



Article

The COVID-19 Outbreak and Risk–Return Spillovers between Main and SME Stock Markets in the MENA Region

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Abstract: This study investigates return and asymmetric volatility spillovers and dynamic correlations between the main and small and medium-sized enterprise (SME) stock markets in Saudi Arabia and Egypt for the periods before and during the COVID-19 pandemic. Return and volatility spillovers are modelled using a VAR-asymmetric BEKK–GARCH (1,1) model, while a VAR-asymmetric DCC–GARCH (1,1) model is employed to model the dynamic conditional correlations between these markets, which are then used to determine and explore portfolio design and hedging implications. The results show that while bidirectional return spillovers between the main and SME stock markets are limited to Saudi Arabia, shock and volatility spillovers have different characteristics and dynamics in both main–SME market pairs. In addition, the dynamic correlations between the main and SME markets are mostly positive and have notably increased during the COVID-19 pandemic, particularly in Saudi Arabia, suggesting that adding SME stocks to a main stock portfolio enhances its risk-adjusted return, especially during tranquil market phases. One practical implication of our results is that the development of SME stock markets can indirectly contribute to economic development via the main market channel and provide an avenue for portfolio diversification and risk management.

Keywords: MENA region; SME stock market; return and volatility spillovers; hedge ratios; optimal portfolio designs

JEL Classification: C32; C58; D53; G11



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1. Introduction

The interdependencies between financial markets, especially during turbulent times, have long attracted considerable interest among finance academics and practitioners. Changes in the dependence structure, particularly during periods of market turmoil, are of great concern to market participants and policymakers. During a crisis, the correlations between equity markets intensify due to spillover effects (see, e.g., Hwang 2014; Markwat et al. 2009; McIver and Kang 2020; Nikkinen et al. 2020; Rose and Spiegel 2010; Samarakoon 2011). In response, investors should adjust their portfolios taking cross-market spillovers into consideration to mitigate contagion risks. Financial market regulators, on the other hand, should take appropriate measures to maintain market stability during crisis episodes (Baumöhl and Lyócsa 2014; Hemche et al. 2016; Karanasos et al. 2014).

The COVID-19 crisis has sent shock waves through the global economy due to the stringent public health measures undertaken by governments around the world. Similar to the spread of the COVID-19 virus itself, the heightened volatility of asset prices during the pandemic was transmitted across markets through the mechanism of contagion, which is amplified by saturated media coverage (Akhtaruzzaman et al. 2021b). The sheer scale of the unfolding pandemic led to an unprecedented proliferation of studies on financial market dynamics, aimed particularly at understanding the linkages within and between

financial markets, including stock, bond, foreign exchange, commodity, and cryptocurrency markets, during the COVID-19 crisis.

While a comprehensive review of the literature is beyond the scope of this paper, notable studies in this strand include those by [Corbet et al. \(2021\)](#), who examine volatility spillovers from Chinese financial markets to gold futures, oil futures, soybean futures, the US dollar/RMB spot exchange rate, and the Bitcoin price; [Akhtaruzzaman et al. \(2021a\)](#), who analyze financial contagion between China and the G7 countries via financial and nonfinancial companies; [Gharib et al. \(2021\)](#), who examine the contagion effects between oil and gold; [Akhtaruzzaman et al. \(2021c\)](#) who examine the hedging or safe-haven asset properties of gold during different stages of the COVID-19 pandemic; [Papadamou et al. \(2021\)](#), who investigate flight-to-quality episodes between 10 major stock and bond markets; and [Umar et al. \(2021\)](#), who explore the linkages between emerging markets and US bonds. [Kinatader et al. \(2021\)](#) examine the bivariate conditional correlations between sovereign bonds, commodities, and major exchange rates.

Despite the mushrooming literature on spillover dynamics between financial markets, the linkages between main and second-tier markets operating within the same stock exchange during the present pandemic represent an untapped area where research can further our understanding. The importance of this study stems from the role of second-tier markets in facilitating small and medium-sized enterprises' (SMEs') access to finance and reducing their reliance on debt¹ by imposing less stringent listing requirements and serving as a stepping-stone² for aspiring SMEs to graduate to the main market. Moreover, second-tier markets (or SME exchanges, as the World Federation of Exchanges refers to them) have expanded globally, becoming an important part of the SME financing ecosystem ([The World Federation of Exchanges 2015](#)). According to [The World Federation of Exchanges \(2018\)](#), the number of listings on these markets has reached 6807 companies, with a total market capitalization of over USD 1.3 trillion across 33 markets spanning 29 exchanges around the world.

Given that the SME market serves as a pipeline to the main market, the extent of the linkages between these markets has important portfolio and risk management implications for investors. If the SME market is only weakly integrated with the main market, external shocks may have limited influence on the SME market, and then investors in the main market can benefit by including the stocks listed in the SME market in their portfolio, as this diversification should reduce risk. In contrast, if the SME market is fully integrated with the main market, volatility in the former may decrease, as it will primarily be determined by volatility in the main market, and investors in the SME market will benefit from a low cost of capital ([Li 2007](#)). However, this is not always the case, as volatility in the main market can also be affected by that in the SME market.

Despite the extensive body of evidence on the linkages between large and small stocks listed in the same main market (see, among others, [Karmakar 2010](#); [Koulakiotis et al. 2016](#); [Lo and MacKinlay 1990](#)), the potential linkages between SMEs and main stock markets have been investigated far less thoroughly. The few studies in this realm include those by [Samitas et al. \(2006\)](#) and [Nguyen et al. \(2020\)](#). [Samitas et al. \(2006\)](#) found unidirectional Granger causality running from the main index to the parallel (second-tier) index in the Greek stock exchange. [Nguyen et al. \(2020\)](#) examine both the return and volatility transmission between the main and second-tier markets in Hong Kong, Singapore, Thailand, and Malaysia. Their results show that significant unidirectional return transmission from the SME to the main market is present only in Hong Kong, while return transmission runs in the reverse direction in the remaining markets. Volatility spillovers, however, are relatively weak, with statistically significant asymmetric volatility transmission only apparent in the case of the Singaporean market and, to a lesser extent and in the opposite direction, in the Hong Kong market, while no trace of volatility transmission is found in the Thai and Malaysian markets.

While an asymmetric return and volatility transmission from large to small stock portfolios and from main to SME markets is documented in most cases, there exists contradictory evidence suggesting a bilateral return and volatility spillovers between large and

small portfolios and, even more remarkably, transmission in the opposite direction from the SME to the main market, which has been interpreted as a potential indirect influence of the SME market on economic development through the main market channel (Nguyen et al. 2020). These mixed findings call for further research on the relation between main and SME markets in different contexts, especially during crisis periods, when diversification and hedging are highly sought after. To the best of the authors' knowledge, no study has simultaneously examined return and volatility spillovers between main and SME stock markets during the COVID-19 pandemic crisis.

Therefore, we aim to extend the analysis of return and volatility spillovers to stock markets in the Middle East and North Africa (MENA) region during the COVID-19 pandemic.³ Our analysis covers the following two exchanges that have liquid SME markets in the region: the Egyptian Exchange and the Saudi stock exchange (Tadawul). Our choice of these markets for the study sample stems from the following considerations: First, the importance of this region in the world economy is growing. Several MENA countries have implemented structural economic reforms to diversify their economies and reduce their traditional reliance on oil and gas revenues (e.g., Saudi Arabia Vision 2030), and an important avenue to achieve this objective is to increase the contribution of SMEs to GDP. These reforms have helped the Saudi market rank among the top 10 largest exchanges globally in terms of market capitalization, accounting for approximately 76% of the market capitalization in the MENA region. Second, Saudi Arabia and Egypt are the largest economies in the MENA region.⁴ Third, Egypt has the largest SME market in the MENA region in terms of the number of listed companies, while Saudi Arabia is the largest in terms of market capitalization. Fourth, MENA markets represent a significant portion of existing shariah-compliant Islamic financial assets. Fifth, the MENA SME markets are in their early stage of development and have specific features that set them apart from their more established counterparts. Relative to the Asian SME markets examined by Nguyen et al. (2020), the SME markets in the MENA region are relatively smaller than their main board counterparts in terms of both market capitalization and number of listings. Thus, it is interesting to investigate the linkages between SME and main markets and determine how these markets have weathered the COVID-19 crisis.⁵

With the above in mind, we contribute to the literature in two ways. First, the return and volatility spillover effects between the main and SME stock markets are investigated over different time periods (the periods before and during the pandemic) to ascertain whether the relationship between these markets has been affected by the widespread pandemic. To this end, a disaggregated VAR-asymmetric BEKK–GARCH and an asymmetric DCC–GARCH approach are used, respectively, to examine return–risk spillovers and the time-varying dynamic correlations between the main and SME stock markets. Second, the results obtained from the asymmetric DCC–GARCH framework are used to build dynamic optimal portfolios and hedging strategies, taking the COVID-19 outbreak into consideration, which shed light on the potential of the SME portfolio in hedging the systematic risk of equity portfolios in the main market.

The empirical analysis reveals contrasting results between the Saudi and Egyptian main–SME market pairs. While significant return and volatility spillovers between the main and SME stocks are found in Saudi Arabia, only volatility spillovers are documented for Egypt. Indeed, the COVID-19 pandemic crisis has intensified the risk spillover among the Saudi main–SME market pairs, which, to our surprise, was not the case for the Egyptian pair. What is more remarkable is that the risk spillover between the Egyptian main and SME markets declined during the pandemic. The dynamic correlations between the main and SME markets are mostly positive and have notably increased during the COVID-19 pandemic, particularly in Saudi Arabia, suggesting that adding SME stocks to a main market stock portfolio can enhance its risk-adjusted return, especially during tranquil market phases.

The remainder of the paper is organized as follows. Section 2 presents the data and the preliminary analysis that justifies the specification of the econometric models that we use

in our empirical analysis. Section 3 discusses the empirical methodology, while Section 4 presents and interprets the results from the asymmetric BEKK and asymmetric DCC models and portfolio management analysis. Section 5 provides concluding remarks along with policy implications, limitations, and future research avenues.

2. Data Definitions, Descriptive Statistics, and Preliminary Analysis

2.1. Data Definitions

The data set comprises the daily closing prices of the main and SME stock market indices in Saudi Arabia and Egypt. The indices used in this paper are the Tadawul All Share Index (TASI) and SME market index (NOMU) for the Saudi market and the Egyptian Exchange Price Index (EGX 30) and SME market index (NILEX) for Egypt. The daily data for the TASI, NOMU and EGX30 are taken from the Bloomberg database, whereas the NILEX data are pooled from the Egyptian Exchange website. The time span of the study runs from July 2013 to November 2020.⁶ To account for the COVID-19 pandemic effect, we have divided the sample into the following two subperiods: the period before the COVID-19 pandemic, which covers the period before the emergence of COVID-19, and the COVID-19 pandemic crisis period, which starts with the declaration of the identification of the virus and continues until the end of our sample period.⁷ Continuously compounded daily returns are calculated on the basis of the following logarithmic filter: $r_{i,t} = 100 \times \ln\left(\frac{p_{i,t}}{p_{i,t-1}}\right)$, where $r_{i,t}$ and $p_{i,t}$ represent the percentage daily return and closing index price on day t , respectively.

2.2. Descriptive Statistics

Table 1 summarizes the descriptive statistics of the daily returns of the main and SME markets in Saudi Arabia and Egypt. Looking at Table 1, it seems that the data characteristics of the return series are considerably different across the full sample and subperiods for both the main and SME market indices. While the NOMU and NILEX saw highly positive returns during the COVID-19 pandemic, the EGX 30 returns experienced a sharp drop and were negative, on average, during the pandemic period. Similarly, the TASI returns witnessed an overall decline after the emergence of COVID-19, although the drop was less severe than that of the EGX30. The volatility (standard deviation) of the daily return was consistently higher across the board during the COVID-19 pandemic than before the pandemic crisis. The findings on skewness are mixed; however, for both the main and SME indices of the Saudi and Egyptian markets. For example, before the COVID-19 pandemic, the Saudi SME stock market, the NOMU, exhibited the most positively skewed returns, indicating that there was a higher probability that investors would earn positive rather than negative returns from the Saudi SME market. Excess kurtosis was found in all the market indices across the entire sample and in all the subperiods, indicating deviations from the normal distribution. These results confirm that the probability distribution of the sample return is asymmetric and leptokurtic, as normality is strongly rejected by the Jarque–Bera test. Furthermore, the ADF (Dickey and Fuller 1981) and PP (Phillips and Perron 1988) unit root tests were used to examine the stochastic properties of the return series. The null hypothesis of a unit root was rejected across the board, indicating that all the return series under study were stationary processes. The results that emerge from the Ljung–Box $Q(5)$ and $Q^2(5)$ tests for the serial correlation of residuals and squared residuals, respectively, as well as the ARCH effect in the return series from the application of the LM–ARCH (5) test highlight the presence of both serial correlation and ARCH effects in all the market indices for the full sample before and during the COVID-19 pandemic, which supports the use of GARCH-type models to investigate the dynamic correlation and volatility spillovers among the main and SME stock markets.

