



# Mixed Logic Dynamic Models for MPC Control of Wind Farm Hydrogen-Based Storage Systems

Muhammad Faisal Shehzad <sup>1,\*</sup>, Muhammad Bakr Abdelghany <sup>1</sup>, Davide Liuzza <sup>2</sup>, Valerio Mariani <sup>1</sup> and Luigi Glielmo <sup>1</sup>

- <sup>1</sup> Group for Research on Automatic Control Engineering, Department of Engineering, University of Sannio, Piazza Roma 21, 82100 Benevento, Italy; bmuhammad@unisannio.it (M.B.A.); vmarian@unisannio.it (V.M.); glielmo@unisannio.it (L.G.)
- <sup>2</sup> ENEA Fusion and Nuclear Safety Department, Via Enrico Fermi 45, 00044 Frascati (Rome), Italy; davide.liuzza@enea.it
- \* Correspondence: mshehzad@unisannio.it

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**Abstract:** The use of electric power by wind generation in actual grids is hampered by its inherent stochastic nature and the penalty deviations adopted in several electricity regulation markets with respect to power quality requirements. Coupling wind farms with advanced Energy Storage Systems (ESS) can help their integration within grids. In this direction, several studies have been conducted, but the problem is still open due to the constraints and limitations regarding the ESSs time autonomy, time response, degradation issues and overall costs. In order to take into account these relevant aspects, advanced control algorithms are needed. In this paper, a Model-Based Predictive Controller (MPC) is presented. Such a controller minimizes the degradation of the ESS and the load tracking error while fulfilling the operational constraints and dynamics. The ESS considered is hydrogen-based and the study has been developed within the EU-FCH 2 JU (European Union Fuel Cells and Hydrogen 2 Joint Undertaking) funded project HAEOLUS aiming at building and integrating advanced control strategies for a hydrogen-based ESS within a wind farm fence. Numerical simulations show the feasibility and the effectiveness of the proposed approach.

**Keywords:** energy storage systems; hydrogen conversion; power to gas; energy management; mixed logic dynamics

# 1. Introduction

Renewable energy sources are subjected to considerable attention for the replacement of fossil fuels. In particular, wind and solar energy are considered as the most promising options [1]. Many studies have been carried out to improve these technologies and to overcome the drawbacks associated with them. In particular, the stochastic nature of the wind, energy production and consumption mismatches and possibly high capital and operational cost are the main hurdles for their utilization at large scale [2].

One solution to mitigate these problems is to setup an energy storage system that can help the wind generation patterns in matching the load patterns along the time even in case of low or nearly zero energy production [2].

The adoption of an Energy Storage System (ESS) combined with a Renewable Energy System (RES) plant appears to be a paradigm shift in the energy market and introduces new operational possibilities [3,4]. However, the increased complexity of the plant itself requires proper management strategies. For this reason, control algorithms for Energy Management Systems (EMSs) have already been addressed in relevant works. Carapellucci et al. [5] presented a power management control



strategy for assessing cost effective performances of renewable energy islands. Such controller also allows to include various electricity generation technologies into the hydrogen storage system. The hybridization of alternate energy sources with Fuel Cell (FC) systems using long and short-term storage strategies with appropriate power controllers and control strategies to meet the load demand has been presented by Uzunog et al. [6]. Castaneda et al. [7] implemented three control strategies to satisfy the load power demand, to regulate the state of charge of the batteries and to reduce the cost of battery cycling, FC and electrolyzer, respectively. Valverde et al. [8] implemented a supervisory Model Predictive Control (MPC) for hydrogen-based ESS for optimal power market management. Trifkovic et al. [9] implemented a hierarchical control system to track the dynamic load demand through the intermittent renewable energy generation and an energy storage. An MPC based on a mixed-integer quadratic programming algorithm was designed by Serna et al. [10] to improve the power balance between the available power and the electrolysis power consumption in an offshore plant using renewable energies.

The mixed-integer linear programming framework for wind–hydrogen plant modeling, including operational costs in the ESS, is used in [11–14] without integrating the degradation issues in the ESS. Vahidi et al. [15,16] applied the MPC to control the load sharing of a hybrid ESS composed of a fuel cell and an ultracapacitor, also including some degradation issues. However, these studies do not take into account the connection to the grid or the start-up/shutdown life cycles associated with the electrolyzer and the fuel cell.

Heuristic algorithms for degradation characterization with respect to the working hours/life cycles of the electrolyzer have been discussed by Bergen et al. [17]. Beside hydrogen-based storage, interesting control approaches for energy flow control in combined heat and power microgrids have been presented by Ferrari-Trecate et al. [18]. Also, the authors developed MPC for hybrid co-generation power plants by introducing a mixed linear dynamic framework [19].

The adoption of storage systems increases the complexity of the overall energy plants in terms of various aspects such as operational strategies, capital cost degradation, maintenance cost and efficiency reduction over time. Furthermore, each ESS technology introduces, together with more operational flexibility, peculiar limitations and constraints on the overall plant. Among the available technologies, the use of the hydrogen as an energy carrier can play an important role in the energy sector. For this reason, hydrogen storage system characteristics have been investigated in several studies, such as [20–24]. Several of them conclude that, among ESSs, the high energy density of the hydrogen may be beneficial in the new energetic paradigm. Hydrogen storage systems are composed of electrolyzers, fuel cells, and storage tanks. The optimal use of hydrogen storage requires the development of a control system, which takes into account all the constraints, limitations, degradation issues, and the economical cost in operating all the equipment. However, the robust performances and the transient responses associated to hydrogen-based ESS are considered as the main barriers in its utilization [25,26].

For all these reasons, in order to use the hydrogen-based ESSs efficiently, and operate them in the most effective way, the need of an advanced EMS is of paramount importance. The latter has to take into account all the operational constraints and limitations, as well as degradation, operational and maintenance cost in order to properly commit all the equipment and satisfy the energy demand profile. Aspects related to cost degradation and economical feasibility of hydrogen-based ESS have been addressed in [27].

