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# Fractal Characteristics and Controlling Factors of Pore-Throat Structure in Tight Sandstone Reservoirs: A Case Study of the 2nd Member of the Kongdian Formation in the Nanpi Slope, Cangdong Sag, Bohai Bay Basin

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#### **Abstract**

Tight sandstone reservoirs generally exhibit poor physical properties and characterization of microscopic pore structure is crucial for evaluating reservoir quality and fluid flow behavior. Fractal dimension provides an effective means to quantify the complexity and heterogeneity of pore structures in such reservoirs. This study investigates tight sandstone reservoirs of the Kongdian Formation in the Nanpi Slope, Cangdong Sag, using cast thin sections, scanning electron microscopy (SEM), high-pressure mercury injection (HPMI), and constant-rate mercury injection (CRMI) experiments. We establish a full-range fractal model to characterize pore-throat distributions and elucidate the correlation between fractal dimensions and reservoir properties, alongside factors influencing pore-structure heterogeneity. Key findings include that (1) pore types are predominantly residual intergranular pores, intergranular dissolution pores, and clay mineral intercrystalline pores, with throats primarily consisting of sheet-like and curved sheet-like types, exhibiting strong pore-structure heterogeneity; (2) full-range fractal dimensions  $D_1$ ,  $D_2$  and  $D_4$  effectively characterize the heterogeneity of pore structure, where higher  $D_1$  and  $D_2$  values correlate with increased macro-mega pore and micro-fine throat abundance, respectively, indicating enhanced pore connectivity and superior flow capacity, while elevated  $D_4$  reflects greater nano throat complexity, degrading reservoir properties and impeding hydrocarbon flow; (3) compared to conventional methods splicing HPMI and CRMI data at 0.12 µm, the fractalderived integration point more accurately resolves full-range pore-throat distributions, revealing significant disparities in pore-throat size populations; (4) the fractal dimensions  $D_1$ ,  $D_2$ , and  $D_4$  are collectively governed by clay mineral content, average throat radius, displacement pressure, and tortuosity.

**Keywords:** tight sandstone reservoirs; fractal dimensions; full-range pore-throat size distribution; the 2nd Member of the Kongdian Formation; Cangdong Sag

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#### 1. Introduction

Amid growing global imbalances in petroleum supply and demand, unconventional hydrocarbon resources have become increasingly critical to worldwide energy security.

Within this spectrum, tight oil and gas reservoirs hold substantial resource potential and are technically viable for stimulation, positioning them as a pragmatic frontier for reserve growth and production enhancement in China. Significant accumulations have been documented in petroleum-bearing basins such as the Ordos, Bohai Bay, and Sichuan [1–5]. Tight sandstone reservoirs—defined here as those with a porosity < 10% and matrix permeability < 0.1 mD under confining pressure [6]—have drawn extensive research attention in recent years due to their vast resource base. Compared to conventional sandstones, tight sandstone reservoirs exhibit inferior petrophysical properties and have undergone intensive diagenetic alteration, resulting in pronounced pore-structure heterogeneity [7–9]. Pore-throat size distribution exerts more direct control on storage capacity and fluid flow behavior than bulk porosity or permeability alone [10], making its characterization essential for evaluating macroscopic reservoir quality and hydrocarbon mobility. These reservoirs typically feature multiscale pore-throat systems spanning nanometers to micrometers. However, their complex pore-throat geometry, small radii, poor connectivity, and strong heterogeneity pose significant challenges for quantitative microscopic characterization [11–13].

Current research on pore structures in tight sandstone reservoirs primarily employs mercury intrusion porosimetry (MIP) [14,15], scanning electron microscopy (SEM) [16], and nuclear magnetic resonance (NMR) [17,18] to qualitatively characterize geometric and topological parameters—including pore-throat morphology, size distribution, and connectivity. Previous studies have confirmed the fractal nature of complex pore systems in reservoir rocks [19–24]. Fractals are defined as self-similar objects exhibiting scale-invariant properties [25], with such structures characterized quantitatively by the fractal dimension (*Df* or *D*) [21]. Since Mandelbrot's conceptualization of fractals [25], fractal theory and methodology have been extensively applied in petroleum exploration and development [22,26,27]. This approach effectively interprets the irregularity, instability, and high complexity inherent to pore structures [27–29], while providing a critical bridge linking microscopic pore architecture (throat size, pore-throat distribution, connectivity) to macroscopic petrophysical properties (porosity, permeability) [22,28].

Previous studies characterizing the fractal dimensions of rock pore structures using mercury injection methods have typically relied on a single technique—either high-pressure mercury injection (HPMI) or constant-rate mercury injection (CRMI). However, due to the shielding effect of HPMI on large pore throats and the pressure limitation of CRMI (maximum 6.2 MPa), both approaches exhibit inherent limitations in comprehensively characterizing pore structure heterogeneity when used independently. Specifically, HPMI provides higher accuracy for small pore-throat distributions, whereas CRMI more precisely resolves large pore-throat distributions. To integrate pore-throat data across the full scale, prior studies often simply spliced HPMI-derived distributions (<0.12 μm) with CRMIderived distributions (>0.12 μm) at a fixed threshold of 0.12 μm. Critically, this splicing approach neglects the overlapping pore-throat range near 0.12 μm observed in both HPMI and CRMI data [30], leading to partial loss of pore-throat distribution data and thus failing to reflect the true full-range pore-throat structure. Furthermore, existing research lacks systematic investigations into the correlations between fractal dimensions (quantifying pore structure heterogeneity) and reservoir properties/fluid flow behaviors, as well as their controlling factors. Consequently, it remains challenging to quantitatively evaluate the impact of pore-throat structures on tight reservoir properties and hydrocarbon migration.

The Nanpi Slope in the Cangdong Sag, a representative tight sandstone oil-gas province within the Huanghua Depression of the Bohai Bay Basin, exhibits complex reservoir characteristics in Member 2 of the Paleogene Kongdian Formation, including inherently low permeability, multiscale pore-throat heterogeneity, elevated capillary resistance, and

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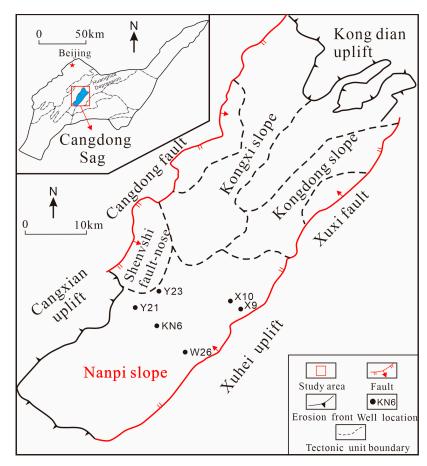
highly variable oil–water relationships and oil saturation [10,30,31]. Critically, prior studies lack systematic characterization of hierarchical (nano-to-micron-scale) pore-throat structures through multi-parameter integration, hindering further exploration and development of tight oil reservoirs. To address this gap, we employ an integrated experimental approach combining cast thin-section imaging, SEM, HPMI and CRMI to comprehensively quantify multiscale pore architecture in the study area. Specifically, we focus on deriving full-range fractal dimensions by synergizing HPMI and CRMI data to characterize pore-throat heterogeneity, establishing quantitative correlations between fractal dimensions, reservoir properties, and fluid flow behavior, and elucidating key controls on fractal signatures. This research provides a novel framework for quantitatively evaluating pore-structure heterogeneity and its impact on fluid mobility, offering critical insights for optimizing tight oil recovery.

## 2. Geological Background

The Cangdong Sag, situated in the southern Huanghua Depression of the Bohai Bay Basin, is bounded by the Kongdian Uplift to the north, Dongguang Uplift to the south, Cangxian Swell to the west, and Xuhei Uplift to the east. As the second-largest hydrocarbon-rich sag within the Huanghua Depression, it covers a total exploration area of 4700 km². This sag developed under a regional extensional regime, evolving into an elongated Cenozoic rift basin that tapers from southwest to northeast. Its structural framework comprises two positive structural belts—the Kongdian Structural Belt and Shenüsi Fault Nose—along with three slope systems: the Western Kongxi Slope, Eastern Kongdong Slope, and Nanpi Slope [31,32].

