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# A Novel Ensemble Neuro-Fuzzy Model for Financial Time Series Forecasting

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Received: 30 June 2019; Accepted: 20 August 2019; Published: 23 August 2019

**Abstract:** Neuro-fuzzy models have a proven record of successful application in finance. Forecasting future values is a crucial element of successful decision making in trading. In this paper, a novel ensemble neuro-fuzzy model is proposed to overcome limitations and improve the previously successfully applied a five-layer multidimensional Gaussian neuro-fuzzy model and its learning. The proposed solution allows skipping the error-prone hyperparameters selection process and shows better accuracy results in real life financial data.

**Keywords:** time series; neuro-fuzzy; ensemble; model averaging; Gaussian; prediction; stochastic gradient descent

## 1. Introduction

Time series forecasting is an important practical problem and a challenge for Artificial Intelligence systems. Financial time series have a particular importance, but they also show an extremely complex nonlinear dynamic behavior, which makes them hard to predict.

Classical statistical methods dominate the field of financial data and have a long history of development. Nevertheless, in many cases they have significant limitations like restrictions on datasets, require complex data preprocessing and additional statistical tests.

Artificial intelligence models and methods have been competing classical statistical approaches in many domains including financial forecasting and analysis. Neuro-fuzzy systems naturally inherit strengths of artificial neural networks and fuzzy inference systems, and have been successfully applied to a variety of problems including forecasting. Rajab and Sharma [1] made a comprehensive review of the application of neuro-fuzzy systems in business.

Historically, ANFIS—Adaptive Network Fuzzy Inference System, proposed by Jang [2], was the first successfully applied neuro-fuzzy model and most of the later works have been based on it.

Examples of successfully applied ANFIS-derived models for stock market prediction are the neuro-fuzzy model with a modification of the Levenberg–Marquardt learning algorithm for Dhaka Stock Exchange day closing price prediction [3] and an ANFIS model based on an indirect approach and tested on Tehran Stock Exchange Indexes [4].

Rajab and Sharma [5] proposed an interpretable neuro-fuzzy approach to stock price forecasting applied to various exchange series.

García et al. [6] applied a hybrid fuzzy neural network to predict price direction in the stock market index, which consists of the 30 major German companies.

In order to improve results by further hybridization, neuro-fuzzy forecasting models in finance were combined with evolutionary computing as, e.g., in Hadavandi et al [7]. Chiu and Chen [8] and Gonzalez et al. [9] described models which use support vector machines (SVM) together with fuzzy models and genetic algorithms. Another effective approach is to exploit the representative capabilities of wavelets (for instance, Bodyanskiy et al. [10], Chandar [11]) and recurrent connections as in Parida et al. [12] and Atsalakis and Valavanis [13]. Cai et al. [14] used ant colony optimization. Some optimization techniques were applied to Type-2 models [15–17]. All such models benefit from combining the strengths of different approaches but may suffer from the growth of parameters to be tuned.

Neuro-fuzzy models in general require many rules to cover complex nonlinear relations, which is known as the curse of dimensionality. In order to overcome this, Vlasenko et al. [18–20] proposed a neuro-fuzzy model for time series forecasting, which exploits multidimensional Gaussians ability to handle nontrivial data dependencies by a relatively small number of computational units. It also displays good computational performance, which is achieved through using a stochastic gradient optimization procedure for tuning consequent layer units and an iterative projective algorithm for tuning their weights.

However, this model also has its limitations, the biggest of which is the necessity to manually choose training hyperparameters and the model sensitivity for this choice. Many different approaches may be applied to hyperparameter tuning, but in general they are greedy for computational resources and may require complex stability analysis. Another issue, despite generally good computational performance, is the inability of the stochastic gradient descent learning procedure to utilize multithreading capabilities of the modern hardware.

The remainder of this paper is organized as follows: Section 2 is devoted to the proposed model architecture and learning, and Section 3 describes the data sets and contains experimental results.

### 2. Proposed Model and Inference

To solve the aforementioned problems, we propose an ensemble model and an initialization procedure for it. It comprises neuro-fuzzy member models  $M_e$ . The general architecture presented in Figure 1.

