



Two-Step Many-Objective Optimal Power Flow Based on Knee Point-Driven Evolutionary Algorithm

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Article

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Abstract: To coordinate the economy, security and environment protection in the power system operation, a two-step many-objective optimal power flow (MaOPF) solution method is proposed. In step 1, it is the first time that knee point-driven evolutionary algorithm (KnEA) is introduced to address the MaOPF problem, and thereby the Pareto-optimal solutions can be obtained. In step 2, an integrated decision analysis technique is utilized to provide decision makers with decision supports by combining fuzzy c-means (FCM) clustering and grey relational projection (GRP) method together. In this way, the best compromise solutions (BCSs) that represent decision makers' different, even conflicting, preferences can be automatically determined from the set of Pareto-optimal solutions. The primary contribution of the proposal is the innovative application of many-objective optimization together with decision analysis for addressing MaOPF problems. Through examining the two-step method via the IEEE 118-bus system and the real-world Hebei provincial power system, it is verified that our approach is suitable for addressing the MaOPF problem of power systems.

Keywords: optimal power flow; optimal operation; power systems; multi-objective optimization; knee point-driven evolutionary algorithm; decision analysis; best compromise solutions

1. Introduction

Optimal power flow (OPF) plays a major part role in guaranteeing the safe and economical operation of power systems [1,2], and it has been receiving the wide-spread attention of professionals and researchers from academia and industry [3,4], especially in the case of large-scale integrations of renewable energy resources [5,6]. The key idea of OPF is to find the optimal operating point with the lowest generation/operating costs under the premise of constraints [7–9], which contain a series of equality and inequality equations [10,11]. However, the conventional mono-objective OPF, which generally seeks optimum economy [12,13], such as active power losses or generation costs, becomes unable to meet the diversified needs of electricity consumers. In [12], an OPF model is proposed for determining optimal operating points of a power system, and the operating costs of the system are set to the mono-objective function in the model. In [13], the adjustable direct current OPF is presented and the objective function is taken as the total generation cost of units. And at the same time, the power flow characteristics of a modern power system are becoming increasingly complex due to the growing penetration of distributed generations [14-17] and the deployments of novel power electronic loads [18-22]. In this context, multi-objective OPF (MOPF) has received the extensive attention of researchers in the field of OPF [23–28], since it can coordinate different-weight or even conflicting multiple objectives. However, MOPF poses challenges in terms of computational complexity due to its inherent non-linear, non-convex, and non-smooth characteristic [23,24], which is hard to solve directly.

Recent research suggests that multi-objective evolutionary algorithms (MOEAs) are promising tools for addressing various challenging optimization tasks in engineering fields [29–32]. In order to optimal distributed generation planning, a MOEA is employed in [29]. Reference [30] reviews the most representative MOEAs that have been reported, and MOEA has developed as an effective method to solve such an optimization problem. In [31], MOEA is employed for planning overtime of software engineers. The layout of wind farms is optimized via MOEA in [32]. In particular, MOEAs can be also applied to solve the OPF issue [23–28]. Unfortunately, the MOPF can only cope with the optimization issue with two to three objectives, which, to a certain extent, limits the practicality of this type of methods. In addition, many-objective optimization problems (MaOPs), considering four or more objective functions in the OPF problem [33–36], are commonly existed phenomenon in the practice of real-world power system operation [33]. In [34], a specially tailored MOEA is presented for tackling the current large-scale MaOPs. Another MOEA based on adaptive search strategy is presented for coping with MaOPs in [35]. In [36], six different evolutionary algorithms (EAs) are tested, and the results prove that MOEAs exhibit their own capabilities in dealing with different MaOPs. For this reason, MaOPs have recently gained a great deal of attention as most existing MOEAs are inadequate for solving OPF problems with four or more objectives, and it has become a hotspot to enhance the ability of MOEAs for addressing MaOPs issues [37-39]. However, manyobjective OPF (MaOPF) is quite challenging for solving since it is generally non-convex and nondeterministic polynomial-time hard (NP-hard). Motivated by the recent work in literature [23], a new powerful MOEA, called knee point-driven evolutionary algorithm (KnEA), is applied for solving this problem in the paper, which is helpful to better adapt the increasingly diversified operating requirements for the construction of the modern power systems.

