Article

Analysis of a Thermal Energy Storage Tank in a Large District Cooling System: A Case Study

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Abstract: This study's primary goal is to evaluate the performance of a large thermal energy storage tank installed in a Gas District Cooling (GDC) plant. The performance parameters considered in this study include thermocline thickness (WT_c), Cumulated Charge (Q_{cum}), and Half Figure of Merit (1/2 FOM). The operation sensor data of a large Thermal Energy Storage (TES) tank was acquired for this analysis. The recorded temperature sensor from the 1st to 7th January and from 12th to 17th October 2019 was considered in this research. GraphPad prism computer software was deployed for analyses, and the temperature distribution data were analyzed to determine the four temperature parameters (hot water temperature (Th), cool water temperature (Tc), cool water depth (C), and slope gradient (S)) using a non-linear regression curve fitting technique and sigmoid Dose Responses function as integrated with the software. At the end of this research, the relationship between the growth of the determined performance parameter with charging hours was analyzed and presented. The research results proved the ability of GraphPad Prism software to assess the temperature distribution in the TES tank and also the corresponding effects on the overall Tank performance. The software offers better advantages in evaluating the performance parameter of the TES tank accurately.

Keywords: thermocline thickness; thermal energy storage; Graphpad Prism; temperature profile; temperature distribution

1. Introduction

District Cooling System (DCS) is a smart solution that provides cooling energy within a centralized region. Thermal Energy Storage (TES) tank with Absorption Chillers (AC) and electrically driven Vapor Compression Chillers (VCC) are used to generate chilled water, which is transported to meet the substantial cooling demands for large spaces such as industrial facilities, universities, airports, and even residential areas [1]. The TES tank usage in GDC helps reduce capital cost, energy cost, carbon emissions, and equipment size, and makes for an improved chillers operation.

The help of the TES tank reduces the use of chillers during peak hours, thereby making it feasible for a higher chiller efficiency to be utilized, removing the disparity between demand and supply of energy [2,3]. In order to optimize energy saving and reduce the cost of TES operation, an optimal chiller plant strategy is developed [4]. In cases of increasing demand for refrigeration during peak hours, the additional chillers were switched over automatically [5].

Hasnain [6] reported that the most sophisticated and cost-efficient system in load management had been the resurgence of cool storage technology. The cooling system can be operated during off-peak night-time hours at low cooling loads using cold ambient temperature. Instead of using a compressor, cooling may be provided during the day at high peak by the circulation of the coolant medium [7].

The simplest form of cool TES makes use of chilled water as the storage medium [8]. TES tank has a distinct separation mechanism between cold and warm water, which is obtained either by providing physical barriers in tanks or by using natural stratification [9]. Physical barrier separation has been implemented with the labyrinth, baffle, and membrane based on the maze mechanism. In contrast, the natural process is achieved in thermally stratified systems, which permit the warm water to float on the top of cold water [10].

Naturally stratified tanks are less complicated, lower in cost, and equal or superior in thermal efficiency compared to other conventional forms of storage, making it a preferable option for TES designs [9]. Charging is done by introducing cool water into the lower nozzle, while warm water is removed from the upper nozzle of the TES tank [11]. Contrarily, discharging is carried out by the removal of cold water from the lower nozzle, while warm water is introduced from the upper nozzle. Both scenarios are pictorially explained in Figure 1.

Figure 1. Charging and discharging scenario in the Thermal Energy Storage (TES) tank: (a) Charging, (b) Discharging.

In a stratified TES tank, warm water settles above cold water without any physical barrier. The separation of the two segments is preserved by the natural density difference between the warm water and cool water known as the thermocline.

Temperature distribution in the TES tank can be used to observe stratified TES tanks for several purposes. These include performance evaluations, parametric studies, and characterization of the determination of mixing effects [12]. The stratification of the TES tank enables cold water to distinctively settle in the bottom layer, while warm water occupies the upper layer of the TES tank, forming an S-curve demarcation where the thermocline is created. The boundary limit between cold and warm water volume is located at the midpoint of thermocline thickness known as the thermocline position C.

Various studies related to the analysis of temperature distribution of stratified TES tanks have been carried out by researchers. Temperature distribution can be used to determine various TES performance parameters [13].

Musser and Bahnfleth [11,14] used the temperature profile of a full-scale stratified chilled water TES tank for determining thermocline thickness at various charging and discharging flow rates. TES tank performance based on evaluating the half-cycle Figure of Merit was also conducted in the study. Musser and Bahnfleth [15] used a dimensionless cut-off temperature on each edge of the profile to bind the region in which most of the overall temperature change occurs. They suggested that the amount of the temperature profile to be discarded should be large enough to eliminate the effects of small temperature fluctuation at the thermocline's extremes but small enough to capture most of the temperature change.

Bahnfleth, et al. [16] used temperature distribution to evaluate thermocline thickness on a full-scale stratified TES tank with slotted pipe diffuser.

Bahnfleth and Jing Song [17], in their study, researched the charging characterization of chilled water TES tank using a pair of ring octagonal slotted pipe diffusers in its configuration. This research was conducted at a constant flow rate. The initial temperature distribution was at a relatively uniform temperature after being fully discharged. In this research, the performance was quantified using thermocline thickness and a half-cycle Figure of Merit.

