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Leakage Model of Tubing and Casing Premium Connection Based on Sinusoidal Contact Simulation between Rough Surfaces

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Abstract: This paper proposed a semi-theoretical model to quantitatively predict leakage rate of tubing and casing premium connections. The geometric parameters of the sealing surface profile approximated by a sinusoidal micro-convex surface were first obtained based on the random normal distribution sampling method. With the actual area prediction formula for elastic–plastic contact of an axisymmetric sinusoidal micro-convex body based on the equivalent simulation principle, the circumferential leakage width and radial average leakage height of the micro-leakage channel between sealing surfaces were then acquired with the surface roughness and geometric mean contact pressure. At last, the actual micro-leakage rate of the premium connection was derived by considering the non-uniform contact pressure distribution between sealing surfaces. An example was investigated to validate the model and reveal the sealing and leakage characteristics, and anti-leakage measures were proposed. The results show that average contact pressure, circumferential leakage width, and radial average leakage height between sealing surfaces were non-uniformly distributed. The leakage rate of a premium connection decreases exponentially with an increase in radial interference between sealing surfaces. In order to reduce leakage rate, it is beneficial to increase radial interference and lower sealing surface roughness.



Citation: Xu, H.; Zhang, Z.; Xiang, S.; Yang, B.; Shi, T. Leakage Model of Tubing and Casing Premium Connection Based on Sinusoidal Contact Simulation between Rough Surfaces. *Processes* **2023**, *11*, 570. <https://doi.org/10.3390/pr11020570>

Academic Editor: Jose Carlos Pinto

Received: 10 January 2023

Revised: 4 February 2023

Accepted: 7 February 2023

Published: 13 February 2023



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Keywords: tubing and casing; premium connection; sealing performance; leakage rate; roughness; sinusoidal contact simulation

1. Introduction

Premium tubing and casing connections, which use special metal-to-metal sealing structures to achieve excellent gas sealing performances, have become one of the key technologies for maintaining wellbore integrity in deep high-temperature and high-pressure (HTHP) gas wells, thermal recovery wells, and gas wells in deep water environments [1–3]. The sealing structures for premium connections mainly include cone-to-cone, ball-to-cone, ball-to-cylinder, and ball-to-ball seals. The cone-to-cone seal is a static coordinated contact seal and the other three are static spherical non-coordinated contact seals. However, due to the influence of roughness on sealing surface, no matter what kind of sealing structure is used, premium connections cannot achieve zero leakage at present. Therefore, determining how to reliably evaluate gas sealing performances of premium connections is very important to ensure integrity of strings in gas wells.

In the API 5C3 and ISO10400 standards, the internal pressure leakage resistance formula of tubing and casing strings connected with API thread is derived based on the critical condition that the elastic contact pressure at the E_1 plane of a round thread and the E_7 plane of a buttress thread, respectively, generated by radial interference of the thread and internal pressure excitation, are equal to the internal pressure in the strings [4,5].

However, this formula is not suitable for sealing performance evaluation of non-coordinated contact seal structures. Gao et al. [6] analyzed gas leakage resistance for rough contact between metal and metal sealing surfaces and proposed a method for improving sealing performance by increasing sealing contact pressure and sealing length as much as possible. Based on experimental testing, Murtagian et al. [7] established a gas sealing criterion of metal-to-metal seals that used the integral of sealing contact pressure multiplied by sealing length to represent gas sealing capacity. Xie et al. [8] also proposed a similar evaluation standard for premium connections in thermal recovery wells.

Based on these evaluation criteria, contact pressure distribution on sealing surfaces has mainly been obtained by the finite element method (FEM) to evaluate sealability of premium connections. Wang [9] and Chen [10] both adopted the FEM to evaluate sealability of cone-to-cone-type and arc-to-cone-type premium connections under complex loads, including make-up torque, tension, bending, and internal pressure loads. Dou et al. [11,12] carried out sealing ability simulation for premium connections based on ISO 13679 CAL IV tests with FEM; the investigations also consider the effects of cyclic load on sealability of premium connections. Kim et al. analyzed the effects of stabbing flank angle and upper stabbing flank corner radius on von Mises stress of premium connections and presented the design criteria [13]. Zhang et al. adopted the viscoelastic finite element model to predict relaxation of contact pressure on premium connections' sealing surface versus time under different temperatures [14]. Yu et al. analyzed the effect of energy dissipation on premium connection sealing surface with the microslip shear layer model [15]. Moreover, some theoretical and testing methods have also been proposed. Xu et al. [16,17] studied theoretically elastic contact pressure on sealing surface of ball-to-cone-type and cone-to-cone-type premium connections and their sealing performances. Yang et al. [18] also proposed a theoretical model to calculate elastic–plastic contact pressure distribution on sealing interfaces for sphere-type premium connections based on make-up torque and adopted gas sealing criterion obtained from Murtagian's experimental results for deducing gas sealing capacity. Hamilton et al. [19] used ultrasonic technology to accurately detect the contact stress on the sealing surface to evaluate the sealability of premium connections in downhole strings.

In fact, the gas sealing test is the most direct and effective method to evaluate the sealing performance of a premium connection, but it is often used for validation because of economic and time cost limitations. According to ISO13679, detection sensitivity of leakage rate under internal pressure action for premium connections is $0.9 \text{ cm}^3/15 \text{ min}$ based on the bubble method and $1 \times 10^{-4} \text{ cm}^3/\text{min}$ based on helium mass spectrometer measurements [20]. Thus, in order to quantitatively evaluate the sealing performance of a premium connection, the leakage rate prediction model is urgently needed based on microscopic contact mechanics between sealing surfaces [21,22]. Xu et al. [23] first applied the microscopic contact mechanism to leakage rate prediction of a premium connection. Their purely theoretical method with assumption of a conical micro-convex body has difficulty accurately modeling the elastic–plastic contact state between sealing surfaces. Thus, the prediction accuracy needs to be further improved. In recent years, scholars have proposed that a sinusoidal micro-convex contact model can better simulate the contact problem on rough surfaces dominated by plastic deformation under heavy loads [24,25]. Further, most existing multiscale rough surface contact models consider multiscale properties of surface roughness by using Fourier series or Weierstrass–Mandelbrot profile functions to convert rough surfaces into a sum of sine or cosine functions [26,27]. Therefore, it should be more reasonable to simulate the elastic–plastic microscopic contact problem for a premium connection with sinusoidal convex body assumptions.

In this study, the surface profile curve of the preset surface roughness was obtained based on random normal distribution sampling, and the simulated geometric parameters of the surface profile approximated by the sinusoidal micro-convex surface were first statistically obtained. With the actual area prediction formula for elastic–plastic contact of axisymmetric sinusoidal micro-convex bodies based on the equivalent simulation

principle [28], the circumferential leakage width and radial average leakage height of the micro-leakage channel between sealing surfaces were then acquired with the surface roughness and geometric mean contact pressure. By dividing the sealing structure into a series of sealing contact units along the axial direction and using the boundary conditions of the fluid leakage pressure and the continuity conditions of the leakage rate of each unit, an actual micro-leakage rate prediction model of a premium connection considering a non-uniform distribution of contact pressure on a sealing surface was finally derived. With the proposed model, an example of a cone-to-cone-type premium connection was investigated to validate the model and reveal the sealing and leakage characteristics of a connection, and anti-leakage measures were proposed. The proposed model provides a fast and quantitative sealability evaluation method for premium connections, which is of great importance for sealing parameters optimization and sealing performance improvement.

2. Model Development

2.1. Seal Structure and Micro-Leakage Channel for Premium Connections

Unlike API standard tubing and casing connections, premium connections achieve excellent gas sealing performance by using a special radial metal-to-metal seal structure and torque shoulder to control make-up torque and assist sealing. The common seal structures of premium connections include cone-to-cone, ball-to-cone, ball-to-cylinder, and ball-to-ball seals. Under the influence of mechanical processing, regardless of which type of sealing structure is adopted, the sealing surface of a premium connection is always unsmooth, and there are always microscopic leakage channels between the sealing surfaces after make-up torque application, as shown in Figure 1. Therefore, accurately modeling the elastic–plastic contact mechanical behavior of the micro-convex body between sealing surfaces and obtaining the micro-leakage channel area between sealing surfaces are the bases for establishing a micro-leakage model for premium connections.

