



Bin Huang \*, Jiaqi Wang and Xiaopeng Shao \*

Advanced Optical Imaging and Devices Laboratory, Hangzhou Institute of Technology, Xidian University, Hangzhou 311231, China

\* Correspondence: huangbin@xidian.edu.cn (B.H.); xpshao@xidian.edu.cn (X.S.)

Abstract: Stimulated Brillouin scattering (SBS) is the major factor that limits the maximum optical fiber output power in narrow linewidth applications, which include important fields such as passive optical networks (PONs), high-power fiber amplifiers, and lasers. Great efforts have been dedicated to suppressing the SBS effect and increasing the maximum optical fiber output power. This paper focuses on key fiber-based techniques to suppress SBS. These techniques take advantages of the properties of optical fibers. We present how these properties (electric modes, acoustic modes, and material properties) could be utilized to suppress SBS. The fiber-based techniques are divided into transverse optical fiber design, longitudinal variant fiber design, and external perturbations (strain and temperature) on optical fibers. Transverse optical fiber design focuses on the mechanism electro-acoustic interaction. Large effective area fiber design and acoustic tailoring techniques have been discussed. Longitudinal variant fiber design considers the nonlinear SBS interaction along propagation distance, and various techniques related have been presented. External perturbations (strain and temperature) on optical fibers emphasize on how external static perturbations could modify the SBS effect.

**Keywords:** stimulated Brillouin scattering; optical fiber; passive optical networks; high-power fiber lasers; fiber amplifiers

# 1. Introduction

Brillouin scattering is a type of inelastic scattering, the theoretical grounds of which were first laid out by Brillouin in around 1922. In 1930, the experimental observation of Brillouin scattering in organic liquids was reported by Evgenii Fedorovich Gross [1] right after the observation of Raman scattering [2]. He pointed out that it is due to the acoustic oscillations of molecules. This is the first experimental observation of spontaneous Brillouin scattering. In that process, the incident light wave is transformed into scattered light and an acoustic wave. The scattered wave is downshifted in frequency. Not until the development of interferometric techniques and the invention of lasers [3,4] was the SBS phenomenon observed. In 1964, Garmire E and Townes CH experimentally demonstrated SBS in solids [5]. In the experiment, an intense laser beam was focused to a crystal and the coherent amplification of scattered light was detected. The mechanism of SBS is found due to electrostriction [6].

In 1972, the effect of SBS in optical fibers was first observed by E.P. Ippen and R.H. Stolen [7], which, for the first time, pointed out the limitation in the optical fiber transmission due to SBS. In the same year, R.G. Smith theoretically predicted that SBS would limit the power transmitted through fibers [8]. In the paper, he considered two types of nonlinear scattering processes, SBS and stimulated Raman scattering (SRS), and determined that SBS should determine the maximum power handling capacity of a fiber. Later, further properties of SBS in optical fibers were studied, including electrostrictive contribution [9–14], temporal response [15,16], polarization properties [17–19], and so on.

After the demonstration of SBS, there has been a lot of work in that realm. SBS has successfully found its applications in various fields, Brillouin amplifiers [20,21], Bril-



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**Copyright:** © 2023 by the authors. Licensee MDPI, Basel, Switzerland. This article is an open access article distributed under the terms and conditions of the Creative Commons Attribution (CC BY) license (https:// creativecommons.org/licenses/by/ 4.0/). louin lasers [22–28], phase conjugation [29–31], beam combining [32–34], pulse compression [35,36], pulse delays [37–39], and many others.

In some areas, however, SBS is viewed as undesirable, especially when high-power light with narrow laser linewidths needs be delivered through optical fibers. These areas include PON transmission [40–42], high-power fiber lasers, and amplifiers [43–46]. The schematics of PON is shown in Figure 1. In PON application, light coded with a signal transmits 10 s of kms to reach the optical line terminal (OLT). Splitters are used so that each optical network unit (ONU) can receive a signal. For PON to cover more ONUs, power budget is the key factor, the constraint of which is SBS. Figure 2 shows the schematic of one type of high-power fiber laser; several laser diodes (LDs) are implemented as pump light. For laser to achieve high output power, SBS must be suppressed.



