

## Supplementary Materials

### Sets of chemical reactions

**Table S1.** Main chemical reactions in blue jets. The rate coefficients are in units of  $s^{-1}$  for uni-molecular,  $cm^3 s^{-1}$  for two-body reaction, and  $cm^6 s^{-1}$  for three-body reactions. T is the gas temperature in Kelvin. M stands for  $N_2$  and  $O_2$  molecule.

No.	Reaction	Rate coefficient	Refer ence
Electron attachment			
1	$e^- + O_3 \rightarrow O_2^- + O$	$10^{-9}$	3
2	$e^- + O_3 \rightarrow O^- + O_2$	$10^{-11}$	3
3	$e^- + O_3 + O_2 \rightarrow O_3^- + O_2$	$10^{-31}$	2
4	$e^- + NO \xrightarrow{M} NO^-$	$10^{-30}$	3
5	$e^- + NO_2 \rightarrow NO_2^-$	$3 \times 10^{-11}$	3
6	$e^- + NO_2 \rightarrow O^- + NO$	$10^{-11}$	3
Electron detachment			
1	$O_2^- + O \rightarrow e^- + O_3$	$1.5 \times 10^{-10}$	3
2	$O_2^- + N \rightarrow e^- + NO_2$	$5 \times 10^{-10}$	3
3	$O^- + O_2(a) \rightarrow e^- + O_3$	$3 \times 10^{-10}$	3
4	$O^- + N_2 \rightarrow e^- + N_2O$	$10^{-12}$	2
5	$O^- + N \rightarrow e^- + NO$	$2.6 \times 10^{-10}$	3
6	$O^- + O_2 \rightarrow e^- + O_3$	$5 \times 10^{-15}$	3
7	$O^- + NO \rightarrow e^- + NO_2$	$2.6 \times 10^{-10}$	3
8	$O^- + O_3 \rightarrow e^- + O_2 + O_2$	$5 \times 10^{-10} \times (T/300)^{0.5}$	5
9	$O_3^- + O \rightarrow e^- + O_2 + O_2$	$3 \times 10^{-10}$	3
10	$O_3^- + O_3 \rightarrow e^- + 3O_2$	$10^{-10}$	2
11	$NO^- + N_2O \rightarrow e^- + NO + N_2O$	$5.1 \times 10^{-12}$	2
12	$NO^- + NO \rightarrow e^- + NO + NO$	$5 \times 10^{-12}$	2
13	$NO_2^- + O \rightarrow e^- + NO_3$	$10^{-12}$	3

Associative and Penning ionization			
1	$N(^2P) + O \rightarrow e^- + NO^+$	$10^{-11}$	2
Positive ion chemistry			
1	$N_2^+ + O \rightarrow NO^+ + N$	$1.3 \times 10^{-10} \times (T/300)^{-0.5}$	3
2	$N_2^+ + O_3 \rightarrow O_2^+ + O + N_2$	$10^{-10}$	3
3	$N_2^+ + N_2O \rightarrow N_2O^+ + N_2$	$5 \times 10^{-10}$	3
4	$N_2^+ + N_2O \rightarrow NO^+ + N + N_2$	$4 \times 10^{-10}$	3
5	$N_2^+ + NO \rightarrow NO^+ + N_2$	$3.3 \times 10^{-10}$	3
6	$N_3^+ + O_2 \rightarrow NO_2^+ + N_2$	$4.4 \times 10^{-11}$	3
7	$N_3^+ + NO \rightarrow N_2O^+ + N_2$	$7 \times 10^{-11} \times (T/300)^{0.5}$	5
8	$N_3^+ + NO \rightarrow NO^+ + N + N_2$	$7 \times 10^{-11}$	3
9	$N_3^+ + NO \rightarrow N_2O^+ + N_2$	$7 \times 10^{-11}$	3
10	$N_4^+ + NO \rightarrow NO^+ + N_2 + N_2$	$4 \times 10^{-10}$	3
11	$N^+ + O \xrightarrow{M} NO^+$	$10^{-29}$	3
12	$N^+ + O_3 \rightarrow NO^+ + O_2$	$5 \times 10^{-10}$	3
13	$N^+ + O_2 \rightarrow NO^+ + O$	$5 \times 10^{-11} \times (T/300)^{0.5}$	5
14	$N^+ + O_2 \rightarrow NO^+ + O(^1D)$	$2 \times 10^{-10} \times (T/300)^{0.5}$	5
15	$N^+ + O_2 \rightarrow O^+ + NO$	$2.8 \times 10^{-11}$	3
16	$N^+ + NO \rightarrow NO^+ + N$	$8 \times 10^{-10}$	3
17	$N^+ + NO \rightarrow N_2^+ + O$	$3 \times 10^{-12}$	3
18	$N^+ + NO \rightarrow O^+ + N_2$	$10^{-12}$	3
19	$N^+ + N_2O \rightarrow NO^+ + N_2$	$5.5 \times 10^{-10}$	3
20	$O_2^+ + N_2 \rightarrow NO^+ + NO$	$4 \times 10^{-21} \times (T/300)^{-2}$	6
21	$O_2^+ + N \rightarrow NO^+ + O$	$1.2 \times 10^{-10}$	3
22	$O_2^+ + NO \rightarrow NO^+ + O_2$	$4.4 \times 10^{-10}$	3
23	$O_2^+ + NO_2 \rightarrow NO_2^+ + O_2$	$6.6 \times 10^{-10}$	3

