



# Article A Novel Continuous Roll-Forming Process of Elastomer Molds

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Abstract: This study proposed a novel continuous roll-forming process of elastomer molds, which can control the deformation of the mold using the rolling belt stack combination method. This study analyzed various rolling belt combinations, assembled the system based on simulation and experimental data according to the deformation requirement design, and obtained a controllable microstructure mold rolling belt with tensile deformation. Mold thickness and microstructure size are key microstructure mold deformation parameters. This study designed and assembled a controllable microstructure mold rolling belt-type imprint molding system and conducted a series of experiments. The impact and application of different experimental system operation procedures and fabrication methods of the auxetic structure rolling belt-type imprint replication molding were analyzed. The innovative controllable microstructure mold rolling belt and controllable microstructure mold rolling belt-type imprint replication molding technique proposed in this study had a stable and controllable mold deformation mechanism. It can control and replicate molding.

Keywords: elastomer; auxetics; UV-imprint lithography; microstructures

# 1. Introduction

The micro/nano imprint molding technique is often applied to the technological manufacturing of micro patterns or micro components [1–20]. The UV-curing step and flash imprint lithography (SFIL) technique [21–23] can be applied to a quick, low-temperature, and low-pressure manufacturing process. It can be applied to curved surfaces [24]. For UVcuring SFIL, imprint molds can be made using flexible materials to facilitate the processing of curved surfaces. However, flexible molds may occasionally have problems with microstructure distortion and deformation. As a result, there are two research directions. The first research direction is improving the microstructure distortion and deformation problem. Li et al. [24] proposed a combination of microstructural rigid light-curable film and polydimethylsiloxane (PDMS) film to prevent the deformation of microstructure patterns during imprint on curved surfaces. The second direction is applying a special processing method to deform flexible molds. Xia et al. [25] proposed applying mechanical deformation or the swelling of PDMS to change the imprint patterns of PDMS molds. However, regarding mechanical deformation, the accuracy of patterns is limited by the deformation system. Regarding swelling of PDMS, the process is complicated, and the degree of deformation is limited. Pokroy et al. [26] conducted mechanical deformation of PDMS molds with a cilia array structure and obtained a customized cilia structure with a high depth-to-width ratio. Liu et al. [27] used PDMS molds with different thicknesses to change microstructure patterns by leveraging different degrees of deformation under mechanical deformation. According to the literature review, the flexible molds' deformation control imprint technique has preliminarily matured. However, most studies focus on the step imprint technique [28–35]. This study aims to develop an innovative UV-curing rolling belt-type SFIL, where most studies focus on the step imprint technique microstructure pattern customization function. The deformation control method was designed with the mold rolling belt and auxetics to obtain a continuous and large-area SFIL with real-time pattern control.



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# 2. Design of Mold Deformation and Simulation Analysis of Auxetic Structure

# 2.1. Design of Mold Deformation System

Most studies on flexible molds with mechanical deformation controlled the degree of deformation by installing several clamps around a mold. However, clamps could not be installed around the rolling mold for the rolling belt-type imprint technique proposed in this study. This study introduced auxetics as the material for making the deformation drive rolling belt stacked with a PDMS mold rolling belt to form a controllable microstructure mold rolling belt (Figure 1). Protrusions were set on both sides for fitting with the specially designed mold rolling belt. The trusswork on both sides of the mold rolling belt was for fitting and even distribution of the tensile force of auxetics and to assist the auxetics in the deformation of the PDMS mold. The trusswork of the mold rolling belt and the PDMS material of the microstructure replication area had different properties. Specially designed elastic rings were installed at three locations to prevent warping of the upper and lower rolling belts during deformation, as shown in Figure 2.



Figure 1. Schematic diagram of the assembly of the auxetics and mold rolling belt.



Figure 2. Installation locations of elastic rings: (A) schematic diagram; (B) side view of the model.