Walmsley et al. [18] used the siphoning method to manage thermocline thickness in an experimental stratified TES tank. The water temperature distribution was used to evaluate the effect of the re-established method on stratified TES tank operations. Joko [12], in his research, accurately determined the performance parameters of a hot stratified Thermal Energy Storage tank by using the temperature distribution profile of an operating TES tank. Joko's analysis was based on a mathematical formulation that utilized the sigmoid Dose–Response equation. He concluded that the significant performance parameters, which include thermocline thickness, half-cycle Figure of Merit, and cumulative cooling capacity, could be accurately determined during the charging cycle of the TES tank. Majid et al. [19] analyzed in their study the thermal energy storage tank performance using thermocline thickness and half-cycle Figure of Merit. They obtained a temperature profile from simulating temperature as distributed in a TES tank by using a non-linear regression curve function and sigmoid Dose–Response. They concluded that based on the values they obtained on performance analysis the chilled water, TES Tank was undergoing degradation.

In this study, an approach for deriving the TES performance parameters, namely thermocline thickness, Half Figure of Merit, and the Accumulative Charge (Q_{cum}), was established. GraphPad prism computer software was used to process the temperature distribution data using a non-linear regression technique to determine the hot water temperature (T_h), cool water temperature (T_c), cool water depth (C), and slope gradient (S) parameter. These determined parameters representing the S-curve temperature profile were used to analyze the TES tank's performance during the charging cycle [12,20]. Data used for the analysis in this research were acquired from a large district gas cooling plant with a remote sensor interval distance that records data every second. This study is a continuation of the research work outlined in the literature. The novelty of this research presents a computerized technique used to understand and compare the performance of a large full-scale TES tank over several months (10 months) of active operation. This study presents a unique and less ambiguous approach with a broader scope as compared to other related research.

System Overview

The GDC plant is installed with two TES tanks with a total holding capacity of 50,000 RTh (Refrigeration Ton-hour (RTh) is the of heat removal rate needed to freeze a metric ton (1000 kg) of water at 0 °C in 24 h) and the dimension of 24.5 m in diameter and 27.8 m in height. Data for analysis in this paper were taken from the daily operations of the Electric Chillers ECC and the TES tank as recorded.

In Figure 2, a block diagram represents the whole configuration of the Chiller plant as integrated into the District cooling plant operation. The set-up consists of four electric chillers, three cooling towers, and two air conditioners. The chillers' heat is disposed of by the cooling towers as the chillers function to supply chilled water to charge the TES tank during low load periods.

Figure 2. Configuration of 4 chillers at a large Gas District Cooling plant using the block diagram.

An hourly temperature dataset of the TES plant, from 1st to 7th January and from 12th to 15th October 2019, was used for the performance analysis. The data were used to obtain a temperature profile used in evaluating the performance parameters of the thermal storage tank. Performance parameters of the TES determined in this study include thermocline thickness, the half figure of performance, and cumulative cooling capacity.

2. Methodology

Usually, the water temperature distributional layout in the stratified TES tank is made up of 3 regions, namely,

- i. warm water at the top (Th),
- ii. cold water at the bottom (Tc), and
- iii. thermocline region in the middle (WTc)

The water temperature profile forms an S-curved shape in which two asymptotes are present in its makeup. The average cold and warm water temperatures are formed by the asymptote values of the cold temperature (Tc) and hot temperature (Th) in the TES tank. The thermocline position (C) defines the boundary line between the cold Tc and warm Th fluid portion of the tank. Therefore, the region limited by the edges of the asymptote curve is referred to as Thermocline thickness.

Sigmoid Dose–Respond SDR function is denoted by Equation (1):

$$T(x) = T(C) + (T_h - T_C)/(1 + 10^{(C-x)S}) \quad (1)$$

The GraphPad computer software uses the sigmoid Dose function technique in analyzing the temperature distribution to produce accurate values for function parameters (Tc, Th, C, and S).

2.1. Performance Parameters

The performance parameters analyzed in this study are thermocline thickness, half-cycle Figure of Merit (FOM) and accumulating charge capacity. These three parameters were employed in evaluating the performance of the TES tank of the DC plant.

2.1.1. Determination of Thermocline thickness

Joko and Amin [21] formulated a mathematical relationship for determining thermocline thickness. Thermocline thickness was formulated based on the function relationship by identifying the function

of the temperature profile. The concept for determining thermocline thickness was achieved by rearranging the equation into the form;

$$\frac{T_h - T_c}{T - T_c} = 1 + 10^{(c-x)s} \quad (2)$$

Using dimensionless cut-off temperature in Equation (3)

$$\Theta = \frac{(T - T_c)}{(T_h - T_c)} \quad (3)$$

Re-arranging and stating the limit point of the thermocline thickness Equation (4) is derived;

$$\frac{1}{\Theta} = 1 + 10^{(c-x)s} \quad (4)$$

From Equation (4), making $C - X$ the subject of formulae, we have;

$$C - X = \frac{\log\left(\frac{1}{\Theta} - 1\right)}{S} \quad (5)$$

Distance from C to X denotes half the thermocline thickness;

$$C - X = \frac{W_{tc}}{2} \quad (6)$$

Therefore, from Equations (5) and (6), thermocline thickness can be expressed as;

$$W_{tc} = \left(\frac{\log\left(\frac{1}{\Theta} - 1\right)}{S} \right) \quad (7)$$

Musser, A. and W.P. Bahnfleth [11] established that the dimensionless cut-off ratio Θ values range from 0 to 0.5, covering minimum and maximum thermocline thickness. $\Theta = 0$ indicates that the thermocline edges profile is located at T_c , and T_h therefore gives a maximum thickness. With $\Theta = 0.5$, the limit points are at the midpoint of the thermocline region, resulting in zero values of the thickness. Moreover, with Θ equal to 0 and 0.5, it revealed ∞ and 0, respectively. The mixing area measured from its edge is known as the thermocline thickness. The edge of the thermocline is referred to as dimensionless cut-off temperature Θ stated in Equation (3).