Table 1. Descriptive statistics of daily stock market returns.

	Full Sample Period				Before the COVID-19 Crisis				During the COVID-19 Crisis			
	Saudi Arabia		Egypt		Saudi Arabia		Egypt		Saudi Arabia		Egypt	
	TASI	NOMU	EGX 30	NILEX	TASI	NOMU	EGX 30	NILEX	TASI	NOMU	EGX 30	NILEX
Mean (%)	0.0213	0.1260	0.0332	0.0087	0.0250	0.0264	0.0527	−0.0379	0.0111	0.462	−0.114	0.383
S.D. (%)	1.898	2.824	1.362	1.011	0.857	2.226	1.299	0.813	2.123	4.186	1.786	1.946
Skew.	−3.633	0.413	−0.500	0.261	−0.033	1.267	−0.181	−0.150	−4.109	−0.249	−1.336	−0.062
Kurt.	6.960	14.380	8.021	5.350	10.678	40.90	6.306	5.294	3.992	7.432	9.931	2.057
J-B [Prob]	12312.1 [0.0000]	12298.3 [0.0000]	2088.45 [0.0000]	461.74 [0.0000]	1820.32 [0.0000]	44567.57 [0.0000]	783.49 [0.0000]	379.27 [0.0000]	13832.7 [0.0000]	192.34 [0.0000]	487.52 [0.0000]	7.989 [0.0184]
ADF test	−11.40 ***	−33.02 ***	−34.48 ***	−27.42 ***	−25.96 ***	−25.65 ***	−33.03 ***	−30.36 ***	−4.89 ***	−17.92 ***	−10.89 ***	−10.13 ***
PP test	−34.43 ***	−33.04 ***	−34.42 ***	−31.08 ***	−26.00 ***	−25.62 ***	−33.02 ***	−29.78 ***	−18.55 ***	−17.92 ***	−10.90 ***	−10.45 ***
ARCH-LM(5)	59.02 ***	79.35 ***	273.66 ***	472.49 ***	11.67 ***	177.4 ***	135.31 ***	235.4 ***	15.23 ***	18.66 ***	66.95 ***	15.37 **
Q(5)	32.21 ***	31.43 ***	8.280 *	15.90 ***	5.43 ***	4.61	5.31	18.125 ***	32.1 ***	3.57	10.2 ***	8.76 *
Q ² (5)	82.85 ***	135.06 ***	455.77 ***	1089.7 ***	11.92 ***	200.34 ***	197.52 ***	459.5 ***	17.79 ***	21.77 ***	108.11 ***	19.52 ***
$\rho_{MAIN/SME}$	0.320	-	0.308	-	0.125	-	0.40	-	0.44	-	0.136	-

Notes: The table reports the descriptive statistics of the return series, including the mean (Mean), standard deviation (S.D.), skewness (Skew.), and kurtosis (Kurt.). The critical values for the ADF (Dickey and Fuller 1981) and PP (Phillips and Perron 1988) tests are −3.436 and −2.864 for the 1% and 5% significance levels, respectively. J-B is the normality test of Jarque and Bera (1980), and its test statistic is reported along with its associated *p*-values in square brackets. The LM-ARCH (5) test refers to the Engle (1982) test for conditional heteroscedasticity. Q(5) represents the 5th lagged Ljung–Box Q statistics for the residuals. Q²(5) represents the 5th lagged Ljung–Box Q statistics for the squared residuals. $\rho_{MAIN/SME}$ is Pearson's correlation coefficient. TASI (NOMU) denotes the Saudi main stock market index (SME stock market index). EGX 30 (NILEX) denotes the Egyptian main stock market index (SME stock market index). *, **, and *** denote significance at the 10%, 5%, and 1% levels, respectively.

Moving to the bivariate correlations, we can see that the unconditional correlation coefficients between the main and SME stock markets were positive and clearly varied across the subperiods. This implies that there was a link between the main and SME stock markets and that both moved in the same direction. The NOMU showed the highest correlation with the TASI during the COVID-19 pandemic, while the NILEX exhibited the highest correlation with the EGX30 before the COVID-19 pandemic. On the other hand, the NILEX was found to be weakly correlated with the EGX30 during the COVID-19 pandemic. Hence, the main markets exhibited mixed correlations with the SME markets in both Saudi Arabia and Egypt, indicating potential short-run portfolio diversification benefits. However, these results should be cautiously interpreted, as linear correlations do not fully capture the time-varying linkages between these markets.

Figure 1 provides a plot of the main versus SME market indices for Saudi Arabia and Egypt. The figure shows evidence of positive co-movement between the main and SME indices in general. The strength of the co-movement, however, varies considerably across markets and subsamples. The NOMU tended to move more closely with the TASI during the pandemic than in the pre-pandemic period. However, the opposite is true for the co-movement between the NILEX and the EGX30, which weakened during the pandemic. The weak co-movement between the two Egyptian indices may be partially driven by the significant capital outflows of more than USD 15 billion that pulled out from the Egyptian market in a flight to safety.⁸ It is plausible to suggest that the sell-off has perhaps affected the main market index more severely compared to the SME market index. Naturally, SME markets are regulated to attract investors with longer horizons and are less prone to hot money flows. This is in line with the variation in correlation coefficients reported earlier in Table 1. In addition, during the COVID-19 pandemic (represented by the shaded area of the graph), we can see that the SME stock markets for both Saudi Arabia and Egypt enjoyed an upward trend, whereas the main stock markets suffered a massive decline in the same period. The apparent resilience of both SME markets, in the beginning of the pandemic,

coincides with the reforms and development programs in the SME markets in Saudi and Egypt. The impact of these reforms is evident by the considerable increase in trading volume between 2019 and 2020 (see Table A1). Indeed, all the indices have rebounded during the later phases of the pandemic thanks to the economic stimulus measures taken by both the Saudi and Egyptian governments, which greatly alleviated the impact of the lockdown. Figure 2 depicts the squared return for the main and SME stock markets. Each series displays several periods of volatility clustering, particularly around the COVID-19 pandemic, with the effect being more pronounced for the SME indices (NILEX and NOMU).

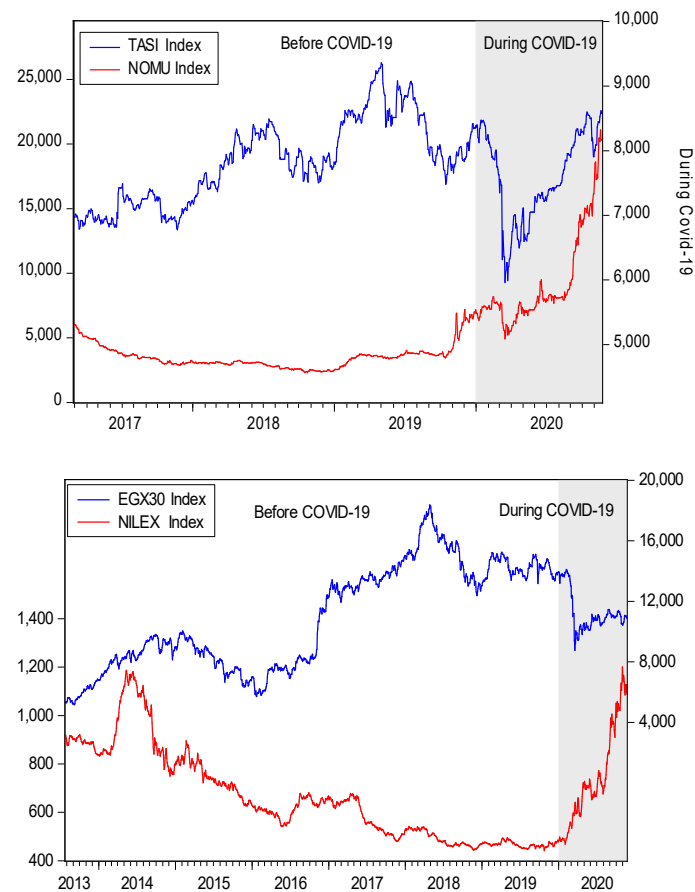


Figure 1. Co-movements between the main and SME stock markets.

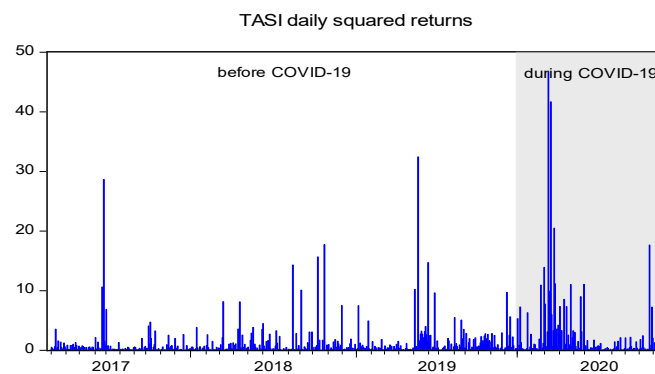


Figure 2. Cont.

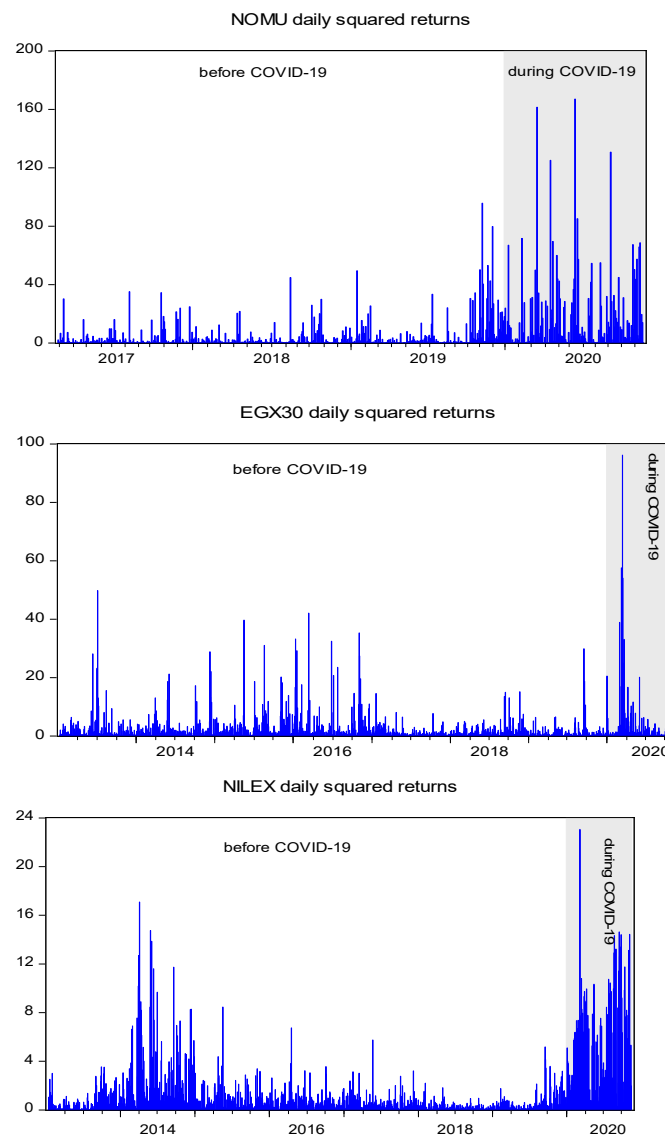


Figure 2. Squared returns of the main and SME stock markets.

