

Article

Combination Compensation Method to Improve the Tolerance of Recording Medium Shrinkage in Collinear Holographic Storage

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Abstract: Holographic optical storage has great potential for enormous data storage, although the recording medium can cause dimensional change, which can deteriorate the quality of the reconstructed hologram. Compensation in traditional off-axial holographic storage systems is sensitive to vibration and requires high precision. In contrast, a collinear system is more compact with better stability, and its compensation would be different. In this paper, the combination compensation method for compensating for the dimensional change of the recording medium by simultaneously adjusting the reading light wavelength and the focal length of the objective lens is established, which was implemented in a collinear system for a high dimension-change-rate $(σ)$ of the medium condition. Its compensation effects for the lateral dimension change and the vertical dimension change were compared as well. The results show that the bit error ratio of the reconstructed hologram could be decreased to 0 for both of the dimensional change conditions with a large adjustment scope under $\sigma = 1.5$ %. Compared with the compensation method, in which only the focal length or the wavelength are adjusted, this combination compensation method can enlarge the compensation scope and improve the tolerance of the recording medium shrinkage in a collinear holographic storage system.

Keywords: collinear holographic storage; combination compensation; material dimension change

1. Introduction

Holographic optical storage is a powerful candidate for the next generation of enormous data storage, owing to its fast data transfer rate, high storage capacity, and long storage life [\[1](#page-9-0)[–6\]](#page-9-1). Compared with the traditional off-axis type of holographic storage system, the collinear type is a more compact system and has better stability $[7-10]$ $[7-10]$, which enables easy miniaturization [\[11\]](#page-9-4), and has a larger wavelength margin [\[12\]](#page-9-5); moreover, a semiconductor laser can be applied to the system. In addition, a collinear holographic storage system can be combined with a servo system, and the compatibility and vibration resistance of the storage system would also become stronger [\[13](#page-9-6)[,14\]](#page-9-7). The recording medium in a holographic storage system would undergo dimensional change [\[15–](#page-9-8)[22\]](#page-10-0). For example, the commonly used photopolymer, which has the advantages of high photosensitivity, a wide dynamic range, good optical properties, low cost, etc. [\[23](#page-10-1)[–25\]](#page-10-2), would encounter the shrinkage [\[15](#page-9-8)[,17](#page-10-3)[–20\]](#page-10-4) and the volume changes induced by varying the temperature [\[21,](#page-10-5)[22,](#page-10-0)[26\]](#page-10-6). The dimension change can result in changes in the holographic gratings that have been stored in the medium and lead to Bragg mismatch [\[26\]](#page-10-6) and a decrease in diffraction efficiency [\[26–](#page-10-6)[28\]](#page-10-7). Thus, the image quality of the reconstructed hologram would be seriously affected, and the bit error ratio (BER) would be increased.

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The compensation for the dimensional change of the recording medium in off-axis holographic storage systems is achieved by adjusting the incident angle or the wavelength of the reading beam, which has been studied systematically before [\[22](#page-10-0)[,29–](#page-10-8)[32\]](#page-10-9). The effectiveness of compensation by wavelength tuning and angle tuning has been demonstrated, though for a certain readout temperature, the adjusted wavelength or the readout angle must be certain values which correspond to the temperature. Usually, the compensation in an off-axial holographic storage system is sensitive to the vibration and requires high precision, whereas a collinear system is more robust to the vibration. In a collinear system, the reference beam is wrapped around the data on the space light modulator (SLM), and the angle of the incident reading beam cannot be adjusted such as that in an off-axis system. Terumasa Ito et al. compensated for the dimension change of the recording medium in a collinear holographic storage system by tuning the magnification and the wavelength of the reading beam appropriately [\[33\]](#page-10-10), for which the magnification and the reading wavelength need to be in one-to-one correspondence with each other while the writing light wavelength and the degree of the media dimension change are fixed. In order to study the feasibility of enlarging the adjustment scope for compensation, e.g., for tuning parameters that do not need to be in one-to-one correspondence, further analysis is still needed to research the compensation in the collinear system.

In this paper, we analyzed the compensation effects in a collinear system based on adjusting the wavelength of the reading light as well as the focal length of the objective lens under a large dimension-change-rate (σ) in the lateral direction and the vertical direction of the medium. This simple method of simultaneously adjusting the wavelength and the focal length for compensation, called the combination compensation method, was investigated in an effort to enlarge the adjustment scope and increase the robustness in a collinear holographic storage system.