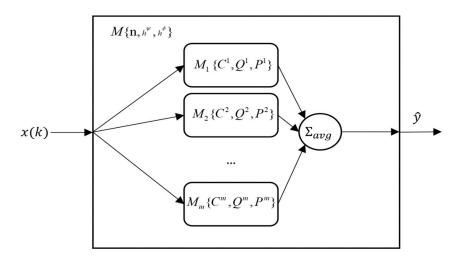


Figure 1. General architecture of the proposed model.

Each input pattern x(k) is propagated to all models  $M_e$ . All models have the same structure which is defined by three parameters—the length of input vector n, number of antecedent layer functions  $h^{\psi}$  and number of consequent node functions  $h^{\varphi}$  (analogous to a number of polynomial

Then all outputs are sent to the output node  $\Sigma_{avg}$ , which computes the resulting value  $\hat{y}$  as an average value:

$$\hat{y} = \frac{\sum_{e=1}^{m} \hat{y}_e}{m}$$

where  $\hat{y}_e$  is a member model output, and *m* is the number of member models. Model averaging is the simplest way to combine different models and achieve better accuracy under the assumption that different models will show partially independent errors, which in turn may lead to better generalization capabilities.

Detailed structure of a five layer member model introduced in [18] is depicted in Figure 2.

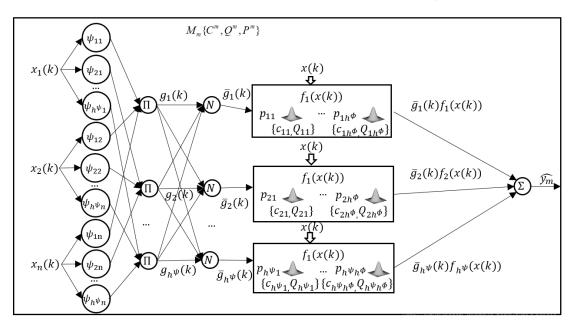


Figure 2. Architecture of the member model.

Each member model performs an inference by the following formulae:

$$\hat{y}_e = p_e^T f_e(x(k))$$

where  $x(k) = (x_1(k), x_2(k), ..., x_n(k))^T$  is an input vector,  $p_e$  is the weights vector (a vector representation of the  $P^e$  matrix), and  $f_e(x(k))$  is a vector of normalized consequent function values:

$$f_{e}(x(k)) = (\bar{g}_{e1}\phi_{e11}(x(k))...\bar{g}_{eh^{\psi}}\phi_{eh^{\psi}h^{\phi}}(x(k)))$$

where  $h^{\psi}$  is the number of functions in the first layer and  $h^{\varphi}$  is the number of multidimensional Gaussians in the fourth layer for each normalized output  $\overline{g}_{el}$ :

$$\overline{g}_{je}(k) = \frac{g_{je}(k)}{\frac{h\Psi}{\sum\limits_{j=1}^{n}g_{je}(k)}} = \frac{\prod\limits_{i=1}^{n}\psi_{jl}e(x_{i}(k))}{\frac{h\Psi}{\sum\limits_{i=1}^{n}\prod\limits_{i=1}^{n}\psi_{jl}e(x_{i}(k))}}$$

The initialization algorithm is shown in Figure 3. Its goal is to initialize member models before training and set training parameters. Results from [18,20] show that  $\beta_c$  and  $\beta_Q$  hyperparameters, which are dumping parameters for optimization of  $C^e$  and  $Q^e$ , respectively, significantly influence accuracy of the model prediction. According to this we create identical member models but set different values for  $\beta_c$  and  $\beta_Q$ . Centers are placed equidistantly and identity matrices are used as receptive before training. After models are created we can start training them in parallel.

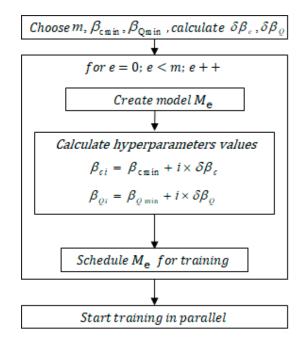


Figure 3. General algorithm of ensemble initialization.