2.1.2. Determination of Half Figure of Merit FOM

Figure of Merit (FOM) is the ratio of integrated discharge capacity for a given volume to the ideal capacity that could have been achieved without mixing and losses to the environment. Although FOM seems straightforward in its definition, it may be challenging to evaluate its parameter in the field because most chilled water storage cannot perform full cycle tests spanning for 24 h or longer. It is therefore desirable to analyze the “half-cycle” performance of tanks over Half Figure of Merit. Half FOM is consequently defined as the ratio of integrated capacity (capacity useful energy stored in TES tank) to the theoretical capacity (capacity of cooling energy stored in the absence of losses) [15].

Half FOM is given as

$$1/2 \text{ FOM} = \frac{C_{int}}{C_{max}} \quad (8)$$

where

$$C_{int} = \frac{A \cdot \rho \cdot C_p \cdot (T_h - T_c)}{S} (\log(1 + 10^{sc}) - \log 2) \quad (9)$$

$$C_{max} = \rho \cdot A \cdot C_p \cdot C(T_h - T_c) \quad (10)$$

Therefore,

$$C_{loss} = C_{max} - C_{int} \quad (11)$$

2.1.3. Determination of Cumulative Cooling Capacity Q_{cum}

This describes the capacity of stored energy during the charging cycle of a stratified thermal storage tank. Joko Waluyo [12] in his research formulated a mathematical expression (in Equation (12)) to calculate the cumulative cooling capacity of a TES tank.

$$Q_{cum} = \frac{A \cdot \rho \cdot C_p \cdot (T_h - T_c)}{S} (\log(1 + 10^{S_c}) - \log(1 + 10^{S(CH)})) \quad (12)$$

where A = Area of circular Tank (m^2)

ρ = Water density (kg/m^3) and

C_p is the specific heat of the water at average temperature ($kJ/kg \text{ } ^\circ C$).

3. Results and Discussion

3.1. Data Acquisition

The data acquired comprise readings of tank datasheets, daily production reports, and the temperature for every layer in the stratified thermal energy storage tank. Data on the TES tank specification and the plant operations were extracted from the datasheet. Temperature distribution and the holding capacity of thermal energy storage were also extracted from the daily TES tank report for January 2019 to October 2019, while for the data of the production of the chilled water were taken from the daily electrical chiller report for January 2019 to October 2019. Table A1 presented in Appendix A shows a sample of the temperature distribution data for the 1st–2nd January 2019.

3.2. Plotting the Temperature Distribution on GraphPad Prism Software (Fitting Profile of Temperature Distribution)

Curve fitting was employed to find the set of parameter values of the function that best approaches the collected data. This thus minimizes the deviation between the observed and expected temperature values of each sensor. For this purpose, the commercial software GraphPad prism was used for its analysis. Hourly plots of different times of the year (1st–7th January to 12th–19th October 2019), which represent the fitting profile of the temperature distribution of the charging cycle, were analyzed on the software and are presented in Figures 3a–f and 4a–f.

Figure 3. Temperature distribution plot for 1st–7th of January 2019 on GraphPad prism software (a–f).

Figure 4. Temperature distribution plot for 12th–17th of October 2019 on GraphPad prism software (a–e).

GraphPad Prism visual plots in Figures 3 and 4 show that the temperature distribution is well fitted, and it followed a regular charging trend. Streams of charge on every hour assumed the S-curve shape on every instance as charging starts from 10 p.m. and ends at 8 a.m. each day.

3.3. Obtaining Curve Fitting and Performance Parameters

After plotting the temperature distribution profile, the metric that best fits the function would then be determined. In this study, parameters T_c , T_h , C , and S were generated using the commercial software GraphPad Prism 8. Tables 1 and A2, Tables A3–A6 contain parameter data from 1st to 7th January 2019,

while Tables A7–A12 contain parameter data from 12th to 17th October 2019. Tables A2–A12 are presented in Appendix A.

Table 1. 1st–2nd January 2019 Curve Fitting and Performance Parameter analysis.

Hours	Θ	Th (°C)	Tc (°C)	C (m)	S	R ²	Wtc	Q _{cum} (kJ)	1/2 FOM
22:00	0.1	10.31	5.557	~22.11	~5.442	0.9921	-	-	-
23:00	0.1	10.27	5.554	21.34	2.036	0.9923	0.9374	1.3×10^9	0.993072
0:00	0.1	10.24	5.576	21.11	1.559	0.9913	1.2242	1.27×10^9	0.990853
1:00	0.1	10.23	5.591	21.3	1.955	0.9912	0.9762	1.28×10^9	0.992771
2:00	0.1	10.22	5.544	21	0.9077	0.9927	2.1026	1.27×10^9	0.984208
3:00	0.1	10.25	5.593	21.18	2.358	0.9915	0.8094	1.27×10^9	0.993972
4:00	0.1	10.27	5.588	21.14	1.028	0.9922	1.8565	1.28×10^9	0.986148
5:00	0.1	10.25	5.555	21.05	1.03	0.9918	1.8529	1.28×10^9	0.986116
6:00	0.1	10.26	5.585	21.18	1.771	0.9917	1.0776	1.28×10^9	0.991975
7:00	0.1	10.21	5.567	21.2	1.592	0.9924	1.1988	1.27×10^9	0.991081
8:00	0.1	10.24	5.565	21.21	1.484	0.9928	1.2860	1.28×10^9	0.990436

The parameter data analysis, as presented in Tables 1 and A2, Tables A3–A12, provides complete information regarding curve fitting temperature parameters and the performance parameter during the hourly charging cycle of the TES tank. The coefficient of determination R² reveals that the correlation between experimental and obtained values in the curve fitting evaluation is well fitted as they all approached the value 1.