2. Theoretical Analysis

2.1. The Compensation for Medium Dimensional Change

In this paper, the Kogelnik theory [\[34\]](#page-10-11) and the point-spread function (PSF) [\[35\]](#page-10-12) were used in a simulation for an optical model of a collinear holographic storage system. We focused on studying the transmission holograms, as they are recorded in the collinear holographic storage system.

To clarify the dimension change model of the recording medium, we took a single grating in the material as an example, as shown in Figure [1a](#page-2-0). The incident angles of the reference beam and the signal beam were θ_1 and θ_2 , respectively. The original grating period was Λ. The dimension change in the recording medium would cause Λ and the fringe surface inclination angle *θⁱ* to change. The change in the fringe angle was mainly caused by the change in thickness, which is called the vertical dimension change in this paper, and correspondingly, the lateral dimension change refers to the changes in the *x–y* plane. Though the change in the grating period is related to both the lateral dimension change and the vertical dimension change, the lateral one would play an important role.

Assuming the wavelengths of the light for writing and reading are *λ* and *λ'*, respectively, λ' can be expressed as $\lambda' = \lambda + \Delta \lambda$, where $\Delta \lambda$ is 0 in the common system without wavelength compensation. Figure [1b](#page-2-0) illustrates the vector diagram in the Ewald sphere, and the radius of the circle is $2\pi/\lambda'$. The length of the grating vector K_0 is equal to $2\pi/\Lambda$. Furthermore, the change in the grating period indicates the changes in the length of the grating vector, as illustrated in Figure [1b](#page-2-0), in which K_0 becomes K_1 . In addition, if the inclination angle of the grating fringe surface changes either, the direction of the grating vector would be rotated as well, which is illustrated as *K*1*'* in Figure [2b](#page-2-1). In the condition that the dimension of the recording medium is changed, the symbol of the grating vector after the change is denoted as *K'*, then, if the light of reading is incident at the original incident angle θ_1 with the original wavelength λ (i.e., $\lambda' = \lambda$), the three vectors (i.e., the read light vector *kp*, the grating vector *K'* and the reconstructed light vector *k^d*) cannot form a closed triangle, which means the Bragg condition cannot be matched, and the diffraction

efficiency would be sharply reduced. As shown in Figure [1b](#page-2-0), the incident angle of the readout light or the wavelength of the reading light should be adjusted so as to make the three vectors re-form a closed triangle and match the Bragg condition, then reacquire a high diffraction efficiency. The wavelength adjustment ($\Delta\lambda \neq 0$) is similar to that in the compensation for the off-axis system, whereas, due to the fact that hologram writing and
reading are performed in a single optical path in a collinear system, the incident angle of reading are performed in a single optical path in a collinear system, the incident angle of the reading light cannot be directly adjusted. the reading light cannot be directly adjusted.

Figure 1. (a) The schematic diagram for the model of the dimension change in the recording medium; (**b**) the illustration of the vector diagram in the Ewald sphere.

In this paper, the incident angle was adjusted by changing the focal length of the objective lens. Figure [2a](#page-2-1) illustrates the principle of the focal length compensation; the light beam on the SLM was focused by the objective lens into the recording medium, and the angles of the light beam directed at the material were determined by the focal length of the focusing objective lens (e.g., in Figure [2a](#page-2-1), the focal length f_1 corresponds to θ_1 , and f_2 corresponds to θ_2). Then, based on increasing or decreasing the focal length of the lens, the angles of the reading light could be adjusted, and the inferior reconstructed hologram caused by the material dimension change could be repaired and compensated. To clarify, Figure [2](#page-2-1) only illustrates the schematic diagrams; the real holographic storage system is more complex, as fine-tuning the focal length could be realized by shifting the relative positions of the relay lens module in the system, and the achromatic lens would be used in the real system.