Korpas et al. [28] implemented a MPC controller to integrate hydrogen ESS in the electrical market system but without accounting for the plant efficiency. Despite the valuable results of these papers, not all the aspects and constraints of both electrolyzer and fuel cells hydrogen-based ESS are considered at the same time.

According to the authors' knowledge, important operational aspects of hydrogen-based storage systems such as degradation, mode operational switchings and stand by consumption of both electrolyzer and fuel cell have not been modeled in the literature. Our paper addresses such issues and

develops preliminary operational models and constraints for a hydrogen-based ESS to be integrated in a wind farm fence under the EU-FCH JU project HAEOLUS—Hydrogen-Aeolic Energy with Optimized eLectrolysers Upstream of Substation [29].

Specifically, the plant is modeled considering Mixed Integer Linear (MIL) constraints for operating states and switchings and non linear dynamics for the hydrogen tank and the efficiency degradation rates. Also, depreciation cost are considered when switching among on (ON), off (OFF) and standby (STB) operational states. A controller is then derived whose goal is to track and meet the reference demand  $P_{ref}$  with the available system power  $P_{avl}$  at the best and in the most economical way. The designed MPC controller takes into account all the devices features here modeled and operates in reducing the operational and degradation cost of the devices while satisfying the constraints. Preliminary numerical results are conducted to show the effectiveness of our approach.

## Nomenclature

The parameters, the forecasts and the decision variables used in the proposed formulation are described, respectively, in Tables 1–3.

Parameters	Description
H <sup>tank</sup>	Hydrogen level in the storage unit [Nm <sup>3</sup> ]
$H^{max}$	Maximum level of the hydrogen storage unit [Nm <sup>3</sup> ]
$H^{\min}$	Minimum level of the hydrogen storage unit [Nm <sup>3</sup> ]
$P_e^{\max}$	Maximum power level of the electrolyzer [kW]
$P_e^{\text{STB}}$	Standby power of the electrolyzer [kW]
$P_e^{\min}$	Minimum power level of the electrolyzer [kW]
$P_f^{\max}$	Maximum power level of the fuel cell [kW]
$P_f^{\min}$	Minimum power level of the fuel cell [kW]
$P_{f}^{STB}$	Standby power of the fuel cell [kW]
ŃHe	Number of life hours of the electrolyzer
$NH_f$	Number of life hours of the fuel cell
$HY_e$	Number of per year life hours of the electrolyzer
$HY_f$	Number of per year life hours of the fuel cell
$d_e$	Degradation rate of the electrolyzer at maximum input power and over the number of yearly life hours
$d_f$	Degradation rate of the fuel cell at maximum output power and over the number of yearly life hours
S <sub>rep,e</sub>	Electrolyzer stack replacement cost [€/kW]
$S_{\rm rep,f}$	Fuel cell stack replacement cost [€/kW]
$T_s$	Sampling period [h]
Т	Simulation horizon [h]

Table	1.	Parameters.
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Table 2. Forecast powers.

Forecasts	Description
$P_w$	Wind power production [kW]
$P_{ref}$	Electrical load demand [kW]

Table 3. Real and logical time varying variables.

Variables	Description
$\delta_e^{ON}$	On state of the electrolyzer
$\delta_{e}^{OFF}$	Off state of the electrolyzer
$\delta_e^{STB}$	Standby state of the electrolyzer
$\delta_f^{ON}$	On state of the fuel cell
$\delta_f^{OFF}$	Off state of the fuel cell
$\delta_f^{\text{STB}}$	Standby state of the fuel cell
$\vec{P}_e$	Electrical power of the electrolyzer [kW]
$P_f$	Electrical power of the fuel cell [kW]
Pavl	Available system electrical power [kW]
Pdump	Dumped electrical power [kW]
z	Electric power formulated as mixed logic dynamic (MLD) variables for the electrolyzer and the fuel cell [W]
$\sigma$	Logical variables ON/OFF/STB states for the electrolyzer and the fuel cell
ζε	Electrolyzer degradation rate [Nm <sup>3</sup> /hW]
$\zeta_f$	Fuel cell degradation rate [hW/Nm <sup>3</sup> ]

#### 2. System Description and Modeling

Figure 1 shows the block diagram of the system under investigation. Red solid lines denote energy flow, green solid lines denote hydrogen flows, and blue dashed lines denote data flows while  $P_w$  denotes the power generated by the wind farm,  $P_e^{in}$  is the electrolyzer input power,  $P_{f}^{out}$  is the fuel cell output power,  $P_{dump}$  is the power that can be dissipated on a dumping load and  $P_{avl}$  is the power available to the load. Dumping of the wind power excess is usually necessary if the power surplus exceeds the transmission capacity of the external grid. However, in the case under investigation the dumping load may be conveniently exploited to mitigate the degradation of the electrolyzer, therefore helping to mitigate the impact of the corresponding operational costs.

In nominal conditions,  $P_w$  is delivered directly to the load demand. However, when an excess of wind power production happens, this is shunted to the electrolyzer and stored as hydrogen in a tank. Conversely, whenever the generated wind power can not satisfy the load demand, the hydrogen is then re-electrified through the fuel cell, thus achieving power supply continuity.



**Figure 1.** Block diagram of the microgrid under investigation.  $P_w$ ,  $P_e^{\text{in}}$ ,  $P_f^{\text{out}}$ ,  $P_{\text{ref}}$  and  $P_{\text{dump}}$  are the power by wind generation, the power inward the electrolyzer, the power outward the fuel cell, the power demand reference and the dumped power, respectively.

## 2.1. Power Demand Reference Model

In our scenario, the power demand reference  $P_{ref}$  is forecasted by an external system, fed into the MPC controller and then used within a tracking error cost function.