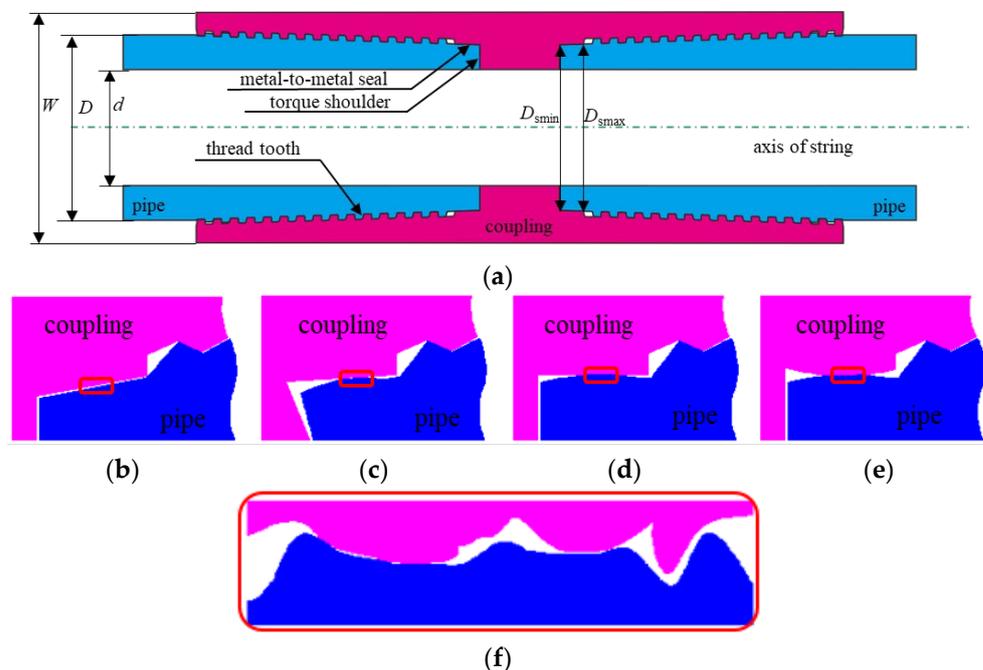


Figure 1. Seal structures and micro-leakage channels for tubing and casing premium connections. (a) Schematic diagram of premium connection; (b) cone-to-cone; (c) ball-to-cone; (d) ball-to-cylinder; (e) ball-to-ball; (f) schematic diagram of micro-leakage channel of sealing surface.

2.2. Micro-Leakage Model for Tubing and Casing Premium Connection

2.2.1. Profile Curve Model of Sealing Surface

Under the assumption that the actual profile height distribution curve of a rough surface follows a Gaussian distribution, Monte Carlo random normal distribution sampling

was used to obtain the height sample sequences of the profile curve with equal spacing on rough surfaces $Z_1, Z_2, \dots, Z_i, \dots, Z_N$ [23]:

$$Z_i = \mu + \sigma(-2 \ln c_1)^{0.5} \sin 2\pi c_2 \quad (1)$$

The Monte Carlo random sampling method was used to simulate the sealing surface's profile. The values of μ and σ of the random sampling for different machining accuracies of the sealing surface and corresponding roughness R_a were determined based on the principle of $\pm 3\sigma$ by corresponding the maximum peak-to-valley distance R_y to the approximate limit range of a Gaussian distribution, as shown in Table 1.

Table 1. Monte Carlo random normal distribution sampling parameters for sealing surface's profile height.

| Grade of Machining Accuracy | $R_a/\mu\text{m}$ | $R_y/\mu\text{m}$ | $\mu/\mu\text{m}$ | $\sigma/\mu\text{m}$ |
|-----------------------------|-------------------|-------------------|-------------------|----------------------|
| 7 | 1.6 | 3.2 | 1.6 | 0.533333 |
| 8 | 0.8 | 1.6 | 0.8 | 0.266667 |
| 9 | 0.4 | 0.8 | 0.4 | 0.133333 |
| 10 | 0.2 | 0.4 | 0.2 | 0.066667 |
| 11 | 0.1 | 0.2 | 0.1 | 0.033333 |

In order to ensure that the simulated sample values of the sealing surface's profile height conformed to the preset surface roughness as closely as possible, the mean error ε_μ and maximum peak-to-valley distance error ε_y for the sealing surface's profile height samples were selected as the test standards, and the relative errors of μ and σ were controlled to be less than 1% by repeated sampling. ε_μ and ε_y are defined as follows:

$$\varepsilon_\mu = \frac{1}{R_a} \left| 1/N \sum_{i=1}^N Z_i - R_a \right|, \quad (2)$$

$$\varepsilon_y = \frac{1}{R_y} |(Z_{i,\max} - Z_{i,\min}) - R_y|, \quad (3)$$

Based on the industry standards [29], the sampling length was selected to be 0.8 mm, the evaluation length was selected to be 1.6 mm, the sampling spacing I was selected to be 0.2, 0.4, 0.6, 0.8, and 1.0 μm , and the corresponding sample number N were 8000, 4000, 2667, 2000, and 1600, respectively. The relative errors ε_μ and ε_y were both less than 1% when the sample number was 1600–8000 for sampling profile height Z_i . Figure 2 shows the profile curve of the rough surface based on Monte Carlo random normal distribution sampling when $R_a = 0.1 \mu\text{m}$ and sample number was 1600 (sampling spacing $I = 1.0 \mu\text{m}$).

2.2.2. Parameter Calculation of Simulated Sine Wave Surface

Whether a two-dimensional, axisymmetric, or three-dimensional sine wave surface is used to generate the profile curve of a real rough surface, the key is to determine the wavelength and amplitude of the wave surface. After local magnification of the simulated profile curve of the rough surface in Figure 2, it was found that the profile curve of the rough surface contained many peaks and valleys, and the horizontal distance between adjacent peaks or valleys and the vertical distance between adjacent peaks or valleys all changed randomly, shown in Figure 3.

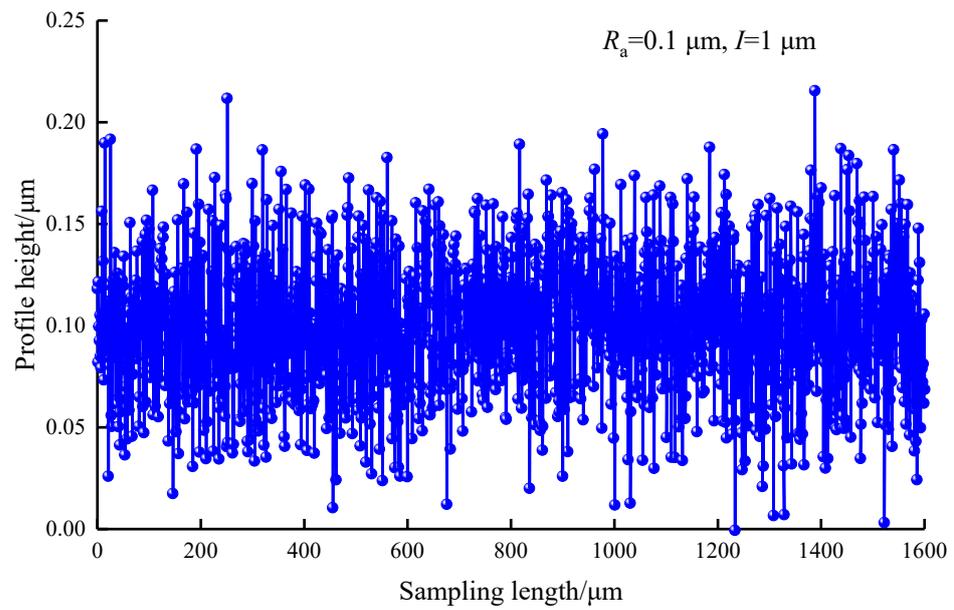


Figure 2. Simulated profile curve of rough surface based on Monte Carlo random normal distribution sampling.