# 2.2. Selection of Auxetics and Their Structures and Simulation Analysis of Mold Rolling Belt2.2.1. Selection of Materials and Setting of Parameters of Simulation Materials

This study used ANSYS software to analyze the transverse stress of auxetics and the mold rolling belt. It numerically designed size parameters. Regarding auxetics, a thermoplastic elastomer material was used. This material is often used for 3D printing. In the analysis, the material was set with a modulus of elasticity of 22.41477 Mpa, Poisson's ratio of 0.499, and tensile strength of 3.26885 Mpa. The material of the trusswork on both sides of the mold rolling belt was PDMS (A:B = 5:1). For analysis, the material was set as follows: modulus of elasticity 1.93171 Mpa, Poisson's ratio 0.499, and tensile strength 0.52859 Mpa. In addition, the material of the microstructure replication area in the middle of the mold rolling belt was PDMS (A:B = 20:1). For analysis, the material was set as follows: modulus of elasticity 0.38577 Mpa, Poisson's ratio 0.499, and tensile strength: 0.10743 Mpa. The longitudinal stress of the auxetics and mold rolling belt was set to 0.05–0.1. The transverse stress of the two was limited to simulate the condition of the rolling belt at Poisson's ratio = 0 or -1, i.e., to simulate the movement of the actual microstructure mold under uniaxial tensile deformation or uniform expansion deformation.

#### 2.2.2. Design and Selection of Auxetic Structure

Regarding auxetic structure, this study proposed a Y-shaped rigid rotational auxetic structure. The limit of Poisson's ratio of the Y-shaped rigid rotational auxetic structure cannot be less than -1. Therefore, this study analyzed the transverse stress at Poisson's ratio = 0. For this structure, the design of Poisson's ratio was affected by the fracture length (*l*)–distance between unit structures ( $L_0$ ) ratio ( $l/L_0$ ). The larger the ratio, the smaller the Poisson's ratio, as shown in Figure 3. This study adopted four designs ( $l/L_0 = 0.5, 0.6, 0.7,$  and 0.8) for the Y-shaped rigid rotational auxetic structure.



Figure 3. Design parameters of the Y-shaped rigid rotational auxetic structure.

2.2.3. Simulation Analysis of the Auxetic Structure and Mechanical Property Testing

In this study, for the Y-shaped rigid rotational auxetic structure and mechanical property testing, during Instron instrument tensile testing (ISO-527 typs standard), we obtained the detailed mechanical properties data of the Y-shaped rigid rotational auxetic structure, as shown in Figure 4.



Figure 4. Mechanical property testing of Y-shaped rigid rotational auxetic structure.

Based on the analysis, the Y-shaped rigid rotational auxetic structure was under the maximum transverse expansion stress (40.7–77.7 kPa) and had an excessive longitudinal tensile stress requirement (100.2–200.5 kPa) at  $l/L_0 = 0.6$ . In such a case, the machine would be too stressed to stretch the rolling belt. At  $l/L_0 = 0.8$ , the transverse expansion stress (18.8–38.9 kPa) was smaller than the design parameter. However, the longitudinal tensile

stress requirement (7.1–26.3 kPa) significantly decreased, as shown in Figure 5. Regarding the Y-shaped rigid rotational auxetic structure, the testing and simulation results with relation to vertical and horizontal tension stress and tension strain are shown in Figure 6. The transverse expansion force can be changed by the thickness of the auxetic structure. Therefore, it can be concluded from the above experiment that the auxetic structure design with a smaller Poisson's ratio would obtain the same transverse expansion force under a smaller longitudinal tensile force.



**Figure 5.** Deformation analysis of Y-shaped rigid rotational auxetic structure with different design parameters at the longitudinal strain of 0.05–0.1 and the Poisson's ratio of 0: (**A**) change in transverse stress and (**B**) change in longitudinal stress.



**Figure 6.** Testing and simulation result with relation to vertical and horizontal tension stress and tension strain: (**A**) change in horizontal stress and (**B**) change in vertical stress.

