	R^2	Equations	R^2
Specific Gravity	Granite	$S.G. = 0.0635 \ln(UPV_{dry}) + 2.1709$	0.67	$S.G. = 0.0471 \ln(R_{dry-value}) + 2.481$	0.07
	Marble	No relation	0.00	No relation	0.00
	Sandstone	$S.G. = -0.258 \ln(UPV_{dry}) + 4.9265$	0.71	$S.G. = -0.398 \ln(R_{dry-value}) + 4.3337$	0.68
Porosity	Granite	$\eta = 121282(UPV_{dry}) - 1.461$	0.75	$\eta = -5.483 \ln(R_{dry-value}) + 23.048$	0.95
	Marble	$\eta = 9778(UPV_{dry}) - 1.427$	0.95	$\eta = -2.483 \ln(R_{dry-value}) + 9.6609$	0.97
	Sandstone	$\eta = -9 \times 10^{-9} (UPV_{dry})^2 - 0.0023(UPV_{dry}) + 13.119$	0.96	$\eta = -17.29 \ln(R_{dry-value}) + 71.253$	0.86
Water Absorption	Granite	$W.A. = 62336 (UPV_{dry}) - 1.501$	0.76	$W.A. = -2.12 \ln(R_{dry-value}) + 8.8997$	0.95
	Marble	$W.A. = -0.00UPV_{dry} + 0.28$	0.94	$W.A. = -0.859 \ln(R_{dry-value}) + 3.35$	0.97

	Sandstone	W.A. = $-4.316 \ln(\text{UPV}_{\text{dry}}) + 37.289$	0.95	W.A. = $-6.436 \ln(\text{R}_{\text{dry-value}}) + 26.52$	0.86
Dry Density	Granite	$q\text{-dry} = 0.1074 \ln(\text{UPV}_{\text{dry}}) + 1.7893$	0.98	$q\text{-dry} = 2.4469 \times 10^{0.0014}(\text{R}_{\text{dry-value}})0.53$	
	Marble	$q\text{-dry} = 0.0153 \ln(\text{UPV}_{\text{dry}}) + 2.5956$	0.51	$q\text{-dry} = 2.6127 \times 10^{0.0008}(\text{R}_{\text{dry-value}})0.67$	
	Sandstone	$q\text{-dry} = 0.0622 \ln(\text{UPV}_{\text{dry}}) + 2.1584$	0.21	$q\text{-dry} = 2.6012 \times 10^{0.0006}(\text{R}_{\text{dry-value}})0.16$	

Similar correlations have been suggested for calculating various physical characteristics in a range of rock types using the UPV [27,28,75] and R-values in previous research. The computed physical parameters were obtained using the equations given in each of the correlative charts (Tables 6 and 7). The zero-intercept slope lines in Figures 8 and 9 demonstrate the magnitude of inaccuracy in estimated and observed physical parameters. The data points that are far from the zero-intercept slope line indicate an error, while those that are above it indicate correctness. Because the computed t-values are bigger than the crucial t-values, the student’s t-test at the 95% confidence level is significant for all associations between the UPV-dry and R-dry versus physical characteristics, as shown in Table 6.

Table 6. Measured and calculated values of physical properties.

Specimen Designation	Specific Gravity		Porosity (%)		Water Absorption (%)		Dry Density (g/cm³)					
	Measured	Calculated	Measured	Calculated	Measured	Calculated	Measured	Calculated				
		UPV (Dry)		R (Dry)		UPV (Dry)		R (Dry)	UPV (Dry)	R (Dry)		
MG	2.65	2.63	2.67	1.25	1.54	1.18	0.47	0.58	0.44	2.62	2.62	2.64
UGA	2.67	2.63	2.66	2.00	1.67	2.02	0.76	0.63	0.77	2.61	2.61	2.61
UGB	2.69	2.66	2.67	0.89	0.87	0.95	0.33	0.32	0.36	2.66	2.66	2.65
NFA	2.72	-	-	0.23	0.23	0.23	0.09	0.09	0.09	2.71	2.71	2.71
NFB	2.72	-	-	0.42	0.42	0.42	0.15	0.16	0.15	2.70	2.70	2.70
MFA	2.72	2.72	2.72	1.09	1.07	1.25	0.41	0.41	0.47	2.69	2.69	2.69
MFB	2.74	2.75	2.74	2.10	2.11	1.86	0.78	0.79	0.70	2.68	2.68	2.69
MFC	2.76	2.75	2.75	2.45	2.39	2.50	0.91	0.90	0.93	2.69	2.68	2.69

Table 7. Results of the t-test for the correlation of UPV (dry) and R-(dry) against the physical properties of the studied rocks.