The Nanpi Slope, situated in the southern Cangdong Sag of the Bohai Bay Basin, comprises four sub-sags and seven secondary structural belts, structurally partitioned into three distinct zones: the Low-Slope Zone, Mid-Slope Zone, and High-Slope Zone (Figure 1). This area hosts a thick succession of the Paleogene Kongdian Formation, formally divided into the Kong 1 (Ek<sub>1</sub>), Kong 2 (Ek<sub>2</sub>), and Kong 3 (Ek<sub>3</sub>) members. During the deposition of the Kong 2 Member, braided river delta systems extensively developed across the gentle paleotopography, with facies distribution controlled by slope gradient: delta plain deposits dominated the High-Slope Zone, delta front facies prevailed in the Mid-Slope Zone, and prodelta to distal lacustrine fan sediments accumulated in the Low-Slope Zone. The Kong 2 reservoirs consist predominantly of gray fine-grained siltstones and sandstones, classified lithologically as arkosic sandstones and lithic arkoses.

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**Figure 1.** Structural unit division and study area location of the Nanpi slope in Cangdong Sag, Baihai Bay Basin (Adapted from [33]).

# 3. Samples and Methods

### 3.1. Sample Characteristics and Analytical Procedures

Forty-one tight sandstone samples were collected from the 2nd member of the Kongdian Formation (Kong 2 Member) in the Nanpi Slope of the Cangdong Sag. These samples were subjected to comprehensive analyses including cast thin section observation, SEM, X-ray diffraction (XRD) and HPMI. Nine representative tight sandstone samples, all identified as gray silt-fine sandstones, were selected for additional coupled analyses of CRMI and micro-CT scanning. The nine selected samples were drilled into standard core plugs with a diameter of 2.5 cm and a length of 3.0 cm, followed by cleaning and oven-drying. A series of sequential experiments were conducted on each core plug: first, conventional porosity and permeability were measured; then, mercury intrusion experiments were performed; finally, the samples were ground into thin sections for optical microscopy observation and SEM analysis.

HPMI experiments were carried out using an AutoPore IV 9505 mercury intrusion porosimeter (Micromeritics, Norcross, GA, USA). The experiments included both mercury intrusion (under increasing pressure) and extrusion (under decreasing pressure) processes, with a maximum applied pressure of 200 MPa, enabling the measurement of pore-throat radii as small as approximately 3.6 nm. Constant-rate mercury intrusion experiments were performed using a Coretest ASPE-730 CRMI instrument (Coretest Systems Inc., Roseville, CA, USA), with a maximum intrusion pressure of 900 psi (6.2 MPa), corresponding to a minimum measurable throat radius of approximately 0.12  $\mu$ m. Mercury was injected into the core samples at a constant ultra-low rate of 0.0001 mL/min under a temperature of 25 °C. The identification of pores and throats in the reservoir was based on the sudden

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drop and subsequent recovery of pressure during the intrusion process. CT scanning was conducted using a Carl Zeiss Xradia 520 Versa 3D X-ray microscope (Carl Zeiss AG, Pleasanton, CA, USA). Based on 3D CT scanning data, image analysis techniques (processed using Avizo 2023 and Image J 1.54 software) were applied to characterize the internal mineral composition, pore structure, and their distribution characteristics within the cores. This included quantifying parameters of pores, throats, and minerals, as well as generating 2D and 3D spatial visualizations to illustrate their morphological features and spatial distributions. Nuclear magnetic resonance (NMR) experiments were conducted using an Oxford-MARAN DRX 2 NMR spectrometer (Oxford Instruments plc, Abingdon, Oxfordshire, UK). The NMR T<sub>2</sub> spectrum was employed to analyze the occurrence state (movable or bound) of fluids within core pores, quantitatively determining both movable fluid saturation and bound fluid saturation. Movable fluid saturation reflects the relative proportion of fluid-flowable pore space within the porous rock media. All the involved equipment information is showed in Table 1.

<b>Experimental Method</b>	Experimental Method Instrument Name/Model		City and Country
HPMI	AutoPore IV 9505	Micromeritics Instrument Corporation	Norcross, GA, USA
CRMI	Coretest ASPE-730	Coretest Systems Inc.	Roseville, CA, USA
Micro CT	Carl Zeiss Xradia 520 Versa	Carl Zeiss AG	Pleasanton, CA, USA
SEM	TM4000plus	Hitachi	Tokyo, Japan
NMR	MARAN DRX 2	Oxford Instruments plc	Abingdon, Oxfordshire, UK
XRD	D8 ADVANCE	Bruker	Karlsruhe, Germany

Table 1. The involved equipment information.

### 3.2. Fractal Theory

Fractal theory is an effective approach to describe the complexity and heterogeneity of pore structures in tight sandstone reservoirs [34]. The internal pore structure of porous rocks typically exhibits a non-integer dimension, with the ideal fractal dimension ranging between 2 and 3 [34]. A fractal dimension closer to 2 indicates a more uniform distribution of pore throats and stronger homogeneity within the rock, whereas a value closer to 3 signifies greater heterogeneity of pore throats. An increase in the fractal dimension reflects a transformation in the pore morphology of tight sandstones from regular to complex, which reduces permeability and impedes the migration of pore fluids [35]. Due to the highly complex nature of pore throats in tight sandstones, their distribution usually encompasses multiple fractal intervals. Consequently, the pore structure can be characterized by multiple fractal dimensions, meaning that tight sandstones possess multifractal dimensions [36,37].

A computational model was established based on mercury intrusion porosimetry (MIP) data to calculate the fractal dimension. This model has been widely applied in the study of pore structures in unconventional reservoirs and exhibits the best performance when used for tight sandstone reservoirs [38]. Based on fractal theory, Reference [37] derived a calculation model for the fractal dimension of pore structures using mercury saturation ( $S_{Hg}$ ) and capillary pressure ( $p_c$ ) obtained from MIP experiments, which is shown as follows:

$$S_{Hg} = ap_c^{-(2-D)},$$
 (1)

where a is a constant; *D* is the fractal dimension.

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Typically, the relationship between mercury saturation and capillary pressure is plotted on a double logarithmic coordinate system, thus yielding the following equation:

$$\lg S_{Hg} = (D-2)\lg p_c + C,\tag{2}$$

where *C* is a constant.

Therefore, the fractal dimension of the tight sandstone pore structure can be obtained by plotting the cross-plot of  $\lg S_{\rm Hg}$  versus  $\lg p_{\rm c}$ . Due to the multifractal characteristics of tight sandstone pore structures [17], the following steps were performed: first, fractal intervals were divided on the cross-plot; second, segmented linear regression was conducted within different fractal intervals to determine the slope K for each interval; finally, the fractal dimension of each fractal interval was derived from the slope, specifically:

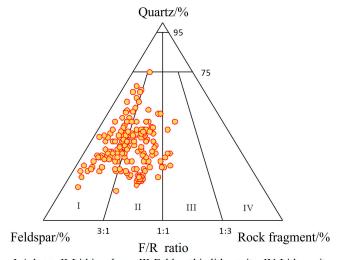
$$D = K + 2 \tag{3}$$

where *K* is the slope of each fractal interval in the cross-plot of  $\lg S_{Hg}$  versus  $\lg p_c$ .

## 4. Characteristics of Pore Structure in Tight Sandstone Reservoirs

### 4.1. Types of Pores and Throats in Tight Sandstone Reservoirs

The reservoir rocks in the 2nd member of the Kongdian Formation (Kong 2 Member) of the Cangdong Sag are predominantly feldspathic sandstones and lithic feldspathic sandstones (Figure 2). The quartz content ranges from 15.6% to 75.1% with an average of 37.12%, while feldspar content varies from 18% to 77.3% (average: 44.48%) and lithic content ranges from 0.8% to 38% (average: 18.2%). The sandstones have a sorting coefficient of 1.3–2.1 and are mainly subangular to subrounded in terms of roundness. Grain sizes are dominated by fine sandstone and siltstone. In the study area, the porosity of the Kong 2 Member ranges from 2.1% to 18.5% with an average of 11.01%, and the permeability varies from 0.01 mD to 73 mD, with a mean value of 5.82 mD.