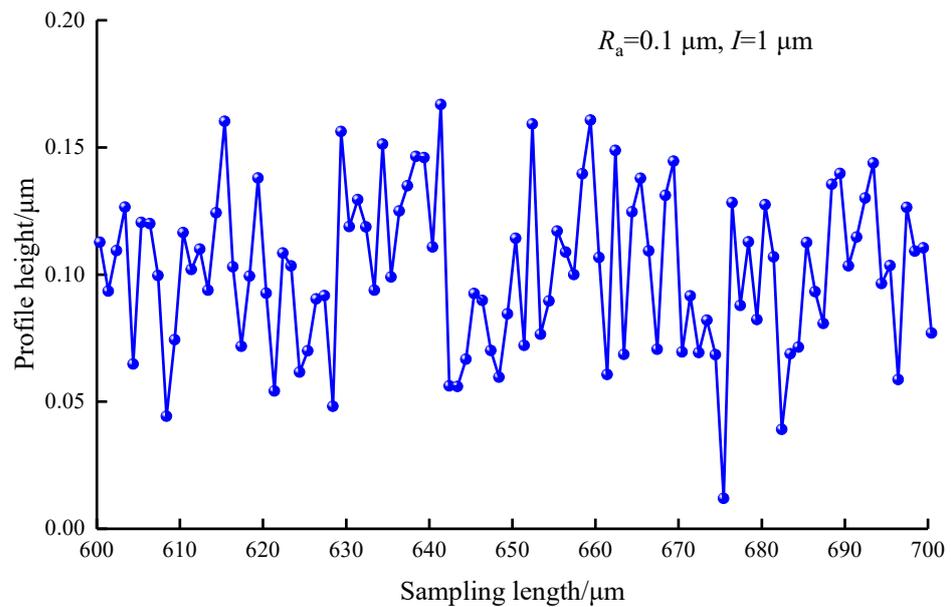


Figure 3. Local magnification of simulated profile curve of rough surface.

In order to obtain fitting parameters of the sinusoidal profile curves, the coordinates of the wave peaks and valleys were first calculated based on the coordinate sequence (x_i, Z_i) of the profile height. When $i = 2, 3, \dots, N - 1$, if $Z_i - Z_{i-1} > 0$ and $Z_i - Z_{i+1} > 0$, then the corresponding coordinate sequence (x_i, Z_i) of the profile height is the peak point. If $Z_i - Z_{i-1} < 0$ and $Z_i - Z_{i+1} < 0$, then the corresponding coordinate sequence (x_i, Z_i) of the profile height is the valley point. Thus, the coordinate sequences of peak points (x_{Pj}, Z_{Pj}) and valley points (x_{Tk}, Z_{Tk}) were both obtained, where $j = 1, 2, \dots, N_P, k = 1, 2, \dots, N_T$.

Then, the horizontal and vertical distances between adjacent peaks or valleys were calculated based on the coordinate sequences of the peaks and valleys:

$$\lambda_{Pj} = x_{P(j+1)} - x_{Pj} \quad (j = 1, 2, \dots, N_P - 1), \quad (4)$$

$$\lambda_{Tk} = x_{T(k+1)} - x_{Tk} \quad (k = 1, 2, \dots, N_T - 1), \quad (5)$$

$$h_j = Z_{Pj} - Z_{Tj} \quad (j = 1, 2, \dots, N_P), \tag{6}$$

Finally, because λ_{Pj} , λ_{Tk} , and h_j were all randomly distributed, their average values were used to calculate the wavelength and amplitude of the profile curve of the fitted sinusoidal curve, respectively, as follows:

$$\lambda = \frac{1}{2}(\overline{\lambda_P} + \overline{\lambda_T}) = \frac{1}{2} \left(\frac{1}{N_P - 1} \sum_{j=1}^{N_P-1} \lambda_{Pj} + \frac{1}{N_T - 1} \sum_{k=1}^{N_T-1} \lambda_{Tk} \right), \tag{7}$$

$$2\Delta = \bar{h} = \frac{1}{N_P} \sum_{j=1}^{N_P} h_j, \tag{8}$$

Table 2 shows the values of N_P , N_T , $\overline{\lambda_P}$, $\overline{\lambda_T}$, \bar{h} , λ , Δ , N_P/N , N_T/N , λ/I , and Δ/R_a calculated from the simulated profile curves with different surface roughness values and sample numbers. By analyzing the data in Table 2, it is easy to observe the following: (1) with an increase in sampling spacing, average horizontal distance between adjacent peaks (or valleys) gradually increased; (2) with an increase in the surface roughness, average vertical distance between adjacent peaks and valleys increased; (3) number of wave peaks was approximately equal to number of wave valleys and was about 1/3 of the sample number; (4) fitted sinusoidal wavelength of rough surface profile was about three times the sampling spacing; (5) fitted sinusoidal amplitude of roughness profile was about 0.28 times the surface roughness.

Table 2. Calculated parameters of simulated profile curves with different surface roughness values and sample numbers.

| $R_a/\mu\text{m}$ | $I/\mu\text{m}$ | N | N_P | N_T | $\overline{\lambda_P}$ | $\overline{\lambda_T}$ | \bar{h} | N_P/N | N_T/N | $\lambda/\mu\text{m}$ | $\Delta/\mu\text{m}$ | λ/I | Δ/R_a |
|-------------------|-----------------|------|-------|-------|------------------------|------------------------|-----------|---------|---------|-----------------------|----------------------|-------------|--------------|
| 0.1 | 0.2 | 8000 | 2679 | 2679 | 0.5972 | 0.5974 | 0.0568 | 0.335 | 0.335 | 0.597 | 0.028 | 2.986 | 0.284 |
| | 0.4 | 4000 | 1356 | 1357 | 1.1802 | 1.1796 | 0.0561 | 0.339 | 0.339 | 1.180 | 0.028 | 2.951 | 0.281 |
| | 0.6 | 2667 | 885 | 886 | 1.8072 | 1.8059 | 0.0571 | 0.332 | 0.332 | 1.807 | 0.029 | 3.012 | 0.286 |
| | 0.8 | 2000 | 662 | 663 | 2.4169 | 2.4157 | 0.0573 | 0.331 | 0.332 | 2.416 | 0.029 | 3.021 | 0.287 |
| | 1 | 1600 | 541 | 542 | 2.9556 | 2.9538 | 0.0558 | 0.338 | 0.339 | 2.955 | 0.028 | 2.956 | 0.279 |
| 0.2 | 0.2 | 8000 | 2669 | 2668 | 0.5996 | 0.5996 | 0.1112 | 0.334 | 0.334 | 0.600 | 0.056 | 2.998 | 0.278 |
| | 0.4 | 4000 | 1324 | 1324 | 1.2085 | 1.2088 | 0.1133 | 0.331 | 0.331 | 1.209 | 0.057 | 3.021 | 0.283 |
| | 0.6 | 2667 | 906 | 905 | 1.7673 | 1.7666 | 0.1119 | 0.340 | 0.339 | 1.767 | 0.056 | 2.946 | 0.280 |
| | 0.8 | 2000 | 666 | 666 | 2.4036 | 2.4024 | 0.1147 | 0.333 | 0.333 | 2.403 | 0.057 | 3.005 | 0.287 |
| | 1 | 1600 | 539 | 539 | 2.9703 | 2.9665 | 0.1104 | 0.337 | 0.337 | 2.968 | 0.055 | 2.970 | 0.276 |
| 0.4 | 0.2 | 8000 | 2684 | 2683 | 0.5962 | 0.5963 | 0.2269 | 0.336 | 0.335 | 0.596 | 0.113 | 2.981 | 0.284 |
| | 0.4 | 4000 | 1334 | 1334 | 1.2000 | 1.1994 | 0.2230 | 0.334 | 0.334 | 1.200 | 0.112 | 3.000 | 0.279 |
| | 0.6 | 2667 | 897 | 897 | 1.7844 | 1.7837 | 0.2226 | 0.336 | 0.336 | 1.784 | 0.111 | 2.974 | 0.278 |
| | 0.8 | 2000 | 665 | 666 | 2.4060 | 2.4036 | 0.2200 | 0.333 | 0.333 | 2.405 | 0.110 | 3.008 | 0.275 |
| | 1 | 1600 | 554 | 553 | 2.8915 | 2.8949 | 0.2194 | 0.346 | 0.346 | 2.893 | 0.110 | 2.892 | 0.274 |
| 0.8 | 0.2 | 8000 | 2686 | 2685 | 0.5958 | 0.5959 | 0.4493 | 0.336 | 0.336 | 0.596 | 0.225 | 2.979 | 0.281 |
| | 0.4 | 4000 | 1323 | 1323 | 1.2094 | 1.2097 | 0.4588 | 0.331 | 0.331 | 1.210 | 0.229 | 3.024 | 0.287 |
| | 0.6 | 2667 | 880 | 880 | 1.8189 | 1.8175 | 0.4622 | 0.330 | 0.330 | 1.818 | 0.231 | 3.032 | 0.289 |
| | 0.8 | 2000 | 681 | 682 | 2.3482 | 2.3471 | 0.4522 | 0.341 | 0.341 | 2.348 | 0.226 | 2.935 | 0.283 |
| | 1 | 1600 | 536 | 535 | 2.9888 | 2.9925 | 0.4579 | 0.335 | 0.334 | 2.991 | 0.229 | 2.989 | 0.286 |
| 1.6 | 0.2 | 8000 | 2631 | 2632 | 0.6082 | 0.6081 | 0.9007 | 0.329 | 0.329 | 0.608 | 0.450 | 3.041 | 0.281 |
| | 0.4 | 4000 | 1340 | 1339 | 1.1946 | 1.1949 | 0.8670 | 0.335 | 0.335 | 1.195 | 0.434 | 2.987 | 0.271 |
| | 0.6 | 2667 | 871 | 871 | 1.8370 | 1.8377 | 0.9134 | 0.327 | 0.327 | 1.837 | 0.457 | 3.062 | 0.285 |
| | 0.8 | 2000 | 687 | 687 | 2.3300 | 2.3312 | 0.8884 | 0.344 | 0.344 | 2.331 | 0.444 | 2.913 | 0.278 |
| | 1 | 1600 | 527 | 528 | 3.0361 | 3.0342 | 0.9186 | 0.329 | 0.330 | 3.035 | 0.459 | 3.036 | 0.287 |