Physical Property	Rock Type	Ultrasonic Pulse Velocity Dry (UPV _{dry})		Rebound-Value, R _{dry} -Value	
		t-Critical	t-Calculated	t-Critical	t-Calculated
Specific Gravity	Granite	2.12	13.46	2.12	32.48
	Marble	-	-	-	-
	Sandstones	2.12	55.54	2.12	84.34
Porosity	Granite	2.12	13.47	2.12	33.13
	Marble	2.23	10.29	2.23	55.00
	Sandstones	2.12	55.55	2.12	81.20
Water Absorption	Granite	2.12	13.47	2.12	33.86
	Marble	2.23	10.29	2.23	55.35
	Sandstones	2.12	55.57	2.12	86.92
Dry Density	Granite	2.12	13.46	2.12	32.51
	Marble	2.23	10.28	2.23	52.02
	Sandstones	2.12	55.54	2.12	84.42

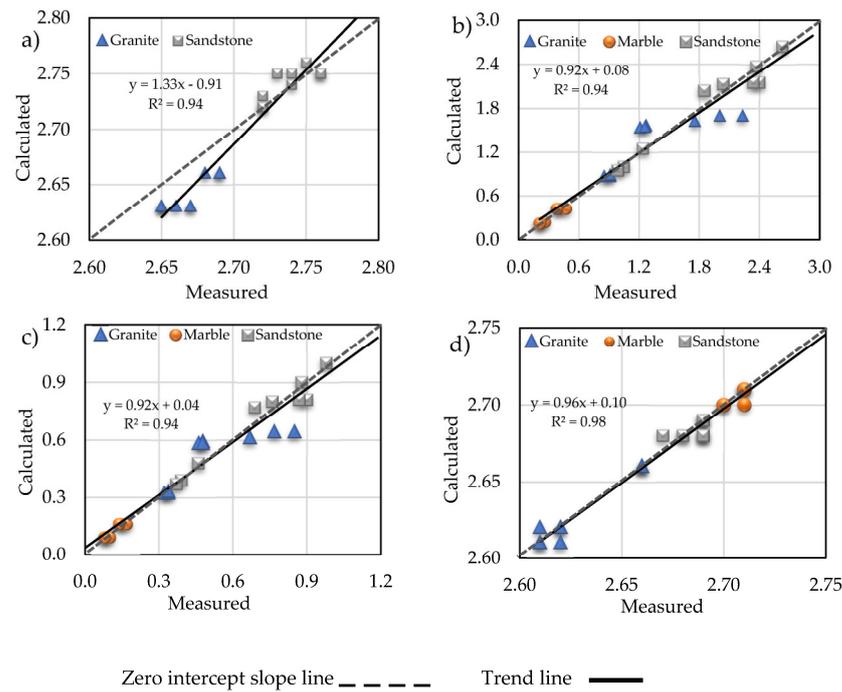


Figure 8. Measured and calculated values of physical properties of the studied rocks obtained from UPV_{dry} (a) specific gravity, (b) porosity, (c) water absorption, and (d) dry density.