#### 3. Experimental Methods

#### 3.1. Design and Development of Imprint System Machine

3.1.1. Design, Simulation, and Selection of Mold Rolling Belt Trusswork

This study proposed two trusswork designs and observed the change in the transverse contraction stress of the mold rolling belt trusswork through four trusswork angles, as shown in Figures 7 and 8. The design shown in Figure 7 was for observing the effect of trusswork angle on transverse contraction stress. The design shown in Figure 8 was for observing the effect of the trusswork aspect ratio on transverse contraction stress. The four trusswork angles are 73.74°, 106.26°, 122.63°, and 132.84°. Based on the analysis, the smaller the trusswork angle, the greater the transverse contraction stress, as shown in Figure 9. The length–thickness ratio of the trusswork support will significantly affect the transverse contraction stress (Figure 10). The trusswork angle of 73.74° provided the best result. The support length-thickness ratio design can be used to control the transverse contraction stress of the trusswork. Table 1 lists the transverse contraction stress data at various trusswork support aspect ratios designed for the Y-shaped rigid rotational auxetic structure. This study analyzed the microstructure replication area in the middle of the mold rolling belt. It prepared the transverse contraction stress simulation data table and the simulation data trendline table (Table 2). Furthermore, the parameter design combination of the auxetics, the mold rolling belt trusswork, and the microstructure replication area was identified through the transverse force value. By doing so, the microstructure mold used in the actual machine can have uniaxial tensile deformation or uniform expansion deformation movement.



**Figure 7.** Four design angles set for analyzing the effect of trusswork angle on transverse contraction stress: **(A)** 73.74°; **(B)** 106.26°; **(C)** 122.63°; **(D)** 132.84°.



**Figure 8.** Four design angles set for analyzing the effect of trusswork support aspect ratio on transverse contraction stress: (**A**) 73.74°; (**B**) 106.26°; (**C**) 122.63°; (**D**) 132.84°.



Figure 9. Effect of trusswork angle on transverse contraction stress.



Figure 10. Effect of trusswork support aspect ratio on transverse contraction stress.

Width (mm)	Horizontal Shrinkage Stress (Vertical Tensile Strain = 0.05) (kPa)	Horizontal Shrinkage Stress (Vertical Tensile Strain = 0.1) (kPa)	Data Trend Line
1.4	10.643	21.286	$Y = 212.86 \times X$
1.5	11.372	22.744	$Y = 227.44 \times X$
1.6	11.945	23.889	$Y = 238.9 \times X$
1.7	12.658	25.316	$Y = 253.16 \times X$
1.8	13.185	26.37	$Y = 263.7 \times X$
1.9	13.484	26.967	$Y = 269.67 \times X$
2	14.195	28.39	$Y = 283.9 \times X$
2.1	14.649	29.298	$Y = 292.98 \times X$
2.2	15.106	30.212	$Y = 302.12 \times X$
2.3	15.537	31.074	$Y = 310.74 \times X$
2.4	15.755	31.51	$Y = 315.1 \times X$
2.5	16.21	32.42	$Y = 324.2 \times X$
2.6	16.254	32.507	$Y = 325.07 \times X$
2.7	16.723	33.446	$Y = 334.46 \times X$
2.8	17.288	34.576	$Y = 345.76 \times X$
2.9	17.739	35.477	$Y = 354.77 \times X$
3	17.878	35.755	$Y = 357.55 \times X$

 Table 1. Transverse contraction stress data at various trusswork support widths.

	Vertical Tensile Strain						
Poisson's Ratio		0.05	0.06	0.07	0.08	0.09	0.1
0		12.859	15.43	18.002	20.574	23.145	25.717
-0.2		18.002	21.603	25.203	28.803	32.404	36.004
-0.4		23.146	27.775	32.404	37.033	41.662	46.291
-0.6		28.289	33.947	39.605	45.263	50.92	56.578
-0.8		33.433	40.119	46.806	53.492	60.179	66.865
-1		38.576	46.291	54.007	61.722	69.437	77.152

**Table 2.** Transverse contraction stress simulation data of the PDMS mold microstructure transfer print area (unit: kPa).