# 2.2. Electrolyzer and Fuel Cell Models

The electrolyzer and the fuel cell have been both modeled as a three states automaton, as shown in Figure 2. For each one, the three possible states are on (ON), off (OFF) and standby (STB). Correspondingly, the mutually exclusive logical variables  $\delta_i^{\alpha}(k)$ , with  $\alpha \in \{OFF, STB, ON\}$  and  $i \in \{e, f\}$ , are used to indicate the operating conditions of the electrolyzer (i = e) and the fuel cell (i = f) at any time k.



**Figure 2.** Automata of the electrolyzer (i = e) and of the fuel cell (i = f). Each node represents a particular state (i.e., operational mode), while the edges represent the state transition, for each  $i \in \{e, f\}$ .

More in detail, each operational state of the electrolyzer and the fuel cell results in a particular product of one logical variable and one corresponding power, which is relevant for that state, to be different from zero. For example, whenever the electrolyzer or the fuel cell is in ON state, the corresponding input or output power is limited within the range  $[P_i^{\min}, P_i^{\max}]$ . Thus, by defining  $P_e(k)\delta_e^{ON}(k) = P_e^{in}$  and  $P_f(k)\delta_f^{ON}(k) = P_f^{out}$ , and since in this case we set  $\delta_e^{ON}(k) = \delta_f^{ON}(k) = 1$ , then it results  $P_e(k) = P_e^{in} \in [P_e^{min}, P_e^{max}]$  and  $P_f(k) = P_f^{out} \in [P_f^{min}, P_f^{max}]$ . Moreover, being by defition mutually exclusive for each  $i \in \{e, f\}$ , all other logical variables are null, instead. On the other hand, whenever the electrolyzer or the fuel cell is in STB state, the relevant powers to be considered are their corresponding stand-by powers  $P_i^{STB}$ , with  $i \in \{e, f\}$ . Therefore, by defining  $P_e(k)\delta_e^{STB}(k) = P_e^{STB}$  and  $P_f(k)\delta_f^{STB}(k) = P_f^{STB}$  it follows that  $P_e(k) = P_e^{STB}$  and  $P_f(k) = P_f^{STB}$  since accordingly  $\delta_e^{STB}(k) = \delta_f^{STB}(k) = 1$ , while, again, all other logical variables are null. Finally, when the electrolyzer or the fuel cell is in OFF state, their corresponding input or output powers along with the power consumptions are null, resulting in  $P_e(k) = P_f(k) = 0$ . Therefore, according to the operating condition of the electrolyzer and of the fuel cell, each  $\delta_i^{\alpha}(k)$  with  $i \in \{e, f\}$  is determined at any time k as follows

$$\begin{cases}
P_i^{\min} \le P_i(k) \le P_i^{\max} & \iff \delta_i^{ON}(k) = 1, \\
P_i(k) = P_i^{STB} & \iff \delta_i^{STB}(k) = 1, \\
P_i(k) = 0 & \iff \delta_i^{OFF}(k) = 1.
\end{cases}$$
(1)

Along with the logical states, also the feasible state transitions among them have to be modeled. To this aim we need the additional logical variables  $\sigma_{\alpha_i}^{\beta}(k)$ , with  $\alpha \neq \beta$ ,  $\beta \in \{\text{OFF}, \text{STB}, \text{ON}\}$  and  $i \in \{e, f\}$  which can be derived by suitably combining the logical states through logical connectives. The transition variables  $\sigma_{\alpha_i}^{\beta}(k)$  assume value  $\sigma_{\alpha_i}^{\beta}(k) = 1$  if the corresponding transition happens at time *k* (available transitions are depicted in Figure 2), while null value otherwise. It is important to notice that  $\delta_i^{\alpha}(k)$ s and  $\sigma_{\alpha_i}^{\beta}(k)$ s are 18 decision variables of the MPC controller that will be presented later. Both state variables and transition variables are codified with mixed integer linear inequalities which will be then included as constraints for the MPC controller. The mathematical formulation of these constraints is reported, for the reader convenience, in the Appendix A.

#### 2.3. Hydrogen Storage Model

The hydrogen storage dynamics are defined as a function of the hydrogen level at the previous time step H(k) [25]. The  $\zeta_e(k)$  and  $\zeta_f(k)$ , are respectively, the efficiency degradations of the electrolizer and of the fuel cell, respectively, and have been modeled as dynamic equations since they change along the time

$$\begin{aligned} \zeta_i(k+1) &= \left(1 - \frac{d_i}{P_i^{\max} HY_i} P_i(k) \delta_i^{ON}(k)\right) \zeta_i(k), \\ H(k+1) &= H(k) + \zeta_e(k) P_e(k) \delta_e^{ON}(k) T_s - \frac{P_f(k) \delta_f^{ON}(k) T_s}{\zeta_f(k)}, \end{aligned}$$
(2)

where  $d_i$  is the degradation rate at the maximum power [30] and over the number of yearly life hours of the electrolyzer (i = e) and of the fuel cell (i = f), HY<sub>i</sub> with  $i \in \{e, f\}$  is the number of the per year life hours of the electrolyzer (i = e) and of the fuel cell (i = f) and  $T_s$  denotes the sampling period. Notice that, according to (2), the electrolyzer and the fuel cell produces and consumes hydrogen only in their ON modes. All the other modes are not associated with the hydrogen production and consumption respectively and, therefore, are not associated to efficiency degradation.

#### 2.4. Feasibility and Operating Constraints

In addition to the constraints due to the considered dynamics, it is necessary to take into account also for the subsystems physical limitations. In fact, the actual ESS can absorb or supply just a limited amount of power. Further, also the power that can be dissipated by the dumping load cannot exceed a limit, which in our case is set to be the power achieved by wind generation

$$P_i^{\min} \le P_i(k) \le P_i^{\max},$$

$$H^{\min} \le H(k) \le H^{\max},$$

$$0 \le P_{dump}(k) \le P_w(k).$$
(3)

## 2.5. Power Balance Constraint

The available power  $P_{avl}$ , which is delivered to the load, is obtained by forcing the power balance at the ESS insertion point

$$P_w(k) - P_e(k)\delta_e^{\text{ON}}(k) + P_f(k)\delta_f^{\text{ON}}(k) - P_{\text{avl}}(k) - P_{\text{dump}}(k) = 0$$
(4)

where  $P_e(k)\delta_e^{ON}(k) = P_e^{in}$  and  $P_f(k)\delta_f^{ON}(k) = P_f^{out}$ . The power balance (4) highlights that the available power  $P_{avl}$  depends on the power  $P_w$  achieved through wind generation and the balancing action of the hydrogen storage system and the dumping load.