24	$O_2^+ + NO_2 \rightarrow NO^+ + O_3$	$10^{-11}$	3
25	$O_4^+ + O \rightarrow O_2^+ + O_3$	$3 \times 10^{-10}$	3
26	$O_4^+ + NO \rightarrow NO^+ + O_2 + O_2$	$10^{-10}$	3
27	$O^+ + N \xrightarrow{M} NO^+$	$10^{-29}$	3
28	$O^+ + N_2 \rightarrow NO^+ + N$	$1.2 \times 10^{-12} \times (T/300)^{-1}$	5
29	$O^+ + N_2 \xrightarrow{M} NO^+ + N$	$6 \times 10^{-29} \times (T/300)^{-2}$	3
30	$O^+ + NO_2 \rightarrow NO_2^+ + O$	$1.6 \times 10^{-9}$	3
31	$O^+ + NO \rightarrow NO^+ + O$	$2.4 \times 10^{-11}$	3
32	$O^+ + NO \rightarrow O_2^+ + N$	$3 \times 10^{-12}$	3
33	$O^+ + N_2O \rightarrow N_2O^+ + O$	$4 \times 10^{-10}$	3
34	$O^+ + N_2O \rightarrow NO^+ + NO$	$2.3 \times 10^{-10}$	3
35	$O^+ + N_2O \rightarrow O_2^+ + N_2$	$2 \times 10^{-11}$	3
36	$O^+ + O_3 \rightarrow O_2^+ + O_2$	$10^{-10}$	3
37	$NO_2^+ + NO \rightarrow NO^+ + NO_2$	$2.9 \times 10^{-10}$	3
38	$N_2O^+ + NO \rightarrow NO^+ + N_2O$	$2.9 \times 10^{-10}$	3
39	$NO^+ + O_3 \rightarrow NO_2^+ + O_2$	$10^{-15}$	3
40	$NO^+ + N_2O_5 \rightarrow NO_2^+ + 2NO_2$	$5.9 \times 10^{-10}$	3
41	$NO^+(N_2) \xrightarrow{M} NO^+ + N_2$	$1.5 \times 10^{-8} \times (T/300)^{-5.3} \times \exp(-2093/T)$	6
42	$NO^+(N_2) + O_2 \rightarrow NO^+ + N_2$	$10^{-9}$	6
43	$NO^+(O_2) + N_2 \rightarrow NO^+ + O_2$	$10^{-9}$	6
Negative ion chemistry			
1	$e^- + O_3 \rightarrow e^- + O_2 + O$	$10^{-8}$	2
2	$O^- + O_2 \rightarrow O_3^- + O$	$5.3 \times 10^{-10}$	3
3	$O^- + O_2 \xrightarrow{M} O_3^-$	$1.1 \times 10^{-30} \times (T/300)^{-1}$	3
4	$O_2^- + O_3 \rightarrow O_3^- + O_2$	$4 \times 10^{-10}$	3
5	$O_3^- + O \rightarrow O_2^- + O_2$	$3.2 \times 10^{-10}$	3