In recent years, MOEAs have been successfully utilized in the field of multi-objective OPF (MOPF) problems in some significant pioneering works. In [24], one of MOEAs, artificial bee colony algorithm, is applied for addressing MOPF issues. For solving similar MOPF issues, the improved strength Pareto evolutionary algorithm is adopted in [25]. In [26], the gravitational search algorithm is employed to cope with this issue. In [27], MOEA is applied for solving the MOPF problems in combined heat and power economic emission dispatch. An approach based on the improved MOEA is proposed to generate Pareto-optimal solutions efficiently in [28]. In [40], a hybrid MOEA is put forward to deal with the MOPF issue by taking into account a set of various constraints. In [41], a model with two optimization objectives representing economy and stability is built for the system, then it can be solved due to the adoption of non-dominated sorting genetic algorithm II (NSGA-II) [42,43]. In [44], an improved MOEA/D algorithm is used for solving MOPF issues of power systems, and the used OPF model considers two and three objective functions in the indices relevant to cost, emissions, power losses, and stability. Unfortunately, most of all the above investigations focus on the OPF problems with two or three objectives for the power system, which is unable to meet the electricity consumers' needs of an increasingly diverse. In particular, there are many requirements that should be satisfied both for electricity suppliers and for users in the actual operation of power systems, which explains the reason why MaOPF is an urgent practical problem. As a matter of fact, the MaOPF has arisen as a consequence of some difficulty to overcome in the context of a research and development project. However, as far as the authors know, very few studies have investigated the MaOPF issue in literatures, thus this work focuses on solving the MaOPF problem.

This paper proposes a novel two-step MaOPF method by combining KnEA and integrated decision making for addressing this problem. The approach includes two-folds: many-objective optimization and decision support. At step 1, the Pareto-optimal solutions can be obtained, through solving the model of MaOPF with employing KnEA; at step 2, the best compromise solutions (BCSs) can be identified according to priority memberships in each group, and each group represents different objective preference. While the fuzzy c-means (FCM) clustering is applied to divide the solutions into several groups, grey relational projection (GRP) method is employed to calculate priority memberships. The primary contribution of the proposal is the innovative application of many-objective optimization into the optimal power flow field.

The rest of this paper is organized as follows. In Section 2, a MaOPF model is built; Section 3 displays the solution methodology based on the model; and then, Section 4 contains case studies; lastly, conclusions are drawn in Section 5.

2. MaOPF Model

This section outlines the model of MaOPF, including the objective functions and related constraints. With the current development of power systems, different requirements need to be met, such as economy, safe and environmental protection. Thus, four objective functions are contained in the MaOPF model. What's more, the equality and inequality constraints are also included in the novelty MaOPF model, and those common constraints in OPF issues are employed in this paper.

2.1. Objective Function

To satisfy the requirements of economic, safety and environmental in power system, the objective functions of MaOPF problem consider generation cost, voltage deviation, *L*-index, and emissions of polluting gases in this work.

2.1.1. Generation Costs

Generally, the minimum generation $\cot f_i$ is the main objective function that must be considered in the OPF problem, which represents the economy of operation of power systems. The expression of the generation cost is [45–47]:

$$f_{1} = \sum_{i=1}^{N_{G}} \left(\alpha_{i} P_{G,i}^{2} + \beta_{i} P_{G,i} + \gamma_{i} \right)$$
(1)

where $P_{G,i}$ denotes the active output power produced by generator *i*, and N_G is the total number of generators; α , β , and γ indicate the quadratic, linear and constant factors of a generator, respectively.

2.1.2. Index of Voltage Deviation

Taking into account that the voltage deviation is an important measure to reflect the voltage quality and safety level of a power system [24,26], the minimize voltage deviation index f_2 is taken as one of the optimization objectives for evaluating system security [47,48]. The expression of f_2 is given by:

$$f_2 = \sum_{i=1}^{N} (U_i - U_{ref,i})^2$$
⁽²⁾

where U_i indicates the voltage amplitude of bus *i* in the system, and the total number is *N*, $U_{nef,i}$ is the pre-defined voltage amplitude of U_i .

2.1.3. Static Voltage Stability Margin

For the static security issue, *L*-index is another evaluation merit in OPF problems. The value of *L*-index can judge how far from the operation point of voltage collapse to that of normal, and *L*-index is defined as [49,50]:

$$L_{j} = \left| 1 - \sum_{i=1}^{N_{G}} F_{ji} \frac{U_{i}}{U_{j}} \angle \left(\theta_{ij} + \delta_{i} - \delta_{j} \right) \right|$$

$$F_{ji} = - \left[\mathbf{Y}_{LL} \right]^{-1} \left[\mathbf{Y}_{LG} \right]$$
(3)

where θ is the phase-angle difference between two buses, and δ is the voltage phase angle of the bus, \mathbf{Y}_{LL} and \mathbf{Y}_{LG} are subarrays in the admittance matrix for nodes. Then, the objective function f_3 ,

which is the minimum value of *L*-index, is employed to describe the static voltage stability margin. The equation of the third objective is shown as follows [49,50]:

$$f_3 = \max\left(L_j\right), \quad j = 1, \dots, N_b \tag{4}$$

where N_{h} is the number of load buses in the system.