#### 3. Implementation of the Proposed MPC Controller

In this section we illustrate the MPC control strategy that has been designed to optimize the problem of satisfying a forecasted power demand in the most economical way [31,32]. The main idea of the MPC is to exploit the model of the plant to predict the future evolution of the system within a prediction horizon. Based on this prediction, at each step k the controller selects a sequence of future command inputs through an optimization procedure, which aims at minimizing a suitable cost function and enforcing the fulfillment of the constraints. Only the control signal calculated for the time instant k is applied to the process. At the next sampling time, the new state of the system is measured or estimated, and a new optimization problem is solved using this new information. The introduction of logical variables makes the system as a mixed logical dynamical system. One of the advantages of MPC over other control methods is its immediate applicability to multivariable control systems.

#### 3.1. Electrolyzer and Fuel cell Cost Functions

The cost incurred in operating the electrolyzer and the fuel cell are summarized in the two respective cost functions derived in this section. Both of them are expressed as a summation of different cost related to the component depreciation, the reduction in the number of life cycles and the energy spent in keeping the units warm during the stand by mode. More in details, the manufacturers of the electrolyzer and the fuel cell defined the life cycles of the devices as a function of number of working hours. It has been noticed in many studies [33–37] that the fluctuating loads and the operating cycles can seriously affect these devices in a number of ways. Therefore, in order to tackle such outlined problems, we propose the following cost

$$J_{e} = \sum_{k=0}^{T-1} \left( \frac{S_{\text{rep},e}}{NH_{e}} + \text{Cost}_{e}^{OM} \right) \delta_{e}^{ON}(k) + \text{Cost}_{OFF_{e}}^{ON} \sigma_{OFF_{e}}^{ON}(k) + \text{Cost}_{ON_{e}}^{OFF} \sigma_{ON_{e}}^{OFF}(k) + \text{Cost}_{ON_{e}}^{STB} \sigma_{ON_{e}}^{STB}(k) + \text{Cost}_{ON_{e}}^{STB} \sigma_{ON_{e}}^{STB}(k) + \text{Cost}_{OFF_{e}}^{STB} \sigma_{OFF_{e}}^{STB}(k) + c(k) P_{e}^{STB} \delta_{e}^{STB}(k),$$

$$J_{f} = \sum_{k=0}^{T-1} \left( \frac{S_{\text{rep},f}}{NH_{f}} + \text{Cost}_{f}^{OM} \right) \delta_{f}^{ON}(k) + \text{Cost}_{OFF_{f}}^{ON} \sigma_{OFF_{f}}^{ON}(k) + \text{Cost}_{OFF_{f}}^{OFF} \sigma_{OFF_{f}}^{ON}(k) + \text{Cost}_{ON_{f}}^{OFF} \sigma_{ON_{f}}^{OFF}(k) + \text{Cost}_{ON_{f}}^{STB} \sigma_{ON_{f}}^{STB}(k) + \text{Cost}_{ON_{f}}^{STB} \sigma_{ON_{f}}^{STB}(k) + \text{Cost}_{OFF_{f}}^{STB} \sigma_{OFF_{f}}^{STB}(k) + \text{Cost}_{OFF_{f}}^{STB} \sigma_{OFF_{f}}^{STB}(k) + c(k) P_{f}^{STB} \delta_{f}^{STB}(k),$$

$$(5)$$

where  $\operatorname{Cost}_{e}^{OM}$  and  $\operatorname{Cost}_{f}^{OM}$  denote the operating and maintenance cost of the electrolyzer and  $\operatorname{NH}_{f}$  is fuel cell, c(k) is the power spot price,  $\operatorname{NH}_{e}$  is the number of life hours of the electrolyzer and  $\operatorname{NH}_{f}$  is the number of life hours of the fuel cell.  $\operatorname{Cost}_{OFF_{i}}^{ON}$ ,  $\operatorname{Cost}_{STB_{i}}^{ON}$ ,  $\operatorname{Cost}_{STB_{i}}^{OFF}$ , and  $\operatorname{Cost}_{OFF_{i}}^{STB}$ describe the startup, shutdown and standby cost of the electrolyzer and the fuel cell, respectively choosing  $i \in \{e, f\}$ . These cost are payed any time a mode switch occurs, since any complete sequence of switching accounts for a working cycle and, therefore, reduces the components' life. We wish to emphasize, for the sake of clarity, that shifting from OFF to ON (cold start) presents usually a higher cost than from STB to ON (warm start). On the other hand, devices in OFF mode do not absorb any power, while this is not true in STB mode. The  $S_{\operatorname{rep},e}$  and  $S_{\operatorname{rep},f}$  represent the stack replacement cost of the electrolyzer and the fuel cell, respectively.

## 3.2. Load Tracking Cost Function

In addition to the minimization of the operating costs of the electroyzer and the fuel cell, the other goal is to track a reference load demand  $P_{ref}$ , that in the scenario under investigation is forecasted. To this aim, the corresponding cost function which will be included in the optimization is given by the square error between the available power downstream the ESS  $P_{avl}$  and the forecasted load demand  $P_{ref}$ 

$$J_l = \sum_{k=0}^{T-1} \left( P_{\text{avl}}(k) - P_{\text{ref}}(k) \right)^2$$
(6)

## 3.3. MPC Formulation

In order to present the MPC policy, let us just consider the hydrogen dynamics in (2) and let us denote by  $\zeta_e(k + j | k)$ ,  $\zeta_f(k + j | k)$  and H(k + j | k), with j > 0, the corresponding state variables at time k + j predicted at time k by means of (2) as well.