Figure 2. The schematics of one type of high-power fiber laser.

To overcome the effects of SBS on these applications, numerous studies have been explored. In this paper, our focus is on the fiber-based techniques to suppress SBS. Other methods such as using phase-broadening techniques [47–55] and optical devices [56–58] are beyond the scope of our paper.

This paper is organized as follows. In Section 2, we provide an introduction to the theoretical background of SBS and discuss the rationale for SBS suppression. In Section 3, we present techniques of SBS suppression. The techniques are presented from four categories: transverse optical fiber design, longitudinal variant fiber design, external perturbations (strain and temperature) on optical fibers, and combined methods. We conclude our paper in Section 4.

# 2. Theoretical Background and Design Rationale

# 2.1. Theoretical Background of Brillouin Scattering in Optical Fibers

In the modern picture, the process of spontaneous Brillouin scattering is due to the interaction with intermolecular vibrations, or, more accurately, with the phonon spectrum's acoustic branch [59–61]. The process can be viewed as an annihilation of the incident photon (with angular frequency  $\omega_p$ ) and creation of a scattered photon ( $\omega_s$ ) and an acoustic phonon ( $\Omega$ ). During the interaction, the energy and momentum must be conserved; thus, we have two relations:

$$\Omega = \omega_p - \omega_s \tag{1}$$

$$\vec{k}_{A} = \vec{k}_{p} - \vec{k}_{s},$$
 (2)

where  $k_A$ ,  $k_p$ , and  $k_s$  are the corresponding wave vectors of the acoustic phonon, incident photon, and scattered photon. The process is shown in Figure 3.



Figure 3. Diagram of Brillouin scattering energy conservation and momentum conservation.

The acoustic phonon frequency  $\Omega$  and the wave vector  $k_A$  satisfy the dispersion relationship that is shown in Equation (3):

$$\Omega = V_{\rm A}|k_{\rm A}| \approx 2V_{\rm A}|k_p|\sin(\theta/2) \tag{3}$$

where  $V_A$  is the scalar acoustic velocity. Equation (3) shows that the shifting frequency of the scattered light depends on the scattering angle  $\theta$ .  $\theta$  is maximum in the backward direction and vanishes in the forward direction.

Next, we introduce the mechanism of SBS in the optical fibers. The structure of the step-index optical fiber consists of a core, a cladding, and a coating. The core has a larger refractive index than the cladding. The most widely adopted optical fiber is single-mode fiber (SMF), which typically has a core size of around 10  $\mu$ m. SMF allows one spatial mode (two vector modes) transmission in the optical fibers. When the core size becomes larger, more spatial modes can be allowed to transmit in optical fibers. These fibers are called few-mode fiber (FMF) or multimode fiber (MMF), depending on how many spatial modes can be supported. The governing equation for solving the scaler spatial modes of optical fiber can be shown by Equation (4):

$$\nabla_{\perp}^2 f_j(r,\theta) + \left[\frac{\omega^2 n_O^2(r,\theta)}{c^2} - \beta_j^2\right] f_j(r,\theta) = 0$$
(4)

where  $\nabla_{\perp}^2$  is the transverse Laplacian operator in cylindrical coordinates;  $f_j(r, \theta)$  is the *j*th transverse electric mode;  $\omega$  is the optical angular frequency;  $n_0$  is the optical refractive index; *c* is the light velocity; and  $\beta_j$  is the propagation constant of the *j*th electric mode. This equation uses the weak guiding approximation and applies to most optical fibers, where the optical fiber's core index is only slightly larger than the cladding index. In this paper, only the fundamental electric mode is considered. For simplicity, we label the fundamental mode f(r), since the fundamental electric mode profile does not depend on  $\theta$ .