Figure 5 shows the plot of the average thermocline position C as against the charging time. As displayed on the chart, the result reveals that the position of thermocline changes with respect to hours of charging, as charging of the thermal energy storage tank proceeds the position of thermocline tends to move upward from the bottom of the tank until charging ends.

Figure 5. Average Thermocline Position (C) with Time.

For thermocline thickness WTC evaluation, the growth of thermocline thickness with charging time is revealed in Tables 1 and A2, Tables A3–A12, with the dimensionless cut-off temperature Θ set at 0.1.

The overall results, as shown in Figure 6 and Tables 1 and A2, Tables A3–A12, revealed that thermocline thickness was mostly constant throughout the charging time. The maximum thermocline thickness was observed at the lower part of the storage tank as a result of the position near the inlet diffuser, where the mixing has a more substantial influence. As the thermocline position moves further away from the inlet diffuser towards the top, improved quality of thermocline was recorded during

charging. This was a result of the reduced mixing that occurred within the tank as the cold mixture moves towards the outlet diffuser. The average thermocline thickness from 1st–7th January was 4.5 m and from 12th–17th October was 2.3 m; this means a 48.9% decrease in thermocline thickness between these months, as revealed in Figure 7. This means there was improved performance of the TES plant in terms of the thermocline.

Figure 6. Average thermocline thickness (Wtc) with time.

Figure 7. Average thermocline thickness trend between January and October 2019.

Results, as shown in Figure 8, reveal that charging started at 10 p.m. and ended at 8 a.m. The cumulative charge was observed to increase with the charging duration. It is also worthy to note that the average cumulative charge capacity (Q_{cum}) dropped between these months as presented in Figure 9. There was a 16.9% drop in the average cumulative charge from January to October 2019 in the TES performance operation.

Figure 8. Average cumulative charge over time.

Figure 9. Average cumulative charge with month.

The result, as shown in Figure 10, reveals that $1/2$ FOM increased as the charging process was initiated as suggested in past literature [12,15,22], and it assumed a steady value (near 1) moments into the charging process. This scenario occurs due to the decrease in the thermocline thickness as the thermocline position C moves upwards towards the top of the stratified TES tank where there is less mixing of cold and warm regions of fluids. Figure 11 reveals that the average half FOM as evaluated from 1st to 7th January was 0.96, and from 12th to 17th October was 0.98. This means that there was a 2.16% increase in the average half FOM in between these months, showing improved performance of the TES tank operation. This implies that the thermal efficiency of the tank improved as there was less conduction loss and mixing occurring in the tank during operation.

Figure 10. The plot of average Half Figure of Merit ($1/2$ FOM) with charging hours.

Figure 11. The average $\frac{1}{2}$ FOM trend between January and October 2019.

Based on the result, a higher temperature difference between the hot and cold regions of the tank makes for a thinner thermocline thickness, thereby improving the efficiency of the tank. Since temperature distribution is significantly affected as a result of mixing near the inlet nozzles [11,13], it is recommended that the designers install appropriate and more efficient diffusers at the nozzle connection [11].

This research further provides keen insight on TES operations for researchers, designers, and maintenance experts. It helps relate the temperature distribution trend in a large full-scale TES tank with various performance parameters over time. This approach provides practitioners with just enough information necessary to understand the internal workings of a large full-scale TES system based on the output temperature sensor readings at each time of operation.

4. Conclusions

Data from the operation of a full-scale Large District Cooling Plant were used for this study. Hourly temperature readings of 51 sensors as installed in the TES tank were acquired for analysis. The charging cycle from 1st to 7th January and from the 12th to 17th October 2019 was used in this analysis and comparison. GraphPad prism computer software was deployed for processing and analyzing the temperature distribution data using a non-linear regression curve fitting technique and a sigmoid Dose–Responses SDR function to determine the four-temperature parameter, namely hot

water temperature (T_h), cool water temperature (T_c), cool water depth (C), and slope gradient (S). These four parameters were used to determine the performance parameters (WT_c , $1/2$ FOM, and Q_{cum}) of the TES tank through established mathematical formulations. Based on the values of the average thermocline thickness and Half Figure of Merit from the results, it was observed that the stratified chilled water TES tank experienced an upgrade in its performance from the month of January to October 2019. Analysis of the operation of the plant revealed that there was a 48.9% decrease in the average thermocline thickness and a 2.16% increase on the average half FOM for the period of January through October 2019. This reveals that the stratified TES tank experienced an upgrade in its performance efficiency. This upgrade might have resulted from an improved general operation of the DGC plant or the replacement or servicing of components like the chillers. It can be suggested that the decrease in thermocline thickness may be as a result of less mixing in the hot and cold region of the fluid, thereby improving the quality of stored energy in the TES tank. The substantial decrease of thermocline thickness led to an increase in the tank's half FOM because a thinner thermocline thickness translates to the less fluid mixture in the stratified tank, which results in a higher $1/2$ FOM.

Based on the result, it can be concluded that GraphPad Prism software provides a less ambiguous technique with less computational time in understanding the behavior of the temperature profile of a full-scale TES tank at any time of operation.