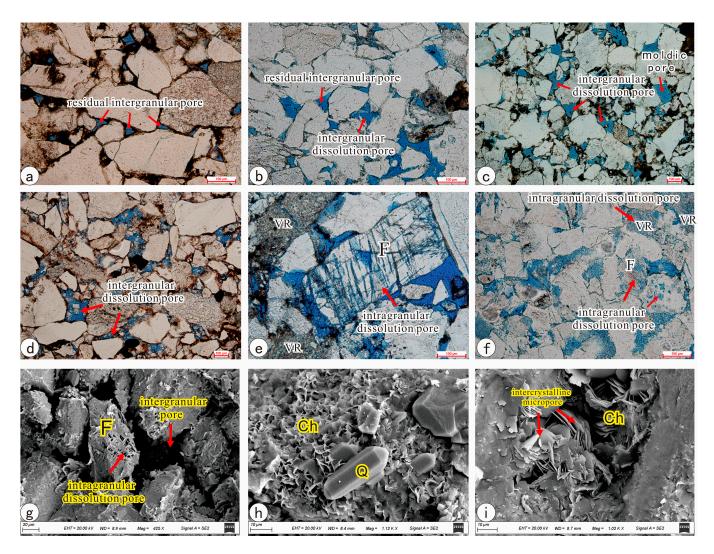


I-Arkose, II-Lithic arkose, III-Feldspathic litharenite, IV-Litharenite

**Figure 2.** Ternary diagram showing the QFL detrital composition of the Kong 2 sandstones in the Nanpi Slope plotted.

Based on observations from cast thin sections and SEM, three types of pores are predominantly developed in the tight sandstones of the Kong 2 Member in the study area: intergranular pores, intragranular pores, and micropores within clay mineral intercrystalline spaces (Figure 3). Among these, intergranular pores are the most widely developed and distributed, dominated by residual intergranular dissolved pores (Figure 3a,b,g), Fractal Fract. 2025, 9, 608 7 of 23

followed by intergranular dissolved pores (Figure 3c). Intragranular dissolved pores primarily include feldspar dissolution pores (Figure 3e,g) and lithic fragment dissolution pores (Figure 3f), with residual debris from particle dissolution visible within the pores (Figure 3d). Micropores within clay mineral intercrystalline spaces are mainly composed of chlorite intercrystalline pores and illite intercrystalline pores (Figure 3h,i).



**Figure 3.** Microscopic characteristics of pore and throat types of tight sandstone reservoirs in the Kongdian Formation in the Nanpi Slope. (a) Residual intergranular pores developed, Well X10, 3547.8 m, PPL; (b) residual intergranular pores and intergranular dissolution pores, Well KN6, 3746 m, PPL; (c) intergranular dissolution pores developed, with locally observed feldspar dissolution cast molds, Well X9, 3524.8 m, PPL; (d) intergranular dissolution pores developed, showing grain dissolution residues, Well X10, 3540.2 m, PPL; (e) feldspar intragranular dissolution pores, Well KN6, 3570.3 m, PPL; (f) lithic fragment and feldspar intragranular dissolution pores developed, Well W26, 3632.3 m, PPL; (g) intergranular pores, feldspar dissolution pores, and clay minerals (e.g., illite-smectite mixed-layer) in intergranular/grain-surface, Well X10, 3545.5 m, SEM; (h) grain-surface microcrystalline quartz and clay minerals (e.g., chlorite), Well X9, 3930.15 m, SEM; (i) intercrystalline micropores in intergranular chlorite, Well X10, 3545.5 m, SEM. F: feldspar; Ch: Chlorite; Q: quartz; VR: volcanic rock fragment.

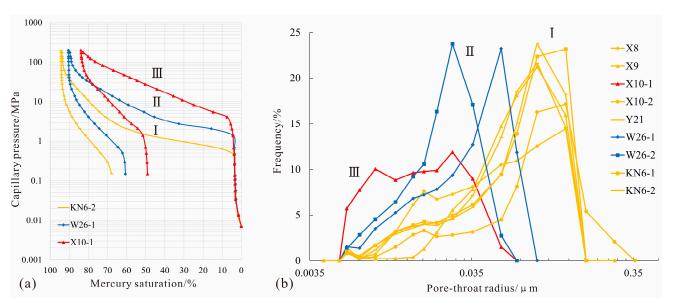
The tight sandstone reservoirs of the Kongdian Formation in the study area are dominated by lamellar and curved-lamellar throats (Figure 3a–c), with local occurrences of tubular-bundle throats (Figure 3f,h,i). Clay minerals typically fill intergranular and intragranular dissolution pores; however, they also form capillary-interwoven tubular-

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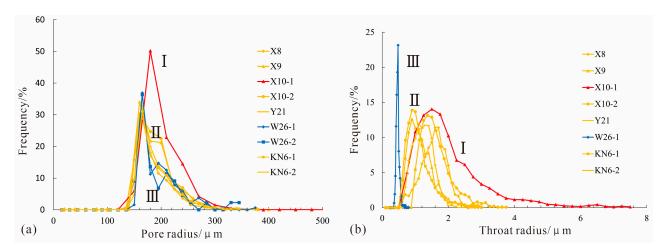
bundle throats, making such throats most prevalent in sandstones rich in clay minerals. During the later stage of hydrocarbon charging, these tubular-bundle throats can act both as storage spaces for fluids and as pathways for fluid migration.

#### 4.2. Pore-Throat Distribution Characteristics of Tight Sandstone Reservoirs

Analysis of the physical property data from the study area reveals that the tight sandstone reservoirs exhibit significant variations in physical properties. The porosity ranges from 4.32% to 12.54% with an average of 9.37%, while the permeability is mainly distributed between 0.021 and 0.634 mD, averaging 0.249 mD. These characteristics classify the reservoirs as typical ultra-low porosity and low permeability reservoirs. Based on the analysis of capillary pressure curves and pore-throat radius distribution characteristics derived from high-pressure mercury intrusion porosimetry (Figures 4 and 5), the nine core samples are categorized into three types (Type I, II, and III) according to the morphology of the capillary pressure curves and other pore structure parameters (Tables 2 and 3).



**Figure 4.** Pore structure classification based on high-pressure mercury injection data (HPMI). (a) Characteristics of capillary pressure curve of different samples; (b) pore-throat radius distribution characteristics of different samples.



**Figure 5.** Characterization of pore radius (a) and throat radius (b) distribution based on constant-rate mercury injection (CRMI) experiments. I, II and III represent the pore structure types, the red dot line is type I, the yellow dot line is type II, and the sky blue dot line is type III.

<b>Table 2.</b> The key characteristic parameters of different type	es of pore structures based on HPMI
experiment.	

Pore Structure Type	Sample No.	Depth /m	Porosity /%	Permeability /mD	Ra /μm	Rp /μm	R50 /μm	Sp	Skp	D	α	SHgmax /%	We /%	Pd /Mpa
I	KN6-2	3750.30	11.78	8.155	1.587	0.488	0.507	2.431	0.589	4.496	0.307	94.332	28.19	0.463
	KN6-1	3746.00	9.97	2.6099	1.585	0.539	0.555	2.028	0.525	3.38	0.34	98.319	29.164	0.464
	X8	3484.20	8.19	0.355	1.577	0.442	0.232	2.584	0.305	6.404	0.28	89.353	29.597	0.466
	Y21	3511.60	11.44	0.31	1.579	0.445	0.458	1.98	0.481	3.968	0.282	96.988	24.034	0.465
	X10-2	3547.80	7.86	0.281	2.844	0.685	0.366	3.446	0.507	6.186	0.241	71.048	21.052	0.258
	X9	3522.70	6.91	0.271	1.578	0.457	0.466	2.145	0.495	4.137	0.289	90.079	24.111	0.466
II	W26-1	3623.30	11.31	0.078	0.533	0.19	0.145	2.176	0.451	12.204	0.356	90.497	33.008	1.379
	W26-2	3634.30	12.54	0.044	0.269	0.091	0.085	1.707	0.418	18.029	0.338	94.668	32.115	2.737
III	X10-1	3533.85	4.32	0.021	0.268	0.063	0.028	2.132	0.036	39.109	0.235	83.928	41.565	2.746

Ra: maximum pore-throat radius; Rp: average pore-throat radius; R50: median pore-throat radius; Sp: sorting coefficient; Skp: skewness; D: relative sorting coefficient;  $\alpha$ : homogeneity coefficient;  $S_{Hg}$ max: maximum mercury intrusion saturation; We: mercury withdrawal efficiency; Pd: displacement pressure.