The general training process is depicted in Figure 4. We use historical data as a training set and feed vectors of historical gap values to each model. Then reference value y(k) is used to calculate error  $e_e$  for each local model. Error is then propagated and used to calculate deltas  $\Delta_m \{C^m, Q^m, P^m\}$  to adjust the model's free parameters  $C^e, Q^e, P^e$ .

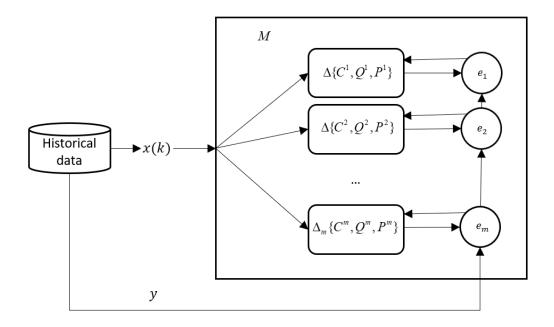


Figure 4. Visualization of ensemble learning.

The training process is focused on multidimensional Gaussian functions of the fourth layer and their weights.

Consequent Gaussians have the following form:

$$\phi_{aje}(x(k)) = \exp\left(-\frac{(x(k) - c_{aje}^{\phi})^{T} Q_{aje}^{-1}(x(k) - c_{aje}^{\phi}(k))}{2}\right),$$

where x(k) represents an input values vector,  $c_{aje}^{\phi}$  is a center of the current Gaussian, and  $Q_{aje}$  is the receptive field matrix. Figure 5 shows an example of an initialized Gaussian in a two-dimensional case.

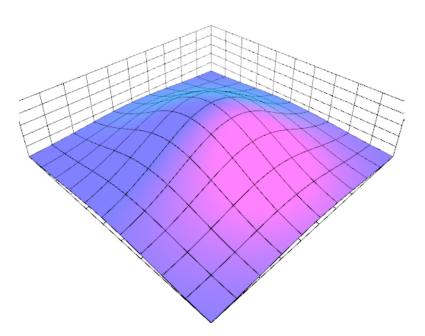


Figure 5. An example of a multidimensional Gaussian with an identity receptive field matrix.

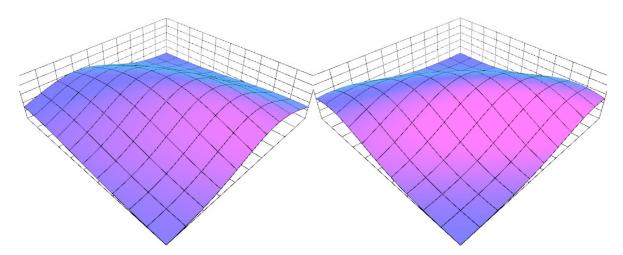
The first-order stochastic gradient descent, based on the standard mean square error criterion, is used for optimization of  $C^e$  and  $Q^e$ . Stochastic gradient optimization methods update free model parameters after processing each input pattern, and they successfully compete batch gradient methods, which compute the full gradient over all dataset in batches, in real-life optimization problems including machine learning applications [21,22]. Their main advantage arises from the intrinsic noise in the gradient's calculation. The significant disadvantage is that they cannot be effectively parallelized as batch methods [23], but in the case of an ensemble model we can train member models in parallel.

The center vectors  $c_{ejl}^{\phi} \in C^{e}$  and covariance matrices  $Q_{ejl} \in Q^{e}$  are tuned by the following procedure:

$$\begin{cases} c_{ejl}^{\phi}(k+1) = c_{ejl}^{\phi}(k) + \lambda_{c} \frac{\tau_{ejl}^{c}(k)e(k)}{\eta_{c}(k)} \\ \eta_{ec}(k+1) = \beta_{c}\eta_{ec}(k) + \tau_{ejl}^{c}\tau_{ejl}^{c} \\ Q_{ejl}(k+1) = Q_{ejl}(k) + \lambda_{Q} \frac{\tau_{ejl}^{Q}(k)e(k)}{\eta_{eq}(k)} \\ \eta_{eQ}(k+1) = \beta_{Qe}\eta_{eQ}(k) + Tr(\tau_{ejl}^{Q}\tau_{ejl}^{Q}) \end{cases}$$