As shown in Figure [2b](#page-2-1), the light wave emitted from each pixel (x_i, y_j) on the SLM would be a plane wave incident into the recording medium after propagating through the focusing objective lens. In the writing procedure, the *k* vector of the plane wave is given by Equation (1) [\[35\]](#page-10-12), where k_0 is equal to $2\pi/\lambda$, *f* is the focal length of the lens and *n* is the refractive index of the recording medium. The grating vector written by the plane waves from two different pixels on the SLM can be calculated by the subtraction of the two *k* vectors [\[35\]](#page-10-12).

$$
k_{ij} = \left(-k_0 \frac{x_i}{f}, -k_0 \frac{y_j}{f}, \sqrt{(nk_0)^2 - \left(\frac{k_0 x_i}{f}\right)^2 - \left(\frac{k_0 y_j}{f}\right)^2} \right)
$$
(1)

The grating vector K_0 formed by writing is denoted as $K_0 = [K_{0x}, K_{0y}, K_{0z}]$, which is the original grating vector. The original length and the thickness of the recording medium are *L*⁰ and *T*0, respectively, and *L'* and *T'* represent the corresponding dimensions after the volume change of the medium. The rate of dimension change in the lateral plane (*σL*) is assumed to be isotropic, which is defined by Equation (2), and the vertical dimension change rate (σ_V) is defined by Equation (3). When the dimension of the recording medium has been changed, the corresponding grating vector *K*' is described by Equation (4).

$$
\sigma_L = \sigma_x = \sigma_y = \frac{L_0 - L'}{L_0} \tag{2}
$$

$$
\sigma_V = \sigma_z = \frac{T_0 - T'}{T_0} \tag{3}
$$

$$
K' = \left[\frac{K_{0x}}{1 - \sigma_L}, \frac{K_{0y}}{1 - \sigma_L}, \frac{K_{0z}}{1 - \sigma_V}\right]
$$
\n
$$
(4)
$$

In the reading procedure, the *k* vector of the reading wave, which corresponds to the pixel (x_{rk}, y_{rl}) in the reading light pattern on the SLM, is given as Equation (5), where $k'_{0} = 2\pi/\lambda' = 2\pi/(\lambda + \Delta\lambda)$ and Δf is the amount of change in focal length (the focal length after adjustment is f' , which is equal to $f + \Delta f$).

$$
k_{rkl} = \left(-k_0' \frac{x_{rk}}{(f+\Delta f)}, -k_0' \frac{y_{rl}}{(f+\Delta f)}, \sqrt{(nk_0')^2 - \left(\frac{k_0' x_{rk}}{(f+\Delta f)}\right)^2 - \left(\frac{k_0' y_{rl}}{(f+\Delta f)}\right)^2}\right) (5)
$$

Then, the complex amplitude of the diffracted light wave can be calculated by the Kogelnik theory [\[34\]](#page-10-11), and under the condition that the dimension of the recording medium has been changed, the reconstructed hologram with the compensation can be obtained by the sum of all the waves emitted from all the pixels in the reading light pattern and diffracted by all the gratings in the medium.

The bit error ratio (BER) defined by Equation (6) was used to evaluate the quality of the reconstructed hologram and was an indicator of the effect of the compensation method.

$$
BER = \frac{N_{error}}{N_{total}}
$$
 (6)

where *Nerror* represents the number of the symbol units with errors in the reconstructed signal light pattern, and *Ntotal* is the total number of symbols in the original signal pattern, and each symbol corresponds to a block of 4×4 pixels on the SLM.

2.2. Parameters in the Simulation

Figure [3](#page-4-0) is the intensity pattern of the signal light pattern and the reference light pattern, in which the illumination was spatially coherent. The outside pattern was the reference light as shown in Figure [3b](#page-4-0), for which the radial line reference pattern was used [\[35\]](#page-10-12), and the inner pattern was the signal data page, which had 12 symbols in both the length and width directions and contained four sync marks for location [\[36\]](#page-10-13). The wavelength of the light for writing was 532 nm, the pixel pitch of the SLM was 13.7 µm and the original focal length for the achromatic objective lens was 5 mm. Furthermore, the diffracted light from each single pixel in the SLM was in the Fraunhofer region directly in front of the lens [\[35\]](#page-10-12). The thickness of the medium was 1 mm, the PQ-PMMA photopolymer was used as the recording medium, the refractive index of the medium was 1.5 and the spatial modulation of the refractive index was 1×10^{-4} . spatial modulation of the refractive index was 1×10^{-4} . and the original focal length for the achromatic objective lens was 5 mm. Furthermore, the

wavelength of the light for writing was 532 nm, the pixel pixel

Figure 3. (a) The reference light pattern and the signal light pattern uploaded on the SLM; (**b**) the reference light pattern, which is also the reading light pattern. $\frac{d}{dt}$ direction would be $\frac{d}{dt}$ direction would be $\frac{d}{dt}$