**Table 3.** The key characteristic parameters of different types of pore structures based on CRMI experiment.

Pore Structure Type	Sample No.	Depth /m	Porosity /%	Permeability /mD	Rt /μm	Rp /μm	η	Rmax /μm	Sf /%	Sp /%	St /%	ε	λ	Pd /MPa
I	KN6-2	3750.30	11.78	8.155	1.116	190.579	197.033	5.568	56.102	19.046	37.056	0.514	2.766	0.132
	KN6-1	3746.00	9.97	2.6099	1.113	190.225	196.131	2.082	65.413	26.650	38.763	0.688	10.797	0.353
	X8	3484.20	8.19	0.355	1.562	185.848	131.349	1.667	47.218	8.642	38.576	0.224	11.490	0.441
	Y21	3511.60	11.44	0.31	1.234	189.573	171.072	1.581	73.849	26.937	46.912	0.574	20.714	0.465
	X10-2	3547.80	7.86	0.281	1.621	192.413	129.019	1.525	70.423	29.156	41.267	0.707	17.422	0.482
	X9	3522.70	6.91	0.271	1.188	190.889	185.782	1.503	60.060	17.757	42.303	0.420	13.976	0.489
II	W26-1	3623.30	11.31	0.078	0.468	196.453	411.507	0.929	50.312	5.895	44.417	0.133	30.275	0.791
	W26-2	3634.30	12.54	0.044	7.000	194.318	436.071	0.745	42.446	0.860	41.586	0.021	33.796	0.986
III	X10-1	3533.85	4.32	0.021	16.250	205.313	100.000	0.560	31.031	0.387	30.644	0.013	25.372	1.312

Rt: average throat radius; Rp: average pore radius;  $\eta$ : average pore-throat radius ratio; Rmax: maximum connected pore-throat radius; Sf: final mercury injection saturation; Sp: total pore mercury injection saturation; St: total throat mercury injection saturation;  $\epsilon$ : total pore/throat volume ratio;  $\lambda$ : tortuosity; Pd: displacement pressure.

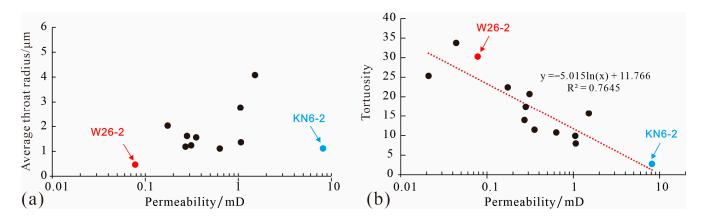
Type I samples include X-8, X-9, X10-2, Y21, KN6-1, and KN6-2, which are characterized by a flat middle segment in the mercury intrusion curve and coarse skewness (Figure 4a). The average displacement pressure and maximum pore-throat radius are 0.39 MPa and 1.79 µm, respectively. The pore-throat distribution frequency is predominantly unimodal (Figure 4b), with the peak ranging from 0.05 to 0.17 μm, showing a high and more concentrated peak. Samples of this type have larger pores, better physical properties, relatively concentrated pore-throat distribution, and good sorting and connectivity. Type II samples include W26-1 and W26-2. Their mercury intrusion curves exhibit a relatively flat middle segment with coarse skewness (Figure 4a). The pore-throat distribution frequency is mainly unimodal, with the peak primarily distributed between 0.017 and 0.026 μm. The average displacement pressure and maximum pore-throat radius are 2.05 MPa and 1.48 µm, respectively. Compared with Type I samples, Type II samples have poorer pore size; the presence of more small pores results in worse sorting and connectivity. Type III samples are represented by X10-1, featuring a non-flat middle segment with an indistinct platform and fine skewness in the mercury intrusion curve (Figure 4a). The average displacement pressure and maximum pore-throat radius are 2.75 MPa and 0.27 µm, respectively. The pore-throat distribution frequency is dominated by an indistinct bimodal pattern (Figure 4b), with peaks mainly distributed in the range of 0.005–0.035 μm and a wide distribution range. Samples of this type have high displacement pressure, poor pore-throat connectivity and sorting, the most complex pore structure, and strong heterogeneity.

Constant-rate mercury intrusion experiments were performed on tight sandstone samples from the study area. The results showed that the average values of final mercury saturation, total pore mercury saturation, and total throat mercury saturation across all

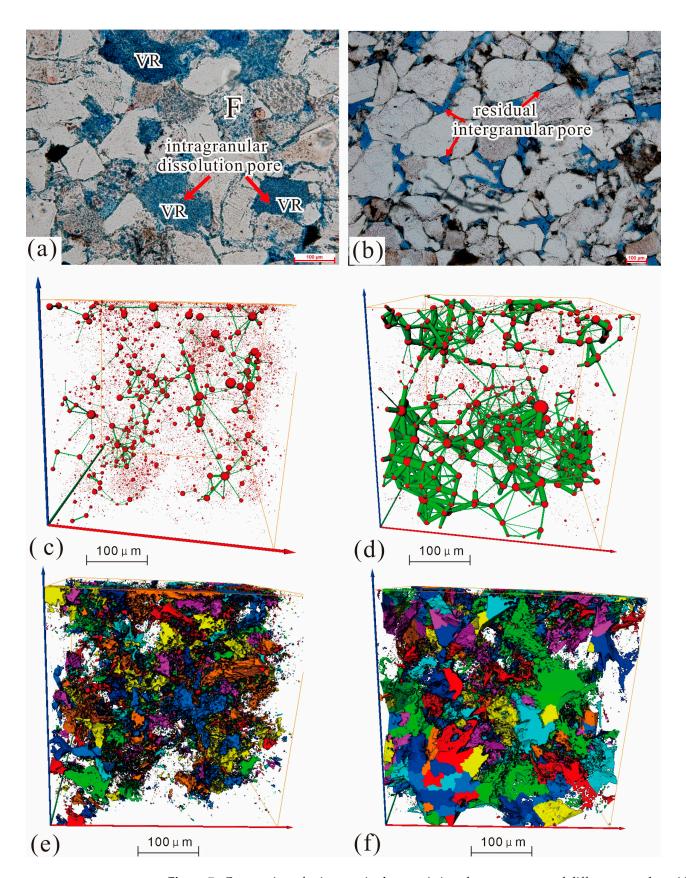
samples were 55.206%, 15.037%, and 40.169%, respectively. Notably, the pore mercury saturation was significantly lower than the throat mercury saturation, indicating poor pore connectivity. This suggests that a large number of isolated pores are present, which are not connected by throats.

Analysis of the distribution frequency curves of pores and throats reveals that the pore radii of all samples are mainly distributed in the range of 150 to 300  $\mu$ m (Figure 5a), with a relatively consistent distribution pattern. The average pore radius ranges from 185.85 to 205.31  $\mu$ m, with a peak value around 190  $\mu$ m. In contrast, the average throat radius varies significantly from 0.468 to 16.25  $\mu$ m (Figure 5b), showing a distinct differential distribution. This marked variability in throat distribution results in abnormally large pore-throat ratios. The pore-throat radius ratios of the samples exhibit a wide range of variation, with their average values ranging from 100.01 to 436.07.

The pore-throat morphologies of tight sandstone samples in the study area are complex. In addition to the controls of pore and throat sizes on reservoir physical properties, the morphology (tortuosity) of pore throats also exerts a significant influence on permeability (Figure 6). For instance, sample W26-2 has a porosity of 11.31%, permeability of 0.078 mD, average throat radius of 0.47 µm, and tortuosity of 30.27; in contrast, sample KN6-2 exhibits a porosity of 11.78%, permeability of 8.155 mD, average throat radius of 1.12 μm, and tortuosity of 2.76. Under the condition that the differences in porosity and average throat radius are insignificant, sample W26-2 has low permeability due to its dominant pore types being intraclastic micropores and intra-matrix micropores (Figure 7a), accompanied by well-developed micro-nano throats with complex morphologies and high tortuosity. CT results indicate that sample W26-2 contains fine throats and poor pore connectivity (Figure 7c,e). Sample KN6-2 is characterized by residual intergranular pores and intergranular dissolution pores as the main pore types, with sheet-like and necking-type throats as the dominant throat types (Figure 7b). The simple throat morphology and low tortuosity contribute to its high permeability. CT results reveal that sample KN6-2 has coarser throats and better pore connectivity (Figure 7d,f).



**Figure 6.** Plots showing correlation between permeability and average throat radius (**a**), and correlation between permeability and tortuosity (**b**) in tight sandstone samples in the Kongdian Formation in the Nanpi Slope.