2.2.3. Contact Model of Axisymmetric Sinusoidal Micro-Convex Surface

Assuming that the actual rough surface is formed by a continuous axisymmetric sinusoidal micro-convex function with wavelength λ and amplitude Δ , as shown in Figure 4, then the height of a single sinusoidal micro-convex surface can be described as

$$Z(r) = \Delta \left[1 + \cos\left(\frac{2\pi r}{\lambda}\right) \right], \quad 0 \leq r \leq \frac{\lambda}{2}, \quad (9)$$

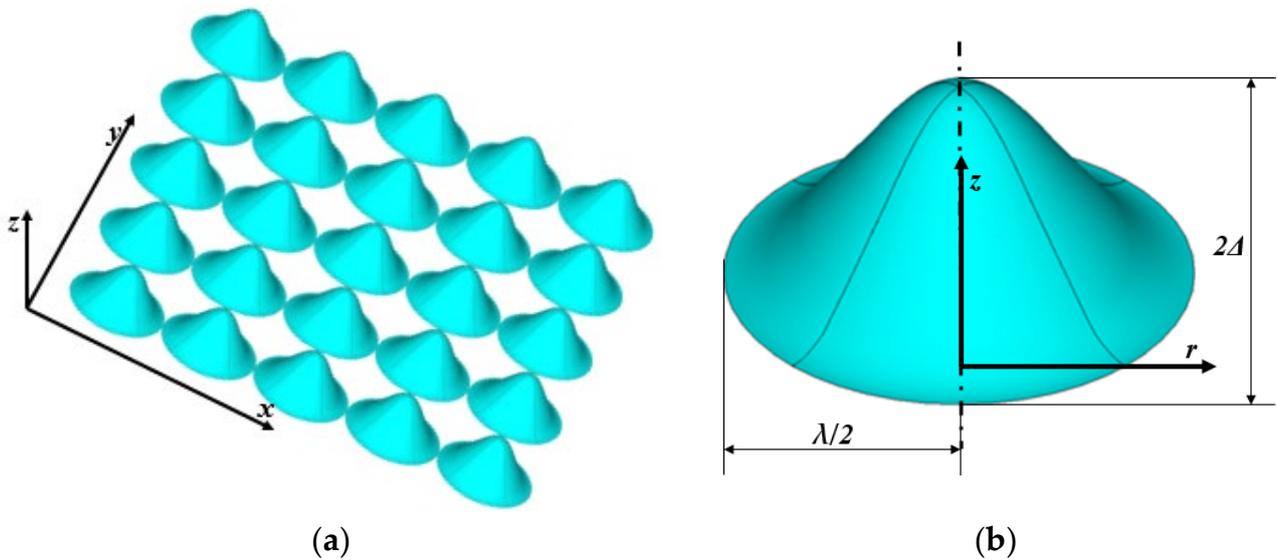


Figure 4. Schematic diagram of axisymmetric sinusoidal micro-convex surface for rough surface model. (a) Three-dimensional morphology; (b) single micro-convex body.

Combined with the principle of equivalent simulation in contact mechanics [30], the microscopic contact between the two rough surfaces is equivalent to the contact between the axisymmetric sinusoidal micro-convex surface with the equivalent elastic modulus E^* and a rigid plane; E^* can be calculated as follows

$$E^* = \frac{E_1 E_2}{E_1(1 - \nu_2^2) + E_2(1 - \nu_1^2)}, \quad (10)$$

Figure 5 shows the simulated microscopic contact process between the axisymmetric sinusoidal micro-convex body and the rigid plane in the xoz cross section, where (a) denotes initial contact, (b) denotes partial contact, and (c) denotes complete contact. With an increase in geometric average pressure \bar{p} , the contact between the sinusoidal micro-convex body and the rigid plane changed from point contact to surface contact and finally developed into complete contact without clearance. The flattening distance of the sinusoidal micro-convex body gradually increased, while the clearance between the contact surfaces gradually decreased until the sinusoidal surface completely fit the rigid plane.

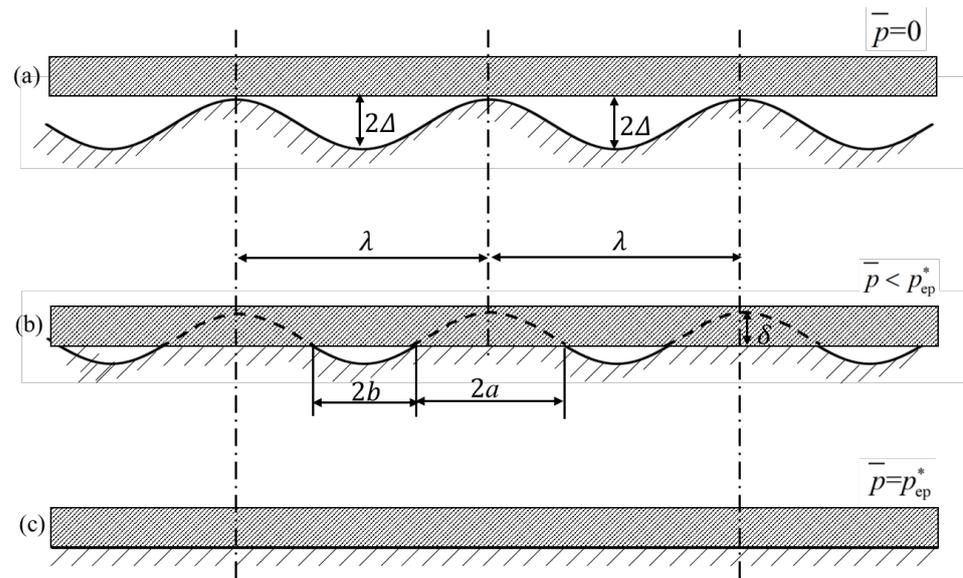


Figure 5. Simulated microscopic contact process between axisymmetric sinusoidal micro-convex body and rigid plane in the xoz cross section. (a) Initial contact; (b) partial contact; (c) complete contact.

According to the study of Saha et al. [28], the interactions between adjacent sinusoidal micro-convex bodies and the influence of the sinusoidal micro-convex base were effectively considered by setting a constraint boundary at the outer radius of the sinusoidal micro-convex base. The bilinear hardening deformation characteristics of micro-convex bodies were also considered by setting the tangent modulus to $0.01 E^*$. Through several finite element parameterization studies, they proposed an empirical formula for predicting the elastic–plastic contact state of the axially symmetric sinusoidal micro-convex body based on two dimensionless parameters: E^*/S_y and Δ/λ . The applicable range was $25 \text{ MPa} < S_y < 40,000 \text{ MPa}$, $50 \text{ GPa} < E^* < 400 \text{ GPa}$, and $0.00005 < \Delta/\lambda < 0.0125$. According to the above research results, the fitted sinusoidal wavelength of the rough surface profile was about three times the sampling spacing, and the fitted sinusoidal amplitude of the roughness profile was about 0.28 times the surface roughness. Thus, Δ/λ should satisfy

$$0.00005 < \frac{\Delta}{\lambda} = \frac{0.28R_a}{3I} < 0.0125. \quad (11)$$

That is, the sampling spacing should satisfy the following condition:

$$7.47R_a < I < 1886.6R_a. \quad (12)$$

According to the research conclusions in the literature [28] and in combination with Equation (11), a prediction formula for the actual elastic–plastic contact area was obtained between a rigid plane and a single axisymmetric sinusoidal micro-convex body that was based on preset surface roughness and sampling spacing:

$$\begin{aligned} A_{ep} &= A_{ep}^* \pi \left(\frac{\lambda}{2} \right)^2 \\ &= 4.5I^2 \left(\frac{\bar{p}}{p_{ep}^*} \right)^{\left\{ 0.64 + \left[1.14 - \frac{1}{1.25} \left(\frac{0.28R_a}{3I} \frac{E^*}{S_y} \right)^{0.32} \right] \right\}} \left(\bar{p}/p_{ep}^* \right) \left\{ \sin^{-1} \left[\left(\frac{\bar{p}}{p_{ep}^*} \right)^{0.16} \right] \right\}^{\left[1 + \frac{1}{200} \left(\frac{0.28R_a}{3I} \frac{E^*}{S_y} \right) \right]}, \end{aligned} \quad (13)$$