2.1.4. Emissions of Polluting Gases

In the proposed MaOPF model, the fourth objective function f_4 considers the environmental demand of power system, thus the minimum emissions of polluting gases are utilized. The expression of f_4 is as follows [51,52]:

$$f_4 = \sum_{i=1}^{N_G} \left(a_i P_{G,i}^2 + b_i P_{G,i} + c_i \right)$$
(5)

where a_i , b_i and c_i denote the quadratic, linear and constant polluting gases emissions coefficients of generator *i*.

2.2. Constraints in Power Systems

In the power system, the used main constraints in the MaOPF model are introduced in this section.

2.2.1. Constraints of Equality

In the OPF problem, the equality constraints are universally considered and enforced, which can be written as nonlinear equations as follows [24,26]:

$$P_{g,i} - P_{d,i} = U_i \sum_{j \in i} U_j \left(G_{ij} \sin \theta_{ij} + B_{ij} \cos \theta_{ij} \right)$$

$$Q_{g,i} - Q_{d,i} = U_i \sum_{j \in i} U_j \left(G_{ij} \sin \theta_{ij} - B_{ij} \cos \theta_{ij} \right)$$
(6)

where $P_{g,i}$ and $P_{d,i}$ are the injected active power and active load in bus *i*, while $Q_{g,i}$ and $Q_{d,i}$ are the reactive injected power and reactive load, G_{ij} and B_{ij} are respectively the conductance and susceptance between buses *i* and *j*. This equation suggests that the active and reactive powers need to keep balance in the power system.

2.2.2. Constraints of Inequality

Herein, the bounds of variables in the power system are considered for the purpose of ensuring the power system in a safe state during operation, and they can be formulated as [24,26]:

$$\begin{split} P_{G,i}^{\min} &\leq P_{G,i} \leq P_{G,i}^{\max} , \ i = 1, ..., N_G \\ Q_{G,i}^{\min} &\leq Q_{G,i} \leq Q_{G,i}^{\max} , \ i = 1, ..., N_G \\ U_i^{\min} &\leq U_i \leq U_i^{\max} , \quad i = 1, ..., N \\ T_i^{\min} &\leq T_i \leq T_i^{\max} , \quad i = 1, ..., N_T \\ Q_{C,i}^{\min} &\leq Q_{C,i} \leq Q_{C,i}^{\max} , \quad i = 1, ..., N_C \\ S_{Lii}^{\min} &\leq S_{Li} \leq S_{Lii}^{\max} , \quad i = 1, ..., N_L \end{split}$$
(7)

where $Q_{c,i}$ represents the reactive power produced by generator *i*; T_i indicates the tap of adjustable transformer *i*, and the number of transformers is N_T ; $Q_{c,i}$ expresses the reactive power of compensation device *i*, and the number of devices is N_c ; $S_{L,i}$ denotes the power flow in the branch

i of the system, and N_L expresses the number of branches; each variable has its upper and lower limits, which are respectively represented by the subscript 'max' and 'min'.

3. Two-Step Solution Approach

The proposal is divided into two phases: an optimization process with many objectives and the following decision support procedure. At step 1, the set of Pareto optimal solutions is gained with the employment of KnEA. Then at step 2, FCM clustering is adopted to classify the set obtained in the first step. GRP method is applied to automatically select BCSs from each group.

3.1. Optimization Process with Many Objectives

The first step is introduced in this section. By solving MaOPF model with KnEA, the set of Pareto optimals is obtained.

3.1.1. KnEA-Based Many-Objective Optimization

The key concept of the KnEA is knee points (KPs). Different from other MOEAs, the KnEA employs a prevailing non-dominance selection criterion strategy and a secondary selection criterion strategy whose reference is the KPs in the optimization process [33]. After the environmental selection process, the diversity of the population is improved. In addition, mating selection adopting tournament strategy is applied in KnEA, and weighted distance is a metric of the strategy. The weighted distance WD(p) of solution p is defined as [33]:

$$WD(p) = \sum_{i=1}^{k} wd_{p_{i}} dis_{pp_{i}}$$

s.t. $wd_{p_{i}} = \frac{rd_{p_{i}}}{\sum_{i=1}^{k} rd_{p_{i}}}$
 $rd_{p_{i}} = \frac{1}{\left| dis_{pp_{i}} - \frac{1}{k} \sum_{i=1}^{k} dis_{pp_{i}} \right|}$ (8)

where p_i is the *i*th nearest neighbor of solution p; wd_{p_i} and rd_{p_i} are respectively the weight and rank of p_i ; dis_{p_i} denotes the Euclidean distance between p and p_i .