6	$O_4^- + O \rightarrow O_3^- + O_2$	$4 \times 10^{-10}$	3
7	$O^- + NO \xrightarrow{M} NO_2^-$	$10^{-29}$	3
8	$O^- + NO_2 \rightarrow NO_2^- + O$	$1.2 \times 10^{-9}$	3
9	$O^- + N_2O \rightarrow NO^- + NO$	$2 \times 10^{-10}$	3
10	$O_2^- + NO_2 \rightarrow NO_2^- + O_2$	$8 \times 10^{-10}$	3
11	$O_3^- + NO \rightarrow NO_2^- + O_2$	$2.6 \times 10^{-12}$	3
12	$O_3^- + NO \rightarrow NO_3^- + O$	$10^{-11}$	3
13	$O_3^- + NO_2 \rightarrow NO_2^- + O_3$	$7 \times 10^{-10}$	3
14	$O_3^- + NO_2 \rightarrow NO_3^- + O_2$	$2 \times 10^{-11}$	3
15	$O_3^- + NO_3 \rightarrow NO_3^- + O_3$	$5 \times 10^{-10}$	3
16	$NO^- + O_2 \rightarrow O_2^- + NO$	$5 \times 10^{-10}$	3
17	$NO^- + NO_2 \rightarrow NO_2^- + NO$	$7.4 \times 10^{-16}$	3
18	$NO^- + N_2O \rightarrow NO_2^- + N_2$	$2.8 \times 10^{-14}$	3
19	$NO_2^- + O_3 \rightarrow NO_3^- + O_2$	$1.8 \times 10^{-11}$	3
20	$NO_2^- + NO_2 \rightarrow NO_3^- + NO$	$4 \times 10^{-12}$	3
21	$NO_2^- + NO_3 \rightarrow NO_3^- + NO_2$	$5 \times 10^{-10}$	3
22	$NO_3^- + NO \rightarrow NO_2^- + NO_2$	$3 \times 10^{-15}$	3
Electron-ion recombination			
1	$e^- + NO^+ \xrightarrow{M} NO$	$6 \times 10^{-27} \times (T/300)^{-1.5}$	3
2	$e^- + NO^+ \rightarrow N + O$	$4 \times 10^{-7} \times (T/300)^{-1.5}$	3
3	$e^- + NO^+ \rightarrow N(^2D) + O$	$3 \times 10^{-7} \times (T/300)^{-1}$	3
4	$e^- + NO^+(N_2) \rightarrow NO + N_2$	$1.3 \times 10^{-6} \times (T/300)^{-0.5}$	3
5	$e^- + NO^+(O_2) \rightarrow NO + O_2$	$1.3 \times 10^{-6} \times (T/300)^{-0.5}$	3
6	$e^- + NO_2^+ \rightarrow NO + O$	$2 \times 10^{-7} \times (T/300)^{-0.5}$	3
7	$e^- + N_2O^+ \rightarrow O + N_2$	$1.3 \times 10^{-6} \times (T/300)^{-0.5}$	3
Neutral chemistry			