The characterization of various performance parameters based on the behavior of the temperature profile as revealed in this research will further provide designers, maintenance experts, and researchers more useful insight on the working of a large TES plant during its charging cycle. It helps relate the temperature distribution trend in a large full-scale TES tank with various performance parameters over time. Although the scope of this research is broader in terms of TES size and the time considered in performance comparison, the conclusion made correlates with findings in other literature work that made use of various techniques in understanding the temperature distribution in the TES tank.

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Nomenclatures

Symbols	Description	Units
C	Thermocline position	m
C_{int}	Integrated capacity	kJ
C_{lost}	Lost capacity	kJ
C_{max}	Theoretical capacity	kJ
C_p	Specific heat of water	kJ
FoM	Figure of Merit	%
$1/2$ FoM	Half Figure of Merit	%
H	Tank water depth	m
Q_{cum}	Cumulative charge	kJ
S	Slope of Gradient	Dimensionless
T_c	Cold water temperature	°C
T_h	Hot water temperature	°C
WT_c	Thermocline thickness	m

Greek Symbols		Units
Θ	Dimensionless temperature	Dimensionless
ρ	Density	kg/m ³
Abbreviation	Description	
AC	Absorption Chiller	
ECC	Electric Chiller	
GDC	Gas District Cooling	
HVAC	Heat Vapour Air Conditioning	
RTh	Refrigeration Ton-hour	
VCC	Vapour Compression Chiller	

Appendix A

Table A1. Sample of Sensor temperature Readings in a DC plant (for 1st–2nd October 2019).

Sensor Elevation	Temperatures (°C) at Various Charging Time					
	22:00 p.m.	0:00 a.m.	2:00 a.m.	4:00 a.m.	6:00 a.m.	8:00 a.m.
51	11.54	11.69	11.62	11.69	11.14	9.12
50	11.64	11.64	11.66	11.64	11.12	9.06
49	11.59	11.58	11.54	11.58	10.55	6.92
48	11.56	11.71	11.6	11.56	7.61	5.35
47	11.09	11.19	11.16	11.03	5.74	5.04
46	11.43	11.45	11.47	11.25	5.56	5.4
45	11.25	11.37	11.29	11.09	5.35	5.22
44	11.44	11.5	11.44	11.25	5.48	5.4
43	11.28	11.29	11.27	10.91	5.4	5.22
42	11.43	11.43	11.43	11.09	5.4	5.23
41	11.15	11.2	11.14	10.72	5.12	5.09
40	11.61	11.58	11.53	10.91	5.4	5.22
39	11.51	11.54	11.43	8.16	5.22	5.08
38	11.58	11.58	11.4	6.08	5.22	5.22
37	11.45	11.45	11.12	5.43	5.09	5.09
36	11.64	11.64	11.3	5.43	5.35	5.07
35	11.64	11.64	11.3	5.38	5.3	5.08
34	11.48	11.48	11.12	5.2	5.12	4.94
33	11.48	11.48	11.09	5.13	5.12	4.99
32	11.6	11.61	11.1	5.3	5.17	5.06
31	11.12	11.11	10.55	4.91	4.96	4.73
30	11.61	11.61	9.87	5.19	5.27	5.19
29	11.35	11.2	6.61	5.07	5.07	4.88
28	11.58	11.3	5.77	5.13	5.22	5.06
27	11.51	11.2	5.45	5.14	5.17	4.99
26	11.32	11.04	5.19	5	5.07	4.94
25	11.64	11.22	5.43	5.25	5.3	5.08
24	11.64	11.12	5.43	5.25	5.38	5.23
23	11.64	11.12	5.43	5.25	5.3	5.12
22	11.35	10.86	5.14	5.1	5.15	4.96
21	10.88	10.03	4.7	4.64	4.68	4.61
20	10.94	6.65	4.75	4.75	4.76	4.75
19	10.76	5.53	4.86	4.68	4.7	4.7
18	10.6	4.91	4.73	4.67	4.58	4.55
17	10.65	4.94	4.78	4.78	4.78	4.78
16	10.65	4.94	4.78	4.7	4.71	4.66
15	10.42	4.83	4.7	4.58	4.7	4.65
14	10.65	4.94	4.78	4.78	4.78	4.78

Table A1. Cont.

Sensor Elevation	Temperatures (°C) at Various Charging Time					
	22:00 p.m.	0:00 a.m.	2:00 a.m.	4:00 a.m.	6:00 a.m.	8:00 a.m.
13	10.6	4.79	4.78	4.78	4.78	4.78
12	10.42	4.83	4.7	4.7	4.73	4.7
11	8.41	4.78	4.78	4.62	4.68	4.62
10	6.31	4.94	4.93	4.83	4.84	4.78
9	5.14	4.81	4.81	4.81	4.83	4.78
8	4.83	4.65	4.65	4.65	4.68	4.56
7	4.68	4.68	4.68	4.68	4.7	4.68
6	4.8	4.66	4.57	4.62	4.57	4.62
5	5.01	4.87	4.78	4.83	4.78	4.83
4	4.93	4.8	4.68	4.81	4.68	4.62
3	4.93	4.86	4.68	4.81	4.85	4.75
2	4.88	4.81	4.62	4.7	4.62	4.7
1	4.7	4.62	4.62	4.7	4.62	4.56

Table A2. 2nd–3rd January 2019 Curve Fitting and Performance Parameter analysis.