# 3.1.2. Design, Erection, and Actuating Program of System Machine

In terms of the design and erection of the machine proposed in this study, the controllable microstructure mold rolling belt was wound around two upper fixed rollers and one tensile control roller. The tensile control roller moves up and down through the screws on both sides to control the tensile force of the microstructure mold rolling belt. The auxetic structure rolling belt trusswork and the flexible mold rolling belt trusswork cause a transverse expansion movement on the microstructure transfer print area in the middle of the flexible mold rolling belt. In addition, the lower transparent PE film was used as the conveyor rolling belt. The UV light shined onto the imprint area from the bottom. The source of imprint pressure was the upward movement of two lower rollers through the pneumatic cylinder. In addition, a coating bar was fixed at the entrance of the imprint coil stock of the machine to preliminarily scrape excessive photoresist to facilitate subsequent imprint actions, as shown in Figure 11. Figure 12 shows the rolling uniformity testing of pressure-sensitive film (FUJIFILM's Ultra Low Pressure, 0.2~0.6 MPa).



Figure 11. (A) Machine roll imprint process; (B) actual machine photo.





Figure 12. Rolling uniformity testing of pressure-sensitive film.

#### 3.2. Microstructure Size and Selection of Photoresist

Perforated array aluminum sheets were fabricated by a laser to make the machine replicate convex array structures (diameter:  $200 \ \mu m$ ,  $250 \ \mu m$ ,  $300 \ \mu m$ , and  $400 \ \mu m$ ). PC plastic sheets were hot imprinted. Thin PC sheets that were transfer printed into convex array structures were used to fabricate PDMS rolling belts with a concave array structure through the mold filling of PDMS. Convex array structures of corresponding sizes were obtained through the UV-curing imprint process of the PDMS rolling belts with a concave array structure. In addition, the photoresist used in the UV-curing imprint process was SU8 UV-curing photoresist with an excellent pattern transfer print rate, moisture resistance, and acid and alkali resistance.

#### 3.3. Imprint Replication Molding Procedure

The replication molding procedure in this study was as follows. (1) The controllable microstructure mold rolling belts were stretched to the preset length during the idling operation. (2) After stretching the rolling belts to the preset length, the idling operation was continued to enable the uniform deformation of the controllable microstructure mold rolling belts. (3) The UV-curing imprint process was implemented. (4) The imprint result was obtained.

#### 4. Results and Discussion

4.1. Simulation Analysis and Discussion on Microstructure Replication Molding

This part used a hemispherical concave structure array for simulation analysis. The longitudinal tensile stress was set to 0.05 and 0.1 for uniaxial tensile and uniform expansion deformation, respectively. The material was set as the same as the material of the microstructure replication area of the PDMS rolling belt. The modulus of elasticity, Poisson's ratio, and tensile strength were 0.38577 Mpa, 0.499, and 0.10743 Mpa, respectively.

4.1.1. Effect of the Thickness of the PDMS Rolling Belt on the Deformation Degree of the Microstructure

A hemispherical concave structure with a diameter of 100  $\mu$ m was used for simulation analysis on PDMS rolling belts with thicknesses of 1 mm, 2 mm, and 3 mm. Based on simulations under both uniaxial tensile deformation and uniform expansion deformation, the thickness of the PDMS rolling belt had no impact on the deformation degree of the microstructure. The transverse force between the auxetic structure rolling belt and the PDMS mold rolling belt could be controlled through the thickness without changing the degree of deformation on the microstructure (Tables 3 and 4).

**Table 3.** Deformation analysis result of a concave microstructure array mold with a diameter of  $100 \mu m$  at the longitudinal stress of 0.1 and the Poisson's ratio of 0.

Thickness	1 mm	2 mm	3 mm
Vertical strain of shape	0.228	0.23	0.228
Horizontal strain of shape	0.0418	0.0421	0.0423
Depth strain of shape	-0.10598	-0.1062	-0.1062
Vertical strain of position spacing	0.1004	0.1006	0.1008
Horizontal strain of position spacing	0	0	0

**Table 4.** Deformation analysis result of a concave microstructure array mold with a diameter of 100  $\mu$ m at the longitudinal stress of 0.1 and the Poisson's ratio of -1.