In the KnEA, a KP is defined as the point with the maximum distance to the hyperplane within neighborhood scope in the objective functions space [53]. In the *g*th generation, the neighborhood scope R_g^i corresponding to the objective function f_i is given by:

$$R_{g}^{i} = \left(f_{i,g}^{\max} - f_{i,g}^{\min}\right) \cdot r_{g}$$
s.t. $r_{g} = r_{g-1} \cdot e^{-\frac{1 - t_{g-1} / TH}{N_{obj}}}$
(9)

where the upper and lower limits of the *i*th objective function f_i are respectively represented by the superscript 'max' and 'min', and the total number of functions is N_{obj} ; *r* denotes the proportion of neighborhood scope in the objective span; *g* represents the *g*th generation; *t* is the proportion of the KPs in the whole population; 0 < TH < 1 expresses the boundary.

3.1.2. Procedure of Many-Objective Optimization

The flowchart of the optimization procedure using the KnEA is shown in Figure 1, and the specific steps are as follows [33].



Figure 1. Process of optimization scheme by using knee point-driven evolutionary algorithm (KnEA).

Step 1: Enter the initial variables. The variables mainly incorporate three-folds as follows.

- (1) The network parameters: the related information of power systems.
- (2) The controlled variable parameters: the bounds which are shown as (7), and the steps of $_T$ and Q_c . The considering controlled variable are listed as follow:

$$\left(\underbrace{P_{G,1},\cdots,P_{G,i},\cdots,P_{G,N_{G}},U_{G,1},\cdots,U_{G,i},\cdots,U_{G,N_{G}}}_{\text{continuous variables}},\underbrace{T_{1},\cdots,T_{i},\cdots,T_{N_{T}},Q_{C,1},\cdots,Q_{C,i},\cdots,Q_{C,N_{C}}}_{\text{discrete variables}}\right)$$

where U_{G} is the generator terminal voltage.

(3) The algorithm parameters: the population size N_{pop} , the maximum generation number g_{max} , the set of KPs κ , the ratio of size r, the rate of KPs in population t, the number of objectives N_{obj} which is taken as 4 in this paper.

Step 2: Create an initial population Pop_0 , initial the set of KPs K which is an empty set, and set the generation counter g=0, $r_0=1$, $t_0=0$ Considering that the variables T and Q_c are discrete variables while others are continuous variables, a hybrid coding scheme is employed in the initialization process.

Step 3: Generate population Pop_g' by adopting binary tournament mating selection with three strategies for distinguishing solutions, that is, dominance comparison, KP criterion, and WD(p) in Equation (8) [33]. If the non-dominance selection and the secondary selection criterion strategy fail to discriminate solutions in Pop_g' , they can be chosen eventually according to the value of WD(p). Then, the population Pop_g' is formed by the solutions with the mating selection.

Step 4: Update the population Pop_g with genetic variations. The two operations, simulated binary crossover, and polynomial mutation, are implemented in Pop_g '. The population Pop_g is then updated based on the individuals in Pop_g and Pop_g ', and $Pop_g = Pop_g \cup Pop_g$ '.

Step 5: Compute the values of objective functions $F = \{f_1, f_2, f_3, f_4\}$, and then the non-dominated solutions are identified from Pop_q .

Step 6: Renovate the set κ . The KPs are chosen according to (9), and the set of KPs κ are recorded and renovated in the optimization process.

Step 7: Based on the set κ and the objective function values, generate the next generation population Pop_{g+1} based on the environmental selection strategy [33].

Step 8: Judge the termination criteria. If $g < g_{max}$, return to Step 3 after adding 1 to the current generation *g*; otherwise, output the Pareto-optimal solutions.

3.2. Decision Support

In real-world practice, it is quite challenging for decision makers to figure out whether a Paretooptimal solution is a BCS or not from among the non-inferior solutions. First, considering the fact that there are a lot of generated Pareto-optimal solutions, the references of decision makers might be different for a specific operation point. Another issue is that for a specific system the preference of the same decision maker may also vary according to changing operational requirements. Therefore, in the second step, that is, the decision support process, FCM and GRP method are adopted to evaluating Pareto optimal solutions, and BCSs are identified which are represent decision-makers' different, even conflicting, preferences.