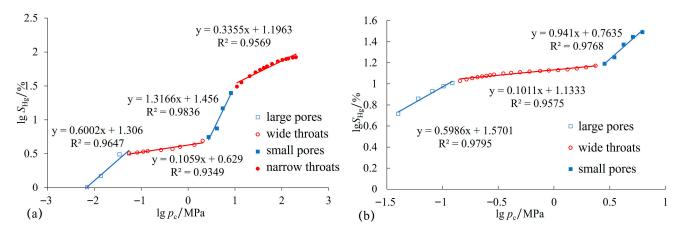


**Figure 7.** Compaction of microscopic characteristics of pore structure of different samples with different tortuosity. (**a**,**b**) Casting thin photograph showing the characteristics of various pores and throats, occurred in blue color; (**c**,**d**) Sphere-stick model of pore and throats, the red spheres represent pores and green sticks represent throats; (**e**,**f**) 3D visualization of pore connectivity network of the sub-volumes, the pores colored in the same color are connected. (**a**,**c**,**e**) from sample W26-2, 3632.3 m, (**b**,**d**,**f**) from sample KN6-2, 3750.3 m. F: feldspar; VR: volcanic rock fragment.

#### 4.3. Fractal Characteristics of Pore-Throat in Tight Sandstone Reservoirs

# 4.3.1. Fractal Dimensions Based on High-Pressure Mercury Intrusion and Constant-Rate Mercury Intrusion

Based on the capillary pressure curves derived from high-pressure mercury intrusion and constant-rate mercury intrusion experiments, scatter plots were generated to illustrate the relationship between the logarithm of mercury saturation ( $\lg S_{Hg}$ ) and the logarithm of capillary pressure ( $\lg p_c$ ) for each sample. Taking sample X10-1 as an example (Figure 8), analysis of the fractal dimension fitting curves from high-pressure and constant-rate mercury intrusion data of the nine samples revealed that most fractal fitting curves exhibit 3 or 4 segments. Segmented linear fitting was performed using the least squares method, and the fitting correlation coefficients ( $R^2$ ) for each segment range mainly from 0.6481 to 0.9920, with an average of 0.9560 (Tables 4 and 5). These results indicate that the pore-throat structures of the tight sandstones in the Kongdian Formation of the study area possess distinct multifractal characteristics.



**Figure 8.** Fractal dimension fitting curve for sample X10-1 based on high-pressure mercury injection method (**a**) and constant-rate mercury injection method (**b**).

<b>Table 4.</b> Fractal dimension ( $D$ ), $R^2$ value, and cross-point throat radius from high-pressure mercury
injection (HPMI) for tight sandstone samples in the study area.

Sample No.	Depth /m	Porosity /%	Permeability /mD	$D_{\mathrm{h}1}$	$R^2$	$D_{ m h2}$	$R^2$	$D_{\mathrm{h3}}$	R <sup>2</sup>	$D_{ m h4}$	$R^2$	r <sub>h1</sub> /μm	r <sub>h2/</sub> μm	r <sub>h3/</sub> μm
KN6-2	3750.30	11.78	8.155			2.1881	0.8922	3.3166	0.9836	2.0786	0.9041		2.8283	0.3564
KN6-1	3746.00	9.97	2.6099	0.9903	0.9617	2.1224	0.9817	3.3166	0.9836	2.0803		21.3951	2.8587	0.3596
X8	3484.20	8.19	0.355	2.6176	0.9985	2.1791	0.9826	4.0343	0.9329	2.1547	0.8453	21.3932	1.5768	0.5398
Y21	3511.60	11.44	0.31			2.1676	0.9686	3.3166	0.9836	2.091	0.8451		2.8431	0.3589
X10-2	3547.80	7.86	0.281	2.542	0.9803	2.1542	0.9514	3.3166	0.9836	2.0657	0.8899	21.3920	2.8442	0.3583
X9	3522.70	6.91	0.271	2.6776	0.9999	2.1413	0.9661	3.6906	0.9818	2.0424	0.6481	21.3932	2.8496	0.3578
W26-1	3623.30	11.31	0.078	2.6541	0.9908	2.0768	0.9583	3.3166	0.9836	2.1456	0.8847	21.3951	1.0845	0.5329
W26-2	3634.30	12.54	0.044			2.1077	0.9603	3.3166	0.9836	2.1316	0.87	0.5405	0.0667	
X10-1	3533.85	4.32	0.021	2.6002	0.9647	2.1059	0.9349	3.3166	0.9836	2.3355	0.9569	21.4051	0.3585	0.0890

**Table 5.** Fractal dimension (D),  $R^2$  value, and cross-point throat radius from constant-rate mercury injection (CRMI) for tight sandstone samples in the study area.

Sample No.	Depth /m	Porosity /%	Permeability /mD	$D_{c1}$	$R^2$	$D_{c2}$	$R^2$	$D_{c3}$	$R^2$	$D_{c4}$	$R^2$	$r_{c1}/\mu m$	$r_{c2}/\mu m$	$r_{c3}/\mu m$
KN6-2 KN6-1 X8 Y21 X10-2 X9 W26-1 W26-2 X10-1	3750.30 3746.00 3484.20 3511.60 3547.80 3522.70 3623.30 3634.30 3533.85	11.78 9.97 8.19 11.44 7.86 6.91 11.31 12.54 4.32	8.155 0.634 0.355 0.31 0.281 0.271 0.078 0.044 0.021	3.5696 2.7259 2.7805 2.8106 2.7979 2.7336 2.6914 2.6328 2.5986	0.9509 0.9941 0.9949 0.9922 0.9945 0.9983 0.9813 0.9875 0.9795	2.4013 2.39 2.321 2.288 2.4157 2.3638 2.1379 2.1261 2.1011	0.9951 0.9613 0.9948 0.9898 0.9962 0.9956 0.9613 0.9586 0.9575	3.3481 3.7054 3.33398 3.7311 3.2486 3.0984 3.7054 3.2778 2.941	0.9785 0.9992 0.9882 0.9892 0.9817 0.992 0.9992 0.8876 0.9768	2.2406 2.3605 2.4025 2.2346 2.1377 2.2798 2.3605	0.9416 0.9852 0.9822 0.9357 0.9317 0.9572 0.9852	11.1097 7.0058 8.6380 8.6273 8.8572 8.7925 6.9818 5.9017 5.9932	1.8374 2.5205 2.5128 2.0721 2.5275 2.5255 0.6874 0.3123 0.3112	0.6875 0.5507 1.2133 0.9800 0.9808 0.6780 0.3820

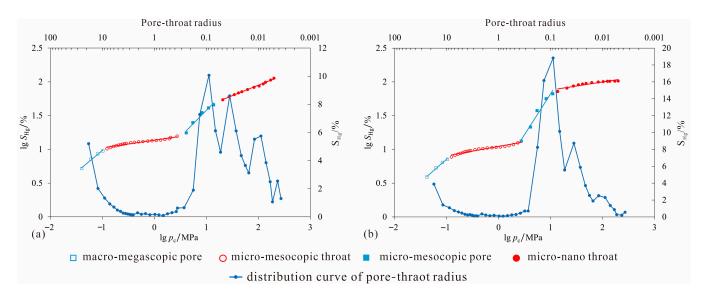
Since the fractal dimension fitting curve is derived from the scatter points converted from the mercury intrusion curve, the morphology of the fractal curve is in good agreement with that of the mercury intrusion curve. When the mercury intrusion curve has a high slope, the linear fitting slope of the converted fractal curve is also high, resulting in a larger fractal dimension; conversely, a smaller fractal dimension is generated [37–39]. Considering that both high-pressure mercury intrusion and constant-rate mercury intrusion experiments involve a continuous mercury intrusion process, it is assumed that mercury preferentially enters large pore-throat spaces first and then small ones. With a certain initial pressure applied, the non-wetting mercury first enters larger pores. Subsequently, as the pressure increases, the amount of mercury intrusion becomes very small, indicating that the non-wetting mercury is entering the throats. Based on this principle, pores and throats can be distinguished using the fractal dimension fitting curve.

In this study, the fractal dimensions corresponding to the two left segments of the fractal dimension fitting curves derived from high-pressure mercury intrusion and constant-rate mercury intrusion—representing large pores and wide throats—are defined as  $D_{h1}$ ,  $D_{h2}$  and  $D_{c1}$ ,  $D_{c2}$ , respectively. The fractal dimensions corresponding to the two right segments, which reflect small pores and narrow throats, are defined as  $D_{h3}$ ,  $D_{h4}$  and  $D_{c3}$ ,  $D_{c4}$ , respectively. The pore-throat radii at the intersection points are defined as  $r_{h1}$ ,  $r_{h2}$ ,  $r_{h3}$  and  $r_{c1}$ ,  $r_{c2}$ ,  $r_{c3}$ , corresponding to the boundary radii of large pores, wide throats, small pores, and narrow throats (Tables 4 and 5).