Hours	Θ	Th (°C)	Tc (°C)	C(m)	S	R ²	Wtc	Q _{cum} (kJ)	1/2 FOM
22:00	0.1	10.08	9.885	~11.75	~2748	0.1059	-	-	-
23:00	0.1	10.09	5.732	3.055	1.163	0.9551	1.6410	1.72×10^8	0.915308
0:00	0.1	10.08	5.513	7.358	1.588	0.9859	1.2018	4.34×10^8	0.974237
1:00	0.1	10.12	5.325	11.5	2.175	0.9923	0.8775	7.13×10^8	0.987965
2:00	0.1	10.09	5.206	16.17	1.059	0.9923	1.8022	1.02×10^9	0.982421
3:00	0.1	10.09	5.151	20.55	1.149	0.9945	1.6610	1.31×10^9	0.987251
4:00	0.1	10.06	5.166	25.17	1.334	0.9927	1.4306	1.59×10^9	0.991035
5:00	0.1	10.05	5.146	29.6	1.05	0.9938	1.8176	1.88×10^9	0.990314
6:00	0.1	10.18	5.167	34.26	1.262	0.9947	1.5123	2.22×10^9	0.993038
7:00	0.1	10.02	5.09	38.53	1.123	0.9937	1.6995	2.45×10^9	0.993043
8:00	0.1	10.23	5.115	40.33	1.063	0.9908	1.7954	2.67×10^9	0.992978

Table A3. 3rd–4th January 2019 Curve Fitting and Performance Parameter analysis.

Hours	Θ	Th (°C)	Tc (°C)	C(m)	S	R ²	Wtc	Q _{cum} (kJ)	1/2 FOM
22:00	0.1	11.66	5.164	8.797	0.2842	0.968	6.7153	7.39×10^8	0.880141
23:00	0.1	11.63	5.396	11.59	0.2963	0.976	6.4411	9.34×10^8	0.912388
0:00	0.1	11.57	5.339	15.97	0.3151	0.9791	6.0568	1.29×10^9	0.940179
1:00	0.1	11.41	5.339	20.47	0.4009	0.9833	4.7605	1.61×10^9	0.963318
2:00	0.1	11.27	5.33	24.71	0.5043	0.9847	3.7844	1.9×10^9	0.975843
3:00	0.1	11.39	5.271	29.55	0.2613	0.9852	7.3038	2.34×10^9	0.961014
4:00	0.1	11.06	5.314	33.83	0.5656	0.9899	3.3743	2.51×10^9	0.984267
5:00	0.1	10.98	5.256	38.15	0.5865	0.9888	3.2540	2.82×10^9	0.986546
6:00	0.1	10.65	5.255	42.46	1.046	0.9828	1.8246	2.96×10^9	0.993222
7:00	0.1	10.24	5.222	46.94	0.577	0.9693	3.3076	3.04×10^9	0.988885
8:00	0.1	10.9	5.165	47.32	0.9585	0.9802	1.9911	3.51×10^9	0.993363

Table A4. 4th–5th January 2019 Curve Fitting and Performance Parameter analysis.

Hours	Θ	Th (°C)	Tc (°C)	C (m)	S	R ²	Wtc	Q _{cum} (kJ)	1/2 FOM
22:00	0.1	11.54	5.151	9.87	0.6719	0.9944	2.8404	8.15×10^8	0.954607
23:00	0.1	11.61	5.216	13.43	0.6502	0.9937	2.9352	1.11×10^9	0.965526
0:00	0.1	11.61	5.204	18.09	0.9347	0.9956	2.0418	1.5×10^9	0.982197
1:00	0.1	11.51	5.145	22.62	0.7224	0.9958	2.6419	1.86×10^9	0.981578
2:00	0.1	11.46	5.174	27.1	0.8382	0.9931	2.2769	2.2×10^9	0.986748
3:00	0.1	11.53	5.118	31.6	0.6434	0.9959	2.9662	2.62×10^9	0.985194
4:00	0.1	11.51	5.113	36.04	0.8508	0.9967	2.2432	2.98×10^9	0.990183
5:00	0.1	11.38	5.119	40.54	0.6774	0.9951	2.8174	3.28×10^9	0.989038
6:00	0.1	11.27	5.134	44.81	0.6097	0.9898	3.1302	3.55×10^9	0.988982
7:00	0.1	10.95	5.106	48.99	0.8535	0.9745	2.2361	3.7×10^9	0.992801
8:00	0.1	10.71	5.066	45.23	1.322	0.9874	1.4436	3.3×10^9	0.994966

Table A5. 5th–6th January 2019 Curve Fitting and Performance Parameter analysis.

Hours	Θ	Th (°C)	Tc (°C)	C (m)	S	R ²	Wtc	Q _{cum} (kJ)	1/2 FOM
22:00	0.1	11.51	5.102	9.635	0.6643	0.9836	2.8729	7.98×10^8	0.952968
23:00	0.1	11.46	5.221	13.19	0.8007	0.9909	2.3835	1.06×10^9	0.971497
0:00	0.1	11.47	5.213	17.85	0.8019	0.9902	2.3800	1.44×10^9	0.978969
1:00	0.1	11.34	5.233	22.34	0.9946	0.9904	1.9188	1.76×10^9	0.986452
2:00	0.1	11.29	5.237	26.77	0.7057	0.9912	2.7044	2.09×10^9	0.984065
3:00	0.1	11.15	5.255	31.29	0.7361	0.9948	2.5927	2.38×10^9	0.98693
4:00	0.1	11.07	5.177	35.83	0.8262	0.9954	2.3100	2.73×10^9	0.989831
5:00	0.1	10.99	5.141	40.27	0.7912	0.9932	2.4121	3.04×10^9	0.990552
6:00	0.1	10.84	5.121	44.63	0.7695	0.9894	2.4802	3.3×10^9	0.991235
7:00	0.1	11.02	5.096	48.99	0.6965	0.9702	2.7401	3.75×10^9	0.991178
8:00	0.1	10.62	5.086	44.48	0.8465	0.9928	2.2546	3.18×10^9	0.992005

Table A6. 6th–7th January 2019 Curve Fitting and Performance Parameter analysis.