3.2.1. Fuzzy c-Means

FCM is a classical unsupervised clustering algorithm. After processing of FCM clustering, the similarities between the solutions in the same group are the largest, while the similarities between the solutions in different groups are the smallest. The model of FCM can be formulated as [54–56]:

$$\min \ J_m = \sum_{i=1}^{N_p} \sum_{j=1}^{N_c} \mu_{ij}^m \left\| w_i - c_j \right\|^2$$

s.t.
$$\sum_{i=1}^{N_c} \mu_{ij} = 1$$
 (10)

where *J* expresses loss function for judging the convergent degree, $m(m \ge 1)$ is a constant for controlling the clustering fuzziness, $\mu_{ij} (\mu_{ij} \in [0,1])$ is the membership degree between solution w_i and center c_j , while w_i denotes the *i*th Pareto optimal solution in the whole set, c_j is the *j*th clustering center; N_p and N_c are the number of solutions and clusters, respectively. Here, N_c is taken as 4 (corresponding to the considered four objective functions).

3.2.2. GRP Method

As one of the decision methods, GRP method is especially suitable for evaluating the solutions with grey relationships in the MaOPs, which is based on grey system theory and vector projection [23]. The projection $V_l^{t(-)}$ of the *l*th solution in the ideal scheme can be written as [57,58]:

$$V_{l}^{+(-)} = \sum_{k=1}^{N_{p}} \gamma_{lk}^{+(-)} \frac{\omega_{k}^{2}}{\sqrt{\sum_{k=1}^{N_{l}} (\omega_{k})^{2}}}$$
(11)

where plus sign denotes positive scheme, minus sign represents negative scheme, γ_{lk} indicates the grey relational factor of the *k*th objective in *l*th solution. ω_k is the weight of the *k*th objective, the corresponding weights of four objectives are set to the same value in this paper, and the operators can adjust the weights according to the actual working condition or personal preference. Then, the priority membership $PM_l(0 \le PM_l \le 1)$ of solution *l* can be written as follows:

$$PM_{l} = \frac{(V_{0} - V_{l}^{-})^{2}}{(V_{0} - V_{l}^{-})^{2} + (V_{0} - V_{l}^{+})^{2}}$$
(12)

where V_0 equals to the value of V_1 when V_1 takes 1. The greater the membership of the solutions is, the closer it is to the ideal scheme; and vice versa. In this way, the solutions with the highest PM values in each group are regarded as the BCSs.

4. Case Studies

For examining validity of the approach provided in this paper, two test systems with varied complexity levels, i.e., the IEEE standard system and the system applied in Hebei province, are taken as test cases. And furthermore, to properly measure the optimization performance of our approach, two state-of-the-art MOEAs for solving MaOPs, i.e., the reference vector guided evolutionary algorithm (RVEA) and non-dominated sorting genetic algorithm III (NSGA-III), are employed as comparison algorithms. All programs in this work are carried out by a desktop computer with 3.40 GHz CPU basic frequency and 4 GB memory.

4.1. IEEE 118-Bus System

The first step is introduced in this section. By solving MaOPF model with KnEA, the set of Pareto optimals is obtained.

4.1.1. Introduction to the System

As a well-known test system, IEEE 118-bus system is extensively studied in previous literature [26]. This system with base capacity 100 MVA includes 14 active generators, 132 branches, 9 adjustable transformers. In the system, bus 69 is the slack bus. The related coefficients of generator *i*, such as α_i , β_i , γ_i , α_i , b_i , and c_i , are extracted from literature [26].

The limits of controlled variables are listed as follows: the lower and upper bounds of the voltage are respectively 0.95 p.u. and 1.10 p.u., the tap $_T$ varies from 0.9 p.u. to 1.1 p.u., and the lower and upper bounds of Q_c are 0 and 0.5 p.u.; the step-size of $_T$ and Q_c are respectively 0.0125 p.u. and 0.01 p.u.; the upper bound of the branch transmission capacity is 300 MVA.

4.1.2. Algorithm Comparison

As mentioned above, three algorithms are employed to solve MaOPF problem. In order to facilitate comparison, N_{pop} and g_{max} of all three algorithms are respectively 50 and 100. The three algorithms repeatedly run 20 times independently. Among all the results of the 20 runs for each algorithm, without loss of generality, one result (i.e., a set of Pareto optimals) is randomly taken as an instance for the consequent analysis. The distributions of three selected results with four objective functions are shown in Figures 2–4.



Figure 2. Distribute condition of Pareto-optimal solutions of KnEA.



Figure 3. Distribute condition of Pareto-optimal solutions of reference vector guided evolutionary algorithm (RVEA).



Figure 4. Distribution of Pareto-optimal solutions of non-dominated sorting genetic algorithm III (NSGA-III).