3. Simulation Results and Discussion condition (*oL* \overline{a} 0) were analyzed condition (*o***l** \overline{b} 0) were analyzed condition (*o***l** \overline{b} 0) were analyzed condition (*o***l** \overline{b} 0) were analyzed condi

3. Senerally, the dimension change rates of the recording medium in the lateral direction
respectively, so as the computation effects. $(\sigma_V \equiv 0)$ and the vertical dimension change condition ($\sigma_L \equiv 0$) were analyzed respectively, so as to clearly investigate and compare the compensation effects. and the vertical direction would be quite different. The lateral dimension change condition

Figure 4 shows the BER of the reconstructed signal pattern for different lateral or respectively, so as to clearly investigate and compare the compensation effects. kinds of dimension changes, the corresponding BER began to grow when *σ* reached about 1%, and then the BER increased sharply as σ increased. In addition, it can be also deduced that, compared with the vertical dimension change under the same σ value ($\sigma > 1\%$), the change could influence the quality of the reconstructed hologram more severely than the change could influence the quality of the reconstructed hologram more severely than the vertical dimension change. **In addition, in addition, it can be also deduced sharply as of the also deduced sharply** vertical dimension change rates σ without any compensation. It can be seen that for both lateral dimension change could obtain a higher BER, which means the lateral dimension

Figure 4. Without any compensation, the BER of the reconstructed signal pattern for different lateral dimension change rates σ_L and vertical dimension change rates σ_V . ($\sigma = \sigma_L$, $\sigma = \sigma_V$).

change was 0.5417.

In order to prove the effectiveness of the compensation method, we made an effort to $\frac{1}{2}$ compensate for the conditions when σ_L and σ_V were as high as 1.5%, where the BER for the lateral dimension change increased to 0.7153, and the BER for the vertical dimension range was 0.5417.

Firstly, the compensation that only utilized the wavelength adjustment was implemented, and Figure [5](#page-5-0) depicts the results for the lateral dimension change condition and the vertical dimension change condition. Although there was a large adjustment range the vertical dimension change condition. Although there was a large adjustment range for decreasing or increasing the wavelength (i.e., Δλ∈[-20, 20] nm, where the wavelength interval was 1 nm, and each wavelength comes from a narrow-band laser), the BER did not reach zero for either kind of dimension change condition, and the BER was not significantly reduced. Under the lateral dimension change condition, and the BER was not significantly reduced. Under the lateral dimension change condition, the minimum BER only decreased to 0.5903, though the wavelength needed to be decreased by 19 nm, which we attempted to no avail. Then, under the vertical dimension change condition, the minimum BER decreased to 0.4583 while the wavelength only increased by 4 nm.

change condition (σ_L = 1.5%) and the vertical dimension change condition (σ_V = 1.5%) when the focal length of the objective lens was unchanged. **Figure 5.** The BER with different wavelength adjustments of the reading light for the lateral dimension

was impremented as a companison, and the restats shown in Figure 8 marche that the compensation effect was better than that of the former wavelength compensation method, and the BER was reduced to zero both for the lateral dimension change condition and the vertical dimension change condition. As can be seen from Figure 6, the focal length range
 ϵ Larger than that of the lateral dimension change condition (i.e., $(65, 25)$ μ m, about 5 μ m), about 5 μ m), which means it would be easier to adjust to zero BER for the vertical dimension change condition. From the results in Figures 5 and 6, it can be deduced that the comp[en](#page-5-0)sati[on](#page-6-0) V and the lateral dimension change condition would be more dimension θ about 5 and 1.61 are *σ* value. Secondly, the compensation based on changing the focal length of the objective lens was implemented as a comparison, and the results shown in Figure [6](#page-6-0) indicate that the of zero BER for the vertical dimension change condition (i.e., $(65, 25)$ µm, about 40 µm) was for the lateral dimension change condition would be more difficult to achieve than for the