In Equation (13), p_{ep}^* , the critical contact pressure for a single sinusoidal convex body in complete elastoplastic contact with a rigid plane can be calculated by the following formula:

$$p_{ep}^* = \frac{0.0469}{0.653 \left(\frac{0.28R_a E^*}{3I S_y} \right)^{-0.0027} + 0.22 \left(\frac{0.28R_a E^*}{3I S_y} \right)^{1.6 \left(\frac{0.28R_a E^*}{3I S_y} \right)^{-0.141}}} \frac{\pi E^* R_a}{I}. \quad (14)$$

2.2.4. Micro-Leakage Model for Premium Connections

After obtaining the actual contact area A_{ep} of a single sinusoidal micro-convex body, the contact half-width and non-contact half-width of a single micro-convex body in the cross section and the flattening distance of the micro-convex body can be calculated from Figure 5 using the following equations:

$$a = \sqrt{\frac{A_{ep}}{\pi}}, \quad b = \frac{\lambda}{2} - a = \frac{\lambda}{2} - \sqrt{\frac{A_{ep}}{\pi}}, \quad (15)$$

$$\delta = 2\Delta\delta^* = 2\Delta - Z(a) = \Delta \left[1 - \cos \left(\frac{2\pi}{\lambda} \sqrt{\frac{A_{ep}}{\pi}} \right) \right], \quad (16)$$

Considering that the contact pressure on the sealing surface is evenly distributed along the circumferential direction of the tubing and casing strings, the total circumferential leakage width on the sealing surface is obtained as follows:

$$B = \pi D_s \times \frac{2b}{\lambda} = \pi D_s \times \frac{2}{\lambda} \left(\frac{\lambda}{2} - \sqrt{\frac{A_{ep}}{\pi}} \right) = \pi D_s \left(1 - \frac{2}{\lambda} \sqrt{\frac{A_{ep}}{\pi}} \right), \quad (17)$$

Considering that the cross section of the leakage channel is still a sinusoidal curve, the height function of the leakage channel can be expressed as

$$Z_L(r) = Z(r) - \delta, \quad 0 \leq r \leq b. \quad (18)$$

Substituting Equations (9) and (16) into Equation (18),

$$Z_L(r) = \Delta \left[\cos \left(\frac{2\pi r}{\lambda} \right) + \cos \left(\frac{2\pi}{\lambda} \sqrt{\frac{A_{ep}}{\pi}} \right) \right], \quad 0 \leq r \leq b. \quad (19)$$

Furthermore, the radial average leakage height on the sealing surface for the premium connection can be calculated as follows:

$$\begin{aligned} H &= \frac{1}{b} \int_0^b Z_L(r) dr = \frac{\Delta}{b} \left[\frac{\lambda}{2\pi} \sin \left(\frac{2\pi r}{\lambda} \right) + r \cos \left(\frac{2\pi}{\lambda} \sqrt{\frac{A_{ep}}{\pi}} \right) \right]_0^b \\ &= \Delta \left[\frac{\lambda}{2\pi} \left(\frac{\lambda}{2} - \sqrt{\frac{A_{ep}}{\pi}} \right)^{-1} \sin \left(\frac{2\pi}{\lambda} \left(\frac{\lambda}{2} - \sqrt{\frac{A_{ep}}{\pi}} \right) \right) + \cos \left(\frac{2\pi}{\lambda} \sqrt{\frac{A_{ep}}{\pi}} \right) \right], \end{aligned} \quad (20)$$

After B and H are both known, the volume leakage rate of the premium connection can be calculated according to the parallel plate model [31]:

$$\begin{aligned} Q_v &= \frac{BH^3(p_{in} - p_{out})}{12L_s\eta} = \frac{\pi D_s(p_{in} - p_{out})}{12L_s\eta} \left(1 - \frac{2}{\lambda} \sqrt{\frac{A_{ep}}{\pi}} \right) \times \\ &\left\{ \Delta \left[\frac{\lambda}{2\pi} \left(\frac{\lambda}{2} - \sqrt{\frac{A_{ep}}{\pi}} \right)^{-1} \sin \left(\frac{2\pi}{\lambda} \left(\frac{\lambda}{2} - \sqrt{\frac{A_{ep}}{\pi}} \right) \right) + \cos \left(\frac{2\pi}{\lambda} \sqrt{\frac{A_{ep}}{\pi}} \right) \right] \right\}^3 \\ &= \frac{D_s(p_{in} - p_{out})}{L_s\eta} g(A_{ep}, \Delta, \lambda) \end{aligned} \quad (21)$$

In Equation (21),

$$g(A_{ep}, \Delta, \lambda) = \frac{\pi}{12} \left(1 - \frac{2}{\lambda} \sqrt{\frac{A_{ep}}{\pi}} \right) \left\{ \Delta \left[\sin \left(\frac{2\pi}{\lambda} \left(\frac{\lambda}{2} - \sqrt{\frac{A_{ep}}{\pi}} \right) \right) + \cos \left(\frac{2\pi}{\lambda} \sqrt{\frac{A_{ep}}{\pi}} \right) \right] \right\}^3,$$

By analyzing Equation (13) and (21) simultaneously, it can be found that, when material parameters E^* and S_y of the sealing surface, the roughness of the sealing surface, and the sampling length (which determine λ and Δ) are all given, g is only related to the nominal average contact pressure on the sealing surface, i.e.,

$$g = g(\bar{p}). \quad (22)$$

In this case, Equation (21) can be simplified to

$$Q_v = \frac{D_s}{L_s} \frac{(p_{in} - p_{out})}{\eta} g(\bar{p}). \quad (23)$$

Generally, if the connection is ideally centered, the contact pressure distribution on the sealing surface is axially symmetric, but the contact pressure on sealing surface is usually non-uniform along the axial direction of the pipe string, especially for a spherical premium connection. At this point, the cross-sectional area of the leakage channel along the axial direction of the string is non-uniform, so the sealing structure can be divided into several contact elements along the axial direction. When the number of contact elements is large enough, the sealing contact pressure in a single contact element can be regarded as a constant. Therefore, for each contact element, the leakage rate can be calculated by Equation (21). As an example, for the cone-to-cone sealing structure, the sealing structure is divided into several sealing contact elements equally along the axial direction of the string, which are numbered 1, 2, 3, ..., k , ..., n , as shown in Figure 6.

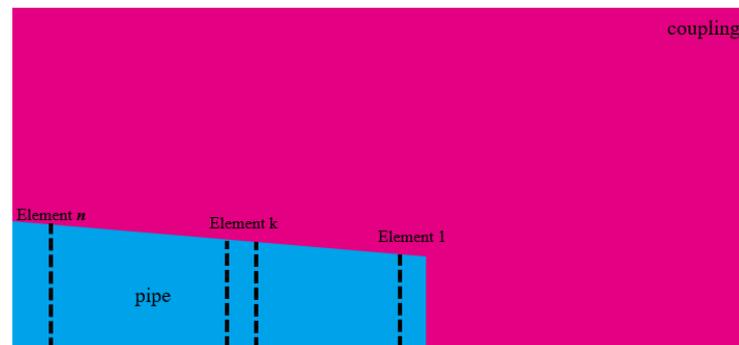


Figure 6. Axial sealing contact element of cone-to-cone sealing structure for premium connections.