The comparison of extreme values of the four objective functions obtained by each algorithm is shown in Table 1, and the smallest values in each line of Table 1 have been marked with bold fonts. According to the results in Table 1, it is obvious that the extreme values of the four objectives obtained by KnEA are smaller than that of the other two algorithms when solving the MaOPF problem. To a certain extent, the extreme value can evaluate the performance of MOEAs. The smaller extreme value means that the optimization performance is more effective, thus KnEA has the best performance in the three algorithms only from the view of extreme values.

Objective Function	Extreme Value	KnEA	RVEA	NSGA-III
(//104 # //)	Maximum value	2.3062	2.3413	2.3507
J1/(10* \$/n)	Minimum value	2.2808	2.2826	2.2831
<i>f</i> ₂ /(p.u.)	Maximum value	0.0224	0.3147	0.0408
	Minimum value	0.0165	0.2451	0.0177
<i>f</i> ₃ /(p.u.)	Maximum value	0.0449	0.0456	0.0496
	Minimum value	0.0301	0.0406	0.0361
<i>f</i> ₄ /(10 ⁴ lb/h)	Maximum value	2.2539	2.3151	2.2857
	Minimum value	2.2036	2.2078	2.2058

Table 1. Comparison of extreme values of KnEA, RVEA, and NSGA-III. (KnEA: knee point-driven evolutionary algorithm; RVEA: reference vector guided evolutionary algorithm; NSGA-III: non-dominated sorting genetic algorithm III).

How to assess the performance of MOEAs has recently been attracting concerns. Unfortunately, this is still an open question at the moment. In general, a good evaluation indicator should have good convergence and distribution characteristic [23]. Two quantitative indicators, which can assess the optimization performances of three different algorithms in different aspects, are employed in this study.

(1) Generational distance

The first indicator is the well-known generational distance (GD), which represents the convergence conditions of the set [23]. For measuring the convergence of obtained solutions, the formulation of GD is given as follows:

$$GD = \frac{\sqrt{\sum_{i=1}^{N_p} D_i^2}}{N_p}$$
(13)

where D_i denotes the Euclidean distance in objective function space, which is calculated between each two nearest solutions.

(2) Spacing

The spacing (SP) is another popular indication for estimating the distribution of a Pareto front, and its expression is given by [23]:

$$SP = \sqrt{\frac{1}{N_p - 1} \sum_{i=1}^{N_p} (\overline{D} - D_i)^2}$$
(14)

where \overline{D} represents the average value of D_i . It should be noted that a solution with smaller values of the above two metrics has better performances about convergence and diversity.

In view of the randomness of MOEAs to optimal results [23], all the used three algorithms are independently carried out 20 times. In Table 2, the obtained best, average and worst values of two metrics are listed.

Table 2. Statistical values of two metrics for the three algorithms (GD: generational distance; SP: spacing).

Algorithm	Metrics	Best	Average	Worst
VnΕA	GD	4133.68	4515.35	4868.10
KNEA	SP	15.23	16.40	17.92
RVEA	GD	5347.71	5893.61	6286.75
	SP	40.16	65.99	69.43
NICCA III	GD	4879.06	5430.93	6250.68
N5GA-III	SP	17.37	19.67	21.35

From Table 2, we can see that the metrics GD and SP of the KnEA are better than those of the RVEA and NSGA-III. These results suggest that the KnEA has advantages over the other alternatives in the convergence and distribution performances.

Subsequently, the average calculation times of the three algorithms in 20 runs are presented in Table 3. And it is easy to judge from the average times in Table 3, comparing with RVEA and NSGA-III, the optimization speed of KnEA for solving MaOPF problem is better.

Table 3. Average times of each algorithm.

Algorithm	KnEA	RVEA	NSGA-III
Average Time (s)	88.12	93.45	90.69

From the above comparison, it is clear that KnEA is superior to RVEA and NSGA-III in optimization effects and solution efficiency in solving the MaOPF problem.

4.1.3. Result Analysis

Taking the representative Pareto-optimal solutions obtained by KnEA as an example, the solutions are divided into four groups, which corresponds to the four objective functions, through the FCM clustering, and the distribution of four groups of solutions is shown via different colors in Figure 5.



Figure 5. Distribution of Pareto-optimal solutions of KnEA after Fuzzy c-Means (FCM) clustering.

In Figure 5, each line denotes one solution in the set, and the lines with red, green, blue and yellow colors represent that decision makers prefer for f_1 , f_2 , f_3 , f_4 , respectively. When many lines cross between two adjacent objectives, it indicates that the two objectives are in a conflicting relationship. It should be noted that each Pareto-optimal solution acquired from KnEA is not the best for every objective since, for a MaOPF problem, they are only non-inferior solutions.