This study focuses on characterizing the full-pore-size fractal features by combining HPMI and CRMI data. Specifically, the average value of two critical radii was first calculated:  $r_{h2}$ , the boundary radius separating large and small pore throats derived from the fractal dimension fitting curve of HPMI (Table 4), and  $r_{c2}$ , the corresponding boundary radius from the fractal dimension fitting curve of CRMI (Table 5). Using this average radius as the splicing point, the right segment of the HPMI curve (reflecting small pores and narrow throats) was merged with the CRMI curve (reflecting large pores and wide throats) for each sample to generate a full-pore-size fractal dimension fitting curve. This integrated curve was then used to investigate the fractal characteristics across the entire pore size range.

As shown in Figure 9, the full-pore-size fractal dimension fitting curve of tight sandstone samples exhibits a good coupling relationship with the pore-throat radius distribution curve. Since mercury intrusion porosimetry involves a continuous mercury injection process, with a certain initial pressure applied, the non-wetting mercury preferentially enters larger pores. Subsequently, as the pressure continues to increase, the amount of mercury intrusion becomes minimal, indicating that the non-wetting mercury is entering the throats. This allows the differentiation between pores and throats using the fractal dimension fitting curve [37]. In addition, because the fractal dimension fitting curve is derived from the scatter fitting of the transformed mercury intrusion curve, a high slope of the mercury intrusion curve corresponds to a high linear fitting slope of the transformed fractal curve, resulting in a larger fractal dimension; conversely, a lower slope leads to a smaller fractal dimension [37,39]. Based on the above principles and with reference to the pore-throat classification criteria proposed by Hartmann and Beaumont [40], the full-pore-size fractal dimensions of tight sandstone samples in the study area are divided into four intervals: macro-mega pores, micro-fine throats, micro-small pores, and micro-nano throats, which are defined as  $D_1$ ,  $D_2$ ,  $D_3$ , and  $D_4$ , respectively. Taking samples X10-1 and W26-2 as examples, the superposition of the full-pore-size fractal dimension fitting curve and the pore-throat radius distribution curve (Figure 9a,b) shows that non-wetting mercury first enters mega pores larger than 10.00 µm, corresponding to the full-pore-size fractal dimension  $D_1$ . Subsequently, as the pressure increases within the range of 0.50–10.00  $\mu$ m, the amount

of non-wetting mercury intrusion remains minimal, indicating that mercury is entering relatively wide micro-fine throats, which corresponds to the full-pore-size fractal dimension  $D_2$ . When the mercury intrusion pressure increases slightly within the range of 0.10 to 0.50  $\mu$ m, the mercury intrusion volume surges, indicating that mercury is entering micro-medium pores, corresponding to the full-pore-size fractal dimension  $D_3$ . Finally, mercury enters micro-nano throats smaller than 0.10  $\mu$ m, which corresponds to the full-pore-size fractal dimension  $D_4$ .

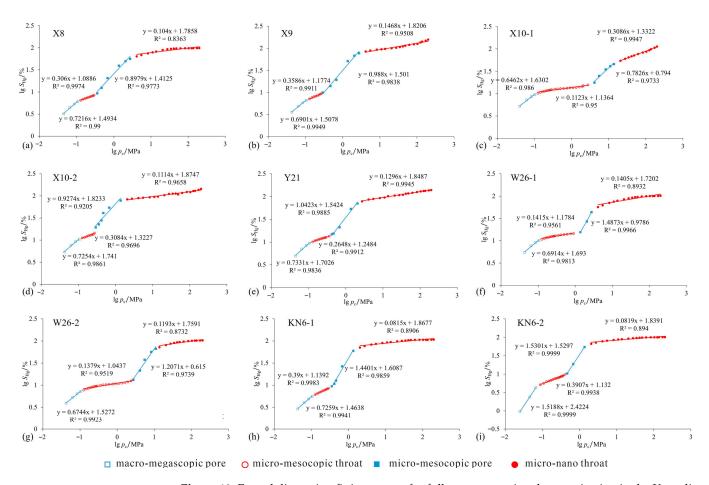


**Figure 9.** Fractal dimension fitting curves and throat radius distribution plots for sample X10-1 (a) and sample W26-2 (b).

Analysis of the full-pore-size fractal fitting curves (Figure 10) reveals that all samples exhibit four distinct segments in their fractal dimension fitting curves, which provides a more reasonable characterization of the fractal features of pore structures compared to using high-pressure mercury intrusion porosimetry or constant-rate mercury intrusion alone. As shown in Table 6, the fractal dimensions of macro–mega pores ( $D_1$ ), micro-fine throats ( $D_2$ ), and micro–nano throats ( $D_4$ ) range from 2.7919 to 3.5188, 2.2678 to 2.3907, and 2.1359 to 2.3086, with average values of 2.6462, 2.1123, and 2.0815, respectively. In contrast, the full-pore-size fractal dimension of micro-small pores ( $D_3$ ) is generally greater than 3 (Table 6). Since the ideal fractal dimension for the internal pore structure of rocks is recognized to fall within the range of 2 to 3 [34], this interval ( $D_3$ ) does not exhibit ideal fractal characteristics. Therefore, subsequent analyses will focus primarily on the fractal dimensions of macro–mega pores ( $D_1$ ), micro-fine throats ( $D_2$ ), and micro–nano throats ( $D_4$ ).

**Table 6.** Full-range pore size fractal dimensions and  $R^2$  coefficients characterized by integrated HPMI and CRMI in the Kongdian Formation tight sandstones.

Sample No.	Depth /m	Porosity /%	Permeability /mD	$D_1$	$R^2$	$D_2$	$R^2$	$D_3$	$R^2$	$D_4$
KN6-2	3750.30	11.78	8.155	3.5188	0.9999	2.3907	0.9938	3.5301	0.9999	2.0819
KN6-1	3746.00	9.97	2.6099	2.7259	0.9941	2.39	0.9983	3.4401	0.9859	2.0815
X8	3484.20	8.19	0.355	2.7216	0.9900	2.306	0.9974	2.8979	0.9773	2.1040
Y21	3511.60	11.44	0.31	2.7331	0.9836	2.2648	0.9912	3.0423	0.9885	2.1296
X10-2	3547.80	7.86	0.281	2.7254	0.9861	2.3084	0.9696	2.9274	0.9205	2.1114
X9	3522.70	6.91	0.271	2.6901	0.9949	2.3586	0.9911	3.043	0.9853	2.1468
W26-1	3623.30	11.31	0.078	2.6914	0.9813	2.1415	0.9561	3.4873	0.9966	2.1405
W26-2	3634.30	12.54	0.044	2.6744	0.9923	2.1379	0.9519	3.2071	0.9319	2.1193
X10-1	3533.85	4.32	0.021	2.6462	0.9860	2.1123	0.9500	2.7826	0.9733	2.3086



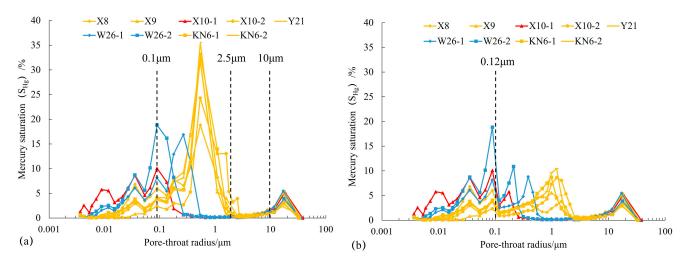
**Figure 10.** Fractal dimension fitting curves for full-range pore size characterization in the Kongdian Formation tight sandstones via synergistic integration of HPMI and CRMI.

# 4.3.2. Combined Characterization of Full-Pore-Size Distribution Using High-Pressure Mercury Intrusion and Constant-Rate Mercury Intrusion

The radius at the splicing point for the full-aperture pore-throat distribution was determined as the average of  $r_{h2}$  and  $r_{c2}$ , where  $r_{h2}$  represents the boundary radius between large and small pore-throats derived from the fractal dimension fitting curve of high-pressure mercury intrusion porosimetry for each sample, and  $r_{c2}$  denotes the corresponding boundary radius from the fractal dimension fitting curve of constant-rate mercury intrusion (Tables 4 and 5). Thus, each sample has its own unique splicing point. Taking sample X10-2 as an example, the boundary radii  $r_{h2}$  and  $r_{c2}$ , between large and small pore-throats are 2.8442  $\mu$ m and 2.5275  $\mu$ m, respectively (Tables 4 and 5), with an average value of 2.6859  $\mu$ m. The full-aperture pore-throat distribution was then obtained by combining the high-pressure mercury intrusion data for pore-throat radii smaller than 2.8442  $\mu$ m with the constant-rate mercury intrusion data for pore-throat radii larger than 2.5275  $\mu$ m (Figure 11a).