1	$\text{N} + \text{O}_2 \rightarrow \text{NO} + \text{O}$	$1.5 \times 10^{-11} \times \exp(-3600/T)$	4
2	$\text{N} + \text{O}_3 \rightarrow \text{NO} + \text{O}_2$	$10^{-16}$	4
3	$\text{N} + \text{NO} \rightarrow \text{N}_2 + \text{O}$	$2.1 \times 10^{-11} \times \exp(-100/T)$	4
4	$\text{N} + \text{NO}_2 \rightarrow \text{N}_2\text{O} + \text{O}$	$3 \times 10^{-12}$	3
5	$\text{N} + \text{NO}_2 \rightarrow \text{NO} + \text{NO}$	$2.3 \times 10^{-12}$	3
6	$\text{N} + \text{NO}_2 \rightarrow \text{N}_2 + \text{O}$	$9.1 \times 10^{-13}$	3
7	$\text{N} + \text{NO}_2 \rightarrow \text{N}_2 + \text{O}_2$	$7 \times 10^{-13}$	3
8	$\text{N} + \text{O} \xrightarrow{\text{M}} \text{NO}$	$1.76 \times 10^{-31} \times T^{-0.5}$	3
9	$\text{O} + \text{O}_3 \rightarrow \text{O}_2 + \text{O}_2$	$8 \times 10^{-12} \times \exp(-2060/T)$	4
10	$\text{O} + \text{NO}_2 \rightarrow \text{NO} + \text{O}_2$	$5.1 \times 10^{-12} \times \exp(210/T)$	4
11	$\text{O} + \text{NO}_3 \rightarrow \text{NO}_2 + \text{O}_2$	$10^{-11}$	4
12	$\text{O} + \text{O}_2 \xrightarrow{\text{M}} \text{O}_3$	$6 \times 10^{-34} \times (T/300)^{-2.4}$	4
13	$\text{O} + \text{NO} \xrightarrow{\text{M}} \text{NO}_2$	$9 \times 10^{-32} \times (T/300)^{-1.5}$	4
14	$\text{O} + \text{O}_3 + \text{O}_2 \rightarrow \text{O}_3 + \text{O}_3 + \text{O}_2$	$1.5 \times 10^{-34} \times \exp(750/T)$	2
15	$\text{O} + \text{O} + \text{O}_2 \rightarrow \text{O}_2 + \text{O}_3 + \text{O}$	$2.15 \times 10^{-34} \times \exp(345/T)$	2
16	$\text{O} + \text{NO}_2 \xrightarrow{\text{M}} \text{NO}_3$	$2.5 \times 10^{-31} \times (T/300)^{-1.8}$	4
17	$\text{O} + \text{NO} \rightarrow \text{NO}_2$	$3.02 \times 10^{-11} \times (T/300)^{-0.75}$	2
18	$\text{NO} + \text{NO}_3 \rightarrow \text{NO}_2 + \text{NO}_2$	$1.5 \times 10^{-11} \times \exp(170/T)$	4
19	$\text{NO} + \text{O}_3 \rightarrow \text{NO}_2 + \text{O}_2$	$3 \times 10^{-12} \times \exp(-1500/T)$	4
20	$\text{NO}_2 + \text{O}_3 \rightarrow \text{NO}_3 + \text{O}_2$	$1.2 \times 10^{-13} \times \exp(-2450/T)$	4
21	$\text{NO}_2 + \text{NO}_3 \rightarrow \text{NO} + \text{NO}_2 + \text{O}_2$	$2.3 \times 10^{-13} \times \exp(-1600/T)$	9
22	$\text{NO}_2 + \text{NO}_3 \xrightarrow{\text{M}} \text{N}_2\text{O}_5$	$2.4 \times 10^{-30} \times (T/300)^{-3}$	4
23	$\text{NO}_3 + \text{NO}_3 \rightarrow \text{NO}_2 + \text{NO}_2 + \text{O}_2$	$8.5 \times 10^{-13} \times \exp(-2450/T)$	4
24	$\text{N}(^2\text{D}) + \text{O}_2 \rightarrow \text{NO} + \text{O}$	$1.5 \times 10^{-12} \times (T/300)^{0.5}$	3
25	$\text{N}(^2\text{D}) + \text{O}_2 \rightarrow \text{NO} + \text{O}(^1\text{D})$	$6 \times 10^{-12} \times (T/300)^{0.5}$	3
26	$\text{N}(^2\text{D}) + \text{N}_2\text{O} \rightarrow \text{NO} + \text{N}_2$	$3.5 \times 10^{-12}$	2