At each *k*, given the initial state H(k),  $\zeta_e(k)$  and  $\zeta_f(k)$ , the MPC provides the optimal control sequences  $\mathbf{P}_{i,k}^{T-1}$ ,  $\mathbf{P}_{dump,k}^{T-1}$ ,  $\sigma_{\alpha_i,k}^{\beta,T-1}$ ,  $\sigma_{\alpha_i,k}^{\beta,T-1}$  and  $\mathbf{z}_{i,k}^{\gamma,T-1}$  for each  $i \in \{e, f\}$ ,  $\alpha, \beta \in \{\text{ON}, \text{STB}, \text{OFF}\}$ ,  $\alpha \neq \beta$  and  $\gamma \in \{\geq 0, \leq 0, \geq P_i^{\text{STP}}, \leq P_i^{\text{STB}}, \geq P_i^{\text{min}}, \leq P_i^{\text{max}}\}$ , and where

$$\mathbf{P}_{i,k}^{T-1} = \left(P_i(k)\dots P_i(k+T-1)\right)^{\top},$$

$$\mathbf{P}_{dump,k}^{T-1} = \left(P_{dump}(k)\dots P_{dump}(k+T-1)\right)^{\top},$$

$$\delta_{i,k}^{\alpha,T-1} = \left(\delta_i^{\alpha}(k)\dots \delta_i^{\alpha}(k+T-1)\right)^{\top},$$

$$\sigma_{\alpha_{i,k}}^{\beta,T-1} = \left(\sigma_{\alpha_i}^{\beta}(k)\dots \sigma_{\alpha_i}^{\beta}(k+T-1)\right)^{\top},$$

$$\mathbf{z}_{i,k}^{\gamma,T-1} = \left(z_i^{\gamma}(k)\dots z_i^{\gamma}(k+T-1)\right)^{\top},$$
(7)

by solving

$$\min_{\substack{\mathbf{P}_{i,k}^{T-1}, \\ \dim p_{k'}^{\alpha,T-1}, \\ \sigma_{i,k}^{\alpha,T-1}, \\ \sigma_{k,k}^{\beta,T-1}, \\ z_{i,k}^{\gamma,T-1}}} \sum_{j=0}^{T-1} \rho_l J_l(k+j) + \rho_e J_e(k+j) + \rho_f J_f(k+j)$$

s.t.

Discrete logical states (A2) , (A3), mode transitions (A5), storage dynamics (2), physical constraints (3), power balancing equation (4),  $\delta_i^{\alpha} \in [0, 1],$  $\sigma_{\alpha_i}^{\beta} \in [0, 1],$  $z_i^{\gamma} \in \{0, 1\},$  (8)

with being  $\rho_l$ ,  $\rho_e$  and  $\rho_f$  some weights. Since the problem (8) is re-formulated at time k + 1, an optimal feedback policy is designed.

Summarizing, the following objectives have been explicitly taken into account:

- 1. protection of the hydrogen storage tank from excessive discharging and overcharging;
- 2. limitation of the power rate of the fuel cell and of the electrolyzer to protect them;
- 3. tracking of the power reference request according to the forecasted conditions;
- 4. in case an expected event occurs, the fuel cell is employed as a contingent energy storage system to satisfy the power demand.

The block diagram of the proposed controller is detailed in Figure 3.  $\delta_e^{\alpha}$  and  $\delta_f^{\alpha}$  represent the discrete states of the electrolyzer and the fuel cell, where  $\alpha \in {OFF, STB, ON}$  indexes their logical states.



Figure 3. Proposed MPC Control Scheme.

# 4. Case Study

The model of the proposed EMS consisting of discrete operational states of the electrolyzer and of the fuel cell, the corresponding MLD constraints and the continuous dynamics have been implemented using MATLAB/YALMIP. The controller was implemented using the solver ILOG's CPLEX 12.8; all computations are performed on a laptop with an Intel Core (TM) i7 - 7700HQ 2.8 GHz processor and 16 GB of memory. Optimization results are obtained in less than 1 minute. The MPC is tuned mainly penalizing the electrolyzer and the fuel cell cost functions with respect to the load tracking one. In order to finalize the controller setup, the prediction horizon is T = 24 h with sampling time  $T_s = 1$  h. The cost values considered in our study are reported in Table 4. The switching cost for the standby state of both devices is lower in comparison with OFF to ON or ON to OFF states. The advantage of keeping the devices to their standby states is to avoid their cold start, and so a lower cost has to be paid for state switching. However, on the other hand the constant  $P_e^{\text{STB}} = P_f^{\text{STB}} = 1$  kW power is supplied to both devices to keep them in their standby state. The electrolyzer and of the fuel cell degradation rates are both set to  $d_i = 0.02$ , with  $i \in \{e, f\}$ , and the stack replacement cost  $S_{\text{rep},i}$  of the electrolyzer (i = e) and of the fuel cell (i = f) have been determined according to

$$S_{\text{rep},i} = \frac{2 \times \text{Capex}_i \times 0.4}{3} \bigg|_{i \in \{e, f\}}$$
(9)

where Capex<sub>*i*</sub>, for each  $i \in \{e, f\}$ , is reported in Table 4 as well as other used values. Also, the considered initial conditions for efficiency degradations  $\zeta_e$  and  $\zeta_f$  are 0.23 Nm<sup>3</sup>/kW and 1.32 kW/Nm<sup>3</sup>, respectively.

The degradation factor considered in this study is provided by the developer and the manufacturer of the PEM technology electrolyzer and the fuel cell [30]. Since the HAEOLUS project (the one founding our research and studied in the manuscript) is in its first year and will end in 2022, better degradation factors will be considered leveraging on the working plan data (up to now, the site is under construction).