Thickness	1 mm	2 mm	3 mm
Vertical strain of shape	0.272	0.276	0.273
Horizontal strain of shape	0.26856	0.2687	0.27043
Depth strain of shape	-0.174	-0.1706	-0.1702
Vertical strain of position spacing	0.1002	0.1006	0.1014
Horizontal strain of position spacing	0.098486	0.10053	0.1007

#### 4.1.2. Effect of Microstructure Size on the Deformation Degree

Uniaxial tensile deformation and uniform expansion deformation were implemented with/at diameters of 100  $\mu$ m, 150  $\mu$ m, 200  $\mu$ m, 250  $\mu$ m, 300  $\mu$ m, and 400  $\mu$ m and longitudinal tensile stresses of 0.05 and 0.1. A smaller size of the hemispherical concave structure would lead to a higher degree of pattern deformation (Tables 5–8). To change the pattern of a concave microstructure of a minimum size, only a moderate degree of tensile deformation of the PDMS mold rolling belt carried by the structure was required. In addition, the degree of pattern deformation of the microstructure and the degree of expansion between locations were different.

**Table 5.** Simulation result of different microstructure sizes at the longitudinal stress of 0.05 and the Poisson's ratio of 0.

Microstructure Diameter	100 µm	150 μm	200 µm	250 μm	300 µm	400 μm
Vertical strain of shape	0.114	0.11067	0.109	0.1028	0.0933	0.07125
Horizontal strain of shape	0.021175	0.019645	0.020104	0.021265	0.01594	0.0098
Depth strain of shape	-0.053	-0.05173	-0.0508	-0.04456	-0.0476	-0.04695
Vertical strain of position spacing	0.05	0.0506	0.0506	0.0506	0.0512	0.0546
Horizontal strain of position spacing	0	0	0	0	0	0

Microstructure Diameter	100 µm	150 µm	200 µm	250 µm	300 µm	400 um
Vertical strain of shape	0.23	0.2233	0.2175	0.2052	0.188	0.1/175
Horizontal strain of shape	0.042182	0.041306	0.03507	0.036203	0.0305	0.018192
Depth strain of shape	-0.1062	-0.105867	-0.1029	-0.1	-0.0977	-0.09205
Vertical strain of position spacing	0.1006	0.1002	0.1014	0.1034	0.1024	0.1088
Horizontal strain of position spacing	0	0	0	0	0	0

**Table 6.** Simulation result of different microstructure sizes at the longitudinal stress of 0.1 and the Poisson's ratio of 0.

**Table 7.** Simulation result of different microstructure sizes at the longitudinal stress of 0.05 and the Poisson's ratio of -1.

Microstructure Diameter	100 µm	150 μm	200 µm	250 µm	300 µm	400 µm
Vertical strain of shape Horizontal strain of shape	0.136 0.134278	0.133 0.13015	0.131 0.12854	0.126 0.120692	0.1107 0.11016	0.0825 0.078815
Depth strain of shape	-0.08694	-0.08493	-0.08262	-0.082344	-0.07728	-0.074935
Vertical strain of position spacing	0.05	0.0508	0.05	0.0516	0.0518	0.0556
Horizontal strain of position spacing	0.0492	0.0507	0.0512	0.0517	0.0531	0.0566

**Table 8.** Simulation result of different microstructure sizes at the longitudinal stress of 0.1 and the Poisson's ratio of -1.