27	$\text{N}(^2\text{D}) + \text{NO} \rightarrow \text{N}_2 + \text{O}$	$1.8 \times 10^{-10}$	2
28	$\text{N}(^2\text{D}) + \text{NO} \rightarrow \text{N}_2\text{O}$	$6 \times 10^{-11}$	3
29	$\text{N}(^2\text{P}) + \text{O}_2 \rightarrow \text{NO} + \text{O}$	$2.6 \times 10^{-12}$	3
30	$\text{N}(^2\text{P}) + \text{NO} \rightarrow \text{O} + \text{N}_2$	$3 \times 10^{-11}$	2
31	$\text{O}(^1\text{D}) + \text{O}_3 \rightarrow 2\text{O} + \text{O}_2$	$2.4 \times 10^{-10}$	4
32	$\text{O}(^1\text{D}) + \text{O}_3 \rightarrow \text{O}_2 + \text{O}_2$	$2.4 \times 10^{-10}$	4
33	$\text{O}(^1\text{D}) + \text{O}_3 \rightarrow \text{O} + \text{O}_3$	$2.4 \times 10^{-10}$	4
34	$\text{O}(^1\text{D}) + \text{N}_2\text{O} \rightarrow \text{NO} + \text{NO}$	$1.19 \times 10^{-10} \times \exp(20/T)$	4
35	$\text{O}(^1\text{D}) + \text{N}_2\text{O} \rightarrow \text{N}_2 + \text{O}_2$	$1.19 \times 10^{-10} \times \exp(20/T)$	4
36	$\text{O}(^1\text{D}) + \text{N}_2\text{O} \rightarrow \text{O} + \text{N}_2\text{O}$	$1.19 \times 10^{-10} \times \exp(20/T)$	4
37	$\text{O}(^1\text{D}) + \text{NO} \rightarrow \text{N} + \text{O}_2$	$1.7 \times 10^{-10}$	3
38	$\text{O}(^1\text{D}) + \text{NO}_2 \rightarrow \text{NO} + \text{O}_2$	$3 \times 10^{-10}$	2
39	$\text{O}(^1\text{S}) + \text{O}_3 \rightarrow \text{O}(^1\text{D}) + \text{O} + \text{O}_2$	$2.9 \times 10^{-10}$	3
40	$\text{O}(^1\text{S}) + \text{O}_3 \rightarrow \text{O}_2 + \text{O}_2$	$2.9 \times 10^{-10}$	3
41	$\text{O}(^1\text{S}) + \text{NO} \rightarrow \text{NO} + \text{O}$	$1.8 \times 10^{-10}$	3
42	$\text{O}(^1\text{S}) + \text{NO} \rightarrow \text{O}(^1\text{D}) + \text{NO}$	$3.2 \times 10^{-10}$	3
43	$\text{O}(^1\text{S}) + \text{N}_2\text{O} \rightarrow \text{N}_2\text{O} + \text{O}$	$6.3 \times 10^{-12}$	3
44	$\text{O}(^1\text{S}) + \text{N}_2\text{O} \rightarrow \text{O}(^1\text{D}) + \text{N}_2\text{O}$	$3.1 \times 10^{-12}$	3
45	$\text{O}_2(\text{a}) + \text{N} \rightarrow \text{O} + \text{NO}$	$2 \times 10^{-14} \times \exp(-600/T)$	3
46	$\text{O}_2(\text{a}) + \text{NO} \rightarrow \text{O} + \text{NO}_2$	$4.88 \times 10^{-18}$	2
47	$\text{O}_2(\text{a}) + \text{NO} \rightarrow \text{NO} + \text{O}_2$	$2.48 \times 10^{-17}$	7
48	$\text{O}_2(\text{a}) + \text{O}_3 \rightarrow \text{O}(^1\text{D}) + \text{O}_2 + \text{O}_2$	$5.2 \times 10^{-11} \times \exp(-2840/T)$	5
49	$\text{O}_2(\text{a}) + \text{O}_3 \rightarrow \text{O} + \text{O}_2 + \text{O}_2$	$5.2 \times 10^{-11} \times \exp(-2840/T)$	4
50	$\text{O}_2(\text{a}) + \text{O}_2(\text{a}) + \text{O}_2 \rightarrow \text{O}_3 + \text{O}_3 + \text{O}_2$	$10^{-31} \times (T/300)^{0.5}$	5
51	$\text{O}_2(\text{b}) + \text{O}_3 \rightarrow 2\text{O}_2(\text{a}) + \text{O}$	$3.5 \times 10^{-11} \times \exp(-135/T)$	4
52	$\text{O}_2(\text{b}) + \text{NO} \rightarrow \text{O}_2(\text{a}) + \text{NO}$	$4 \times 10^{-14}$	3

53	$N_2(A) + O_2 \rightarrow N_2O + O$	$7.8 \times 10^{-14}$	3
54	$N_2(A) + O \rightarrow N(^2D) + NO$	$7 \times 10^{-12}$	3
55	$N_2(A) + NO \rightarrow N_2 + NO$	$7 \times 10^{-11}$	3
56	$N_2(A) + N_2O \rightarrow N_2 + N + NO$	$10^{-11}$	3
57	$N_2(B) + NO \rightarrow N_2(A) + NO$	$2.4 \times 10^{-10}$	3
58	$N_2(a'^1) + NO \rightarrow N_2 + N + O$	$3.6 \times 10^{-10}$	3
59	$N_2(a^1) + NO \rightarrow N_2 + N + O$	$3.6 \times 10^{-10}$	2
60	$O_3 \xrightarrow{h\nu} O_2 + O$	$f(h\nu)$	1
61	$O_3 \xrightarrow{h\nu} O_2 + O(^1D)$	$f(h\nu)$	1
62	$NO \xrightarrow{h\nu} N + O$	$f(h\nu)$	1
63	$NO_2 \xrightarrow{h\nu} NO + O$	$f(h\nu)$	1
64	$NO_3 \xrightarrow{h\nu} NO_2 + O$	$f(h\nu)$	1
65	$N_2O \xrightarrow{h\nu} O(^1D) + N_2$	$f(h\nu)$	1
Ion-ion recombination			
1	$A^- + (BC)^+ \rightarrow A + B + C$	$10^{-7}$	3
	$A^- = [O_3^-, NO^-, NO_2^-]$ and $(BC)^+ = [NO^+, NO_2^+, N_2O^+]$		
2	$O_3^- + A^+ \rightarrow 2O_2 + A$	$10^{-7}$	3
	$A^+ = [NO^+, NO_2^+, N_2O^+]$		
3	$A^- + B^+ \rightarrow A + B$	$2 \times 10^{-7} \times (T/300)^{-0.5}$	3
	$A^- = [O_3^-, NO^-, NO_2^-]$ and $B^+ = [NO_2^+, N_2O^+]$		

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