Then, the sealing length of each sealing element is

$$L_{sk} = \frac{D_{smax} - D_{smin}}{2n \sin \gamma_s}, \quad (24)$$

The average sealing diameter of the k th sealing element is

$$D_{sk} = D_{smin} + \left(k - \frac{1}{2} \right) \frac{D_{smax} - D_{smin}}{n}, \quad (25)$$

It is assumed that the average contact pressure for the k th sealing contact element is \overline{p}_k , which consists of two parts: a contact pressure generated by the interference fit between sealing surface and a contact pressure induced by internal pressure in the string [23]:

$$\begin{aligned}\overline{p}_k &= \left[(\overline{p}_k)_{\delta_r} + (\overline{p}_k)_{p_{in}} \right] \cos \gamma_s \\ &= \left[\frac{\delta_r E (D_{sk}^2 - d^2) (W^2 - D_{sk}^2)}{D_{sk}^3 (W^2 - d^2)} + \frac{p_{in} d^2 (W^2 - D_{sk}^2)}{D_{sk}^2 (W^2 - d^2)} \right] \cos \gamma_s,\end{aligned}\quad (26)$$

Then, the actual contact area A_{epk} of a single micro-convex body in every contact element can still be calculated by Equation (13), and, thus, $g_k(\overline{p}_k)$ can be obtained by Equation (21). Assuming that the pressure at the inlet and outlet of the k th sealing contact element are p_{k-1} and p_k , respectively, the leakage rate Q_{vk} can also be obtained by Equation (23) as follows:

$$Q_{vk} = \frac{D_{sk} (p_{k-1} - p_k)}{L_{sk} \eta} g_k(\overline{p}_k). \quad (27)$$

Thus, the pressure at the outlet of the k th sealing contact element is

$$p_k = p_{k-1} - \frac{L_{sk} \eta}{D_{sk} g_k(\overline{p}_k)} Q_{vk}. \quad (28)$$

According to Equation (28), the outlet pressure of the first sealing contact element can be calculated by the internal gas pressure in the string:

$$p_1 = p_{in} - \frac{L_{s1} \eta}{D_{s1} g_1(\overline{p}_1)} Q_{v1}. \quad (29)$$

Based on the boundary conditions of gas leakage pressure along sealing surface, it can be known that the outlet pressure of the k th sealing contact element is the inlet pressure of the $(k + 1)$ th sealing contact element, so the outlet pressures of the 2nd, 3rd, ..., n th sealing contact elements can be obtained, e.g.,

$$p_2 = p_1 - \frac{L_{s2} \eta}{D_{s2} g_2(\overline{p}_2)} Q_{v2}, \quad (30)$$

$$p_3 = p_2 - \frac{L_{s3} \eta}{D_{s3} g_3(\overline{p}_3)} Q_{v3}, \quad (31)$$

and so on. By adding the left and right sides of Equations (29)–(31), we can obtain the outlet pressure of the 3rd sealing contact element:

$$p_3 = p_{in} - \frac{L_{s1} \eta}{D_{s1} g_1(\overline{p}_1)} Q_{v1} - \frac{L_{s2} \eta}{D_{s2} g_2(\overline{p}_2)} Q_{v2} - \frac{L_{s3} \eta}{D_{s3} g_3(\overline{p}_3)} Q_{v3}. \quad (32)$$

By analogy, the outlet pressure of the n th sealing contact element can be obtained:

$$\begin{aligned}p_{out} &= p_{in} - \frac{L_{s1} \eta}{D_{s1} g_1(\overline{p}_1)} Q_{v1} - \frac{L_{s2} \eta}{D_{s2} g_2(\overline{p}_2)} Q_{v2} - \frac{L_{s3} \eta}{D_{s3} g_3(\overline{p}_3)} Q_{v3} - \\ &\dots - \frac{L_{sk} \eta}{D_{sk} g_k(\overline{p}_k)} Q_{vk} \dots - \frac{L_{sn} \eta}{D_{sn} g_n(\overline{p}_n)} Q_{vn}.\end{aligned}\quad (33)$$

According to the continuity condition of gas flow in the leakage passage, the following must be satisfied:

$$Q_{v1} = Q_{v2} = Q_{v3} = \dots = Q_{vk} \dots = Q_{vn} = Q_v. \quad (34)$$

Finally, the gas leakage rate Q_v for a premium connection can be obtained from Equations (33) and (34) as follows:

$$Q_v = \frac{n(p_{in} - p_{out})}{\frac{L_{s1}\eta}{D_{s1}g_1(\bar{p}_1)} + \frac{L_{s2}\eta}{D_{s2}g_2(\bar{p}_2)} + \frac{L_{s3}\eta}{D_{s3}g_3(\bar{p}_3)} + \dots + \frac{L_{sk}\eta}{D_{sk}g_k(\bar{p}_k)} \dots + \frac{L_{sn}\eta}{D_{sn}g_n(\bar{p}_n)}} \quad (35)$$

$$= \frac{n(p_{in} - p_{out})}{\sum_{k=1}^n \frac{L_{sk}\eta}{D_{sk}g_k(\bar{p}_k)}}$$

3. Results and Discussion

3.1. Basic Parameters

A 177.8 mm × 10.36 mm P110 casing with a cone-to-cone-type premium connection was chosen for the example analysis [23]. Its basic parameters for calculating the leakage rate of the premium connection are listed in Table 3.

Table 3. Basic parameters for calculating leakage rate of premium connection.

| Symbol | Value | Unit | Symbol | Value | Unit |
|------------|---------|------|-----------|------------------------|---------------|
| W | 194.31 | mm | p_{in} | 50 | MPa |
| d | 157.08 | mm | p_{out} | 0 | MPa |
| D_{smax} | 171.132 | mm | η | 1.660×10^{-6} | MPa·s |
| D_{smin} | 163.08 | mm | E_2 | 100 | GPa |
| L_s | 15.556 | mm | ν_2 | 0.32 | dimensionless |
| γ_s | 15 | ° | S_y | 250 | MPa |

3.2. Model Validation

The roughness R_a of the sealing surface was set to be 0.1 μm , and the sampling spacing I was 0.8 μm . First, model validation analysis was carried out. Figure 7 compares the theoretical leakage rate predicted by the model in this paper with the predicted value by a model in the literature [23] and previously reported experimental values in Ref. [32]. The proposed model could predict the leakage rate with a consistent variation trend to those of the other model predictions and test results, although there were some numerical differences because of the testing condition not exactly disagreeing with the calculation condition. Meanwhile, under the same average contact pressure on sealing surface, the predicted leakage rate with the model in this paper is closer to the testing value in Ref. [32], which indicates that it is more reasonable to simulate the elastic–plastic microscopic contact problem between sealing surfaces for a premium connection with sinusoidal convex body assumptions compared with a conical micro-convex body in the literature [23]. In addition, it is also obvious that, when the average contact pressure on the sealing surface increases to about 580 MPa, that is close to two times the yield strength of contact material 250 MPa; the actual leakage rate approaches nearly zero finally, which is conformed to the actual situation. Consequently, the model presented in this paper was in better agreement with the experimental results, indicating its correctness and reliability.

3.3. Results Analysis

Considering different amounts of radial interference between sealing surfaces, the average contact pressure, total circumferential leakage width, radial average leakage height on the sealing surface for each axial sealing contact unit, and gas leakage volume rate of the premium connection were obtained by the model proposed in this paper, and the results are shown in Figure 8a–d.