Microstructure Diameter	100 µm	150 μm	200 µm	250 µm	300 µm	400 µm
Vertical strain of shape	0.272	0.2673	0.2615	0.2524	0.2217	0.16475
Horizontal strain of shape	0.26856	0.2603	0.2571	0.24138	0.2203	0.15763
Depth strain of shape	-0.174	-0.17	-0.1652	-0.16472	-0.15457	-0.14985
Vertical strain of position spacing	0.1002	0.1014	0.1002	0.1032	0.1034	0.1112
Horizontal strain of position spacing	0.0985	0.10146	0.10252	0.1034	0.1064	0.1133

#### 4.2. Discussion on the Study of Replication Molding

In this study, a concave microstructure with a diameter of 300  $\mu$ m was processed through the UV-curing rolling belt-type imprint molding technique. During the process, the auxetic structure rolling belt parameters were designed with  $l/L_0$  being 0.8 and thickness being 2 mm.

4.2.1. Y-Shaped Rigid Rotational Auxetic Structure—Effect of Truss Structure Thickness and PDMS Mold Rolling Belt Thickness

The parameters of truss structure and the PDMS mold rolling belt were designed with a thickness of 0.5 mm. The PDMS mold rolling belt trusswork parameters were designed at an angle of  $73.74^{\circ}$  and support thickness of 5 mm. Table 9 shows the experimental results.

The average replication rates (truss structure thickness 0.5 mm and PDMS mold rolling belt thickness 0.5 mm) are 91.67% (diameter = 200  $\mu$ m), 95.83% (diameter = 300  $\mu$ m), and 95.33% (diameter = 400  $\mu$ m).

The parameters of truss structure and the PDMS mold rolling belt were designed with a thickness of 1.5 mm. The PDMS mold rolling belt trusswork parameters were designed at an angle of  $73.74^{\circ}$  and support thickness of 5 mm. Table 10 shows the experimental results.

The average replication rates (truss structure thickness 1.5 mm and PDMS mold rolling belt thickness 1.5 mm) are 96% (diameter = 200  $\mu$ m) and 90.67% (diameter = 400  $\mu$ m). Furthermore, the PDMS mold rolling belt trusswork parameters were designed at an angle of 73.74° and support thickness of 5 mm. A longitudinal stress of 0.05 was exerted on the entire controllable microstructure mold rolling belt. If the imprint result showed a longitudinal stress of 0.05 and a transverse stress of 0, resulting from uniaxial tensile deformation, this paper suggests that the causes of this result are as follows. On the one hand, elastic rings limit the transverse deformation during the deformation. This can be addressed by improving the machine operation process. On the other hand, the

Uni-microstructural height (µm)

Replication rate (%)

Longitudinal period distance of microstructure (µm)

Lateral period distance of microstructure (µm)

mechanical properties of the auxetic structure rolling belt differed slightly from the data in the simulation analysis. In this experiment, the auxetic structure rolling belt was 3D printed, and the wire rod stack method would affect the physical properties of a 3D-printed object. As a result, the mechanical properties differed slightly from the simulation.

Longitudinal Tensile Strain 0.05 0.07 0.09 0.06 0.08 0.1 Microstructure Diameter (µm) 200 250 260 255.7 270.4264.5 276.5 Uni-microstructural longitudinal length (µm) 300 308.3 311.4 313.4 320.1 331.8 349.8 400 477.5 474.1 489.5 465.4 462.8 481 200 225.6 237.3 240.5 240.3 234.5 231.2 300 325.6 322.5 310.8 Uni-microstructural lateral length (µm) 312.6 333 324.4400 435 438.7 447 437.7 421.6 422.6

23

39

35

511.5

510.6

526

495.5

507.6

501.5

87 92

93

200

300

400

200

300

400

200

300

400

200

300

400

**Table 9.** Effect of truss structure thickness 0.5 mm and PDMS mold rolling belt thickness 0.5 mm of replication molding and replication rate.

23

40

35

516.6

515.4

529.8

501.5

511.7

510.7

89

96

94

23

40

35

528.8

514

529.1

504.5

514

507.8

90 97

96

23

39

35

529.4

523.7

535.8

504.8

520.7

510.7

91

96 97 24

39

34

532.3

538

548

503

510.6

513.6

96 97

94

24

39

35

547.2

538

563

505.6

514.2

504.6

97

97

98

**Table 10.** Effect of truss structure thickness 1.5 mm and PDMS mold rolling belt thickness 1.5 mm of replication molding and replication rate.