PEM Electrolyzer Parameters		
$\operatorname{Cost}_{e}^{\operatorname{STB}} = 0.0042 \in$	$NH_e = 40,000 h$	
$\operatorname{Cost}_{e}^{\operatorname{ON}} = 0.123 \in$	$\operatorname{Cost}_{e}^{\operatorname{OFF}} = 0.0062 \in$	
$\operatorname{Cost}_{[\operatorname{deg},e]} = 0.05 \in$	$Capex_e = 1.55 €/kW$	
$\operatorname{Cost}_{e}^{OM} = 0.00210  \text{€/h}$	$P_e^{\max} = 3000 \mathrm{kW}$	
$P_e^{\min} = 300 \mathrm{kW}$	$P_e^{\text{STB}} = 1 \text{kW}$	
$NY_e = 8000 h$		
PEM Fuel cell Parameters		
$\operatorname{Cost}_{f}^{\operatorname{STB}} = 0.003 \in$	$NH_f = 40,000 h$	
$\operatorname{Cost}_{f}^{ON} = 0.01 \in$	$\operatorname{Cost}_{f}^{\operatorname{OFF}} = 0.005 \in$	
$\operatorname{Cost}_{[\operatorname{deg} f]} = 0.01 \in$	$Capex_f = 1.55 \in /kW$	
$\operatorname{Cost}_{OM}^{f} = 0.01  {\epsilon}/h$	$P_f^{\text{max}} = 132 \text{kW}$	
$P_f^{\min} = 12 \mathrm{kW}$	$\dot{P_f^{STB}} = 1  \mathrm{kW}$	
$NY_f = 8000 \text{ h}$	,	
Hydrogen Tank Parameters		
Volume = $20 \text{ Nm}^3$	Pressure = 30 bar	

Table 4. Cost Factor values utilized by the MPC, data based on the literature [25,38,39].

#### 5. Simulations and Numerical Results

## 5.1. Example 1

The main contribution of this paper relies in the derivation of preliminary operating models needed for running the hydrogen-based ESS for long control periods as being implemented within the EU-FCH 2 JU funded project HAEOLUS [29]. However, in order to test the system, a power demand tracking is considered. The tuning of the load tracking cost function weights seeks for a soft tracking of the output variables towards the given references and an efficient use of the energy. More specifically, if there exists a big difference between the demanded energy and the energy by wind generation, the controller operates the ESS in order to track the demand however with a major preference for minimizing operating costs. Accordingly, the prioritization weights  $\rho_l$ ,  $\rho_e$  and  $\rho_f$  have been adjusted by trial and error. In the simulations,  $H(0) = 4\text{Nm}^3$  is considered as the initial level of the hydrogen in the tank.

In our numerical examples, the wind power production and the reference power demand are such that both exceeding and missing power are considered, with a power flow towards or from the storage. In order to show the effectiveness of the implemented algorithm, the devices switching states have been shown for a case with frequent imbalances between the reference demand and the wind power over the 24 h simulation. Figure 4a, b show the electrical reference demand  $P_{ref}$  and the wind power  $P_{w}$ , respectively. It can be seen that the difference between the wind power and the reference demand is positive for the first 6 h, so the reference demand is met through the wind power only and the exceeding power is shunted to the electrolyzer (which was set by the controller to its ON state) for hydrogen production according to the current level of hydrogen and the physical constraints of the storage (Figure 4c). Figure 4e shows that the level of hydrogen in the storage has increased according to the storage constraints from H<sup>min</sup> to H<sup>max</sup> during the excess wind hours. Figure 4d shows the fuel cell power. It can be clearly observed from Figure 4d that the fuel cell does not supply power (in its OFF state) to the load when the wind power availability is higher than the reference demand. It is important to note that the controller is designed to switch the electrolyzer and the fuel cell to their STB state if it predicts the need to switch them on again in the near future, i.e., hours 7 and 15 for the electrolyzer and hour 8 for the fuel cell. Figure 4g,h show the switching states of the electrolyzer and the fuel cell, respectively. On the other hand, during the hours when the demand is higher than the wind power production (that even falls at zero for hours 9–10 and 21). The fuel cell provides back up power for re-electrification, switching from OFF to ON states. The needed power is so provided by the previously stored hydrogen in the tank. The opposite, instead, happens to the electrolyzer since there is not enough power to be stored Figure 4c. Dumping of excess wind power  $P_{dump}$  is necessary when the power surplus exceeds the storage capacity of the hydrogen tank and the transmission capacity of the external grid. Figure 4f shows that the load is being dumped during hours 7 and 9. The power surplus during these hours cannot be stored into the storage tank since the hydrogen level has already reached the tank upper bound constraint (3).



Figure 4. Numerical results for Example 1. (a) Electrical Reference Demand. (b) Forecasted Wind Power. (c) Power of the Electrolyzer. (d) Power of the Fuel Cell. (e) Level of Hydrogen. (f) Dump Load. (g) Electrolyzer Switching States. (h) Fuel cell Switching States.

## 5.2. Example 2

In order to show the effectiveness of the implemented algorithm, a stressing plant scenario has been considered in this example. As discussed above, the goal of the study is to track the reference power  $P_{ref}$  as much as possible with  $P_{avl}$ . In the case considered, the power  $P_{avl}$  is lower than the load demand  $P_{ref}$ , and the controller will only be able to deliver what is available in the system, which necessarily leads to a poor performance in meeting the desired requested power  $P_{ref}$ .

The load demand and the wind power profiles considered in this example are shown in Figure 5a,b, respectively. Figure 5c,d show the electrolyzer and the fuel cell powers for hydrogen production and consumption over the 24 h simulation horizon. It can be clearly observed from Figure 5e that during the hours 10, 11 and 18, the hydrogen in the tank is at its minimum threshold  $H^{min}$  because of low

or nearly zero wind power availability. So, the power available in the system  $P_{avl}$  is less than the power needed to meet the desired load demand  $P_{ref}$  for the said hours. This higher requested load demand can not be fully met, which results in system poor performance. Still, even in this case, the MPC controller guarantees optimal performances without violating hard physical constraints. The electrolyzer and the fuel cell switching states are shown in Figure 5f,g, respectively. Notice also that no dumping load has been observed in this scenario, because the hydrogen level has not exceeded the maximum threshold  $H^{max}$ .