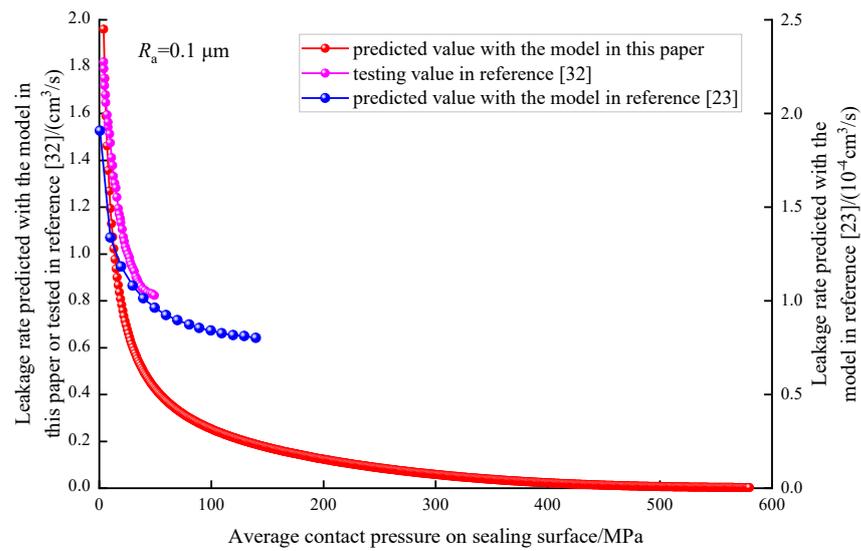
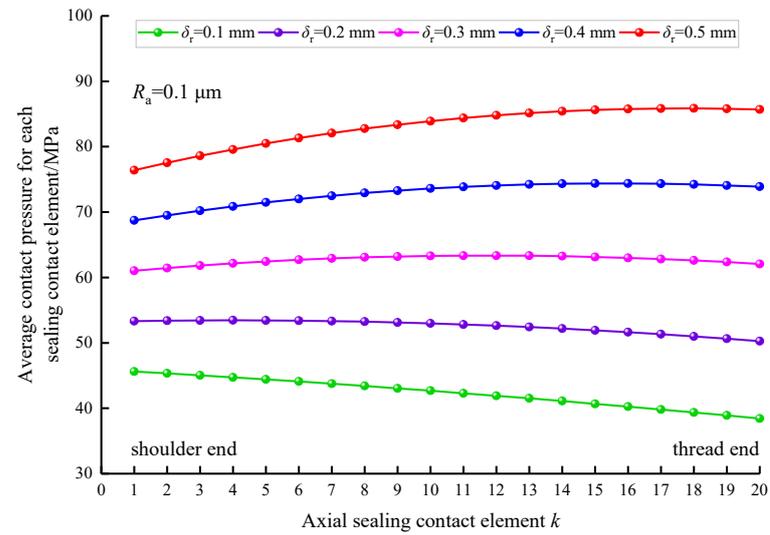
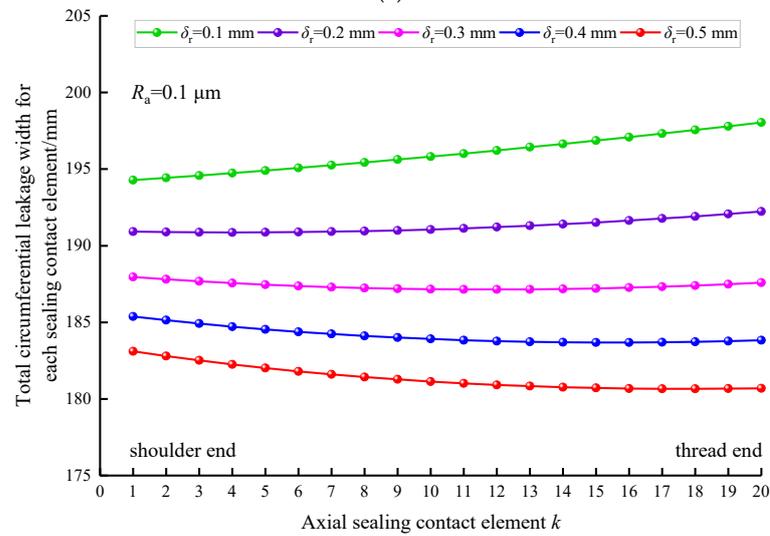


Figure 7. Comparison of leakage rates.



(a)



(b)

Figure 8. Cont.

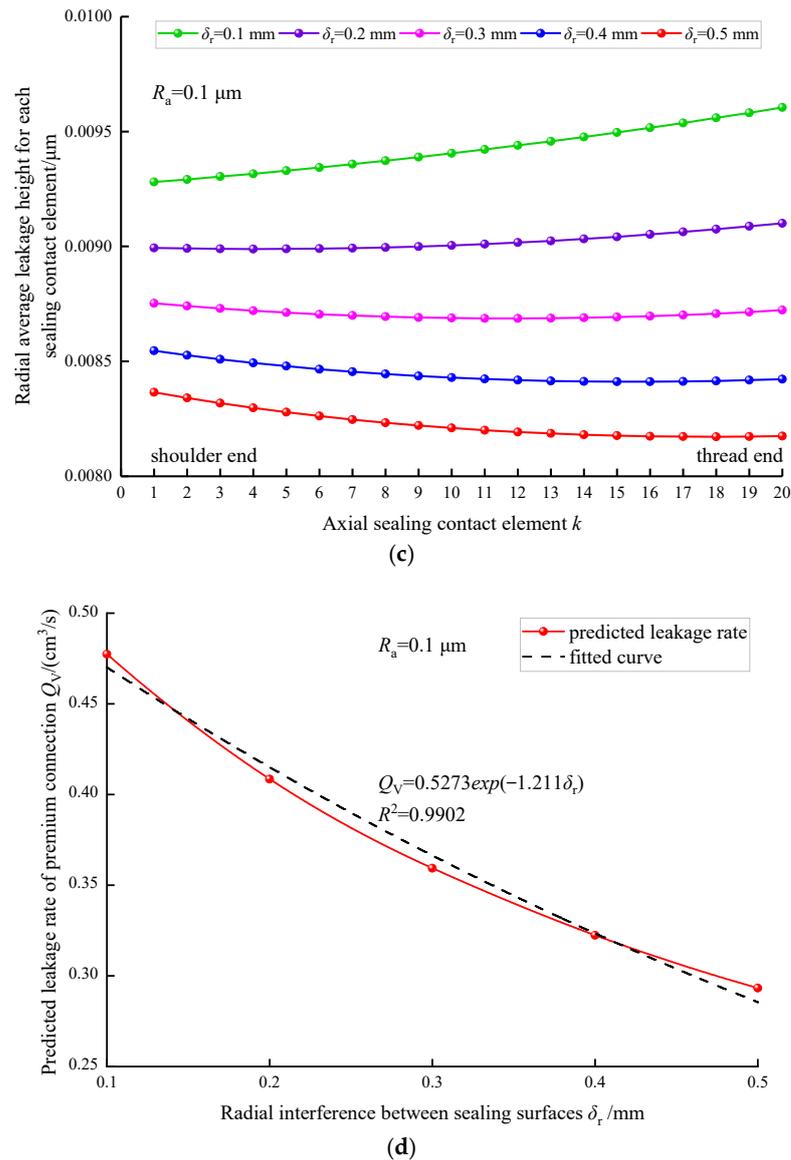


Figure 8. Predicted sealing parameters of each axial sealing contact unit and leakage rate for cone-to-cone-type premium connection for different amounts of radial interference between sealing surfaces. (a) Average contact pressure for each sealing contact element. (b) Total circumferential leakage width for each sealing contact element. (c) Radial average leakage height for each sealing contact element. (d) Predicted leakage rate of premium connection.

Figure 8a shows that average contact pressure had an uneven axial distribution for each sealing contact element, and average contact pressure increased with an increase in radial interference between sealing surfaces. Figure 8b,c shows that, under the influence of unevenly distributed contact pressure, the total circumferential leakage width and radial average leakage height for each sealing contact element were also uneven, and both decreased with an increase in radial interference between the sealing surfaces. Figure 8d shows that the gas leakage volume rate of the premium connection decreased exponentially with an increase in radial interference between sealing surfaces.

Comprehensive analysis of Figure 8a–d shows that, when the sealing surface roughness was constant, increasing the radial interference between the sealing surfaces could help to reduce the leakage channel cross-sectional area, significantly reducing the leakage rate and improving the gas sealing performance of the premium connection. Figure 9

compares the influence of average contact pressure on the sealing surface on the leakage rates for two roughness values.

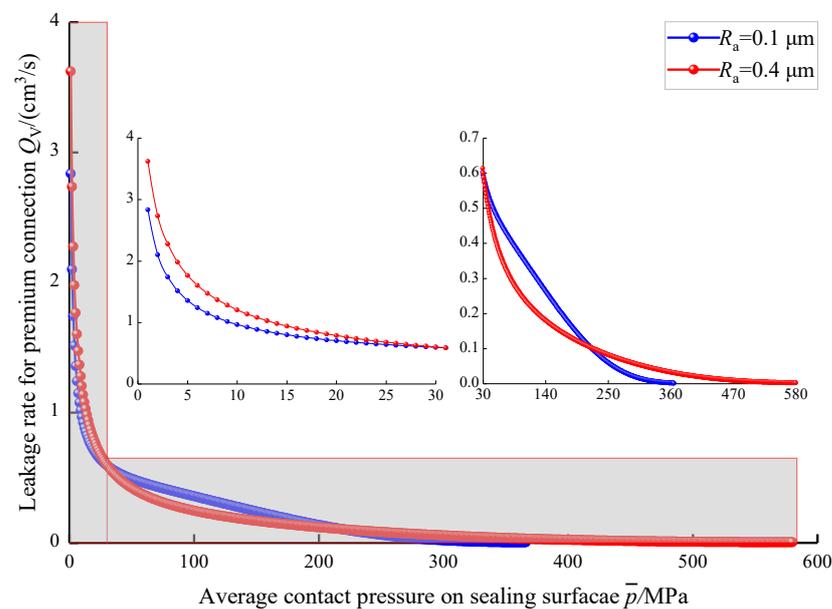


Figure 9. Influence of average contact pressure on sealing surface on leakage rate for two roughness values.