As sho[w](#page-6-0)n in Figure 6a, the focal length adjustment range for reducing the BER to zero was narrow for the lateral dimension change condition. In order to widen the focal compensation for the lateral dimension change condition would be more difficult to simultaneously adjusting the focal length and the wavelength was introduced. Considering the lateral dimensio[n](#page-5-0) change curve in Figure 5, when the wavelength decreased by 9 nm (i.e., −9 nm), though it did not achieve the smallest BER value, it still corresponded to length adjustment range for compensation, the combination compensation method of the local minimum value, 0.6389; thus, the focal length adjustment was implemented and

analyzed under the condition that the wavelength was decreased by 9 nm, and Figure [7](#page-6-1) shows the results of this combination compensation method for the lateral dimension change condition. It can be observed that on the basis of the wavelength adjustment, the corresponding focal length adjustment range for compensation was $(30, 80)$ μ m, and the range width was 10 times that shown in Figure [6a](#page-6-0). It needs to be clarified that the focal length change with the wavelength change induced by dispersion was not considered in the simulations, as such a focal length change would be too small to be considered if an achromatic lens were to be used, since the wavelength change would only be tens of nanometers. shimultaneously adjusted. The focal length and the wavelength and the wavelength was internal the wavelength w

Figure 6. The BER with different objective focal length adjustments for (a) the lateral dimension change condition (σ_L = 1.5%) and (b) the vertical dimension change condition (σ_V = 1.5%) when the wavelength of the reading light was unchanged. wavelength of the reading light was unchanged.

 \mathbf{c} is the simulation of the simulations, as such a focal length change when the would path of the reading light considered in an achieve to be used, since the wavelength change would only used, since the wavelength change would only used, since the wavelength change would only used, which we can get a wavelength change would be a s was reduced by 9 nm and *σ*_{*L*} was 1.5%. **Figure 7.** The BER with different focal length adjustments when the wavelength of the reading light **Figure 7.** The BER with different focal length adjustments when the wavelength of the reading light

In order to directly observe and analyze the reconstructed signal patterns related to results in Figure [7,](#page-6-1) Figure [8\(](#page-7-0)c1–i1) show the reconstructed signal patterns with focal length changes $\Delta f = 0$ µm, 10 µm, 30 µm, 50 µm, 60 µm, 80 µm and 110 µm, respectively, while the wavelength of the reading light was reduced by 9 nm. In comparison, Figure 8(a1,b1) show the reconstructed diagrams without any compensation under σ ^L = 0 and 1.5%, respectively. The pictures denoted as Figure 8(a2–c2), etc., immediately to the right of the reconstru[cte](#page-7-0)d patterns, are the corresponding symbol error diagrams. In these diagrams, each of the tiny In order to directly observe and analyze the reconstructed signal patterns related to the bright squares, denoted as *'An error symbol'* in Figure [8\(](#page-7-0)d2), represents error within the symbol located there, and the bright space is the composition of these error symbols. The compensation results in Figure [8e](#page-7-0)–h directly show the effectiveness of this combination compensation method.

Figure 8. (**a**) The reconstructed signal pattern without the dimension change of the recording **Figure 8.** (**a**) The reconstructed signal pattern without the dimension change of the recording medium; (**b**) the reconstructed signal pattern with σ_L = 1.5% and without any compensation. When σ_L = 1.5%, *σ L* = 1.5%, *compensation method, for the reconstructed signal patterns with the compensation method, the reconstructed signal patterns with the complex signal patterns with the compensation of the compensation of the* for the reconstructed signal patterns with the combination compensation method, the reading light the reading light wavelength was decreased by 9 nm and the focal length was changed by (c) $0\,\mu$ m, (**d**) $10\,\mu$ m, (e) $30\,\mu$ m, (f) 50 μm, (g) 60 μm, (h) 80 μm and (i) 110 μm. The corresponding symbol error diagrams are depicted to the right of the correlated reconstructed signal patterns.