Analysis of the full-range pore-throat size distribution characterized by fractal dimension splicing points (Figure 11a) reveals that the total pore-throat radius ranges from 3.60 nm to 29.67  $\mu$ m. Most pore-throats are concentrated in the radius range of less than 2.5  $\mu$ m, with fewer developed between 2.5 and 10  $\mu$ m. Within the range of <2.5  $\mu$ m, the distribution curves exhibit diverse morphologies with multiple peaks (multimodal distribution) and significant differences in peak values, primarily attributed to variations in the combinations of pore-throat sizes in tight sandstone reservoirs. The full-range pore-throat distribution curve is divided into three intervals: pore-throat radius < 0.1  $\mu$ m, 0.1–2.5  $\mu$ m, and >10  $\mu$ m. The tight sandstone reservoirs in the study area are predominantly distributed

in the ranges of 0.1–2.5  $\mu m$  and <0.1  $\mu m$ . A prominent peak occurs in the 0.1–2.5  $\mu m$  interval, indicating that micropores and meso-pores are the most developed in the study area. In the <0.1  $\mu m$  interval, all samples show a certain amount of mercury intrusion, with mercury saturation generally around 5%. This is due to the widespread development of micro–nano scale pore-throats in the study area, which can provide certain storage space and seepage channels. In the >10  $\mu m$  interval, a distinct peak of mercury intrusion is observed, suggesting the presence of some macro-pores, which correspond to various dissolution pores with larger sizes. In summary, the full-range pore-throat distribution characteristics are consistent with the observations from cast thin sections and scanning electron microscopy, indicating that the full-range pore-throat distribution characterized by fractal dimension splicing points can effectively represent the pore-throat structure of tight sandstone reservoirs.



**Figure 11.** Full-range pore-throat distribution via HPMI-CRMI integration, (a) characterized by fractal-dimension transition point; (b) integration of pore-throat distribution at fixed radius threshold of  $0.12 \mu m$ .

Previous studies typically characterize the full-range pore-throat distribution by simply splicing the pore size distribution < 0.12  $\mu m$  obtained from SEMHPMI with that >0.12  $\mu m$  derived from CRMI (Figure 11b). Comparison with the full-range pore-throat distribution characterized by the fractal dimension splicing point of HPMI and CRMI (Figure 11a) reveals that, for the pore-throat distribution characterized by splicing HPMI and CRMI at 0.12  $\mu m$ , all samples exhibit a certain degree of mercury saturation loss relative to that characterized by the fractal dimension splicing point. In other words, this splicing method leads to a certain loss of pore-throats, with the most significant loss occurring in the 0.1 to 2.5  $\mu m$  interval. This indicates that splicing HPMI and CRMI at 0.12  $\mu m$  cannot truly and effectively characterize the full-range pore-throat distribution. Instead, using the fractal dimensions obtained from HPMI and CRMI as the splicing point to characterize the full-range pore-throat distribution is more reasonable. This method holds important significance for studying the full-range micropore-throat distribution in tight sandstone reservoirs.

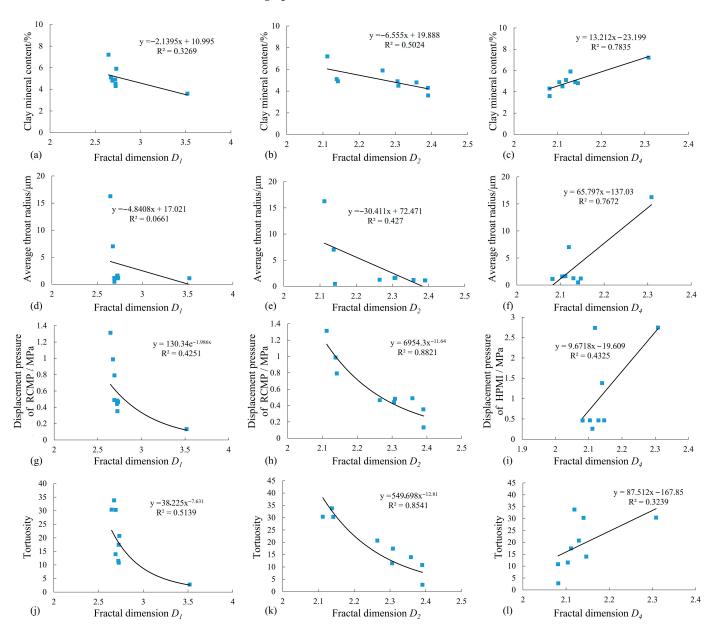
# 5. Factors Influencing Fractal Characteristics of Pore Structure, and Connection Between Fractal Results and Reservoir Performance

#### 5.1. Factors Influencing Fractal Dimensions

To investigate the factors affecting the magnitude of fractal dimensions, fitting curves were plotted between fractal dimensions and clay mineral contents as well as pore structure characteristic parameters (Figure 12). The results of correlation analysis between min-

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eral contents and fractal dimensions (Figure 12) show that the macro–mega pore fractal dimension  $D_1$  and micro-fine throat fractal dimension  $D_2$  are negatively correlated with clay mineral contents (Figure 12a,b), while the micro–nano throat fractal dimension  $D_4$  is positively correlated (Figure 12c). The content of authigenic clay minerals in the study area is relatively high, which usually attach to the surfaces of mineral particles and fill in pores, reducing the connectivity of pore throats. Meanwhile, they also form certain micro–nano-scale pore throats, increasing the specific surface area of pore throats. In addition, due to the extreme instability of clay minerals, these properties can all affect the magnitude of fractal dimensions. Therefore, the clay mineral content is significantly positively correlated with the micro–nano throat fractal dimension  $D_4$ , but weakly negatively correlated with the macro–mega pore fractal dimension  $D_1$  and micro-fine throat fractal dimension  $D_2$ .



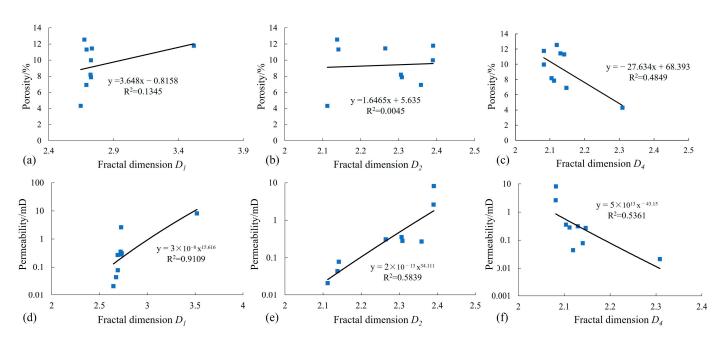
**Figure 12.** Relationship between full-pore-size fractal dimensions and clay mineral content, pore structure characteristic parameters of tight sandstone samples in the study area. ( $\mathbf{a}$ - $\mathbf{c}$ ) relationship between full-range fractal dimensions  $D_1$ ,  $D_2$  and  $D_4$  and clay mineral contents; ( $\mathbf{d}$ - $\mathbf{f}$ ) relationship between full-range fractal dimensions  $D_1$ ,  $D_2$  and  $D_4$  and average throat radius; ( $\mathbf{g}$ - $\mathbf{i}$ ) relationship between full-range fractal dimensions  $D_1$ ,  $D_2$  and  $D_4$  and displacement pressure; ( $\mathbf{j}$ - $\mathbf{l}$ ) relationship between full-range fractal dimensions  $D_1$ ,  $D_2$  and  $D_4$  and tortuosity.