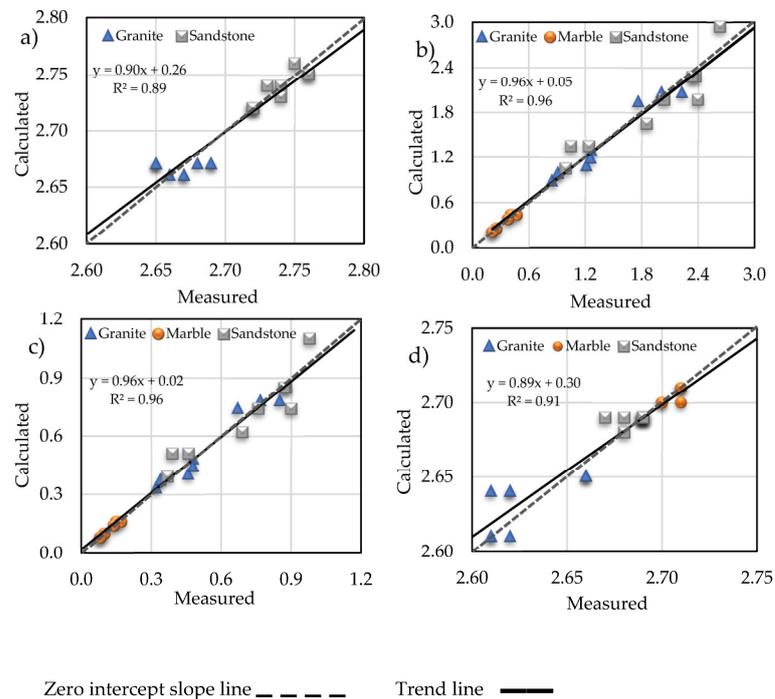


Figure 9. Measured and calculated values of physical properties of the studied rocks obtained from R_{dr}-value (a) specific gravity, (b) porosity, (c) water absorption, and (d) dry density.

5.1.4. Correlation Between NDTs and Strength Properties

For different rocks, many studies have provided various curve fits for calculating UCS using UPV and R-values [67,76,77]. This research also looks at UTS's ties to NDTs, in addition to UCS. Using a simple regression analysis, the findings of the dry-state NDTs (UPV_{dry} and R_{dry}-value) were linked against UCS and UTS in Figure 10. The correlation

coefficient (R^2) and statistical connections of NDT with strength attributes are also shown (Table 8).

Table 8. Statistical relations of dry-state NDTs with strength properties.

Strength Property	Rock Type	Ultrasonic Pulse Velocity, UPV (Dry)		Rebound-Value R-(Dry)	
		Equations	R^2	Equations	R^2
UCS	Granite	$UCS = 135.22 \ln(UPV_{dry}) - 960.41$	0.43	$UCS = 478.13 \ln(R_{dry-value}) - 1791.3$	0.98
	Marble	$UCS = 0.0067 (UPV_{dry}) + 26.567$	0.72	$UCS = 57.911 \ln(R_{dry-value}) - 181.44$	0.88
	Sandstone	$UCS = 513.39 \ln(UPV_{dry}) - 4240.2$	0.50	$UCS = 967.58 \ln(R_{dry-value}) - 3770.9$	0.74
UTS	Granite	$UTS = 0.0037 (UPV_{dry}) - 3.8636$	0.94	$UTS = 0.0905 (R_{dry-value})^2 - 8.8367 R_{dry} + 218.8$	0.87
	Marble	$UTS = 0.3554 (UPV_{dry})^{0.2858}$	0.80	$UTS = 0.007 (R_{dry-value})^{1.5966}$	0.83
	Sandstone	$UTS = 49.649 \ln(UPV_{dry}) - 405.73$	0.73	$UTS = -0.0945 (R_{dry-value})^2 + 11.97 (R_{dry-value}) - 357.46$	0.91

Figure 10a shows a linear best-fit curve ($R^2 = 0.72$) for marble and weak logarithmic connections ($R^2 = 0.43$ and 0.50 , respectively) for granite and sandstone. Similarly, for granite ($R^2 = 0.80$), marble ($R^2 = 0.94$), and sandstone ($R^2 = 0.73$), the plot of UPV_{dry} vs UTS (Figure 10b) indicates significant positive, linear, power, and logarithmic connections. Plotting R-dry-values against corresponding UCS (Figure 10c) reveals logarithmic curves for granite, marble, and sandstone ($R^2 = 0.98, 0.88$, and 0.74 , respectively), and plotting R-dry-values against UTS (Figure 10d) shows a polynomial for granite and sandstone ($R^2 = 0.87$ and 0.91 , respectively) and a power relation for marble ($R^2 = 0.83$).