The normalized pixel intensity histogram was used to analyze the reconstructed The normalized pixel intensity histogram was used to analyze the reconstructed signal pattern, as shown in Figure [9,](#page-8-0) where the abscissa represents the normalized intensity of each pixel, and the vertical axis represents the quantity of the pixels with a certain intensity.
Figure 8(4), and the vertical axis represents the quantity of the pixels with a certain intensity. which is the original one without any dimension change of the medium. It can be observed nal one without any dimension change of the medium. It can be observed from Figure [9a](#page-8-0) that the intensities of the 'bright pixels' were mainly distributed within the abscissa value that the intensities of the 'bright pixels' were mainly distributed within the abscissa value abscissa value within (0.8, 1), while the intensities of the 'dark pixels' were mainly within (0.8, 1), while the intensities of the 'dark pixels' were mainly distributed within distributed within (0, 0.4), and there was no overlapping between the dark and the bright (0, 0.4), and there was no overlapping between the dark and the bright pixels along the pixels along the abscissa, which means the dark and the bright spots can be clearly abscissa, which means the dark and the bright spots can be clearly distinguished. However, when the dimension change occurred in the material with $\sigma_L = 1.5\%$, the intensity distri-bution of the dark and the bright pixels became consecutive, as shown in Figure [9b](#page-8-0). In Figure [9c](#page-8-0),d,i, when the wavelength decreased by 9 nm, the focal length was not sufficient to ensure an effective compensation. When the focal length adjustment increased to the range of (30, 80) μm, as shown in Figure [9e](#page-8-0)–h, the dark and the bright pixels were separated again without overlapping along the abscissa. The results also suggest that the combination compensation method of the focal length and the wavelength adjustments can maintain a BER of 0 in a larger selection range of focal length. Figure [9a](#page-8-0) corresponds to the reconstructed signal pattern in Figure 8 (a1), which is the origi-

To further demonstrate the feasibility of the combination compensation method for To further demonstrate the feasibility of the combination compensation method for the lateral dimension change condition $(\sigma_L = 1.5\%)$ and the vertical dimension change condition (σ_V = 1.5%), we systematically analyzed the compensation effects by varying the wavelength and the focal length of the objective lens in a large scope. The compensation wavelength and the focal length of the objective lens in a large scope. The compensation effects are shown in Figure [10;](#page-8-1) it can be seen that for both of the lateral dimension change and the vertical dimension change, the scopes when adjusting the wavelength and the focal length for realizing zero BER compensation are relatively large. There are plenty of combinations of wavelength and focal length that result in a BER value of zero, for which one-to-one correspondence between the wavelength and the focal length is not required, whereas under the different wavelength values, the range of options for the focal length adjustment would be different. It is suggested that the wavelength compensation be scanned first, as under a wavelength which leads to a smaller BER, the range for a successful focal length compensation would be larger. Compared with the compensation method, which only adjusts the wavelength or the focal length, the combination compensation method can enlarge the compensation scope and thus increase the robustness of the collinear system.

whereas under the different wavelength values, the range of options for the focal length values, the focal length values, the focal length values, the focal length values, α

Figure 9. The normalized pixel distribution histograms of (**a**) the original reconstructed signal **Figure 9.** The normalized pixel distribution histograms of (**a**) the original reconstructed signal pattern; (b) the reconstructed signal pattern under σ_L was 1.5% and without any compensation; the reconstructed signal patterns under *σL* were 1.5% with the combination compensation method, in reconstructed signal patterns under *σ^L* were 1.5% with the combination compensation method, in which the reading light wavelength was decreased by 9 nm and the focal length was changed by (c) 0μ m, (d) 10μ m, (e) 30μ m, (f) 50μ m, (g) 60μ m, (h) 80μ m and (i) 110μ m.

Figure 10. The compensation effects of the combination compensation method for (**a**) the lateral **Figure 10.** The compensation effects of the combination compensation method for (**a**) the lateral dimension change condition (σ_L = 1.5%) and (b) the vertical dimension change condition (σ_V = 1.5%).

4. Conclusions

In this paper, we systematically analyzed a combination method of simultaneously adjusting the focal length and the reading light wavelength for compensating large dimensional change within the recording medium in a collinear holographic storage system and compared the compensation effects under lateral dimension change and vertical dimension change conditions. The analysis suggests that though the compensation for the lateral dimension change would be more difficult to achieve than that for the vertical dimension change, this combination compensation method can decrease the BER to 0 with a large adjustment scope both for the lateral and vertical dimension change conditions under a high dimension change rate ($\sigma_{\rm L} = 1.5\%$, $\sigma_{\rm V} = 1.5\%$). The combination compensation method can enlarge the adjustment scope, and the two adjustment parameters (the wavelength of the reading light and the focal length of the lens) do not need to be in one-to-one correspondence to each other. The large compensation scope would facilitate the experiment, and the simulation results can be used to instruct the implementation of collinear holographic storage systems. Based on results achieved for the combination compensation method, the tolerance of the volume change in the recording medium in a collinear holographic storage system could be improved as well.

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