where  $\lambda_c$  and  $\lambda_Q$  are learning step hyperparameters,  $\beta_{ce}$  and  $\beta_{Qe}$  are dumping parameters for the current member model, vector  $\tau^c_{ajl}$  and matrix  $\tau^Q_{ejl}$  of back propagated error gradient values with respect to  $c^{\phi}_{ejl}$  and  $Q_{ejl}$ . Vectors  $\eta_{ec}$  and matrices  $\eta_{eQ}$  represent the decaying average values of previous gradients. The algorithm initializes with  $\eta_{ec} = \eta_{eQ} = 10,000$ .

Figure 6 shows examples of multidimensional Gaussians from different local models after learning is finished—they were initialized identically and trained on the same dataset, the only difference is in random weights initialization and hyperparameters, which defined learning dynamics.



**Figure 6.** Examples of Gaussian units that were identically initialized, but tuned with different hyperparameters.

Weights learning  $P^e$  has the following form:

$$p_{e}(k+1) = p_{e}(k) + \frac{e_{a}}{f_{e}^{T}(x(k))f_{e}(x(k))} f_{e}(x(k)),$$

where  $p_a(k)$  is a weight in a vector form for simplicity of computation.

Figure 7 displays an error decay process during the model training. The average model output shows both faster error decay and better stability—individual models are tending to a bigger dispersion.

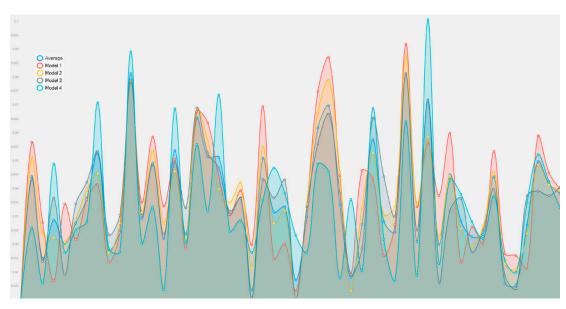


Figure 7. Error decay.

# 3. Experimental Results

We used the following datasets in order to verify our model accuracy and computational performance:

- Cisco stock with 6329 records.
- Alcoa stock with 2528 records.

- American Express stock with 2528 records.
- Disney stock with 2528 records.

Disney stock with 2528 records. The dataset has one column with numerical values. We selected this dataset as a basis framework due to its well-studied properties and real-life nature. The original datasets can be found in Tsay [24,25] and Table 1 contains a randomly chosen block of 10 lines from the first one — both original raw values and normalized, which were used in order to properly compare different models.

| Cisco    | Normalized |  |
|----------|------------|--|
| -0.05382 | 0.50755    |  |
| 0.01827  | 0.63085    |  |
| -0.00909 | 0.58405    |  |
| 0.00909  | 0.61515    |  |
| -0.02752 | 0.55253    |  |
| -0.01878 | 0.56748    |  |
| 0.01878  | 0.63172    |  |
| 0.08895  | 0.75173    |  |
| -0.00855 | 0.58498    |  |
| 0.01702  | 0.62871    |  |

Table 1. Records example of the Cisco stock daily returns dataset.

We divided each dataset into a validation set of 800 records and a training set with the rest.

In addition to the proposed model, we performed tests with single neuro-fuzzy models and competing models:

- Bipolar sigmoid neural network. To train the neural network, we used the well-known Levenberg–Marquardt algorithm [26] and parallel implementation of the resilient backpropagation learning algorithm (RPROP) [27] as the popular batch optimization methods.
- Support vector machines with sequential minimal optimization.
- Restricted Boltzmann machines as an example of a stochastic neural network. We also used a
  resilient backpropagation learning algorithm for their learning.

We created custom software for the neuro-fuzzy model written on Microsoft .Net Framework with the Math.NET Numerics package [28] as a linear algebra library. The Accord.NET package [29] was used for the competing models' implementations.