Hours	Θ	Th (°C)	Tc (°C)	C (m)	S	R ²	Wtc	Q _{cum} (kJ)	1/2 FOM
22:00	0.1	11.51	5.2	8.329	1.381	0.9905	1.3820	6.79×10^8	0.973829
23:00	0.1	11.47	5.256	12.53	1.656	0.9897	1.1525	1.01×10^9	0.985492
0:00	0.1	11.47	5.19	16.96	1.1	0.99	1.7350	1.38×10^9	0.983864
1:00	0.1	11.45	5.163	21.62	1.069	0.99	1.7853	1.76×10^9	0.986975
2:00	0.1	11.33	5.159	25.99	1.077	0.9902	1.7720	2.07×10^9	0.989246
3:00	0.1	11.29	5.187	30.53	1.412	0.9896	1.3516	2.41×10^9	0.993017
4:00	0.1	11.3	5.155	35.05	1.132	0.9889	1.6859	2.78×10^9	0.992413
5:00	0.1	11.12	5.144	39.48	1.415	0.9911	1.3488	3.05×10^9	0.994611
6:00	0.1	11.02	5.106	43.8	1.032	0.9897	1.8493	3.35×10^9	0.99334
7:00	0.1	10.87	5.111	48.4	1.183	0.9894	1.6133	3.6×10^9	0.994742
8:00	0.1	10.12	5.115	48.44	2.052	0.9915	0.9301	3.13×10^9	0.996971

Table A7. 12th–13th October 2019 Curve Fitting and Performance Parameter analysis.

Hours	Θ	Th (°C)	Tc (°C)	C (m)	S	R ²	Wtc	Q _{cum} (kJ)	1/2 FOM
22:00	0.1	10.41	5.212	12.38	0.8551	0.9941	2.2319	8.32×10^8	0.971564
23:00	0.1	10.39	5.407	14.01	1.018	0.9945	1.8747	9.02×10^8	0.978893
0:00	0.1	10.37	5.26	18.77	0.984	0.9959	1.9395	1.24×10^9	0.983701
1:00	0.1	10.37	5.232	24.08	1.058	0.9946	1.8039	1.6×10^9	0.988184
2:00	0.1	10.34	5.172	28.98	0.7894	0.9932	2.4176	1.94×10^9	0.986841
3:00	0.1	10.38	5.216	33.98	0.8591	0.9918	2.2215	2.27×10^9	0.989688
4:00	0.1	10.38	5.174	39	0.7527	0.9881	2.5355	2.62×10^9	0.989745
5:00	0.1	10.26	5.159	44	0.8933	0.9863	2.1364	2.9×10^9	0.992341
6:00	0.1	10.43	5.225	49.26	0.729	0.9331	2.6179	3.31×10^9	0.991617
7:00	0.1	~1913	5.022	~91.63	0.07786	0.7862	24.5118	-	-
8:00	0.1	10.82	5.104	47.7	0.8641	0.9756	2.2086	3.52×10^9	0.992697

Table A8. 13th–14th October 2019 Curve Fitting and Performance Parameter analysis.

Hours	Θ	Th (°C)	Tc (°C)	C (m)	S	R ²	Wtc	Q _{cum} (kJ)	1/2 FOM (%)
22:00	0.1	11.24	11.08	17.59	~55.24	0.2325	-	-	-
23:00	0.1	11.24	5.637	1.35	0.3179	0.913	6.0034	1.29×10^8	0.618802
0:00	0.1	11.29	6.502	6.507	0.3645	0.9824	5.2359	4.03×10^8	0.873856
1:00	0.1	11.34	5.509	10.93	0.3056	0.9938	6.2450	8.24×10^8	0.909936
2:00	0.1	11.3	5.267	15.71	0.2935	0.9951	6.5025	1.22×10^9	0.934715
3:00	0.1	11.3	5.18	20.73	0.282	0.9955	6.7677	1.64×10^9	0.948506
4:00	0.1	11.3	5.168	25.69	0.283	0.996	6.7438	2.04×10^9	0.958594
5:00	0.1	11.31	5.147	30.65	0.267	0.9951	7.1479	2.44×10^9	0.963215
6:00	0.1	11.26	5.141	35.84	0.271	0.9934	7.0424	2.83×10^9	0.969006
7:00	0.1	11.23	5.165	40.1	0.2904	0.9919	6.5719	3.14×10^9	0.97415
8:00	0.1	11.21	5.166	37.19	0.2828	0.995	6.7485	2.9×10^9	0.971378

Table A9. 14th–15th October 2019 Curve Fitting and Performance Parameter analysis.