When the intensity of the narrow bandwidth light (typically in the fundamental mode) in optical fibers becomes large, SBS could be observed experimentally. The interaction picture could be illustrated in Figure 4. When light (pump wave) is incident on the

optical fiber, the backscattered Stokes light (initially from spontaneous Brillouin scattering) interferes with the input pump light and generates an acoustic wave through the effect of electrostriction. The forward propagating acoustic wave acts as a Bragg grating, which scatters even more light in the backward direction. At a steady state, the strength of SBS is nonlinearly dependent on the input power.



**Amplified Stokes Wave** 

Figure 4. SBS schematic diagram.

The longitudinal propagating acoustic wave in optical fibers can be described by the following function with static state assumption:

$$\nabla_{\perp}^{2}\xi_{m}(r,\theta) + \left(\frac{\Omega_{m}^{2}}{V_{L}^{2}(r,\theta)} - q^{2}\right)\xi_{m}(r,\theta) = 0$$
(5)

where  $\xi_m(r, \theta)$  is the *m*th transverse profiles of the fundamental acoustic mode;  $V_L$  is the longitudinal acoustic velocity profile across the fiber; and *q* is the propagation constant of the acoustic mode. The acoustic mode in the optical fiber can be calculated numerically [62–64]. Figure 5 shows the electric mode and acoustic mode under different index profiles (conventional SMF and Corning large effective area fiber). The three lowest order acoustic modes non-dependent on angle  $\theta$  are displaced.

The physics to describe the interaction of incident light and SBS light along the uniform optical fiber is described by:

$$\begin{cases} \frac{dP_p(z)}{dz} = -\gamma_m \mathcal{L}(v) P_p P_s - \alpha P_p(z) \\ \frac{dP_s(z)}{dz} = -\gamma_m \mathcal{L}(v) P_p P_s + \alpha P_s(z) \end{cases}$$
(6)

where  $P_p$  is the incident pump power;  $P_s$  is the SBS power;  $\gamma_m$  is the peak SBS efficiency for the acoustic mode; and  $\alpha$  is the fiber loss. Equation (6) could be solved numerically and the Stokes power  $P_s(0)$  can be calculated; this has the physics, meaning that input power  $P_0$  is how much power is converted to SBS power at the fiber input. Figure 6 shows the measured dependence of the Stokes power  $P_s(0)$  on the input power  $P_0$  for various fiber lengths.



**Figure 5.** The electric mode and acoustic mode under different profiles. (**a**) The profiles of the single mode fiber, (**b**) The profile of Corning large effective area fiber. [Reprinted/Adapted] with permission from [65] © The Optical Society.



**Figure 6.** The measured dependence of the Stokes power  $P_s(0)$  on the input power  $P_0$  for various fiber lengths. [Reprinted/Adapted] with permission from [61] © The Optical Society.

The Brillouin Gain Spectrum (BGS) can be described as

$$\mathcal{L}(v) = \frac{(w_m/2)^2}{(v - v_p - v_B)^2 + (w_m/2)^2}$$
(7)

where  $v_p = c/\lambda_p$  is the pump frequency; and  $v_B$  and  $w_m$  are the frequency shift and FWHM width of the *m*th line in the BGS.

#### 2.2. Fiber-Based Technique of SBS Suppression Rationale

To develop the fiber-based technique that suppresses SBS, the major parameter of concern is the SBS threshold. The SBS threshold is the maximum optical power allowed so that the ratio of  $P_s(0)$  over  $P_0$  does not exceed a certain threshold value [66]. The threshold value differs from paper to paper though, and the SBS threshold gain in dB still catches the essential physics.