**Figure 5.** Numerical results for Example 2. (a) Electrical Reference Demand. (b) Forecasted Wind Power. (c) Power of the Electrolyzer. (d) Power of the Fuel Cell. (e) Level of Hydrogen. (f) Electrolyzer Switching States. (g) Fuel cell Switching States.

# 6. Conclusions

In this work, we developed models for operating, with optimal control strategies, a hydrogen-based energy storage system to be coupled to a wind farm. The models both encode discrete logical states representing operating device modes and continuous dynamics. The cost functions take into account the cost that each device introduces any time it switches between logical states, thus decreasing the number of life cycles and degrading the efficiency along its working conditions. Furthermore, all other physical constraints and costs, such as the power consumption in standby mode, are considered. The cost related to each device and the models developed will then be included in a suitable control architecture and implemented on a real wind farm under the EU-FCH 2 JU project HAEOLUS [29]. To preliminary test the proposed models, in this paper we considered

a power demand reference tracking goal over an optimization horizon of 24 h. Numerical results show the correct behavior of the devices and their switching among the different operating modes. The power is correctly stored or retrieved via hydrogen conversion to help the wind production in determine the total available power and match the power requests.

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### Appendix A.

Appendix A.1. Constraints Formulation of the Logical States

In order to cope with an optimal control framework we need to introduce 12 auxiliary Boolean variables  $z_i^{\gamma}(k) \in \{0,1\}$ , with  $\gamma \in \{\geq 0, \leq 0, \geq P_i^{\text{STB}}, \leq P_i^{\text{STB}}, \geq P_i^{\text{min}}, \leq P_i^{\text{max}}\}$  and  $i \in \{e, f\}$  [40]

$$z_i^{\geq 0}(k) = \begin{cases} 1 & P_i(k) \geq 0, \\ 0 & P_i(k) < 0, \end{cases}$$
(A1a)

$$z_i^{\leq 0}(k) = \begin{cases} 0 & P_i(k) > 0, \\ 1 & P_i(k) \le 0, \end{cases}$$
(A1b)

$$z_i^{\geq P_i^{\text{STB}}}(k) = \begin{cases} 1 & P_i(k) \geq P_i^{\text{STB}}, \\ 0 & P_i(k) < P_i^{\text{STB}}, \end{cases}$$
(A1c)

$$z_{i}^{\leq P_{i}^{\text{STB}}}(k) = \begin{cases} 0 & P_{i}(k) > P_{i}^{\text{STB}}, \\ 1 & P_{i}(k) \le P_{i}^{\text{STB}}, \end{cases}$$
(A1d)

$$z_{i}^{\geq P_{i}^{\min}}(k) = \begin{cases} 1 & P_{i}(k) \geq P_{i}^{\min}, \\ 0 & P_{i}(k) < P_{i}^{\min}, \end{cases}$$
(A1e)

$$z_{i}^{\leq P_{i}^{\max}}(k) = \begin{cases} 0 & P_{i}(k) > P_{i}^{\max}, \\ 1 & P_{i}(k) \le P_{i}^{\max}. \end{cases}$$
(A1f)

Then, (A1) can be expressed as

$$P_i(k) < M z_i^{\geq 0}(k),$$
  
 $-P_i(k) \le M(1 - z_i^{\geq 0}(k));$  (A2a)

$$-P_i(k) < M z_i^{\leq 0}(k),$$
  
 $P_i(k) \leq M(1 - z_i^{\leq 0}(k));$ 
(A2b)

$$P_i(k) - P_i^{\text{STB}} < M z_i^{\ge P_i^{\text{STB}}}(k),$$
(A2c)

$$-P_i(k) + P_i^{\text{STB}} \le M(1 - z_i^{\ge P_i^{\text{STB}}}(k));$$

$$P_i(k) + P_i^{\text{STB}} \le M z^{\le P_i^{\text{STB}}}(k)$$

$$P_{i}(k) - P_{i}^{\min} < M z_{i}^{\geq P_{i}^{\min}}(k),$$
  
- $P_{i}(k) + P_{i}^{\min} \leq M(1 - z_{i}^{\geq P_{i}^{\min}}(k));$  (A2e)

$$-P_i(k) + P_i^{\max} < M z_i^{\leq P_i^{\max}}(k),$$

$$P_i(k) - P_i^{\max} \leq M(1 - z_i^{\leq P_i^{\max}}(k)),$$
(A2f)

where *M* is a sufficiently large positive number.

The auxiliary variables codified by the inequalities (A2) are then exploited to model the Mixed-Linear Dynamic (MLD) by linking the discrete logical variables of each device with the corresponding operating power, according to (1). Namely, for  $i \in \{e, f\}$ ,  $\alpha \in \{OFF, STB, ON\}$ , the variables  $\delta_i^{\alpha}(k) \in [0, 1]$  are determined by

$$(1 - \delta_i^{\text{ON}}(k)) + z_i^{\geq P_i^{\min}}(k) \ge 1,$$
(A3a)

$$(1 - \delta_i^{\text{ON}}(k)) + z_i^{\leq P_i^{\text{max}}}(k) \ge 1;$$
(A3b)

$$(1 - \delta_i^{\text{STB}}(k)) + z_i^{\geq P_i^{\text{STB}}}(k) \ge 1, \tag{A3c}$$

$$(1 - \delta_i^{\text{STB}}(k)) + z_i^{\leq P_i^{\text{STB}}}(k) \ge 1;$$
(A3d)
$$(1 - \delta_i^{\text{OFE}}(k)) + z_i^{\geq 0}(k) \ge 1$$

$$(1 - \delta_i^{OFF}(k)) + z_i^{\leq 0}(k) \ge 1,$$
(A3e)
$$(1 - \delta_i^{OFF}(k)) + z_i^{\leq 0}(k) \ge 1,$$
(A3e)

$$(1 - \delta_i^{OFF}(k)) + z_i^{\leq 0}(k) \geq 1;$$
(A3f)

$$\delta_i^{\text{ON}}(k) + \delta_i^{\text{OFF}}(k) + \delta_i^{\text{STB}}(k) = 1.$$
(A3g)

Notice that, despite  $\delta_i^{\alpha}(k)$  being continuous, they can only assume the binary values {0,1} due to (A3), that is in practice  $\delta_i^{\alpha}(k)$ s are logical.