The experiments were performed on a computer with 32 GB of memory and with Intel<sup>®</sup> Core (TM) Core i5-8400 processor (Intel, Santa Clara, CA, USA), which has six physical cores, a base speed of 2.81 GHz and 9 mb of cache memory.

Root Mean Square Error (*RMSE*) and Symmetric Mean Absolute Percent Error (*SMAPE*) criteria were used to estimate prediction accuracy:

$$RMSE = \sqrt{\frac{\sum_{k=1}^{N} (y(k) - \hat{y}(k))^{2}}{N}},$$
$$SMAPE = \frac{2}{N} \sum_{k=1}^{N} \frac{|\hat{y}(k) - y(k)|}{\hat{y}(k) + y(k)},$$

where y(k) is a real value,  $\hat{y}(k)$  is a predicted value, and *N* is the training set length.

Visualization of the learning process is presented in Figures 8 and 9. Figure 8 shows the improvement in the forecasting plot obtained by averaging.

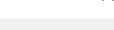




Figure 8. Ensemble model prediction plot.

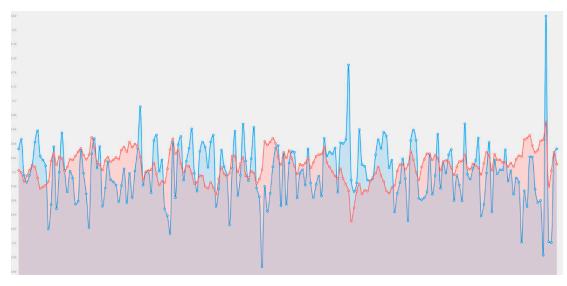


Figure 9. The best performing single neuro-fuzzy model.

The proposed model, as can be seen from Table 2, allows better accuracy to be achieved by small amount of member models and with a tolerable cost in computational resources.

| Table 2 | 2. Expe | erimental | results. |
|---------|---------|-----------|----------|
|---------|---------|-----------|----------|

| Model   | Cisco Stock Daily Log Returns |             |              |
|---|-------------------------------|-------------|--------------|
|   | Execution Time<br>(ms)        | RMSE<br>(%) | SMAPE<br>(%) |
| Proposed model $m = 4$ , $h^{\phi} = 2$                         | 196                           | 4.007       | 5.08246      |
| $m=6$ , $h^{\phi}=2$  | 279                           | 4.007       | 5.09458      |
| $m=8$ , $h^{\phi}=2$  | 361                           | 4.104       | 5.16344      |
| $m = 12$ , $h^{\phi} = 2$                                       | 417                           | 4.058       | 5.14296      |
| Single model $h^{\phi} = 2, \beta_{c} = 0.65, \beta_{Q} = 0.91$ | 92                            | 4.012       | 5.14493      |
| Bipolar Sigmoid Network Resilient BackProp                      | 307                           | 4.022       | 5.14132      |