GRP method is used to evaluate the solutions after adopting FCM clustering, and each group belongs to one scheme. After the membership of each solution is computed, the BCSs, which have the highest membership values in each group, are listed in Table 4.

BCSs	<i>f</i> 1 (10 ⁴ \$/h)	<i>f</i> ² (p.u.)	<i>f</i> ₃ (p.u.)	<i>f</i> ₄ (10 ⁴ lb/h)	PM
Prefer for <i>f</i> ¹	2.2828	0.0174	0.0309	2.2417	0.7553
Prefer for f2	2.2831	0.0167	0.0364	2.2413	0.7423
Prefer for f ₃	2.2919	0.0173	0.0303	2.2206	0.6885
Prefer for <i>f</i> ₄	2.2926	0.0185	0.0355	2.2190	0.6848

Table 4. Best compromise solutions (BCSs) of IEEE 118-bus system.

According to the BCSs shown in Table 4, the two-step mean is capable of addressing the MaOPF problem. Not only a complete and evenly distributed set is achieved, but also the BCSs can be identified.

The BCS prefer for f_1 is an example, and comparison results of generator variables are displayed in Table 5, before and after adopting KnEA. Furtherly, the comparison of objective functions before optimization and BCS prefer for f_1 are shown in Table 6.

Comerchana	Before Optimization			After Optimization		
Generators	<i>P</i> _G (p.u.)	QG (p.u.)	U G (p.u.)	PG (p.u.)	QG (p.u.)	U G (p.u.)
G1	4.500	0	1.050	4.471	-0.856	1.019
G2	0.850	0	0.990	0.935	0.489	0.987
G3	2.200	0	1.050	2.420	1.811	1.015
G4	3.140	0	1.015	3.454	-1.897	1.004
G5	2.040	0	1.025	2.244	0.331	1.009
G6	0.480	0	0.955	0.528	0.301	0.983
<i>G</i> 7	1.550	0	0.985	1.705	0.793	1.005
G8	1.600	0	0.995	1.760	-0.310	1.002
G9	3.910	0	1.005	4.300	3.749	1.000
G10	3.920	0	1.050	4.312	-3.919	1.019
G11	5.164	0	1.035	3.690	-0.772	1.031
G12	4.770	0	1.040	4.501	0.026	1.019
G13	6.070	0	1.005	5.463	-0.154	1.015
G14	2.520	0	1.017	2.772	0.304	1.008

Table 5. Comparison results of generator variables.

Table 6. Comparison	results before and	after optimization.
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Optimization Condition	<i>f</i> 1 (10 ⁴ \$/h)	<i>f</i> ² (p.u.)	<i>f</i> ₃ (p.u.)	<i>f</i> ⁴ (10 ⁴ lb/h)
Before optimization	13.1221	0.0416	1.8729	2.9153
After optimization	2.2828	0.0174	0.0309	2.2417

From the above table, it can be seen that the variables are all in the predefined range, and the distribution of power flow becomes more reasonable through optimization, which embodies the four objective functions after optimization are superior to their corresponding values before optimization. Accordingly, it can be concluded that the presented algorithm is an efficient tool to determine the BCSs for the MaOPF problem, which helps to provide more realistic options representing decision makers' different references.

4.2. Application to the Hebei Provincial System

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The two-step mean is employed to an actual physical power system to evaluate the applicability, and the Hebei provincial power system located in China is further tested in this paper. This system contains 45 active generators, 169 substations with voltage grades 220 kV and above, and some compensation equipment [29]. In addition, the system has 17 channels which can extended to other power systems.

Given the maximum generation number $g_{max} = 150$, the optimization results via the approach are shown in Figure 6.



Figure 6. Distribute condition of solutions of the Hebei provincial system.

And then, FCM is applied for clustering the solutions, which is acquired by KnEA, into four groups, and the distributions using different colors is illustrated in Figure 7.



Figure 7. Distribute condition of Solutions of Hebei provincial system after FCM clustering.

Similar to Figure 5, the lines with different colors in Figure 7 denote different preferences of decision makers. Table 7 shows the BCSs with the maximum memberships in four groups after using GRP method.

BCSs	<i>f</i> 1 (10 ⁵ \$/h)	<i>f</i> ² (p.u.)	<i>f</i> ₃ (p.u.)	<i>f</i> ₄ (10 ⁵ lb/h)	PM
Prefer for f_1	6.8019	4.9166	7.1676	1.3378	0.8082
Prefer for f_2	11.0076	1.4871	4.2874	1.4632	0.8471
Prefer for <i>f</i> ³	7.8233	3.3164	2.5808	1.4277	0.7163
Prefer for <i>f</i> ₄	7.8030	3.0755	5.2818	1.3366	0.8213

Table 7. BCSs of the Hebei provincial power system.