2.3. Preliminary Analysis

2.3.1. Asymmetric Causality Test between the Main and SME Stock Markets

We examine the possibility of asymmetric causality between each pair of main/SME stock indices for both Saudi Arabia and Egypt by using the cumulative sums of positive and negative shocks. The main desirable feature of the asymmetric causality test is its ability to distinguish the potential causal impacts of positive shocks from those of negative shocks, which provides insights for the portfolio selection based on different market phases (see, e.g., [Jin et al. 2020](#); [Nguyen et al. 2015](#); [Tiwari and Albulescu 2016](#); [Yarovaya and Lau 2016](#)). To this end, we employ the asymmetric causality test proposed by [Hatemi-J \(2012\)](#), whereby the level price of each index is modelled as a driftless random walk process as follows:

$$P_t = P_{t-1} + \varepsilon_t = P_0 + \sum_{i=1}^t \varepsilon_i \quad (1)$$

where $t = 1, 2, \dots, T$ is the number of observations, and the constant P_0 is the initial price of the underlying index. ε_t is a white noise disturbance term of the underlying index. Positive and negative shocks to each index are first defined as $\varepsilon_i^+ = \text{Max}(\varepsilon_i; 0)$, $\varepsilon_i^- = \text{Min}(\varepsilon_i; 0)$. Then, the positive and negative shocks to each index are defined in a cumulative form

as $P_t^+ = \sum_{i=1}^t \varepsilon_i^+$, $P_t^- = \sum_{i=1}^t \varepsilon_i^-$. Next, the asymmetric causality effect between each pair of main/SME indices is calculated. For example, to determine the impact of decreases in the TASI return on decreases in the NOMU return, we test the hypothesis of Granger causality from the return of $P_{TASI,t}^-$ to the return of $P_{NOMU,t}^-$ within the context of a bivariate VAR system.

Table 2 presents the results of the asymmetric causality test for the full sample, for the period before the COVID-19 pandemic and for the period during the COVID-19 pandemic. The results show that on the one hand, the transmission of both positive and negative shocks from the SME market to the main market is evident over the full sample period (except in the case of the hypothesis that $NILEX^+ \nRightarrow EGX30^-$, which cannot be rejected). The causality structure, in fact, changes across subsamples (the periods before and during the COVID-19 pandemic) and across markets. On the other hand, reverse information transmission, running from the main market to the SME market, is also evident for the same market phases. However, causality is more apparent during the COVID-19 pandemic crisis than before the outbreak of COVID-19, particularly for Saudi Arabia. For example, positive returns on the NOMU drove positive returns on the TASI during the COVID-19 pandemic, while negative returns on the TASI did not necessarily cause negative returns on the NOMU in the same period. Therefore, the negative changes in the NOMU caused a positive change in the TASI, while an effect in the reverse direction is not evident. The asymmetric causality test indicates no causal linkages between the NILEX and the EGX30 during the COVID-19 pandemic. As we mentioned earlier, the weak linkages may be due to the sell-off by investors predominantly in the main market while the SME market did not experience pull-outs of the same intensity. The overall evidence displays a pattern of rich asymmetric causality between the main and SME stock market returns and clearly suggests that ignoring the asymmetry in their relationships may lead to erroneous conclusions.

Table 2. Asymmetric causality between the main and SME stock markets.

Null Hypothesis	Full Sample Period		Before COVID-19		During COVID-19	
	F Statistic	Prob.	F Statistic	Prob.	F Statistic	Prob.
Panel A: Saudi Arabia						
$TASI^- \nRightarrow NOMU^-$	6.150	0.2531	2.689	0.2606	7.9111	0.2447
$TASI^+ \nRightarrow NOMU^+$	4.697	0.6975	14.067 *	0.0800	11.689	0.1112
$TASI^- \nRightarrow NOMU^+$	17.790 **	0.0129	10.7162	0.2183	7.2451	0.5104
$TASI^+ \nRightarrow NOMU^-$	49.037 ***	0.0000	5.676	0.1285	71.596 ***	0.0000
$NOMU^- \nRightarrow TASI^-$	62.792 ***	0.0000	10.375 ***	0.0056	34.181 ***	0.0000
$NOMU^+ \nRightarrow TASI^+$	31.515 ***	0.0001	8.1965	0.4145	17.133 ***	0.0001
$NOMU^- \nRightarrow TASI^+$	21.510 ***	0.0001	13.983	0.1000	21.790 ***	0.0003
$NOMU^+ \nRightarrow TASI^-$	21.226 ***	0.0017	3.5871	0.3096	9.3461	0.1550
Panel B: Egypt						
$EGX30^- \nRightarrow NILEX^-$	23.157 **	0.0016	13.680 ***	0.0084	9.341 *	0.0531
$EGX30^+ \nRightarrow NILEX^+$	14.222 **	0.0143	13.123 ***	0.0004	5.7398	0.1250
$EGX30^- \nRightarrow NILEX^+$	2.011	0.8475	9.369 *	0.0952	1.5012	0.8460
$EGX30^+ \nRightarrow NILEX^-$	24.279 ***	0.0001	28.693 ***	0.0000	3.1651	0.2054
$NILEX^- \nRightarrow EGX30^-$	17.421 **	0.0149	10.203 ***	0.0001	6.2447	0.1816
$NILEX^+ \nRightarrow EGX30^+$	36.819 ***	0.0000	5.0603	0.1674	7.201 ***	0.0007
$NILEX^- \nRightarrow EGX30^+$	17.955 ***	0.0030	9.0561	0.1069	0.2396	0.9934
$NILEX^+ \nRightarrow EGX30^-$	1.428	0.8392	0.4557	0.9777	0.2762	0.8710

Notes: This table reports the Hatemi-J (2012) asymmetric causality test F statistics and p-values. $A \nRightarrow B$ means that variable A does not Granger cause variable B. (+) denotes positive shocks, while (−) denotes negative shocks. The VAR system of order 1 is selected using the Akaike information criterion (AIC). TASI (NOMU) denotes the Saudi main stock market index (SME stock market index). EGX30 (NILEX) denotes the Egyptian main stock market index (SME stock market index). *, **, and *** denote significance at the 10%, 5%, and 1% levels, respectively.

2.3.2. Directional Connectedness between the Main and SME Stock Markets

To examine the nature of the volatility connectedness between the main and SME stock markets, we use the spillover index approach developed by [Diebold and Yilmaz \(2014\)](#). This approach is based on forecast error variance decomposition, in which the forecast error variance of a variable is decomposed into parts attributed to the other variable in the VAR system. The main goal of this spillover index approach is to explore the total, directional, and net directional spillover effects for cross-stocks (see, e.g., [Al-Yahyaee et al. 2019](#); [Bahloul and Khemakhem 2021](#); [Jin et al. 2020](#); [Wu et al. 2019](#); [Xu et al. 2019](#); [Zhang and Hamori 2021](#)). Following [Diebold and Yilmaz \(2014\)](#), we denote $d_{i,j}(H)$ as the fraction of variable i 's H -step forecast error variance due to shocks in variable j . The total directional connectedness from others to variable i is $TDC_{i\leftarrow}(H) = \sum_{j=1, j \neq i}^2 d_{i,j}(H)$, and the total directional connectedness from others to j is $TDC_{\leftarrow j}(H) = \sum_{i=1, i \neq j}^2 d_{i,j}(H)$. The net total directional connectedness (NTDC)⁹ to others is obtained by taking the difference between the total directional connectedness to others and the total directional connectedness from others.

Table 3 reports the decomposition of the total volatility spillover index between the main and SME stock market volatilities for a forecast horizon of 10 days before and during the COVID-19 pandemic. Panel A of Table 3 shows that the volatility spillovers during the COVID-19 pandemic were significantly higher than those before the COVID-19 pandemic for Saudi Arabia. The total spillover index reached 12.7%, which indicates the importance of spillovers during the COVID-19 pandemic relative to those during the pre-COVID-19 period, when the total spillover index was only 1.6%. Conversely, panel B of Table 3 provides contrasting results for Egypt, as the total spillover index is found to be substantially higher before the pandemic (8% before the COVID-19 crisis and only 1% during the crisis). Overall, the main stock markets in both Saudi Arabia and Egypt are identified as net transmitters of volatility in the periods before and during the COVID-19 pandemic.

Table 3. Total and directional spillovers between the main and SME markets.

Before COVID-19 Crisis				During COVID-19 Crisis		
Panel A: Saudi Arabia						
	TASI	NOMU	From others	TASI	NOMU	From others
TASI	99.8	0.2	0.2	94.4	5.6	5.6
NOMU	3	97	3	19.8	80.2	19.8
To others	3	0.2		19.8	5.6	
Net spillover	2.8	−2.8	Total spillover index = 1.6%	14.2	−14.2	Total spillover index = 12.7%
Panel B: Egypt						
	EGX 30	NILEX	From others	EGX 30	NILEX	From others
EGX30	99.8	0.2	0.2	100	00	00
NILEX	15.8	84.2	15.8	1.7	98.3	1.7
To others	15.8	0.2		1.7	00	
Net spillover	15.6	−15.6	Total spillover index = 8%	1.7	−1.7	Total spillover index = 1%

Notes: This table reports total, directional, and pairwise spillover values based on the approach of [Diebold and Yilmaz \(2014\)](#). The upper-left 2×2 block in each panel contains the variance decomposition based on 10-step-ahead forecasts. The off-diagonal entries measure the pairwise directional connectedness, while the bottom-right element is the total spillover index, which is the average of the 'from others' column or the 'to others' row. The underlying variance decomposition is based upon a bivariate VAR of order 1, which is selected using the Akaike information criterion (AIC). The main and SME market volatilities are measured by the conditional variances obtained from the GJR–GARCH model of [Glosten et al. \(1993\)](#). TASI (NOMU) denotes the volatility of Saudi main stock market index (SME stock market index) returns. EGX30 (NILEX) denotes the volatility of Egyptian main stock market index (SME stock market index) returns.

Figure 3 displays the dynamics of the total spillover index and shows substantial fluctuations in the volatility spillovers between the main and SME markets in both Saudi Arabia and Egypt. Before the COVID-19 pandemic, the volatility spillovers between the TASI and NOMU moved relatively smoothly, fluctuating between 2 and 7%. However, with the onset of the pandemic, spillovers jumped to 12% at the beginning of March 2020 and steadily declined, hovering at approximately 7% until the end of the sample period, a result that is in line with previous studies, including those by [Akhtaruzzaman et al. \(2021a\)](#) and [Elsayed and Yarovaya \(2019\)](#). For Egypt, Figure 3 points to a different story, as the values of the total spillover index decreased sharply during the COVID-19 pandemic. The average volatility spillovers of the EGX30 and NILEX appear higher for the period before the COVID-19 crisis than the average spillovers for the COVID-19 pandemic period. Indeed, these findings are commensurate with results obtained from preliminary analyses. Among the possible explanations for this seemingly perplexing result is that the trading and investment strategies of market participants vary across the different time scales in association with different trading and investment horizons ([Wang et al. 2016, 2017](#); [Xu and Hamori 2012](#)). This is evident with the benefit of hindsight as the Egyptian exchange experienced a huge sell-off during the early phases of the pandemic in the main rather than the SME market. Portfolio managers and speculators should, therefore, consider crisis periods when designing risk management portfolios.

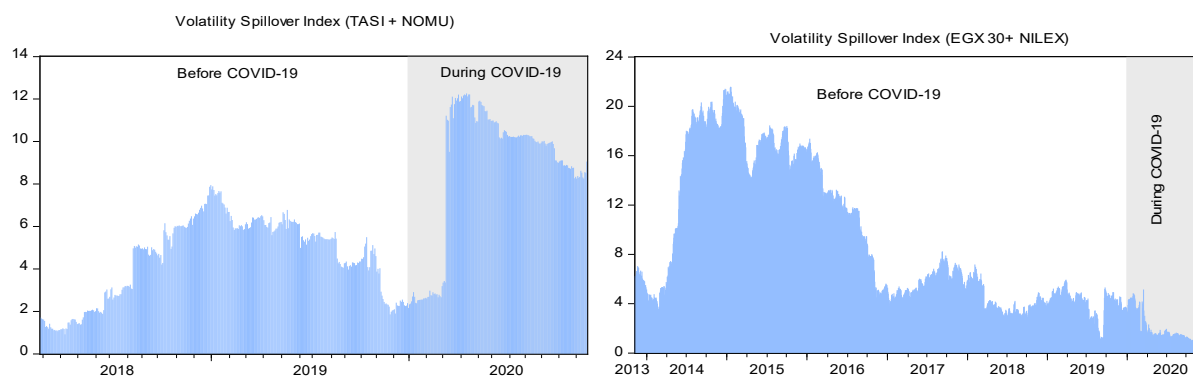


Figure 3. Dynamic total volatility spillover indices based on the [Diebold and Yilmaz \(2014\)](#) framework. Notes: Dynamic spillover indices are calculated from the forecast error variance decompositions on 10-step-ahead forecasts. The total spillover indices are estimated by using 200-day rolling windows for the full sample period. TASI (NOMU) denotes the Saudi main stock market index (SME stock market index). EGX30 (NILEX) denotes the Egyptian main stock market index (SME stock market index).