Combined with Functions (6) and (7), the SBS effective gain factor *G* can be expressed as [67]:

$$GL_{\rm eff}(v) = \int_{0}^{l} \int_{-\infty}^{\infty} P_P(v) g_B e^{-\alpha z} \frac{1}{A_{\rm eff}} \frac{1}{\left(\frac{v - v_P - v_B}{w_m/2}\right)^2} dv dz \tag{8}$$

where *G* is the SBS effective gain factor;  $L_{\text{eff}} = (1 - e^{-\alpha L}) / \alpha$  is the fiber effective interaction length;  $P_P(v)$  is the laser spectrum; and  $A_{\text{eff}}$  is the mode effective area.

The SBS threshold using Smith's condition is described as:

$$P_{th} = \frac{21A_{\rm eff}}{g_{\rm B}L_{\rm eff}} \tag{9}$$

where  $g_B$  is the peak Brillouin gain.

$$g_B = \frac{4\pi n_O^8 p_{12}^2}{c\lambda_D^3 \rho_0 v_B w_m}$$
(10)

where  $n_O$  is the effective refractive index of the fiber;  $p_{12}$  is the respective component of the electrostriction tensor;  $\lambda_p$  is the incident pump wavelength; and  $\rho_0$  is the mean value of the material density of the fiber.

Equations (8) and (9) provide the guidance for the fiber-based techniques development. Equation (9) provides the guidance of SBS on the longitudinal direction and Equation (8) shed some light on the transverse dimension.

### 3. Fiber-Based Techniques for SBS Suppression

### 3.1. Transverse Optical Fiber Design

### 3.1.1. Large Mode Area Fiber

One idea to suppress SBS is to design optical fibers in terms of a fiber dopant and waveguide structure. In the early days, it was found that dispersion non-shifted fiber has better performance in terms of the SBS threshold than SSMF [68]. Additionally, various studies have been conducted to study the SBS in optical fibers with different core sizes, dopant concentrations, and dopant types. Nori Shibata researched three different core types (pure silica core, GeO<sub>2</sub> dopant core, and P<sub>2</sub>O<sub>5</sub> dopant core) with different waveguide structures and tailored the spectrum of SBS [69], which opens the door for future design. Y. Koyamada simulated the BGS by accounting for the contributions from all the acoustic modes along the fiber axis [64]. The model includes how the dopant type and concentration affect the acoustic velocity and refractive index, which is summarized from the empirical data [70–72].

One viable technique is to design the optical fibers that have a large mode area (LMA) [73]. From Equation (9), a large effective area has a linear relationship with the SBS threshold. One way to increase the mode effective area is to lower the core refractive index and increase the core diameter. Figure 7 shows the relationship between the core diameter and mode effective area for the GeO<sub>2</sub>-doped step-index fiber with different numerical aperture (NA). The mode effective area increases when the core diameter exceeds a certain value. Below that value, the core diameter is not large enough to confine the electric mode.

However, this method has constraint. The first constraint is that the optical fiber need be single mode. That means, when core diameter increases, the index difference must be decreased. However, the control of the small index steps in the glass manufacturing process can be difficult, which puts a limit to that method. The state-of-the-art conventional large-mode-area (LMA) fibers are generally limited in practice to diameters that are less than  $30 \ \mu m$  [74].



Figure 7. The relationship between the core diameter and mode effective area.

To further increase the mode effective area, photonic crystal fibers (PCFs) are proposed. PCF is an optical fiber with an ordered array of microscopic airholes running along its length. In such a fiber, the guidance is determined by the geometry of the pattern of airholes rather than by the material [75]. The introduction of micron-sized air holes in a fiber allows for a more precise control of the effective index of refraction of the cladding. The fabrication method applied is stacking and drawing, which could achieve the high precision of geometric index. Right after the first PCF laser was reported [76], the first LMA PCF laser was demonstrated [77]. Figure 8 shows an optical micrograph of this rod embedded in a PCF preform. The core area is in the middle, which consists of 425 small doped regions. With further fiber structure design and fabrication improvements [74,78–81], the reported mode effective area has increased significantly. Additionally, the results of LMA fiber lasers have been reported [82–84].