Longitudinal Tensile Strain					
Microstructure	Diameter (µm)	0.01	0.02	0.03	
Uni-microstructural longitudinal length (µm)	200	240.2	258.4	243.2	
	400	423.4	423.2	417.1	
Uni-microstructural lateral length (µm)	200 400	238.9 398.8	$240.5 \\ 405.4$	229.2 401.5	
Uni-microstructural height (µm)	200	14	14	14	
	400	9	9	9	
Longitudinal period distance of microstructure (µm)	200	514.2	520	517.6	
	400	511.1	515.4	518.9	
Lateral period distance of microstructure (µm)	200 400	501 483.3	$\begin{array}{c} 498.4\\ 468.8\end{array}$	496.5 485.4	
Replication rate (%)	200	95	96	97	
	400	90	90	92	

#### 4.2.2. Effect of Poisson's Ration

Figure 13 shows the Poisson's ratio distributions of different truss structure thicknesses and PDMS mold rolling belt thicknesses. The innovative controllable microstructure mold rolling belt-type imprint replication molding technique proposed in this study had a stable and controllable mold deformation mechanism. It can control and replicate molding.



**Figure 13.** Poisson's ratio distributions of different truss structure thicknesses and PDMS mold rolling belt thicknesses: (**A**) PDMS mold rolling belt was designed with a thickness of 0.5 mm and (**B**) PDMS mold rolling belt was designed with a thickness of 1.5 mm.

#### 5. Conclusions

The novel continuous roll-forming process of elastomer molds proposed in this study utilized the rolling belt stack combination method. This study used different rolling belt combinations for analysis. It designed and assembled a controllable microstructure mold rolling belt with tensile deformation as the microstructure deformation control method. Based on the analysis, the thickness of the microstructure carrier in the rolling belt deformation had no impact on the deformation movement of the microstructure; the Y-shaped rigid rotational auxetic structure was under the maximum transverse expansion stress (40.7~77.7 kPa) and had an excessive longitudinal tensile stress requirement  $(100.2 \sim 200.5 \text{ kPa})$  at  $l/L_0 = 0.6$ . The four trusswork angles are  $73.74^\circ$ ,  $106.26^\circ$ ,  $122.63^\circ$ , and 132.84°. Based on the analysis, the smaller the trusswork angle, the greater the transverse contraction stress. In this study, uniaxial tensile deformation and uniform expansion deformation were implemented with/at diameters of 100 µm, 150 µm, 200 µm, 250 µm, 300 µm, and 400  $\mu$ m, and the microstructure size affected the degree of pattern deformation of the microstructure. A smaller size would lead to a higher degree of deformation. The pattern control of the microstructure would be affected by the stress of macro deformation and the microstructure size. Therefore, the location and pattern controls of the microstructure needed to be further checked to achieve a stable imprint. In this study, for a Y-shaped rigid rotational auxetic structure (the auxetic structure rolling belt parameters were designed with  $l/L_0$  being 0.8 and thickness being 2 mm), the parameters of truss structure and the PDMS mold rolling belt were designed with a thickness of 0.5 mm and 1.5 mm, and the PDMS mold rolling belt trusswork parameters were designed at an angle of 73.74° and support thickness of 5 mm. The average replication rates were 91.67% (diameter =  $200 \mu$ m), 95.83% (diameter = 300  $\mu$ m), 95.33% (diameter = 400  $\mu$ m), 91.67% (diameter = 200  $\mu$ m), 95.83% (diameter = 300  $\mu$ m), and 95.33% (diameter = 400  $\mu$ m). This study proposed a novel continuous roll-forming process of elastomer molds, which can control the deformation of the mold using the rolling belt stack combination method. The molding technique proposed in this study had a stable and controllable mold deformation mechanism. It could control and replicate molding through the precise control of the machine operation process and the fabrication of the auxetic structure rolling belt.

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