Hours	Θ	Th (°C)	Tc (°C)	C (m)	S	R ²	Wtc	Q _{cum} (kJ)	1/2 FOM
22:00	0.1	11.87	8.424	-0.8578	0.07459	0.8242	25.5863	1.61×10^8	0.481601
23:00	0.1	11.72	6.237	6.026	0.5745	0.9683	3.3220	4.27×10^8	0.913089
0:00	0.1	11.76	5.842	10.9	0.5159	0.9838	3.6993	8.34×10^8	0.946468
1:00	0.1	11.73	5.677	15.65	0.5193	0.9912	3.6751	1.22×10^9	0.962959
2:00	0.1	11.69	5.656	20.92	0.6096	0.9937	3.1307	1.63×10^9	0.976395
3:00	0.1	11.68	5.632	25.82	0.5305	0.9936	3.5975	2.02×10^9	0.978023
4:00	0.1	11.55	5.629	30.85	0.5741	0.9934	3.3243	2.36×10^9	0.983003
5:00	0.1	11.45	5.598	36.04	0.6639	0.9936	2.8747	2.73×10^9	0.987419
6:00	0.1	11.31	5.576	40.84	0.6198	0.9906	3.0792	3.03×10^9	0.988108
7:00	0.1	11.19	5.506	44.48	0.5714	0.9804	3.3400	3.27×10^9	0.988156
8:00	0.1	11.43	5.552	41.63	0.6199	0.9869	3.0787	3.16×10^9	0.988335

Table A10. 15th–16th October 2019 Curve Fitting and Performance Parameter analysis.

Hours	Θ	Th	Tc	C	S	R ²	Wtc	Q _{cum} (KJ)	1/2 FOM
22:00	0.1	11.87	8.424	-0.8578	0.07459	0.8242	25.5863	1.61×10^8	0.481601
23:00	0.1	11.72	6.237	6.026	0.5745	0.9683	3.3220	4.27×10^8	0.913089
0:00	0.1	11.76	5.842	10.9	0.5159	0.9838	3.6993	8.34×10^8	0.946468
1:00	0.1	11.73	5.677	15.65	0.5193	0.9912	3.6751	1.22×10^9	0.962959
2:00	0.1	11.69	5.656	20.92	0.6096	0.9937	3.1307	1.63×10^9	0.976395
3:00	0.1	11.68	5.632	25.82	0.5305	0.9936	3.5975	2.02×10^9	0.978023
4:00	0.1	11.55	5.629	30.85	0.5741	0.9934	3.3243	2.36×10^9	0.983003
5:00	0.1	11.45	5.598	36.04	0.6639	0.9936	2.8747	2.73×10^9	0.987419
6:00	0.1	11.31	5.576	40.84	0.6198	0.9906	3.0792	3.03×10^9	0.988108
7:00	0.1	11.19	5.506	44.48	0.5714	0.9804	3.3400	3.27×10^9	0.988156
8:00	0.1	11.43	5.552	41.63	0.6199	0.9869	3.0787	3.16×10^9	0.988335

Table A11. 16th–17th October 2019 Curve Fitting and Performance Parameter analysis.

Hours	Θ	Th (°C)	Tc (°C)	C (m)	S	R ²	Wtc	Q _{cum} (kJ)	1/2 FOM
22:00	0.1	11.5	5.837	46.6	0.7649	0.9878	2.4951	3.41×10^9	0.991555
23:00	0.1	11.52	5.863	46.56	0.7611	0.9894	2.5075	3.4×10^9	0.991505
0:00	0.1	11.52	5.883	46.56	0.7478	0.9875	2.5521	3.39×10^9	0.991354
1:00	0.1	11.6	5.888	46.56	0.7362	0.9877	2.5923	3.44×10^9	0.991218
2:00	0.1	11.58	5.89	46.58	0.7536	0.9885	2.5325	3.42×10^9	0.991424
3:00	0.1	11.56	5.922	46.55	0.7347	0.9881	2.5976	3.39×10^9	0.991198
4:00	0.1	11.58	5.904	46.51	0.6924	0.9894	2.7563	3.41×10^9	0.990652
5:00	0.1	11.43	5.908	46.52	0.8113	0.9908	2.3524	3.32×10^9	0.992024
6:00	0.1	11.59	5.91	46.51	0.7165	0.9893	2.6636	3.41×10^9	0.990967
7:00	0.1	11.56	5.909	46.52	0.7363	0.9893	2.5920	3.4×10^9	0.991211
8:00	0.1	11.62	5.948	46.57	0.7138	0.9888	2.6737	3.41×10^9	0.990944

Table A12. 18th–19th October 2019 Curve Fitting and Performance Parameter analysis.

Hours	Θ	Th (°C)	Tc (°C)	C (m)	S	R ²	Wtc	Q _{cum} (kJ)	1/2 FOM
22:00	0.1	11.45	5.881	46.36	0.6708	0.9905	2.8451	3.34×10^9	0.99032
23:00	0.1	11.45	5.897	46.38	0.6726	0.9897	2.8375	3.33×10^9	0.99035
0:00	0.1	11.47	5.921	46.34	0.6365	0.99	2.9984	3.32×10^9	0.989794
1:00	0.1	11.45	5.914	46.31	0.6539	0.99	2.9186	3.31×10^9	0.990059
2:00	0.1	11.43	5.93	46.34	0.6756	0.9902	2.8249	3.29×10^9	0.990385
3:00	0.1	11.47	5.926	46.32	0.624	0.9896	3.0585	3.32×10^9	0.989585
4:00	0.1	11.41	5.94	46.32	0.6596	0.9889	2.8934	3.27×10^9	0.990147
5:00	0.1	11.46	5.935	46.37	0.6437	0.9911	2.9649	3.31×10^9	0.989915
6:00	0.1	11.46	5.989	46.32	0.6255	0.9897	3.0511	3.27×10^9	0.98961
7:00	0.1	11.61	5.968	46.33	0.602	0.9894	3.1702	3.38×10^9	0.989207
8:00	0.1	12.28	5.957	45.04	0.4934	0.9915	3.8680	3.68×10^9	0.986454

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