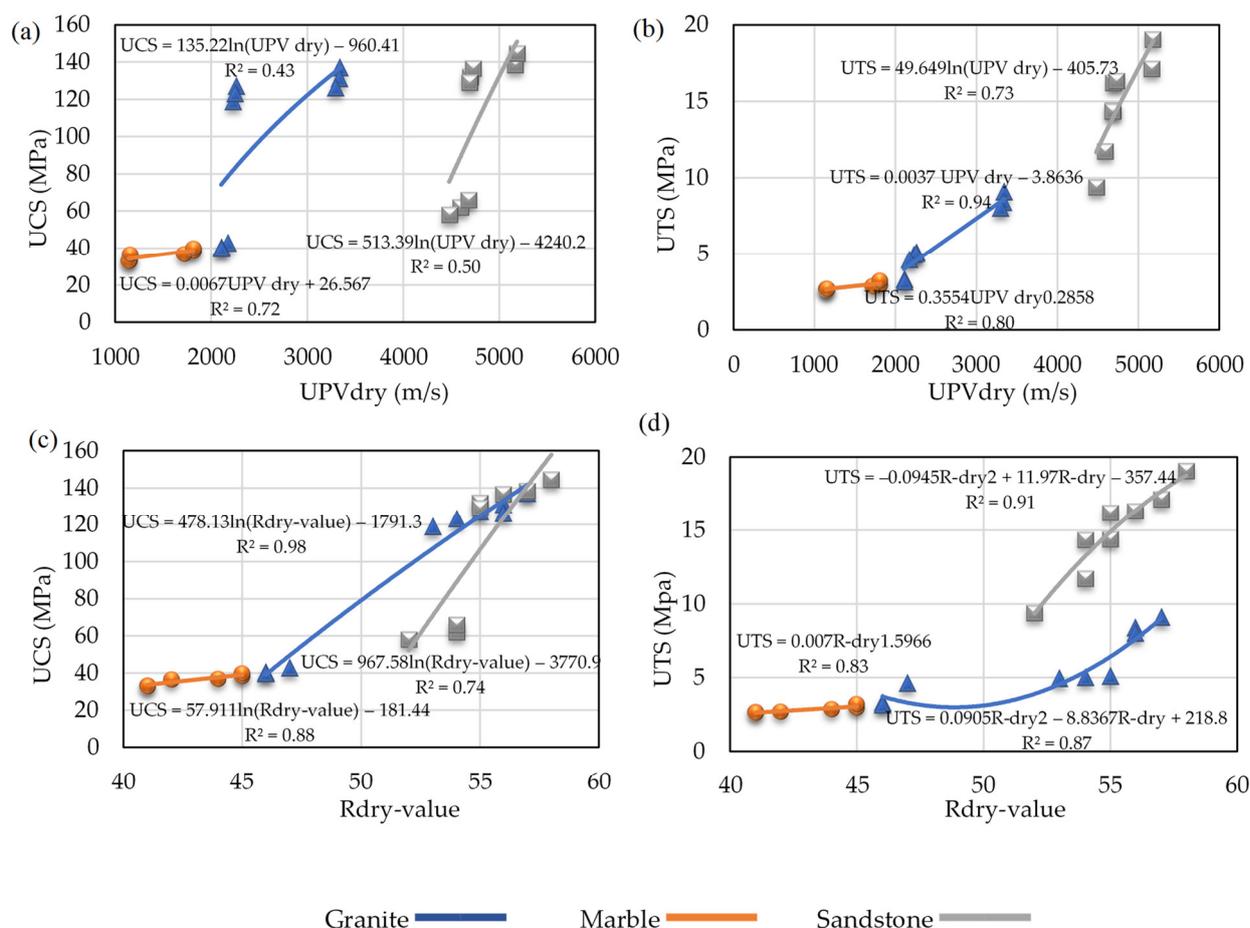


Figure 10. Correlation of NDT against UCS and UTS for granite, marble, and sandstone (a) USC vs UPVdry (b) UTS vs UPVdry (c) UCS vs Rdry-value (d) UTS vs Rdry-value.