Figure 9 shows that the influence of roughness on the leakage rate was not monotonic due to the elastic–plastic deformation of the sinusoidal micro-convex body on the sealing surface. When the average contact pressure on the sealing surface \bar{p} was less than 30 MPa, the leakage rate with R_a of 0.1 μm is obviously lower than that with R_a of 0.4 μm . When \bar{p} was between 30 and 220 MPa, the thin and tall micro-convex body with a larger roughness was more likely to produce plastic deformation and fill the leakage channel, so its leakage rate was relatively low. However, when \bar{p} was higher than 220 MPa, the dumpy micro-convex with a smaller roughness was more likely to produce plastic deformation, while the thin and tall micro-convex body with a larger roughness was more and more difficult to flatten, so its leakage rate was relatively high. However, in general, the smaller the roughness, the faster the sealing surface entered a completely plastic contact state, completely locking the leakage channel between the sealing surfaces. Assuming that the critical allowable leakage rate of the premium connection was $0.9 \text{ cm}^3/15 \text{ min}$ ($0.001 \text{ cm}^3/\text{s}$) based on ISO13679, the critical average contact pressure on the sealing surface should be greater than 366 and 580 MPa for roughness values of 0.1 and 0.4 μm , respectively. During sealing parameters design for premium connections, it is very convenient to use this critical \bar{p} for sealing parameters optimization. Meanwhile, in order to improve the gas sealing performance of a premium connection, the machining accuracy of the sealing surface should be improved properly to reduce sealing surface roughness.

4. Conclusions

- (1) A semi-theoretical model to quantitatively predict leakage rate of tubing and casing premium connections has been proposed based on sinusoidal contact simulation on rough surfaces. The geometric parameters of the sealing surface profile approximated by a sinusoidal micro-convex surface were obtained based on the random normal distribution sampling method. With the actual area prediction formula for the elastic–plastic contact of an axisymmetric sinusoidal micro-convex body, the circumferential leakage width and radial average leakage height of the micro-leakage channel between sealing surfaces were acquired. The actual micro-leakage rate of the premium connection was derived by dividing the sealing structure into a series of sealing contact units along the axial direction of connection and using the boundary

conditions of the fluid leakage pressure and the continuity conditions of the leakage rate of each unit.

- (2) A cone-to-cone-type premium connection was taken as an example investigation to validate the model and reveal the sealing and leakage characteristics of a connection.
 - Affected by the uneven distribution of the contact pressure on the sealing surface, the circumferential leakage width and radial average leakage height between sealing surfaces are both non-uniformly distributed.
 - The leakage rate of a premium connection decreases exponentially with an increase in radial interference between sealing surfaces.
 - The lower the roughness of a sealing surface, the smaller the mean contact pressure to completely lock the leakage channel. In the example when the roughness values were 0.1 and 0.4 μm , the mean contact pressures of the sealing surface corresponding to the critical allowable leakage rate of 0.9 $\text{cm}^3/15 \text{ min}$ should be greater than 366 and 580 MPa, respectively.
- (3) To improve the gas sealability of a premium connection, the radial interference between the sealing surfaces should be increased to reduce the leakage channel cross-sectional area, and the machining accuracy of the sealing surface should be improved to reduce the roughness of the sealing surface.
- (4) The proposed model in this paper provides a fast and quantitative sealability evaluation method for premium connections. However, some affecting factors, including additional sealing from torque shoulder, more sealing structure types, thread grease's effects, and contact pressure relaxation in high-pressure and high-temperature environments, have not been comprehensively considered, and the model was also validated mainly by the previous literature. Consequently, some corresponding full-scale experimental testing and model refinement should be carried out to further improve model reliability in later work.

Author Contributions: Conceptualization, H.X.; Methodology, H.X. and Z.Z.; Validation, H.X.; Formal analysis, H.X.; Investigation, H.X., S.X. and B.Y.; Writing—original draft, H.X.; Writing—review and editing, H.X. and S.X.; Supervision, Z.Z. and T.S. All authors have read and agreed to the published version of the manuscript.

Funding: This research was funded by the National Natural Science Foundation of China [grant no. 51804060], the Open Fund [grant no. PLN2022-23] of the State Key Laboratory of Oil and Gas Reservoir Geology and Exploitation (Southwest Petroleum University), and the Natural Science Foundation of Chongqing, China [grant no. CSTB2022NSCQ-MSX0989]. We also thank LetPub (www.letpub.com, accessed on 9 January 2023) for its linguistic assistance during preparation of this manuscript.

Data Availability Statement: The data used to support the findings of this study are available from the corresponding author upon request.

Conflicts of Interest: The authors declare no conflict of interest.

Nomenclature

| | |
|--------------------------|---|
| Z_i | height sample of roughness profile, μm |
| N | number of Z_i , integer |
| μ | mean value of Z_i , μm |
| σ | standard deviation of Z_i , μm |
| c_1, c_2 | random numbers distributed uniformly between zero and one |
| R_a | surface roughness, μm |
| R_y | maximum peak-to-valley distance of roughness profile, μm |
| ε_μ | mean error of Z_i , dimensionless |
| ε_y | maximum peak-to-valley distance error, dimensionless |
| $Z_{i,\max}, Z_{i,\min}$ | maximum and minimum values of profile height samples, respectively, μm |
| I | sampling spacing, μm |

| | |
|-------------------------------|---|
| x_i | coordinate value along sampling length, μm |
| N_P | total number of peak points of the profile curve, integer |
| N_T | total number of valley points of the profile curve, integer |
| λ_{Pj} | horizontal distance between adjacent wave peaks, μm |
| λ_{Tk} | horizontal distance between adjacent valleys, μm |
| h_j | vertical distance between adjacent peaks and valleys, μm |
| $\overline{\lambda_P}$ | average horizontal distance between adjacent wave peaks, μm |
| $\overline{\lambda_T}$ | average horizontal distance between adjacent valleys, μm |
| \overline{h} | average vertical distance between adjacent peaks and valleys, μm |
| λ | fitted sinusoidal wavelength of the roughness profile, μm |
| Δ | fitted sinusoidal amplitude of the roughness profile, μm |
| r | corresponding radial coordinate at the height of the axisymmetric sinusoidal micro-convex surface, μm |
| E | elastic modulus of string, MPa |
| E^* | equivalent elastic modulus of the contact pair, MPa |
| S_y | yield strength of the softer material for sealing contact pair, MPa |
| E_1, E_2 | elastic moduli of the materials of the two contact surfaces, respectively, MPa |
| ν_1, ν_2 | Poisson's ratios of two contact surface materials, respectively, dimensionless |
| A_{ep} | actual contact area of a single sinusoidal micro-convex body, μm^2 |
| A_{ep}^* | dimensionless actual contact area of a single sinusoidal micro-convex body, dimensionless |
| \overline{p} | geometric average pressure on sealing surface, MPa |
| p_{ep}^* | critical contact pressure for a single sinusoidal convex body in complete elastoplastic contact with a rigid plane, MPa |
| a, b | contact and non-contact half-widths of a single micro-convex body in the cross section, respectively, μm |
| δ | flattening distance of a single micro-convex body in the cross section, μm |
| δ^* | dimensionless flattening distance, dimensionless |
| B | total circumferential leakage width on sealing surface, mm |
| D_s | average diameter of sealing surface, mm |
| H | radial average leakage height on sealing surface, mm |
| Q_v | gas leakage volume rate of a premium connection, cm^3/s |
| p_{in}, p_{out} | internal and external gas pressures for tubing and casing string with a premium connection, respectively, MPa |
| η | dynamic viscosity of the sealed gas in the strings, MPa·s |
| L_s | total axial length of the sealing surface for a premium connection, mm |
| D_{smax}, D_{smin} | maximum and minimum diameters of the sealing surface, respectively, mm |
| γ_s | cone angle of the sealing surface for cone-to-cone premium connection, $^\circ$ |
| L_{sk} | sealing length of the k th sealing element, mm |
| n | number of sealing elements, integer |
| D_{sk} | average sealing diameter of the k th sealing element, mm |
| $(\overline{p_k})_{\delta_r}$ | sealing contact pressure generated by radial interference between sealing surfaces, MPa |
| $(\overline{p_k})_{p_{in}}$ | additional contact pressure on the sealing surface generated by the gas pressure in the string, MPa |
| δ_r | radial interference between sealing surfaces, mm |
| W | outer diameter of the coupling, mm |
| d | internal diameter of the string, mm |
| i, j, k | respectively, integer |

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