**Figure 8.** Optical micrograph of the core region of a fiber preform, showing 425 small doped regions within the core. Pitch 90 μm. [Reprinted/Adapted] with permission from [78] © The Optical Society.

### 3.1.2. Acoustic Tailoring

Another method is the acoustic tailoring that was proposed by Andrey Kobyakov, etc. [65], who found that the approximation in the derivation of Equation (9) is not necessary for every fiber design. For more complicated fiber geometry, the mode effective area  $A_{\text{eff}}^{ao}$ , needs be replaced by the acousto-optic effective area  $A_{m}^{ao}$ , with the expression:

$$A_m^{ao} = \left[\frac{\langle f^2(r) \rangle}{\langle \xi_m(r) f^2(r) \rangle}\right]^2 \langle \xi_m^2(r) \rangle \tag{11}$$

where the angular brackets denote averaging over the transverse cross section of the fiber, and f(r) and  $\xi_m(r)$  are the radial profiles of the fundamental electric and *m*th acoustic modes of the fiber, respectively. In Equation (11), the dependence  $\theta$  of the acoustic mode is dropped, since, in the overlap, the integral would be negligible if acoustic modes with angle dependence are considered.

The basic idea is to design special fiber structures that reduce the overlap integral between the fundamental electric mode field and acoustic mode field. To effectively reduce the overlap integral, the radial distribution of the aelectric mode field and acoustic mode field need be different. Since the optical fiber system components are designed for a Gaussian-like mode field, it would be convenient to tailor the acoustic mode field from an engineering point of view. It is not very difficult to find that Equations (4) and (5) are quite similar [85]. The optical refractive index  $n_O$  in Equation (4) is similar to  $1/V_L$  in Equation (5); thus, the acoustic refractive index  $n_a$  is defined as:

$$n_a(r) = \frac{V_{clad}}{V_L(r)},\tag{12}$$

where  $V_{clad}$  is the longitudinal velocity in the cladding and  $V_L(r)$  is the longitudinal acoustic velocity in the radial dimension.

A higher optical refractive index has the general effect of concentrating the electric field and so does higher acoustic refractive index on the acoustic field. To achieve the goal of reducing the overlap integral, the radial distributions of the optical refractive index and acoustic refractive index need to have different distributions. Table 1 shows how various dopant types affect the optical refractive index and acoustic refractive index. It can be shown that, if the dopant is  $GeO_2$ , two refractive indices both increase. However, if the dopant is  $Al_2O_3$ , the optical refractive index goes up, while the acoustic refractive index goes down, which is critical for this technique. One design method is proposed by Mingjun Li [86], which is shown in Figure 9. Two types of doping types (GeO<sub>2</sub> and Al<sub>2</sub>O<sub>3</sub>) are used, with (a) the  $Al_2O_3$  dopant at the inner core region and the GeO<sub>2</sub> dopant at the outer core region; (b) the GeO<sub>2</sub> dopant at the inner core region, the  $Al_2O_3$  dopant at the outer core region; and (c) the  $Al_2O_3$  dopant at both the inner core and outer core region. The electric mode profile and acoustic mode profile is shown in dashed lines. These two mode profiles are quite different, meaning SBS can be suppressed. The simulation results show that these designs can have roughly 6.7 dB SBS threshold gain vs. the GeO<sub>2</sub>-doped fibers with same optical refractive profile. This technique does not require the core diameter to be large. The experimental demonstration of the fiber-type design (a) is also fabricated as 12 m for fiber laser application. The SBS threshold gain is measured to be around 6 dB. By further optimizing the overlap integral and fabrication method, improvement has been reported [87–90]. This technique is critical for SBS suppression.

Table 1. Trend of optical and acoustic refractive index with different dopants in silica [86].