3. Materials and Methods

To examine the features of risk and return transmission and the dynamic correlations between main and SME markets, we employed the VAR-asymmetric BEKK–GARCH model to examine the volatility spillover effect and asymmetries in the variance–covariance structure for main and SME returns. Additionally, the asymmetric DCC–GARCH model was employed in this paper with the aim of exploring the dynamic correlations that are used to compute optimal portfolio weights and hedge ratios.¹⁰

3.1. The Asymmetric BEKK–GARCH Model

The asymmetric version of the BEKK–GARCH model introduced by [Engle and Kroner \(1995\)](#) and later developed by [Kroner and Ng \(1998\)](#) was used in this study to examine shock and asymmetric volatility spillovers between markets. This version of the model has shown many advantages for investigations of volatility spillovers among two series (see, e.g., [Boldanov et al. 2016](#); [Majumder and Nag 2018](#); [Vardar et al. 2018](#); [Wen et al. 2014, 2020](#); [Yu et al. 2020](#)). In this paper, we used the bivariate VAR (1)-asymmetric BEKK–GARCH (1,1) model to examine the dynamic spillover effects between main and SME market stocks.

Following Iglesias-Casal et al. (2020) and Asl et al. (2021), the conditional mean equations for the main and SME markets are represented by the following VAR(1) system:

$$R_t = \mu + \Phi R_{t-1} + \varepsilon_t \quad (2)$$

with $R_t = \begin{bmatrix} R_{main,t} \\ R_{SME,t} \end{bmatrix}$, $\mu = \begin{bmatrix} \mu_{main} \\ \mu_{SME} \end{bmatrix}$, $\Phi = \begin{bmatrix} \varphi_{11} & \varphi_{12} \\ \varphi_{21} & \varphi_{22} \end{bmatrix}$, and $R_{t-1} = \begin{bmatrix} R_{main,t-1} \\ R_{SME,t-1} \end{bmatrix}$, and $\varepsilon_t = \begin{bmatrix} \varepsilon_{main,t} \\ \varepsilon_{SME,t} \end{bmatrix}$, where $C = (c_1, c_2)'$ is a (2×1) vector of constant terms; $R_{main,t}$ and $R_{SME,t}$ are the returns of the main and SME stock markets at time t , respectively; and φ_{11} and φ_{22} represent the diagonal elements of the matrix φ , which captures a unidirectional causal relation between past returns and current returns in the same market, whereas the off-diagonal elements φ_{12} and φ_{21} measure the cross-mean spillovers between the main and SME stock markets. $\varepsilon_{main,t}$ and $\varepsilon_{SME,t}$ are the residual terms for the main and SME stock markets' conditional mean equations, respectively, such that $\varepsilon_t = H_t^{1/2} \eta_t$. η_t refers to the innovation (shock) term and is an *i.i.d.* distributed random process: $\eta_t \xrightarrow{iid} N(0, 1)$.

The time-varying conditional variance-covariance matrix H_t is given by the following:

$$H_t = C'C + A'\varepsilon_{t-1}\varepsilon'_{t-1}A + B'H_{t-1}B + D'\nu_{t-1}\nu'_{t-1}D \quad (3)$$

$$\text{with } H_t = \begin{bmatrix} h_{main,t} & h_{main/SME,t} \\ h_{SME/main,t} & h_{SME,t} \end{bmatrix}, C = \begin{bmatrix} C_{11} & 0 \\ C_{21} & C_{22} \end{bmatrix}, A = \begin{bmatrix} a_{11} & a_{12} \\ a_{21} & a_{22} \end{bmatrix}, B = \begin{bmatrix} b_{11} & b_{12} \\ b_{21} & b_{22} \end{bmatrix}, \varepsilon_{t-1}\varepsilon'_{t-1} = \begin{bmatrix} \varepsilon_{main,t-1}^2 & \varepsilon_{main,t-1}\varepsilon_{SME,t-1} \\ \varepsilon_{SME,t-1}\varepsilon_{main,t-1} & \varepsilon_{SME,t-1}^2 \end{bmatrix},$$

$$H_{t-1} = \begin{bmatrix} h_{main,t-1} & h_{main/SME,t-1} \\ h_{SME/main,t-1} & h_{SME,t-1} \end{bmatrix}, \text{ and } D = \begin{bmatrix} d_{11} & d_{12} \\ d_{21} & d_{22} \end{bmatrix}, \nu_{t-1} = \begin{bmatrix} \max(0, -\varepsilon_{1,t-1}) \\ \max(0, -\varepsilon_{2,t-1}) \end{bmatrix},$$

where matrix C is a lower triangular matrix of the constant term. Matrix A represents the ARCH coefficients of the model whose diagonal elements a_{11} and a_{22} capture the own ARCH effect of the fluctuations of the main and SME stock markets, whereas the off-diagonal elements a_{12} and a_{21} of matrix A represent the cross-shock spillover between the main and SME stock markets. Matrix B represents the GARCH coefficients of the model whose diagonal elements b_{11} and b_{22} capture the GARCH effect of the main and SME markets themselves, reflecting the persistence of volatilities in each market, while the off-diagonal elements b_{12} and b_{21} present the cross-volatility spillovers between the main and SME stock markets. D is a matrix of coefficients that capture asymmetry in response to shocks whose diagonal elements d_{11} and d_{22} represent the own-asymmetric shock spillovers and capture the asymmetric response of the current conditional variance to own past negative shocks, whereas off-diagonal elements d_{12} and d_{21} represent the cross-asymmetric shock spillovers and capture the asymmetric response of the current conditional variance due to past negative shocks from another market.

We estimated the bivariate VAR (1)-asymmetric BEKK-GARCH (1,1) model by using the full information maximum-likelihood method (Engle and Kroner 1995; Kroner and Ng 1998). Under the normality assumption,¹¹ the log-likelihood function, $L(\theta)$, can be written as follows:

$$L(\theta) = -T \log(2\pi) - \frac{1}{2} \sum_{t=1}^T \log |H_t(\theta)| - \frac{1}{2} \sum_{t=1}^T \varepsilon_t(\theta)' H_t^{-1} \varepsilon_t(\theta) \quad (4)$$

where T is the number of observations and θ indicates the vector of estimated coefficients. The BFGS algorithm was then used to obtain the final estimates of the variance-covariance matrix and the corresponding standard errors.

3.2. The Asymmetric DCC–GARCH Model

To further investigate the dynamics underlying dynamic volatilities and correlations, we employed an asymmetric DCC–GARCH (1,1) model developed by [Cappiello et al. \(2006\)](#) that is based on the DCC model of [Engle \(2002\)](#). The model takes into account conditional asymmetries in both volatilities and dynamic correlations, and it allows the modelling of time-varying correlations during a period of negative shocks in a multivariate setting (see, e.g., [Basher and Sadorsky 2016](#); [Hou and Li 2016](#)). Indeed, it is necessary to take these asymmetric effects into consideration, especially in constructing portfolio weights and formulating hedging strategies (see, e.g., [Jin et al. 2020](#)). The conditional mean equations of the asymmetric DCC–GARCH (1,1) are represented by the following VAR (1) system:

$$\begin{cases} R_t = \mu + \Phi R_{t-1} + \varepsilon_t \\ \varepsilon_t = H_t^{1/2} \eta_t \end{cases} \quad (5)$$

where R_t , C , and Φ are defined in the mean equation of the asymmetric BEKK model. H_t is the variance–covariance matrix defined as follows:

$$H_t = D_t R_t D_t \quad (6)$$

where $D_t = \text{diag}\left(\sqrt{h_t^{\text{main}}}, \sqrt{h_t^{\text{SME}}}\right)$ represents a diagonal matrix of standard deviations obtained from the estimation of the univariate GARCH (1,1) model, which includes the leverage effect. For each pair of main/SME market indices, the equations for the conditional variance using GJR–GARCH (1,1) with spillovers (see [Ling and McAleer \(2003\)](#), [McAleer et al. \(2009\)](#), [Salisu and Oloko \(2015\)](#) and [Singhal and Ghosh \(2016\)](#)) are given by the following:

$$h_{ii,t} = \omega_{ii} + \sum_{j=1}^2 \alpha_{ij} \varepsilon_{j,t-1}^2 + \sum_{j=1}^2 \beta_{ij} h_{jj,t-1} + d_i \varepsilon_{i,t-1}^2 I(\varepsilon_{i,t-1}) \quad (7)$$

where $I(\varepsilon_{i,t-1})$ is an indicator function that equals 1 if $\varepsilon_{i,t-1} < 0$ and 0 otherwise. Hence, in the asymmetric DCC model, the negative residuals increase the variance more than the positive residuals if the value for d_i is positive. R_t is a time-varying conditional correlation matrix given by the following:

$$R_t = \left[\rho_t^{\text{main/SME}} \right] = \text{diag}(Q_t)^{-1/2} Q_t \text{diag}(Q_t)^{-1/2} \quad (8)$$

[Cappiello et al. \(2006\)](#) define the correlation evolution as follows:

$$Q_t = (\bar{P} - A' \bar{P} A - B' \bar{P} B - G' \bar{N} G) + A' \varepsilon_{t-1} \varepsilon_{t-1}' A + B' Q_{t-1} B + G' \eta_{t-1} \eta_{t-1}' G \quad (9)$$

where \bar{N} and G are the unconditional correlation matrices and $\eta_t = I[\varepsilon_t < 0]$ is equal to 1 and 0 otherwise. In the asymmetric DCC–GARCH (1,1) case, matrices A , B , and G are measured by scalars (a , b , g). To secure the positive definite constraint of Q_t , the intercept $\bar{P} - A' \bar{P} A - B' \bar{P} B - G' \bar{N} G$ must be positive semidefinite, and the initial covariance matrix Q_0 must be positive definite. This model is estimated by using the quasi-maximum likelihood (QML) technique based on the Berndt–Hall–Hall–Hausman (BHHH) optimization algorithm.

3.3. Optimal Portfolio Allocation and Risk Management

3.3.1. Optimal Portfolio Weights

The existence of risk spillovers between the two assets indicates that investors' assets in both markets are more volatile and more susceptible to risk and uncertainty ([Salisu et al. 2021](#)). Indeed, investigating the optimal portfolio structure over the sample period could provide valuable insight as to what extent the COVID-19 pandemic has impacted the investors' asset allocation decision. To this end, we employed the conditional variance and

covariance estimated from the bivariate VAR (1)-asymmetric DCC–GARCH (1,1) model to compute portfolio weights. The approach outlined by Kroner and Ng (1998) was used to form a portfolio that minimizes risk without lowering expected returns. The optimal weight of SME stocks in a one-dollar portfolio of main/SME stocks at time t is given by the following:

$$w_t^{main/SME} = \frac{h_t^{main} - h_t^{main/SME}}{h_t^{main} - 2h_t^{main/SME} + h_t^{SME}} \quad (10)$$

As we assumed that portfolio holdings are fully invested with no short positions allowed, the portfolio weights are constrained to be nonnegative and to sum to one as follows:

$$w_t^{main/SME} = \begin{cases} 0 & \text{if } w_t^{main/SME} < 0 \\ w_t^{main/SME} & \text{if } 0 \leq w_t^{main/SME} \leq 1 \\ 1 & \text{if } w_t^{main/SME} > 1 \end{cases} \quad (11)$$

where $w_t^{main/SME}$ is the weight of SME stock in a one-dollar portfolio of the two assets (from the main and SME stock markets) at time t and the term, h_t^{main} represents the conditional variance of the main market index at time t , $h_t^{main/SME}$ represents the conditional covariance between the main and SME stock markets at time t while h_t^{SME} represents the conditional variance of the SME market index at time t . The corresponding weight of the main index in this portfolio is $1 - w_t^{main/SME}$.

3.3.2. Dynamic Optimal Hedge Ratios

Hedging is the best tool for mitigating the risks of investing in volatile assets. The optimal hedge ratio is defined according to Kroner and Sultan (1993), who consider a portfolio of two assets and argue that the risk of the investment portfolio is minimized when the acquisition of one dollar of the first asset is hedged by a short position of β_t dollars in the second asset. The optimal hedge ratio between main/SME market stocks is given by the following:

$$\beta_t^{main/SME} = \frac{h_t^{main/SME}}{h_t^{SME}} \quad (12)$$

Here, a long position of one dollar in the main market was hedged by shorting $\beta_t^{main/SME}$ dollars in the SME market to minimize the portfolio risk. Then, following Ederington (1979), we computed the hedging effectiveness index (HEI) to gauge the performance of the optimal hedging strategies. The hedging effectiveness index, which represents the gain or loss in the variance of the hedged portfolio in comparison to that of the unhedged portfolio, is defined as follows:

$$HEI = \left[\frac{Var_{unhedged} - Var_{hedged}}{Var_{unhedged}} \right] \quad (13)$$

where variance unhedged represents the variance in the main stock market return and variance hedged represents the variance in the return on the main/SME stock market portfolios. A higher HEI value indicates greater risk reduction, which implies that the investment method can be considered a superior hedging strategy. More interestingly, when the HEI is close to one, it means that the hedge strategy is perfect.