Using NDT’s equations, the computed values of UCS and UTS are displayed against the observed values in Figure 11 (Table 9).

Table 9. Measured and calculated values of the strength properties of the studied rocks.

	Uniaxial Compressive Strength (MPa)			Unconfined Indirect Tensile Strength (MPa)		
	Measured	Calculated		Measured	Calculated	
		UPV _{dry}	R _{dry-Value}		UPV _{dry}	R _{dry-Value}
MG	122.78	82.93	115.90	4.99	4.44	5.58
UGA	40.69	75.77	42.72	3.66	4.01	3.67
UGB	131.20	136.02	136.16	8.47	8.43	7.88
NFA	38.38	38.49	38.58	3.02	3.02	3.01
NFB	34.29	34.25	34.08	2.67	2.66	2.66
MFA	141.33	149.99	149.49	18.07	18.84	18.37
MFB	132.48	100.86	112.33	15.63	14.09	15.54
MFC	61.94	87.77	76.59	11.80	12.82	12.08

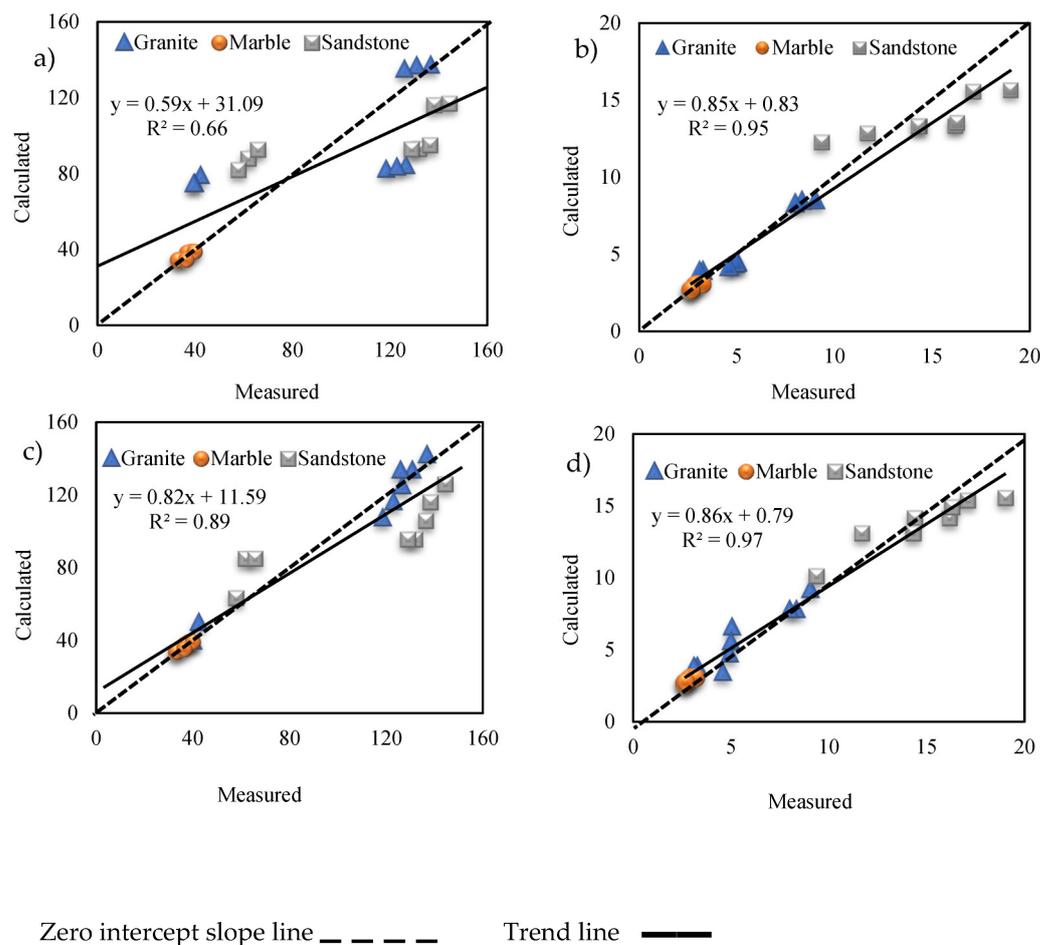


Figure 11. Measured and calculated values of strength properties of the studied rocks obtained from UPV dry (a) UCS MPa from UPV dry (b) UTS MPa from UPV dry (c) UCS MPa from R-value (d) UTS MPa from R-value