	GeO <sub>2</sub>	P <sub>2</sub> O <sub>3</sub>	TiO <sub>2</sub>	B <sub>2</sub> O <sub>3</sub>	F <sub>2</sub>	Al <sub>2</sub> O <sub>3</sub>
Optical refractive index	1	↑	1	$\downarrow$	$\downarrow$	1
Acoustic refractive index	$\uparrow$	$\uparrow$	1	$\uparrow$	$\uparrow$	$\downarrow$



**Figure 9.** Dopant designs for acoustic tailoring. (a) the  $Al_2O_3$  dopant at the inner core region and the GeO<sub>2</sub> dopant at the outer core region, (b) the GeO<sub>2</sub> dopant at the inner core region, the  $Al_2O_3$  dopant at the outer core region, and (c) the  $Al_2O_3$  dopant at both the inner core and outer core region. [Reprinted/Adapted] with permission from [86] © The Optical Society.

# 3.2. Longitudinal Variant Fiber Design

From a longitudinal point of view, SBS suppression can also be achieved by introducing longitudinal variant fiber design. The theoretical background of SBS in nonuniform fibers is laid by X.P. Mao, etc. [67], and later revised by S Rae, etc. [91].

### 3.2.1. Concatenated Optical Fibers

One technique to suppress SBS is to use concatenated fibers. As different fibers have different peak gain spectra, by concatenating different fibers, the total Brillouin backscattered power could be reduced compared with using only one type of fiber. The first experimental result using concatenating fibers was demonstrated by Toshihiko Sugie [92]; 364.3 km of optical fiber transmission was demonstrated and concatenated fibers were used to suppress SBS. The SBS threshold gain was proved to be 3.8 dB. One notable feature of using concatenated fibers is that the forward SBS threshold and backward SBS threshold would be different, which is illustrated in Figure 10. In addition, if two peak Brillouin frequencies of two fibers are separated enough, two frequencies can still be observed [93]. A. Kobyakov, etc., developed and experimentally validated an analytical approach to calculate the SBS threshold in a nonuniform fiber consisting of segments with non-overlapping Brillouin gain spectra [94]. The analytical results allow for the optimization of nonuniform fiber spans in applications where the magnitude of the SBS threshold is critical.



**Figure 10.** TheSBS thresholds of the concatenated fibers, (**a**) concatenation of fiber I and II, (**b**) concatenation of fiber I and fiber III. A is fiber I + fiber II, indicating that the front segment is fiber I and the backend is II, and same for B, C, D. [Reprinted/Adapted] with permission from [61] © The Optical Society.

### 3.2.2. Tapered Optical Fibers

Another technique is to fabricate tapered fibers. One method is to engineer the preform so that the fabricated fibers have core variations in the transmission direction. By changing the core diameter of the optical fiber, the peak Brillouin frequency shifts accordingly, which could effectively suppress SBS. The first experiment reported that the outer diameter of the 320 mm preform varied from 30 mm to 23 mm [68]. A 14 km long fiber was drawn, and the comparison experiment showed that the Brillouin gain was reduced by 3.5 dB. Recently, the fiber tapering method for SBS suppression has been widely explored in the realm of high-power amplifiers and lasers [95–102].

### 3.3. External Perturbations (Temperature and Strain)

Another technique is to apply external perturbations (temperature and strain) on optical fibers. Applying strain distribution and temperature distribution are two different ways to shift the peak Brillouin frequency. They both perturb the fiber preform and distort the fiber refractive index profile, which could shift the peak frequency of SBS. One notable application is Brillouin distributed sensing [103–107], the key to which is to detect local strain or temperature change, hence the local disturbance. In our application, the longitudinal variation along the optical fiber propagation direction due to strain or temperature distribution could be used to suppress SBS.