| Pipelar Sigmaid Natural Lawaphara                               |                                |             |              |  |
|---|--------------------------------|-------------|--------------|--|
| Bipolar Sigmoid Network Levenberg-<br>Marquart                  | 1377                           | 4.054       | 5.16275      |  |
| Support Vector Machine  | 10800                          | 4.021       | 5.13844      |  |
| Restricted Boltzmann Machine                                    | 210                            | 4.018       | 5.14531      |  |
|   | Alcoa Stock Daily Log Returns  |             |              |  |
|   | Execution time (ms)            | RMSE        | SMAPE        |  |
|   |                                | (%)         | (%)          |  |
| Proposed model $m = 4$ , $h^{\phi} = 2$                         | 60                             | 9.017       | 15.299       |  |
| $m=6$ , $h^{\varphi}=2$   | 77                             | 9.032       | 15.385       |  |
| $m=8$ , $h^{\phi}=2$  | 102                            | 9.452       | 16.025       |  |
| $m=12$ , $h^{\phi}=2$   | 145                            | 9.578       | 16.245       |  |
| Single model $h^{\phi} = 2, \beta_c = 0.65, \beta_Q = 0.91$     | 27                             | 9.111       | 15.377       |  |
| Bipolar Sigmoid Network Resilient BackProp                      | 192                            | 9.894       | 16.667       |  |
| Bipolar Sigmoid Network Levenberg-<br>Marquart                  | 472                            | 9.896       | 16.711       |  |
| Support Vector Machine  | 1136                           | 9.910       | 16.634       |  |
| Restricted Boltzmann Machine                                    | 72                             | 9.889       | 16.663       |  |
|   | American Express S             | •           | og Returns   |  |
|   | Execution time (ms)            | RMSE<br>(%) | SMAPE<br>(%) |  |
| Proposed model $m = 4$ , $h^{\phi} = 2$                         | 102                            | 10.028      | 16.880       |  |
| $m=6$ , $h^{\phi}=2$  | 154                            | 10.001      | 16.998       |  |
| $m=8$ , $h^{\phi}=2$  | 189                            | 10.044      | 17.022       |  |
| $m=12$ , $h^{\phi}=2$   | 211                            | 10.045      | 17.025       |  |
| Single model $h^{\phi} = 2, \beta_c = 0.65, \beta_Q = 0.91$     | 58                             | 10.022      | 16.917       |  |
| Bipolar Sigmoid Network Resilient BackProp                      | 188                            | 10.06       | 17.043       |  |
| Bipolar Sigmoid Network Levenberg-<br>Marquart                  | 458                            | 0.999       | 16.885       |  |
| Support Vector Machine  | 1584                           | 10.141      | 17.858       |  |
| Restricted Boltzmann Machine                                    | 87                             | 10.054      | 17.038       |  |
|   | Disney Stock Daily Log Returns |             |              |  |
|   | Execution time (ms)            | RMSE<br>(%) | SMAPE<br>(%) |  |
| Proposed model $m = 4$ , $h^{\phi} = 2$                         | 41                             | 8.90        | 12.908       |  |
|   | 52                             | 8.902       | 12.952       |  |
| $m = 6, h^{\phi} = 2$ $m = 8, h^{\phi} = 2$                     | 102                            | 8.997       | 12.984       |  |
| $m = 12$ , $h^{\phi} = 2$                                       | 145                            | 9.009       | 12.989       |  |
| Single model $h^{\phi} = 2, \beta_{c} = 0.65, \beta_{Q} = 0.91$ | 27                             | 8.960       | 12.983       |  |
| Bipolar Sigmoid Network Resilient BackProp                      | 166                            | 8.991       | 12.953       |  |
| Bipolar Sigmoid Network Levenberg-<br>Marquart                  | 468                            | 9.024       | 12.985       |  |
| Support Vector Machine  | 825                            | 8.997       | 12.949       |  |
| Restricted Boltzmann Machine                                    | 65                             | 8.989       | 12.939       |  |
|   |                                |             |              |  |

#### 4. Conclusions

In this paper, we introduced a novel ensemble neuro-fuzzy model for prediction tasks and a procedure for its initialization. The model output is an averaging of the outputs of its members, which are multiple input single output (MISO) models with multidimensional Gaussian functions in the consequent layer. Such combination leads not only to better accuracy, but also significantly improves the hyperparameter selection phase.

Software numerical simulations of real life financial data have demonstrated the good computational performance due to lightweight member models and ability to train them in parallel. Prediction accuracy of our model has been compared to single neuro-fuzzy models and well-established artificial neural networks.

**Author Contributions:** Conceptualization, O.V. and Y.B.; methodology, O.V. an D.P.; software, A.V.; validation, A.V. and N.V.; formal analysis, O.V. and Y.B.; investigation, A.V.; writing—original draft preparation, A.V.; writing—review and editing O.V. and N.V.; visualization, A.V. and N.V.; supervision, D.P. and Y.B.

Funding: This research received no external funding.

**Acknowledgments:** The authors thank the organizers of the DSMP'2018 conference for the opportunity to publish the article, as well as reviewers for the relevant comments that helped to better present the paper's material.

Conflicts of Interest: The authors declare no conflict of interest.

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