The correlation analysis results between pore structure characteristic parameters and fractal dimensions (Figure 12d–l) show that the macro–mega pore fractal dimension  $D_1$  and micro-fine throat fractal dimension  $D_2$  are negatively correlated with the average throat radius  $r_c$ , constant-rate mercury intrusion displacement pressure  $P_{d1}$ , and tortuosity  $\lambda$ , while the micro–nano throat fractal dimension  $D_4$  shows the opposite trend. The average throat radius has a significant controlling effect on micro-fine throats and micro-nano throats but almost no impact on macro-mega pores. A larger average throat radius corresponds to a greater number of micro-fine throats, leading to better homogeneity, whereas the opposite is true for micro-nano throats. A higher displacement pressure indicates a greater number of micro-nano throats, and these throats surrounding the pores deteriorate the pore-throat connectivity and enhance the heterogeneity, thus resulting in a larger micro-nano throat fractal dimension  $D_4$ , which is contrary to the cases for the macro–mega pore fractal dimension  $D_1$  and micro-fine throat fractal dimension  $D_2$ . Tortuosity has a more significant controlling effect on macro-mega pores and micro-medium throats; a higher tortuosity means more complex throat morphologies and stronger throat heterogeneity, with more irregular throats surrounding the pores and poor pore-throat connectivity, consequently leading to an increase in the macro-mega pore fractal dimension  $D_1$  and micro-fine throat fractal dimension  $D_2$ . Due to the extremely small scale of micro–nano throats, the impact of tortuosity on them is limited. In summary, the full-pore-size fractal dimensions are mainly controlled by the comprehensive effects of clay mineral content, average throat radius, displacement pressure, and tortuosity.

#### 5.2. Relationship Between Fractal Dimension and Physical Properties

Based on the relationship between full-range fractal dimensions and petrophysical properties (Figure 13), the macro–mega pore fractal dimension  $D_1$  (Figure 13a,d) and microfine throat fractal dimension  $D_2$  (Figure 13b,e) exhibit positive correlations with porosity and permeability, with stronger correlations to permeability. This trend arises because the macro–mega pores and micro-fine throats in the study area are primarily provided by various dissolution pores, dominated by feldspar dissolution pores. While these dissolution pores enhance reservoir properties, their formation generates semi-connected to disconnected throats with irregular morphologies. Concurrently, clay minerals partially fill feldspar residues, further complicating the pore-throat systems. Consequently, dissolution pores increase pore-throat heterogeneity, elevating  $D_1$  and  $D_2$  values while exerting minimal impact on porosity. In contrast, the nano throat fractal dimension  $D_4$  displays negative correlations with porosity and permeability (Figure 13c,f), attributed to the prevalence of tubular throats within clay minerals. These tubular throats form complex micro-throat networks with pores; their development degrades tight sandstone reservoir quality, thereby increasing  $D_4$  values [40].

Therefore, the porosity and permeability of tight sandstones in the study area are primarily controlled by the complexity of macro–mega pores, micro-fine throats, and nano–micro throats. The development of various dissolution pores significantly improves reservoir quality, while the tubular throats developed in clay minerals reduce reservoir quality due to their strong heterogeneity. Specifically, higher quantities of macro–mega pores and micro-fine throats, along with larger fractal dimensions  $D_1$  and  $D_2$ , combined with fewer nano–micro throats and a smaller fractal dimension  $D_4$ , result in better reservoir quality in the tight sandstone reservoirs of the study area.



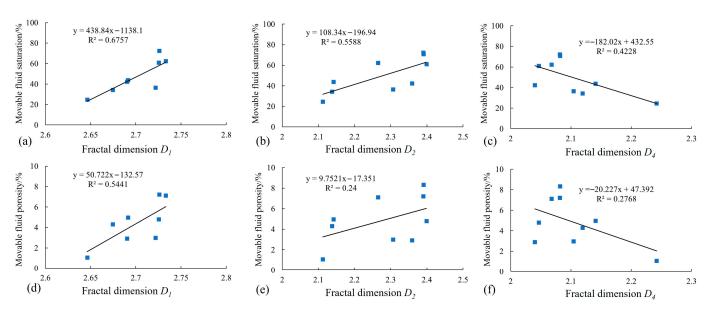
**Figure 13.** Relationship between full-range fractal dimensions  $D_1$ ,  $D_2$  and  $D_4$  and physical properties of tight sandstone samples in the study area. (**a–c**) relationship between  $D_1$ ,  $D_2$  and  $D_4$  and porosity; (**d–f**) relationship between  $D_1$ ,  $D_2$  and  $D_4$  and permeability.

#### 5.3. Fractal Dimension and Fluid Flow Characteristics

In low-permeability tight reservoirs, fluids exhibit two distinct occurrence states within the pores: one portion exists as movable fluid that can be displaced from rock pores under external forces, while the other portion remains immobile due to adsorption by hydrophilic clay minerals or capillary trapping [41,42]. These immobilized fluids cannot be effectively extracted during core centrifugation and is thus classified as immobile fluid. Based on NMR centrifugal experimental data, the movable fluid saturation and movable fluid porosity can be determined for samples with varying pore structures [43]. The average movable fluid saturation in Type I pore-structured reservoirs is 71.57%, while in Type II it is 51.7%. Type III pore-structured reservoirs exhibit the lowest movable fluid saturation, with a minimum value of 34.4% and an average of 39.16%. Movable fluid porosity is calculated based on the relationship between movable fluid saturation and porosity. Due to their lower porosity, Type III reservoirs show the lowest movable fluid porosity at 1.1%, with an average of 2.7%. In contrast, Type I and II reservoirs reach a maximum movable fluid porosity of 10.8%, with an average of 5.2%.

Based on the relationship between full-range fractal dimensions and movable fluid characteristics (Figure 14), the fractal dimensions  $D_1$  (reflecting macro–mega pores) and  $D_2$  (reflecting micrometer-sized large throats) exhibit positive correlations with reservoir movable fluid saturation and movable fluid porosity (Figure 14a,b,d,e). In contrast, the fractal dimension  $D_4$  (reflecting nanometer-sized pore-throat systems) shows negative correlations with these parameters (Figure 14c,f). This is because the low-permeability tight reservoirs in the study area contain numerous fine throats with small radii. These narrow throats require higher displacement pressures for fluid flow, thereby hindering overall reservoir fluid flow processes. Consequently, larger throats generally exert positive influences on fluid storage and flow, enabling relatively easier fluid mobility and predicting higher productivity. Conversely, nanometer-sized throats—predominantly comprising clay mineral-bound tubular throats—form complex micropore-throat systems with pores. Their increased development deteriorates tight sandstone reservoir properties, resulting in higher  $D_4$  fractal dimension values, reduced fluid mobility within pore throats, and inferred lower productivity.

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**Figure 14.** Relationship between full-range fractal dimensions  $D_1$ ,  $D_2$  and  $D_4$  and movable fluid saturation (and movable fluid porosity) of tight sandstone samples in the study area. (**a–c**) relationship between  $D_1$ ,  $D_2$  and  $D_4$  and movable fluid saturation; (**d–f**) relationship between  $D_1$ ,  $D_2$  and  $D_4$  and movable fluid porosity.

#### 6. Conclusions

- (1) The tight sandstone reservoirs in the 2nd member of the Kongdian Formation (Kong 2 Member) exhibit diverse types of pores and throats, with intergranular dissolved pores, residual intergranular pores, and intercrystalline pores of clay minerals being the dominant pore types, and lamellar and curved-lamellar throats being the main throat types, showing strong heterogeneity in pore structure.
- (2) Compared with the conventional method of characterizing the full-pore-size pore-throat distribution by splicing high-pressure and constant-rate mercury intrusion data at 0.12  $\mu$ m, the characterization based on the splicing point of full-pore-size fractal dimensions is more reasonable. The overall curve presents a multi-peak pattern with obvious differences in peak values, the pore-throat distribution range is 3.6 nm to 29.66  $\mu$ m, and the pore-throat distribution shows significant differences.
- (3) The full-pore-size fractal dimensions  $D_1$ ,  $D_2$ , and  $D_4$  can effectively characterize the heterogeneity of pore structure and exhibit good correlations with physical properties. The greater the number of macro-mega pores and micro-fine throats, the larger the fractal dimensions  $D_1$  and  $D_2$ , indicating that the pores often have better connectivity and the tight sandstone reservoirs have better seepage capacity; the greater the number of micro-nano throats, the larger the fractal dimension  $D_4$ , indicating a more complex pore structure, which leads to poorer reservoir physical properties and is unfavorable for hydrocarbon seepage. The full-pore-size fractal dimensions  $D_1$ ,  $D_2$ , and  $D_4$  are mainly controlled by the comprehensive effects of clay mineral content, average throat radius, displacement pressure, and tortuosity.

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#### **Abbreviations**

HPMI High-pressure mercury intrusion
MIP Mercury intrusion porosimetry
NMR Nuclear magnetic resonance
SEM Scanning electron microscopy
CRMI Constant-rate mercury injection

XRD X-ray diffraction

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