3.3.3. Hedging Effectiveness during the COVID-19 Pandemic

Risk management and asset portfolio allocation emerge as important issues during crisis periods. In this sense, Junttila et al. (2018) emphasize the importance of examining hedging performance during market turmoil as the demand for hedging instruments generally increases.¹² To ascertain whether SME stocks are a suitable hedging instrument for main stocks in both the Saudi and Egyptian markets, particularly for the COVID-19 pandemic period, we compared the HEI values during the COVID-19 pandemic with the

HEI values before the pandemic (see, e.g., Jin et al. 2020). Thus, we calculated ΔHEI in the following manner:

$$\Delta HEI = HEI_{during\ COVID-19} - HEI_{before\ the\ COVID-19\ period} \quad (14)$$

A positive value of ΔHEI indicates a better hedging performance during the COVID-19 pandemic.

4. Empirical Results and Discussion

In this section, we first present the results obtained from estimating the bivariate VAR (1)-asymmetric BEKK–GARCH (1,1) and the bivariate VAR (1)-asymmetric DCC–GARCH (1,1) models in Sections 4.1 and 4.2, respectively.¹³ Then, we discuss portfolio weight analysis as well as hedging strategies and their hedging effectiveness, particularly during the COVID-19 pandemic, in Section 4.3.

4.1. Returns and Risk Spillovers between the Main and SME Stock Markets

Table 4 reports the estimation results of the bivariate VAR (1)-asymmetric BEKK–GARCH (1,1) model for the Saudi and Egyptian main and SME stock markets for the full sample period, the period before the COVID-19 pandemic and the period during the COVID-19 pandemic. Panel A of Table 4 shows that the returns on the main market indices (TASI and EGX30) are strongly affected by their own lagged values, as the estimates of the diagonal element (φ_{11}) are found to be statistically significant over the entire sample and the two subsamples at the 5% level at least. These effects are positive in the returns on the TASI and EGX30 for the full sample period and for the period before the COVID-19 pandemic, indicating persistence, but negative in the TASI returns for the COVID-19 pandemic period, indicating a downward drift in the TASI. Similarly, the estimates of the other diagonal element (φ_{22}) indicate that the SME markets (NOMU and NILEX) display significant initial lag dependence across the board at the 5% level at least. While the NILEX is positively affected by its own lagged values, the impact of the NOMU's own lagged value is found to be persistently negative. Thus, we can see that both the main and SME markets in Saudi Arabia and Egypt show short-term predictability, which casts doubt on the efficient market hypothesis in its weak form for both the main and SME markets.

Table 4. Estimation results of the bivariate VAR (1)-asymmetric BEKK–GARCH (1,1) model.

	Full Sample Period		Before the COVID-19 Crisis		During the COVID-19 Crisis	
	TASI and NOMU	EGX30 and NILEX	TASI and NOMU	EGX30 and NILEX	TASI and NOMU	EGX30 and NILEX
Panel A: Mean equation (return spillover effect)						
	Dependent variable : R_{main}					
μ	0.00441 (0.03652)	0.02496 (0.02386)	0.03081 (0.03035)	0.03547 (0.02400)	0.18085 ** (0.07248)	0.00300 (0.07981)
$R_{main}(-1) - \varphi_{11}$	0.16369 *** (0.04343)	0.24139 *** (0.02293)	0.08339 ** (0.04230)	0.23174 *** (0.02495)	−0.19311 *** (0.08229)	0.22984 *** (0.07140)
$R_{SME}(-1) - \varphi_{12}$	0.02293 ** (0.01410)	−0.01629 (0.02555)	0.01402 ** (0.00563)	−0.00342 (0.03445)	0.01955 (0.01786)	−0.04440 (0.04208)
	Dependent variable : R_{SME}					
μ	−0.10026 (0.07192)	−0.02204 (0.01343)	−0.12944 ** (0.05494)	−0.02412 ** (0.01398)	0.676519 * (0.20550)	0.25902 ** (0.11792)
$R_{main}(-1) - \varphi_{21}$	0.20119 ** (0.04570)	0.01249 (0.01108)	0.15090 ** (0.06899)	0.01192 (0.01167)	−0.156405 (0.25054)	−0.03511 (0.07178)
$R_{SME}(-1) - \varphi_{22}$	−0.01695 ** (0.04336)	0.25350 *** (0.02071)	−0.01509 ** (0.04411)	0.24408 *** (0.02433)	−0.140690 *** (0.07654)	0.27365 *** (0.05919)

Table 4. Cont.

	Full Sample Period		Before the COVID-19 Crisis		During the COVID-19 Crisis	
	TASI and NOMU	EGX30 and NILEX	TASI and NOMU	EGX30 and NILEX	TASI and NOMU	EGX30 and NILEX
Panel B: Conditional variance equations (volatility spillover effect)						
C_{11}	0.25100 *** (0.03165)	0.43191 *** (0.03992)	0.23309 *** (0.03576)	0.47387 *** (0.04431)	0.17362 *** (0.07161)	0.18913 (0.11962)
C_{21}	0.05366 (0.14411)	0.06673 *** (0.01349)	0.22025 *** (0.08526)	0.04275 *** (0.01644)	−1.70020 *** (0.28934)	−0.18464 (0.48177)
C_{22}	0.76324 *** (0.09685)	−0.00374 (0.25423)	0.37944 *** (0.06072)	0.00000 (0.03578)	−0.00010 (2.63984)	0.51744 ** (0.30220)
a_{11}	0.18592 ** (0.06413)	0.28356 *** (0.03222)	0.14763 ** (0.04705)	0.30402 *** (0.03688)	−0.17436 ** (0.09028)	−0.25080 ** (0.09743)
a_{12}	−0.3409 ** (0.01228)	0.01858 (0.01240)	−0.33526 *** (0.07529)	0.02033 ** (0.01237)	−0.53576 ** (0.33170)	−0.14173 (0.10435)
a_{21}	0.02236 ** (0.01259)	−0.00077 (0.03448)	0.01115 ** (0.01572)	0.04961 ** (0.04788)	−0.04630 ** (0.02040)	−0.03797 (0.05555)
a_{22}	0.53654 *** (0.05210)	0.23443 *** (0.02194)	0.35297 *** (0.03025)	0.22483 *** (0.02131)	0.39969 *** (0.08641)	0.38042 *** (0.09274)
b_{11}	0.92867 *** (0.01425)	0.84554 *** (0.02298)	0.93871 *** (0.01564)	0.81278 *** (0.03000)	0.87824 *** (0.02634)	0.88801 *** (0.03354)
b_{12}	0.20114 *** (0.07706)	−0.03054 *** (0.00823)	−0.00284 (0.03556)	−0.03157 *** (0.00605)	0.08876 *** (0.07783)	0.03975 (0.04175)
b_{21}	−0.02635 *** (0.00939)	0.01965 ** (0.01159)	−0.00734 (0.00569)	0.05273 *** (0.02078)	0.05948 *** (0.01653)	0.03115 (0.04351)
b_{22}	0.78720 *** (0.03936)	0.97586 *** (0.00646)	0.90426 *** (0.01565)	0.98379 *** (0.00455)	0.74097 *** (0.06429)	0.86587 *** (0.07436)
Panel C: Asymmetric effects						
$d_{11}D_{11}$	0.51250 *** (0.05722)	0.35705 *** (0.04325)	0.29036 *** (0.05282)	0.36441 *** (0.05091)	0.44093 *** (0.13762)	0.39200 *** (0.09881)
$d_{12}D_{12}$	−0.08969 (0.18839)	0.04788 *** (0.01702)	0.04534 (0.12402)	0.04897 *** (0.01610)	0.74479 *** (0.42758)	−0.13556 (0.10703)
$d_{21}D_{21}$	0.00078 (0.03402)	0.14860 *** (0.05123)	0.02321 (0.01910)	0.09098 (0.09086)	−0.0455 (0.03653)	0.13555 *** (0.06543)
$d_{22}D_{22}$	0.04242 (0.09771)	0.10959 *** (0.03762)	0.00803 (0.05792)	0.07632 ** (0.05251)	−0.00715 (0.17922)	0.10675 (0.12857)
LL	−2812.210	−5267.420	−2345.689	−4430.582	−1044.956	−807.398
AIC	7.63521	5.51926	6.35543	5.22611	9.08582	7.70187

Notes: Standard errors in parentheses. LL and AIC are the log-likelihood and Akaike information criterion values, respectively. TASI (NOMU) denotes the Saudi main stock market index (SME stock market index). EGX30 (NILEX) denotes the Egyptian main stock market index (SME stock market index). *, **, and *** denote significance at the 10%, 5%, and 1% levels, respectively.

Moving to the off-diagonal elements of matrix φ , we can see that there are significant positive mean spillovers from the SME to the main market but only for Saudi Arabia, i.e., from NOMU stocks to TASI stocks ($\varphi_{12} = 2.3\%$), reaching statistical significance for the full sample period and the period before the COVID-19 pandemic ($\varphi_{12} = 1.4\%$), which indicates that information in the NOMU is transmitted into the pricing process of the TASI. The estimates of the other diagonal element (φ_{21}) are substantially higher and are statistically significant, indicating that the return spillovers from the returns on the TASI

to the returns on the NOMU are stronger and apparent for the full sample ($\varphi_{21} = 20\%$) and the period before the COVID-19 pandemic ($\varphi_{21} = 15\%$), which indicates in turn that an increase in the returns of the TASI positively influences the returns of the NOMU. In contrast, we find no traces of a mean spillover effect from the main to the SME stock market or vice versa in Egypt for any of the three subsample periods.

The linkages between the NOMU and the TASI are partially consistent with those documented by [Nguyen et al. \(2020\)](#), who find evidence for a unidirectional return transmission running from the SME to the main market in Hong Kong only, while the other markets (Thailand, Singapore and Malaysia) display return transmission but in the opposite direction, that is, from the main to the SME market. A plausible explanation for this finding might be the importance of the NOMU market relative to that of the NILEX market (see Table A1 in the Appendix A) in terms of size with respect to the main market. In addition, the NOMU has thus far successfully fulfilled its role as a steppingstone for aspiring SMEs, with more than half of its listed companies graduating to the main market. Therefore, we can think of the NOMU as an indirect contributor to economic growth via the main market channel.¹⁴ This is not the case for the Nile Exchange, however, as only one company has been able to move to the main board since the exchange's inception ([Enterprise 2020b](#)), which may also explain the lack of integration between the SME and main markets in Egypt in addition to the thin trading and minute size of the Egyptian SME market.

Panel B of Table 4 presents the estimated coefficients for the ARCH and GARCH terms, where the former captures the short-run persistence of volatility shocks while the latter measures the long-run persistence. The estimates of the diagonal elements of matrix *A*, i.e., a_{11} and a_{22} , and matrix *B*, i.e., b_{11} and b_{22} , which measure the effects of the own past shock (past volatility) of the main and SME stock markets on conditional present volatility, are statistically significant at least at the 5% level across the board for the full sample and both subsample periods. This shows that the main stock markets (TASI and EGX30) and the SME stock markets (NOMU and NILEX) have strong short-run (ARCH) and long-run (GARCH) persistence. For each index, we note that the estimated a_{11} and a_{22} values are smaller than their respective estimated b_{11} and b_{22} values, indicating that past volatilities are more important than shocks or news in predicting future volatility, consistent with results reported elsewhere.

We now examine how shocks and volatility spillovers are transmitted between the main and SME stock markets. Here, our focus is directed toward the estimates of the off-diagonal elements of matrix *A*, i.e., a_{12} and a_{21} , and matrix *B*, i.e., b_{12} and b_{21} , which measure the interdependencies between the main and SME stock markets that manifest in the form of shock and volatility spillovers between these markets. Panel B of Table 4 reveals some instances where spillovers are found to be bidirectional or absent depending on the subperiod and the market under consideration. The short-term persistence coefficients a_{12} are found to be negative and statistically significant for the periods before and during the COVID-19 pandemic for Saudi Arabia, indicating that short-term shocks originating in the main market have a calming effect on volatility in the SME market in the short run. Similarly, shocks originating from returns on the NOMU stocks measured by a_{21} affect the variability of returns on the TASI for the three sample periods. However, only for the COVID-19 pandemic period do the signs of the shock spillover from the NOMU to the TASI become negative. On the other hand, a bidirectional shock between the variability of returns of the EGX30 and NILEX stocks is documented but only for the pre-COVID-19 pandemic period.