The zero-intercept slope line was used to indicate the degree of inaccuracy in the estimated numbers. Correctness is represented by data points that sit on the zero-intercept slope line, while a departure from the line denotes an error. When comparing the measured and calculated strength values derived from the R-values to those obtained using UPV ($R^2 = 0.66$ and 0.98), the plots reveal that the measured and calculated strength values derived from the R-values are near the zero-intercept line with high R^2 (0.89 and 0.97) when compared to those obtained using UPV ($R^2 = 0.66$ and 0.98). This shows that R-values are more accurate than other NDTs for assessing rock strength. Table 10 indicates that the t -critical is smaller than the t -calculated in all the relationships, showing that they are valid and useful correlations for practical applications.

Table 10. Results of the t -test for the correlation of NDTs-dry against the strength properties of the studied rocks.

Strength Property	Rock Type	Ultrasonic Pulse Velocity, UPV (Dry)		Rebound-Value, R-(Dry)	
		t-Critical	t-Calculated	t-Critical	t-Calculated
UCS	Granite	2.12	12.92	2.12	3.16
	Marble	2.23	10.04	2.23	4.91
	Sandstone	2.14	50.60	2.14	3.88
UTS	Granite	2.12	13.44	2.12	27.47
	Marble	2.23	10.27	2.23	51.48

Sandstone	2.14	52.18	2.14	31.50
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The estimation of the physical and strength properties of the investigated rocks was made on samples in a dry state. A similar approach can be followed to estimate these properties on samples at different saturation states. Likewise, the combined use of both NDTs, such as the SonReb method, was not investigated. Future studies combining the ultrasonic pulse velocity with Schmidt hammer and Lab hardness methods could improve the reliability of NDTs for UCS estimations [78].

6. Conclusions

The purpose of this research was to see whether efficient non-destructive testing (NDTs) such as ultrasonic pulse velocity and Schmidt hammer (R-value) testing can be used to determine the physical and strength properties of granite, marble, and sandstone from North Pakistan. The emphasis of the discussion was on (a) variables that influence NDTs, (b) correlation analysis between physical and strength characteristics, and (c) statistical correlations between NDTs and physical and strength attributes using basic regression analysis. The following findings have been derived from this research:

Weathering and moisture content affect the values of both NDTs. The porosity, density, and grain size of rock are all affected by weathering. The levels of both NDTs in the examined rocks decreased significantly as the weathering grade increased. The UPV has a direct connection with moisture content, but the R-value has an inverse relationship with moisture content.

Both NDTs were shown to be successful in estimating most of the physical parameters of the examined rocks, with a good correlation value (R^2). Except for granite and marble porosity and water absorption, and marble dry density, the UPV was more accurate in assessing other physical properties. Furthermore, the marble's specific gravity did not correlate with either NDT.

Schmidt hammer R-values for determining strength were more consistent, with R^2 values of 0.98, 0.88, and 0.74 for the UCS of granite, marble, and sandstone, respectively, and 0.83 and 0.91 for the UTS of marble and sandstone, respectively. The Schmidt hammer R-values are around the zero-intercept line (with higher $R^2 = 0.89$ and 0.97) when compared to those obtained for UPV ($R^2 = 0.66$ and 0.95), showing that the Schmidt hammer method provided improved accuracy for estimating rock strength.

The correlation equations established from NDT reveal that the strength and physical properties of regularly used rocks may be predicted rather accurately. Although the performance of all empirical models produced in this research was significant as determined by the student's *t*-test, any non-destructive test with a low R^2 value should be used with caution when predicting the attributes. The resulting equations are accurate, simple, and straightforward to use and may be used in the field to provide early predictions of mechanical and physical properties, serving as a crucial reference for masonry structure strengthening and rehabilitation.

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