## Appendix A.2. Mathematical Model and Constraints Formulation of the State Transitions

As discussed above, the devices models are characterized by three discrete operational states. These operational states imply possible mode transitions for each device. In what follows, we define all of the transitions. The transitions among the states for the each transition is the result of the state change, and can be defined by suitably combining logical variables, thus achieving

$$\sigma_{\text{ON}_i}^{\text{OFF}}(k) = \delta_i^{\text{ON}}(k-1) \wedge \delta_i^{\text{OFF}}(k), \tag{A4a}$$

$$\sigma_{\text{OFF}_i}^{\text{ON}}(k) = \delta_i^{\text{OFF}}(k-1) \wedge \delta_i^{\text{ON}}(k), \tag{A4b}$$

$$\sigma_{\text{ON}_i}^{\text{STB}}(k) = \delta_i^{\text{ON}}(k-1) \wedge \delta_i^{\text{STB}}(k), \tag{A4c}$$

$$\sigma_{\text{STB}_i}^{\text{ON}}(k) = \delta_i^{\text{STB}}(k-1) \wedge \delta_i^{\text{ON}}(k), \tag{A4d}$$

$$\sigma_{\text{STB}_i}^{\text{OFF}}(k) = \delta_i^{\text{STB}}(k-1) \wedge \delta_i^{\text{OFF}}(k), \tag{A4e}$$

$$\sigma_{\text{OFF}_i}^{\text{STB}}(k) = \delta_i^{\text{OFF}}(k-1) \wedge \delta_i^{\text{STB}}(k), \tag{A4f}$$

with  $\alpha$ ,  $\beta \in \{OFF, STB, ON\}$ ,  $\alpha \neq \beta$ . Using the relationships defined by Bemporad and Morari [40], each expression of the (A4) is equivalently converted into three inequalities and introduced in the constraints of MPC controller, thus resulting in the 18 following formulas

$$-\delta_{i}^{\text{ON}}(k-1) + \sigma_{\text{ON}_{i}}^{\text{OFF}}(k) \leq 0,$$
  
$$-\delta_{i}^{\text{OFF}}(k) + \sigma_{\text{ON}_{i}}^{\text{OFF}}(k) \leq 0,$$
  
$$\delta_{i}^{\text{ON}}(k-1) + \delta_{i}^{\text{OFF}}(k) - \sigma_{\text{ON}_{i}}^{\text{OFF}}(k) \leq 1;$$
  
(A5a)

$$\begin{aligned} &-\delta_i^{\text{OFF}}(k-1) + \sigma_{\text{OFF}_i}^{\text{ON}}(k) \leq 0, \\ &-\delta_i^{\text{ON}}(k) + \sigma_{\text{OFF}_i}^{\text{ON}}(k) \leq 0, \end{aligned} \tag{A5b}$$

$$\delta_{i}^{\text{OFF}}(k-1) + \delta_{i}^{\text{ON}}(k) - \sigma_{\text{OFF}_{i}}^{\text{ON}}(k) \leq 1;$$
  
$$-\delta_{i}^{\text{ON}}(k-1) + \sigma_{\text{ON}_{i}}^{\text{STB}}(k) \leq 0,$$
  
$$-\delta_{i}^{\text{STB}}(k) + \sigma_{\text{ON}_{i}}^{\text{STB}}(k) \leq 0,$$
 (A5c)

$$\delta_{i}^{\text{ON}}(k-1) + \delta_{i}^{\text{STB}}(k) - \sigma_{\text{ON}_{i}}^{\text{STB}}(k) \leq 1;$$
  
$$-\delta_{i}^{\text{STB}}(k-1) + \sigma_{\text{STB}_{i}}^{\text{ON}}(k) \leq 0,$$
  
(1997)

$$-\delta_{i}^{\text{ON}}(k) + \sigma_{\text{STB}_{i}}^{\text{ON}}(k) \leq 0, \tag{A5d}$$
$$\delta_{i}^{\text{STB}}(k-1) + \delta_{i}^{\text{ON}}(k) - \sigma_{\text{STB}_{i}}^{\text{ON}}(k) \leq 1;$$

$$-\delta_i^{\text{STB}}(k-1) + \sigma_{\text{STB}_i}^{\text{OFF}}(k) \le 0,$$
  
$$-\delta_i^{\text{OFF}}(k) + \sigma_{\text{STB}_i}^{\text{OFF}}(k) \le 0,$$
  
(A5e)

$$\delta_{i}^{\text{OFF}}(k-1) + \delta_{i}^{\text{OFF}}(k) - \sigma_{\text{OFF}_{i}}^{\text{STB}}(k) \leq 1;$$
  

$$-\delta_{i}^{\text{OFF}}(k-1) + \sigma_{\text{OFF}_{i}}^{\text{STB}}(k) \leq 0,$$
  

$$-\delta_{i}^{\text{STB}}(k) + \sigma_{\text{OFF}_{i}}^{\text{STB}}(k) \leq 0,$$
  

$$\delta_{i}^{\text{OFF}}(k-1) + \delta_{i}^{\text{STB}}(k) - \sigma_{\text{OFF}_{i}}^{\text{STB}}(k) \leq 1,$$
  
(A5f)

where  $\sigma_{\alpha_i}^{\beta} \in [0, 1]$ , and analogously to  $\delta_i^{\alpha}(k)$ s, they can only assume values {0, 1} due to (A5).

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