For the long-term volatility spillovers (b_{12} and b_{21} coefficients), the results show the presence of bidirectional volatility spillovers but with different signs for the full period and the pandemic period, whereas significant spillovers are absent for the pre-pandemic period. For the full sample period, the past volatility of the TASI positively affects the current volatility of the NOMU, whereas the past volatility of the NOMU negatively affects the current volatility of the TASI; however, the role of the TASI is much greater than that of the NOMU, which is a qualitatively similar finding to the results obtained using the

Diebold and Yilmaz approach. The COVID-19 pandemic period, however, witnessed positive bidirectional volatility spillovers between the two markets. Likewise, the main and SME markets in Egypt exhibit bidirectional volatility spillovers with different signs and in opposite directions; that is, past volatility on the EGX30 negatively affects current volatility on the NILEX, whereas past volatility on the NILEX positively affects current volatility on the EGX30, which implies a calming effect, mainly from the SME market, in the long run. However, no volatility spillovers between the Egyptian markets are detected for the COVID-19 pandemic period, indicating that neither market was affected by the riskiness of the other. These results are inconsistent with those of [Nguyen et al. \(2020\)](#), who fail to find strong evidence for either shock or volatility spillovers between the main and SME markets in any of the countries that they examine. That said, volatility linkages between markets can arise from the following two different sources: (i) common information that affects more than one market concurrently and (ii) informational spillovers attributable to cross-market hedging ([Fleming et al. 1998](#), p. 112). This could reconcile our findings with others in the literature; for example, [Karmakar \(2010\)](#), [Koulakiotis et al. \(2016\)](#) and [Kyrkilis et al. \(2018\)](#) find strong evidence for feedback in conditional variance between portfolios of small stocks and of large stocks in the Indian and Greek markets, respectively.

Panel C of Table 4 presents the asymmetric volatility spillover effects.¹⁵ The estimates of the diagonal elements of matrix D measuring the asymmetric own shocks to returns given by d_{11} and d_{22} are mixed. On the one hand, the estimates of d_{11} pertaining to the main markets are found to be positive and strongly significant at the 1% level for both markets and for the entire period and both subsamples, which indicates that negative news from the TASI (EGX30 index) amplifies the volatility of the TASI (EGX30 index) to a greater extent than positive news does. Shocks in the TASI show the largest asymmetric effect on its own conditional volatility. On the other hand, the results pertaining to the SME markets show little evidence for an asymmetric own shock to returns as measured by d_{22} , which is limited to the NILEX for the full sample period only.

Looking at the estimates of the off-diagonal elements of matrix D , we find significant asymmetric shock spillover effects between the main and SME markets in both Saudi Arabia and Egypt. Negative shocks from the NILEX index affect the EGX30 index more than positive shocks for the full sample period and the period during the COVID-19 pandemic. The effect is positive, implying that a negative shock from the NILEX index increases the variability of EGX30 index returns. In contrast, negative shocks from the EGX30 stocks exert a positive asymmetric effect on the variability of NILEX stock returns for the full sample period and the period before the COVID-19 pandemic. In addition, asymmetric volatility spillover effects from the TASI to the NOMU index are found to be significant and positive for the COVID-19 pandemic period only. In contrast, there is no asymmetric volatility spillover from the NOMU to the TASI during any of the three periods.

The major findings of this study are as follows: First, the return transmission from the SME to the main market in Saudi Arabia supports the potential role of the SME market as a contributor to economic growth by operating as a pipeline for the main market, which has a direct impact on economic growth. Therefore, all the policies and initiatives that facilitate the functioning of the SME market are essential for sustaining economic growth.¹⁶ Second, the volatility spillovers documented in both markets can be attributed to common information (macroeconomic information). As the main and SME markets are hosted under the same exchange, they are conducive to cross-market hedging, which in turn enhances volatility linkages. Finally, the results are not universal, as they vary not only between markets but also across different subsample periods (especially for the COVID-19 crisis period). These findings carry important implications for asset allocation and risk management strategies.

4.2. Dynamic Conditional Correlations between the Main and SME Stock Markets

This section reports the empirical results obtained from estimating a bivariate VAR (1)-asymmetric DCC–GARCH (1,1) model for the main–SME stock market pairs in Saudi

Arabia and Egypt. In panel C of Table 5, the estimated coefficients for the correlation equation show that a , b , and g are significantly different from zero and vary for the periods both before and during the COVID-19 crisis. The significance of a and b indicates short- and long-term persistence in the correlation. For each pair of main and SME markets in a country, the dynamic conditional correlation of the pair's returns exhibits significant reversion, as the sum of a and b is less than 1, consistent with the findings of [Tiwari et al. \(2019\)](#), [Alexakis and Pappas \(2018\)](#) and [Jin et al. \(2020\)](#). The significance of g indicates that positive and negative shocks tend to induce different correlations between stock markets. As shown in panel C of Table 5, g is significant and positive for the TASI/NOMU for the full sample period (5.4%). Hence, asymmetry exists in the correlation between the TASI and NOMU markets for the COVID-19 pandemic period (12%). This suggests that the correlation between the main and SME market stocks in Saudi Arabia is greater when markets are falling than when they are rising, in line with the findings of [Campbell et al. \(2002\)](#).¹⁷ For Egypt's main and SME markets, g is not significant for the COVID-19 pandemic period, reinforcing the results obtained using the Diebold and Yilmaz approach.

Table 5. Estimation results of the bivariate VAR (1)-asymmetric DCC–GARCH (1,1) model.

	Full Sample Period		Before the COVID-19 Crisis		During the COVID-19 Crisis	
	TASI and NOMU	EGX30 and NILEX	TASI and NOMU	EGX30 and NILEX	TASI and NOMU	EGX 30 and NILEX
Panel A: Mean equation (return spillover effect)						
	Dependent variable : R_{main}					
μ	0.05657 *** (0.01350)	0.03333 (0.02445)	0.02118 *** (0.00008)	0.04853 *** (0.00897)	0.10913 ** (0.05178)	−0.02097 (0.06075)
$R_{main}(-1) - \varphi_{11}$	0.11829 *** (0.02159)	0.24066 *** (0.02279)	0.08185 *** (0.00120)	0.22646 *** (0.02205)	−0.16544 ** (0.06967)	0.26969 *** (0.07102)
$R_{SME}(-1) - \varphi_{12}$	0.01889 *** (0.00144)	−0.02062 (0.02426)	0.02120 *** (0.00167)	−0.01829 (0.03015)	0.01762 ** (0.00767)	−0.01505 (0.03741)
	Dependent variable : R_{SME}					
μ	0.01350 *** (0.00091)	−0.01152 (0.01342)	−0.11419 *** (0.00481)	−0.01534 (0.01281)	0.77861 *** (0.10711)	0.24797 ** (0.11092)
$R_{main}(-1) - \varphi_{21}$	0.14522 *** (0.04590)	0.00187 (0.01012)	0.17708 *** (0.06223)	0.00817 (0.01053)	−0.23337 (0.21170)	0.01050 (0.06260)
$R_{SME}(-1) - \varphi_{22}$	−0.02941 *** (0.00415)	0.25737 *** (0.02162)	−0.07221 ** (0.04334)	0.26244 *** (0.02063)	−0.12911 *** (0.03970)	0.28056 *** (0.05352)
Panel B: Conditional variance equations (volatility spillover effect)						
ω_{11}	0.08100 *** (0.00624)	0.22313 *** (0.04364)	0.34316 *** (0.00883)	0.40755 *** (0.01414)	−0.03929 *** (0.00273)	0.05606 *** (0.01525)
ω_{22}	0.26446 *** (0.02568)	0.00885 *** (0.00233)	0.22825 *** (0.01010)	0.02833 *** (0.00174)	1.28638 *** (0.09560)	1.65014 *** (0.20122)
α_{11}	0.10580 *** (0.00399)	0.10056 *** (0.02164)	0.03871 *** (0.00131)	0.15492 *** (0.00386)	0.05583 *** (0.00941)	0.14108 *** (0.01465)
α_{12}	−0.00220 *** (0.00004)	0.07170 *** (0.00918)	−0.00102 *** (0.00002)	0.06672 *** (0.02012)	−0.00506 *** (0.00042)	0.02227 *** (0.00384)
d_1	0.23210 *** (0.00706)	0.15413 *** (0.03368)	0.08244 *** (0.02517)	0.14616 *** (0.00152)	0.16293 *** (0.01112)	0.03732 *** (0.01928)
α_{21}	0.22916 *** (0.01963)	0.00327 ** (0.00160)	0.02990 ** (0.01569)	0.01109 *** (0.00008)	1.87141 *** (0.12688)	0.01177 (0.03802)
α_{22}	0.30063 *** (0.00702)	0.08614 *** (0.01178)	0.13128 *** (0.00701)	0.13368 *** (0.00237)	0.06153 *** (0.00819)	0.06463 ** (0.03046)
d_2	−0.30069 *** (0.02520)	−0.03159 ** (0.01461)	−0.14870 *** (0.02038)	−0.05124 *** (0.00263)	−0.14308 *** (0.00202)	0.00605 *** (0.08788)
β_{11}	0.76549 *** (0.00072)	0.68815 *** (0.04510)	0.47170 *** (0.01159)	0.53500 *** (0.00631)	0.85497 *** (0.00549)	0.79428 *** (0.01217)

Table 5. Cont.

	Full Sample Period		Before the COVID-19 Crisis		During the COVID-19 Crisis	
	TASI and NOMU	EGX30 and NILEX	TASI and NOMU	EGX30 and NILEX	TASI and NOMU	EGX 30 and NILEX
β_{12}	0.00444 *** (0.00001)	0.00024 (0.02117)	−0.00062 *** (0.00010)	−0.08176 *** (0.01889)	0.01182 *** (0.00094)	−0.00831 ** (0.00455)
β_{21}	0.09770 *** (0.01957)	−0.00673 *** (0.00255)	0.00971 (0.01440)	−0.02295 *** (0.00051)	−0.44919 *** (0.04882)	−0.00079 (0.04278)
β_{22}	0.75779 *** (0.00467)	0.92731 *** (0.01024)	0.83646 *** (0.00506)	0.88454 *** (0.00562)	0.85314 *** (0.00262)	0.44311 *** (0.05991)
Panel C: Correlation equation (dynamic conditional correlation)						
a	0.01123 *** (0.00005)	0.00917 * (0.00566)	0.06262 *** (0.01081)	0.02821 ** (0.01793)	0.02799 *** (0.02127)	0.01160 (0.04888)
b	0.81885 *** (0.00517)	0.98086 *** (0.00764)	0.62398 *** (0.11106)	0.80909 ** (0.07456)	0.87502 *** (0.02613)	−0.05000 (1.33491)
δ	0.05333 *** (0.00094)	0.01071 ** (0.00740)	−0.08302 *** (0.01209)	0.07106 *** (0.03428)	0.12703 *** (0.04486)	−0.01784 (0.08549)
LL	−2765.8992	−5261.614	−2329.571	−4426.451	−1039.771	−803.425
AIC	7.61288	5.51528	6.31733	5.22360	9.05836	7.68326

Notes: Standard errors in parentheses. LL and AIC are the log-likelihood and Akaike information criterion values, respectively. TASI (NOMU) denotes the Saudi main stock market index (SME stock market index). EGX30 (NILEX) denotes the Egyptian main stock market index (SME stock market index). *, **, and *** denote significance at the 10%, 5%, and 1% levels, respectively.

The movements of the dynamic conditional correlations are depicted in Figure 4, which shows that the correlations between each pair of main–SME market indices are quite volatile and vary over time. Noticeably, negative correlations are occasionally observed for both Saudi Arabia and Egypt when main stocks are paired with SME stocks. We can also see that the dynamic conditional correlations exhibit higher positive co-movement between the TASI and the NOMU, particularly for the COVID-19 pandemic period. In contrast, the dynamic conditional correlations between the EGX30 and the NILEX declined considerably during the outbreak. The documented instability in the dynamic correlation between the main and SME market stocks is indicative of the changing preferences of investors over the sample period, dictating frequent portfolio rebalancing. Methodologically, these findings confirm the inadequacy of relying solely on unconditional correlations and carry important implications for investors making hedging and asset allocation decisions, as discussed in the following section.