# 3.3.1. Temperature Distribution on Optical Fibers

Applying temperature distribution to suppress SBS is mostly used in short length fiber applications, especially high-power lasers or amplifiers from an engineering perspective. The thermal effects on Brillouin scattering has been studied since 1990s [108–110]. The effect of how a temperature change shifts the SBS central frequency is modeled by Equation (13) [111]:

$$\mathcal{L}(v) = g_B \frac{(w_m/2)^2}{(v - (v_B + c_f \Delta T))^2 + (w_m/2)^2}$$
(13)

where  $g_B$  is the peak Brillouin gain;  $c_f$  is the center frequency shift of Brillouin gain spectrum due to temperature gradient; and  $\Delta T$  is the temperature.

J. Hansryd, etc., demonstrated the SBS threshold increase for a short, highly nonlinear GeO<sub>2</sub>-doped fiber by applying different temperature distributions along the fiber [112]. By winding the fiber onto eight spools (100 m) with a temperature difference of 350 °C, an 8 dB increase in the SBS threshold was achieved. Other methods of creating temperature gradient were also demonstrated to be effective in SBS suppression [43,113–115].

### 3.3.2. Strain Distribution on Optical Fibers

Applying strain distribution along the optical fibers could also contribute to SBS suppression, which could be applied to both short and long optical fiber SBS suppression applications. The relationship between the strain  $\varepsilon$  and SBS frequency shift  $v_B(z)$  on longitudinal direction can be expressed as the following [116]:

$$v_B(z) = v_B + \beta \varepsilon(z) \tag{14}$$

where  $\varepsilon(z)$  is the strain applied to the fiber,  $\beta$  is the strain coefficient of the Brillouin frequency, and  $v_B$  is the SBS frequency shift when no strain is applied.

For short-distance applications, various methods could be implemented. One method is to divide the optical fibers into many sections and stretch each section with designed forces so that strain is introduced. Each section serves as an independent element and can be combined to simulate longitudinal strain distribution (stair ramp, triangular, etc.). Using this method, around 8 dB SBS threshold gain were demonstrated for around 500 m fiber [117,118]. Recently, the method of creating arbitrary longitudinal strain distribution was proposed and demonstrated [119]. The schematic of the coiling machine is shown in Figure 11. Fiber stain can be modified by a strain control module that consists of a brake

section and force sensor so that the arbitrary strain can be applied to each coil of the fiber. The strain technique has the advantage of convenient implementation, so it has been widely used to suppress SBS [116,120–122].



Figure 11. Schematic of the fiber coiling machine.

When optical fiber is used for transmission application, the methods are limited. This is mainly due to implementation cost. The main method is cabling. The first experiment applying strain distribution to suppress SBS was conducted by N.Yoshizawa, etc. [123]. In their experiment, strain distribution along the propagation distance was implemented by cabling. It was a double-stranded optical unit structure, where the optical fiber section can be stretched or compressed. Transmission over 3.7 km under-sea optical fiber was demonstrated. Compared with traditional fiber, the bandwidth of the SBS spectrum was expanded 2.9 times, which is the demonstration of SBS suppression. Years later, N. Yoshizawa, etc., optimized their cabling method by using a tight-double-helix structure [124,125].

# 3.4. Combined Techniques

These techniques are in general compatible with each other, thus can be applied in combination to further suppress SBS. Longitudinal variant fiber technique combined with temperature gradient technique [101], longitudinal variant fiber technique with LMA fiber technique [96,97] and acoustic tailoring technique with strain technique [126] were demonstrated.

# 4. Conclusions

In this paper, we have reviewed fiber-based techniques to suppress SBS. These techniques were developed based on rich properties of optical fibers, which cover electromagnetism, acoustics, and materials. Unfortunately, some important techniques (phase broadening, etc.) are beyond the scope of our paper, though they are equally important. The techniques of SBS suppression have been widely adopted in the fiber laser and fiber communication industry. Researchers are encouraged to further explore new techniques.

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