For purpose of assessing the optimization effects of our approach, the result before optimization and the obtained BCS preferring to f_1 are listed in Table 8.

 Table 8. Comparison results before and after optimization.

 timization condition f_1 (10⁵ \$/b) f_2 (p.u.) f_3 (p.u.) f_4 (10⁵ 1)

Optimization condition	<i>f</i> 1 (10 ⁵ \$/h)	<i>f</i> ² (p.u.)	<i>f</i> ₃ (p.u.)	<i>f</i> ₄ (10 ⁵ lb/h)
Before optimization	16.9414	166.2188	70.7107	6.5995
After optimization	6.8019	4.9166	7.1676	1.3378

From the above table, it is clear that all the four objective functions have been improved through the proposed KnEA-based two-step MaOPF approach. Therefore, the conclusion can be drawn safely that the two-step approach is also suitable for addressing the MaOPF problems in a real-world power system.

4.3. Discussions

From the results, the MaOPF issues with more than three objective functions can be effectively solved both in the IEEE standard power systems and in the actual power systems. Meanwhile, KnEA is selected as the most effective algorithm in three MOEAs by comparing evaluation indicators of optimization performance. However, there are still some limitations of the performed work. As an important basic theory research, this work meant to solve the MaOPF issues in practical power systems. A simple OPF model is employed in this paper, and traditional constraints are used. A more practical OPF model will be explored in the future to consider real-world demands, such as dynamic security [41,59], and the reactive power and voltage magnitude [60]. Aimed at security problems in the power system, two safety-related functions are contained in the OPF model. N - 1 security constraints of power systems need also to be considered for preventive and corrective actions. What's more, more static and dynamic security functions and constraints can be added to the MaOPF model for ensuring the safe and stable operation of the power system. Moreover, the configuration of static var compensation devices is also a practical problem in planning, designing, and operation, and this issue is of great significance.

5. Conclusions

A two-step MaOPF approach using KnEA algorithm is presented in this paper. According to the analysis of the IEEE 118-bus system and a real-world power system (i.e., Hebei provincial system, China), the following conclusions are safely drawn:

- Considering the generation cost, voltage deviation, static voltage stability margin and emissions of polluting gases, a MaOPF model is proposed to better adapt the increasingly diversified operating requirements of power systems.
- (2) The proposed solution approach not only can yield multiple well-distributed set of Paretooptimal solutions, but also can further determine BCSs from each group, which represent decision-makers' different, even conflicting, preferences.
- (3) The simulation results on two test cases with varied complexity levels verify the effectiveness of the proposal. More importantly, the KnEA has significant advantages in the optimization performance, compared with the other popular algorithms, such as RVEA and NSGA-III.

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In our future research, distributed and parallel computing techniques will be employed to further improve the problem-solving efficiency of the proposed approach. Furthermore, the definition and validation of performance metrics for multi-objective evolutionary algorithms is an unsolved very important issue nowadays. The OPF with energy storage is another beneficial topic for future study [61,62].

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Abbreviations

OPF	Optimal power flow
MOPF	Multi-objective optimal power flow
MaOPF	Many-objective optimal power flow
MOEA	Multi-objective evolutionary algorithm
MaOP	Many-objective optimization problem
NSGA-III	Non-dominated sorting genetic algorithm III
KnEA	Knee point-driven evolutionary algorithm
RVEA	Reference vector guided evolutionary algorithm
BCS	Best compromise solution
FCM	Fuzzy c-means
GRP	Grey relational projection
P_{G}	Active power output of a generator
Q_{G}	Reactive power output of a generator
N_{G}	The number of generators
U	Voltage amplitude of a bus
U _{ref}	Reference voltage amplitude of a bus
Ν	The number of buses
θ	Phase-angle difference between two buses
δ	Voltage phase angle of a bus
N_{b}	The number of load buses
P_{g}	Injected active power of a load bus
Q_{g}	Injected reactive power of a load bus
P_{d}	Active loads of a load bus
Q_{d}	Reactive load sof a load bus
Т	The tap of a transformer
N_{T}	The number of adjustable transformer taps
Q_c	The switching capacity of a reactive power compensation capacitor
N _c	The number of reactive power compensation capacitors
S _L	The power flow in the branch
N_L	The number of branches
WD	The weighted distance of solutions
PM	The priority membership of solutions
GD	The generational distance
SP	The spacing

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