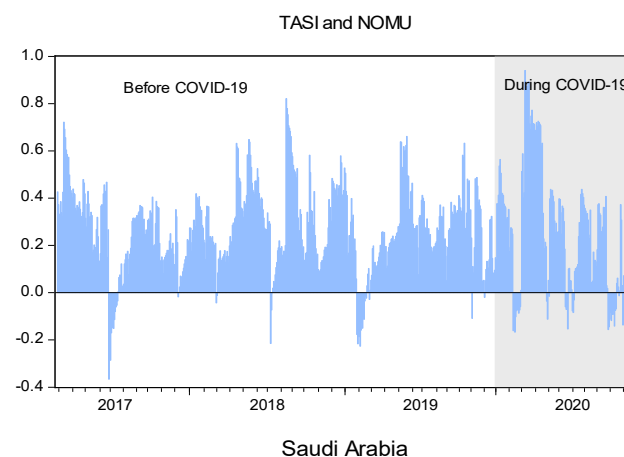


Figure 4. Cont.

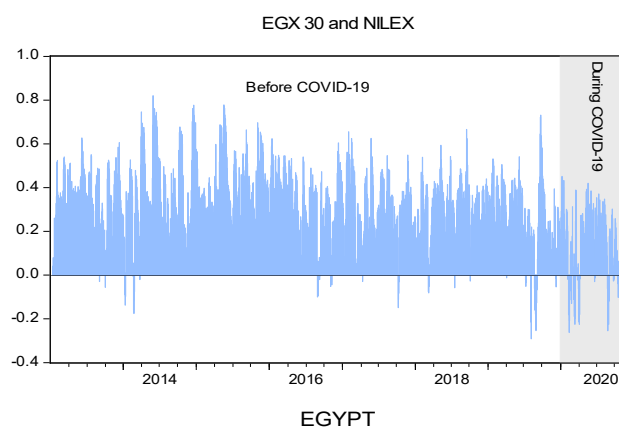


Figure 4. Dynamic conditional correlations between main and SME stock markets estimated from the asymmetric DCC–GARCH (1,1) model.

4.3. Portfolio Weights, Hedge Ratios, and Hedging Effectiveness

The results obtained from the VAR (1)-asymmetric DCC–GARCH (1,1) model are used to compute the optimal weights of the stock portfolios for the main–SME markets. Table 6 reports the averages of the dynamic conditional correlations, optimal weights, and hedge ratios for the full sample and the periods before and during the COVID-19 pandemic. The findings reveal that the weights allocated to SME stocks are substantially lower for both markets for the COVID-19 pandemic period than for the period before the pandemic. This suggests that investors are inclined to hold more SME stocks during stable periods, especially in the Egyptian market, where the weight of SMEs constituted four-fifths of the main–SME stock portfolio before the pandemic. Figure 5 illustrates the dynamics of optimal portfolio weights for each pair of main–SME stock portfolios. The shaded area in Figure 5 shows the same story, as we can clearly see a dramatic decrease in the weight attributed to SME stocks during the COVID-19 pandemic.

Table 6. Dynamic conditional correlations, optimal portfolio weights, hedge ratios and hedging effectiveness (%) for main–SME stock pairs.

	$\rho_{\text{main/SME}}$	$W_{\text{main/SME}}$	$\beta_{\text{main/SME}}$	HEI (%)	ΔHEI (%)
Panel A: Full sample period					
TASI/NOMU	0.265	0.133	0.142	0.323	9.4
EGX 30/NILEX	0.312	0.751	0.561	54.20	−27.21
Panel B: Before the COVID-19 crisis					
TASI/NOMU	0.234	0.159	0.128	0.132	-
EGX 30/NILEX	0.331	0.804	0.614	62.95	-
Panel C: During the COVID-19 crisis					
TASI/NOMU	0.281	0.0720	0.127	0.226	-
EGX 30/NILEX	0.100	0.331	0.0586	35.74	-

Notes: Estimated from the VAR (1)-asymmetric DCC–GARCH (1,1) model. The weights, hedge ratios, hedging effectiveness index, and ΔHEI are calculated using Equations (12)–(15), respectively. All values represent average daily values. TASI (NOMU) denotes the Saudi main stock market index (SME stock market index). EGX30 (NILEX) denotes the Egyptian main stock market index (SME stock market index).

The results pertaining to the optimal hedge ratios and their effectiveness based on Table 6 are mixed not only across markets but also across phases in the same market. On the one hand, we find that the optimal hedge ratio is relatively high, reaching 0.614 for the EGX30/NILEX for the pre-COVID-19 pandemic period, which means that a USD 1 long position in the EGX30 can be hedged by taking a short position of 61.4 cents in the NILEX. On the other hand, during the COVID-19 pandemic, the optimal hedge ratios witnessed a drastic decline for the EGX30/NILEX. The optimal hedge ratios are considerably lower for

the Saudi portfolio; however, they show less variation over the sample period. Figure 6 shows the time-varying hedge ratios for each short-hedged main market portfolio. Notably, the hedge ratios fluctuate significantly over time and are generally lower for the COVID-19 pandemic period than for the period before the pandemic. The decline in hedge ratios implies lower hedging costs during the COVID-19 pandemic period due to the lower number of stocks required to short the SME market. However, to judge the hedging effectiveness, the hedging effectiveness index is calculated for each main–SME stock market pair and is reported in Table 6.

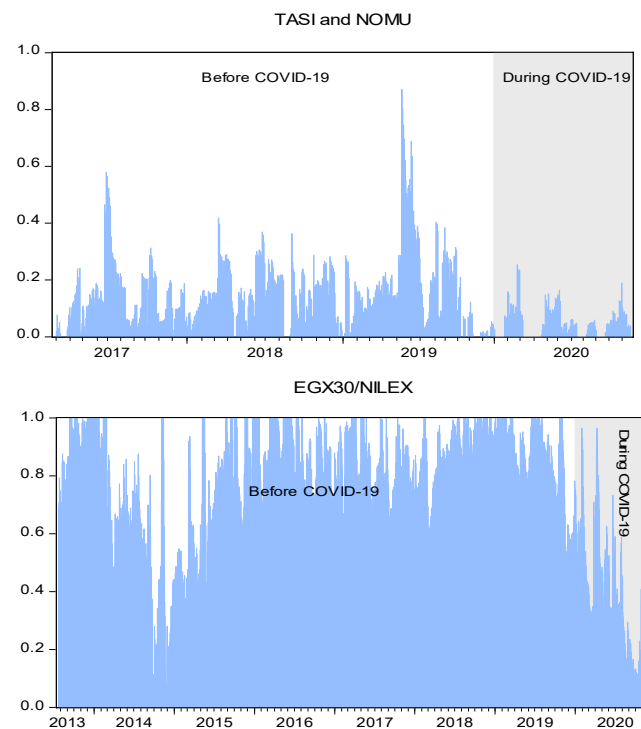


Figure 5. Time-varying portfolio weights computed from the VAR (1)-asymmetric DCC–GARCH (1,1) model.

From Table 6, we can see that when investors include SME stock as part of their hedging strategy, portfolio risk decreases significantly, but only for the Egyptian market. The hedging effectiveness index is higher for the period before the COVID-19 pandemic for the EGX30/NILEX (62.95%), which indicates that shorting the NILEX stocks to hedge the EGX30 significantly reduces the portfolio risk by 62.95% from the level of the unhedged portfolio. For the Saudi Arabian main market (TASI), the SME stock market (NOMU) persistently offers poor hedging performance. Looking at the last column of Table 6, which compares the HEI values for the COVID-19 pandemic and pre-pandemic periods, we find that hedging effectiveness has improved marginally during the pandemic for Saudi Arabia. On the other hand, the values of ΔHEI are negative for the main–SME Egyptian markets, suggesting a less effective hedging performance during the pandemic period. One important takeaway from the results presented in this section is that investors should change their portfolio structure and hedging strategy in accordance with different market conditions (see, e.g., Jiang et al. 2019).

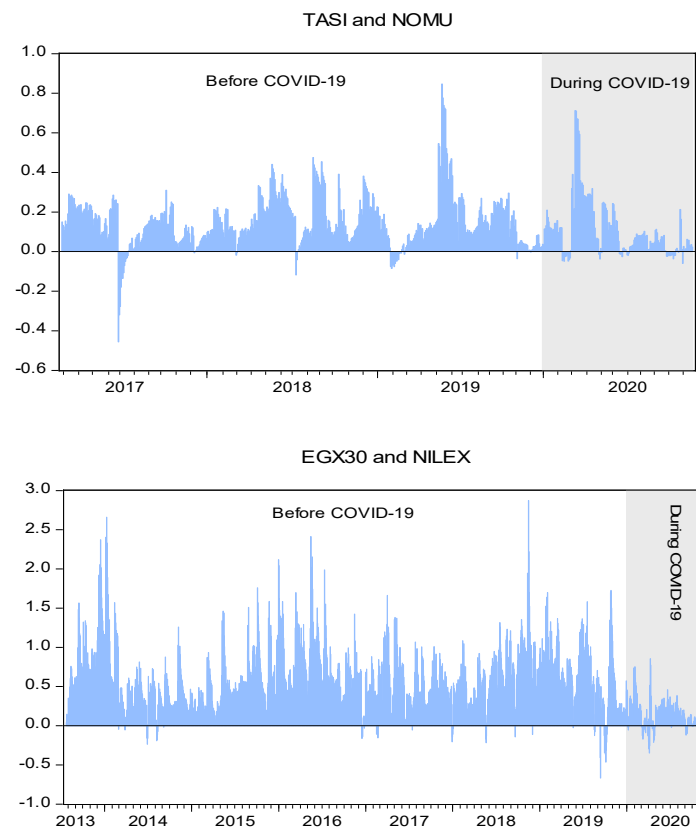


Figure 6. Time-varying hedge ratios computed from the VAR (1)-asymmetric DCC–GARCH (1,1) model.

5. Conclusions and Policy Implications

This paper analyzed how return and volatility spillovers arise within the main and SME markets in Saudi Arabia and Egypt, the two largest economies in the MENA region, and explored the availability of portfolio diversification and hedging opportunities in the periods before and during the COVID-19 pandemic. The equity markets within this region constitute an interesting case due to the growth potential in these economies and the importance of SMEs for achieving ambitious visions for these economies.

A bivariate asymmetric BEKK–GARCH model was employed to estimate the return and volatility spillovers, while a bivariate asymmetric DCC–GARCH model was used to estimate dynamic correlations on the basis of which optimal portfolio weight hedge ratios are computed. The results of the VAR (1) estimation provide evidence of bidirectional return spillovers between the main and SME stock markets only in Saudi Arabia, and these spillovers diminished during the COVID-19 pandemic. The results of the estimation of the MGARCH (1,1) in the asymmetric BEKK formulation provide evidence of shock and volatility spillovers with different characteristics and dynamics between each of the main–SME stock market pairs. The shock and volatility transmission effect has strengthened during the COVID-19 pandemic for the Saudi pair while weakening between the Egyptian main and SME markets, suggesting that the interlinkages between the main and SME stocks in Saudi Arabia are stronger during turbulent periods than those of the Egyptian market, where no shock or volatility spillovers are detected for the COVID-19 pandemic period. The result of the estimation of the asymmetric DCC–GARCH (1,1) model reveals that the time-varying conditional correlations between the main and SME markets are mostly positive and have notably increased during the COVID-19 pandemic, but only in Saudi Arabia. The optimal portfolio weights allocated to SME stocks fluctuated considerably over the sample period, decreasing substantially for both markets during the COVID-19 pandemic period.

The hedge ratio also exhibits a similar pattern, failing to provide meaningful risk reduction during the pandemic.

Policy implications follow naturally from the aforementioned conclusions. First, the documented return spillovers from the SME to the main market in Saudi Arabia support the notion that the SME market, while acting as a pipeline for the main market, indirectly promotes economic growth in Saudi Arabia through its transmission mechanism via the main market. Second, the bidirectional volatility spillovers highlight cross-market hedging and portfolio rebalancing in response to common information that affects the entire economy. Third, the absence of spillovers within the Egyptian markets during the pandemic can be attributed to the sell-offs experienced majorly by the Egyptian main rather SME market as a part of flight-to-safety episode triggered by concerns about the future prospects of emerging markets during the pandemic. Fourth, the results from the portfolio design and hedging analysis suggest that adding SME stocks to a main market stock portfolio enhances the risk-adjusted return, particularly during tranquil market phases when investors adjust their portfolio weight allocations and hedging positions based on different market conditions. Overall, it is imperative for policymakers to take all the necessary measures to attract more listings in addition to promoting the SME market to fund managers who ultimately enhance the liquidity of SME markets and increase investors' confidence in those markets.

A caveat of this study is the narrow sample, which considers the interdependencies between the main and second-tier markets within just two countries. This limitation can be addressed in future work by examining a large sample of countries to explore the potential factors that affect the interdependencies between main and second-tier markets, which may assist in accounting for the heterogeneity of results across countries. Another potentially viable extension of this work is to compare the linkages between large- and small-sized portfolios within the main market against the results obtained by portfolios of companies of a similar size but listed in the second-tier market to explore whether differences in the rules and regulations of the main and second-tier markets impact the nature of the linkages between these portfolios.

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Conflicts of Interest: The authors declare no conflict of interest.

Appendix A

Table A1. Stock market characteristics.

Years	Saudi Arabia				Egypt			
	Main Market		SME Market		Main Market		SME Market	
	2019	2020	2019	2020	2019	2020	2019	2020
Inception ^a	1985		2017		1998		2012	
No. of listed companies	199	203	5 ^d	4	210	209	27 ^e	27
Representative index	TASI		NOMU		EGX 30		NILEX	
Market capitalization ^b	2406.73	2427.15	0.68	3.25	44.13	41.35	0.07	0.06
Percentage of GDP	303.51%	347%	0.09%	0.46%	14.56%	11%	0.02%	0.02%
Percentage of main index	-	-	0.03%	0.13%	-	-	0.16%	0.15%
Trading value ^b	234.7	556.75	0.61	1.90	11.28	16.14	0.016	0.083
Percentage of main index	-	-	0.26%	0.34%	-	-	0.14%	0.51%
Trading volume ^c	33.06	79.32	0.08	0.11	43.74	87.10	0.77	1.58
Percentage of main index	-	-	0.24%	0.14%	-	-	1.8%	1.8%

Source: Annual Statistical Report (2019) published by the Saudi stock exchange (Tadawul), annual and quarterly reports from the Egyptian Exchange and the World Federation of Exchanges' (WFE) statistics portal. Notes: ^a Inception refers to the year in which the respective index was first developed with its base level regardless of subsequent restructurings; ^b in USD billion; ^c in billion shares; ^d the NOMU started 2019 with 10 companies, 5 of which transitioned their shares from the SME (parallel) market to the main market by the end of the year; ^e the NILEX started 2019 with 29 companies; one company was newly listed in the market, and three companies were delisted by the end of the year.

Table A2. Diagnostic tests on standardized residuals.

	Full Sample Period				Before the COVID-19 Crisis				During the COVID-19 Crisis			
	TASI	NOMU	EGX30	NILEX	TASI	NOMU	EGX30	NILEX	TASI	NOMU	EGX30	NILEX
Panel A: VAR (1)-asymmetric BEKK–GARCH (1,1) model												
ARCH–	8.8641	4.4711	6.4930	3.6942	11.9986	7.2395	7.0067	7.4165	5.400	7.9289	3.2929	6.1898.
LM(5)	(0.1146)	(0.4834)	(0.2612)	(0.5942)	(0.3485)	(0.1601)	(0.2201)	(0.2209)	(0.6678)	(0.1602)	(0.8073)	(0.8221)
Q(5)	9.0712	5.5485	6.2715	4.7411	5.7916	5.3610	3.5884	4.5581	3.723	4.091	5.1287	6.7398
	(0.6312)	(0.3214)	(0.1800)	(0.3151)	(0.2154)	(0.2529)	(0.5464)	(0.3367)	(0.4343)	(0.3993)	(0.2742)	(0.2046)
Q ² (5)	9.0953	4.4905	6.6196	3.7643	12.5598	8.2212	7.0025	7.4870	5.655	8.2819	3.3292	6.3895
	(0.1053)	(0.4812)	(0.2516)	(0.584)	(0.3520)	(0.1445)	(0.2221)	(0.1879)	(0.6819)	(0.1415)	(0.8871)	(0.2934)
Panel B: VAR (1)-asymmetric DCC–GARCH (1,1) model												
ARCH–	3.7645	2.9368	3.573	6.7855	10.5801	5.2708	6.8975	7.4975	0.8181	5.8824	2.2472	9.9312
LM(5)	(0.5834)	(0.7079)	(0.6123)	(0.2371)	(0.6042)	(0.3837)	(0.2284)	(0.18625)	(0.9759)	(0.3178)	(0.8140)	(0.7106)
Q(5)	12.007	4.9998	5.2439	6.0145	7.6671	3.4814	4.0498	4.4744	5.0911	3.3827	5.7879	6.4391
	(0.1754)	(0.2872)	(0.2630)	(0.1980)	(0.1066)	(0.1482)	(0.3991)	(0.3468)	(0.1650)	(0.4963)	(0.435)	(0.1693)
Q ² (5)	3.9104	2.9740	3.5939	6.9802	10.3100	5.9150	6.8068	7.6227	0.8712	6.1399	2.2021	9.0987
	(0.5620)	(0.7040)	(0.6090)	(0.2225)	(0.6315)	(0.3562)	(0.2351)	(0.1783)	(0.9720)	(0.2939)	(0.8214)	(0.6859)

Notes: Q(5) and Q²(5) represent the Ljung–Box Q-statistics on the order of 10 for the standardized residuals and squared standardized residuals, respectively, along with their corresponding *p*-values in parentheses. LM–ARCH(10) refers to the Engle (1982) test statistics along with their corresponding *p*-values in parentheses. TASI (NOMU) denotes the Saudi main stock market index (SME stock market index). EGX30 (NILEX) denotes the Egyptian main stock market index (SME stock market index).

Notes

- ¹ Several financing sources exist for SMEs, including venture capital, private equity, private debt, trade credit, initial public offerings (IPOs), business angel finance, and crowdfunding, as well as grants, funding from incubators or accelerators, and support from family and friends (Cumming et al. 2019); however, bank loans remain their main source of funding (Beck et al. 2008; The World Federation of Exchanges 2015). Nonetheless, Cosh et al. (2009) find that SMEs are less likely than larger firms to receive the desired amount of funding from banks. This is primarily due to information asymmetries, a lack of brick-and-mortar collateral, a lack of positive and regular cash flows, and the need for longer maturities to finance capital expenditure (Berger and Udell 2006; Jaffee and Russell 1976; Nassr and Wehinger 2016; Stiglitz and Weiss 1981). Moreover, SMEs are found to be more

vulnerable in financial crises, as several studies have shown that the global financial crisis (GFC) exacerbated credit rationing, thereby undermining SMEs' business and investment activities (see Cowling et al. 2016; D'Amato 2019; Ferrando and Ruggieri 2018).

Other models of second-tier market segmentation include sectoral and demand-side models (see Vismara et al. 2012). However, the sequential segmentation (steppingstone) model is recommended by international bodies (Nassr and Wehinger 2016, p. 70). Under the sequential segmentation (steppingstone) model, second-tier markets are expected to screen small companies in the 'seasoning' market, and if a company is successful, it graduates to the main market.

For more on the specificities of emerging markets, including the MENA region and their interaction with the global economy, see Aroui et al. (2013), while Boubaker et al. (2016) focus on risk management practices in emerging markets.

Based on GDP, PPP (current international USD); see <https://data.worldbank.org/indicator/NY.GDP.MKTP.PP.CD> (accessed on 15 June 2021).

The Nile Exchange (NILEX) was launched under the Egyptian Exchange in 2007, whereas the NOMU—Parallel Market was initiated in 2017 under Tadawul. While both markets had a slow start at the outset, interest has noticeably grown in the past few years (see Table A1 in the Appendix A).

An unbalanced sample is used, where the starting date is selected based on the following two considerations: the first is data availability for the corresponding SME market index, and the second is the desire to avoid any overlap with previous crises, including the European sovereign debt crisis (2010–2012) and the 2013 Egyptian coup d'état. Accordingly, the sample starting date was 24 July 2013, for Egypt, and 27 February 2017, for Saudi Arabia, and the sample ended on 20 November 2020, for both markets.

The starting date of the COVID-19 subsample was 31 December 2019, according to the World Health Organization (WHO) (see WHO 2020).

<https://www.imf.org/en/News/Articles/2021/07/14/na070621-egypt-overcoming-the-COVID-shock-and-maintaining-growth> (accessed on 15 June 2021).

$NTDC_i(H) = TDC_{i \leftarrow j}(H) - TDC_{i \leftarrow k}(H)$, which denotes how shocks in the main stock market are transmitted to the SME stock market $TDC_{i \leftarrow Main\ stock\ market}(H)$ and how the main stock market receives shocks from the SME stock market $TDC_{Main\ stock\ market \leftarrow i}(H)$.

The models' specification is chosen on the basis of a two-step procedure to select the optimal lag structure (according to the AIC). Vrieze (2012) has argued in favour of the superiority of the AIC for model selection.

The normality assumption produces the highest value of the log-likelihood; see, e.g., Liu et al. (2017).

Jin et al. (2020) also examine hedging performance.

Table A2 in the Appendix A displays the postestimation diagnostics for the bivariate VAR (1)-asymmetric BEKK–GARCH (1,1) and VAR (1)-asymmetric DCC–GARCH (1,1) models. The Ljung–Box and Engle ARCH–LM tests at five lags are used to test for the presence of serial correlation and heteroskedasticity in the standardized residuals, respectively. All the models pass the diagnostic tests, suggesting that they are well specified.

Al Rasasi et al. (2019) examine the stock market and economic growth nexus in Saudi Arabia. They find a significant long-run relationship between the real price level of the main market index and real economic activity, indicating that stock prices have a significant impact on real economic growth.

A major advantage of the model is its capacity to account for cross-market asymmetric shock spillovers, which capture whether a positive or a negative shock in one market translates to either a positive or negative shock in another market.

The Egyptian Exchange is embarking on a restructuring plan for the Nile Exchange with the European Bank for Reconstruction and Development (Enterprise 2020a).

Campbell et al. (2002) show that during periods of heightened volatility, stocks tend to become more correlated. This finding has important implications for portfolio and risk management because it means that the benefits of diversification are somewhat undermined just when investors have the greatest need for them.

References

- Akhtaruzzaman, Md, Sabri Boubaker, and Ahmet Sensoy. 2021a. Financial Contagion during COVID-19 Crisis. *Finance Research Letters* 38: 101604. [CrossRef]
- Akhtaruzzaman, Md, Sabri Boubaker, and Zaghun Umar. 2021b. COVID-19 media coverage and ESG leader indices. *Finance Research Letters*, 102170. [CrossRef]
- Akhtaruzzaman, Md, Sabri Boubaker, Brian M. Lucey, and Ahmet Sensoy. 2021c. Is gold a hedge or a safe-haven asset in the COVID–19 crisis? *Economic Modelling* 102: 105588. [CrossRef]
- Al Rasasi, Moayad H., Soleman O. Alsabban, and Omar A. Alarfaj. 2019. Does Stock Market Performance Affect Economic Growth? Empirical Evidence from Saudi Arabia. *International Journal of Economics and Finance* 11: 1–21. [CrossRef]
- Alexakis, Christos, and Vasileios Pappas. 2018. Sectoral dynamics of financial contagion in Europe—The cases of the recent crises episodes. *Economic Modelling* 73: 222–39. [CrossRef]

- Al-Yahyaee, Khamis Hamed, Walid Mensi, Ahmet Sensoy, and Sang Hoon Kang. 2019. Energy, precious metals, and GCC stock markets: Is there any risk spillover? *Pacific-Basin Finance Journal* 56: 45–70. [CrossRef]
- Arouri, Mohammed El Hedi, Sabri Boubaker, and Duc Khuong Nguyen. 2013. *Emerging Markets and the Global Economy: A Handbook*. Cambridge: Academic Press.
- Asl, Mahdi Ghaemi, Giorgio Canarella, and Stephen M. Miller. 2021. Dynamic asymmetric optimal portfolio allocation between energy stocks and energy commodities: Evidence from clean energy and oil and gas companies. *Resources Policy* 71: 101982. [CrossRef]
- Bahloul, Slah, and Imen Khemakhem. 2021. Dynamic return and volatility connectedness between commodities and Islamic stock market indices. *Resources Policy* 71: 101993. [CrossRef]
- Basher, Syed Abul, and Perry Sadorsky. 2016. Hedging emerging market stock prices with oil, gold, VIX, and bonds: A comparison between DCC, ADCC and GO-GARCH. *Energy Economics* 54: 235–47. [CrossRef]
- Baumöhl, Eduard, and Štefan Lyócsa. 2014. Volatility and dynamic conditional correlations of worldwide emerging and frontier markets. *Economic Modelling* 38: 175–83. [CrossRef]
- Beck, Thorsten, Asli Demirgüç-Kunt, and Vojislav Maksimovic. 2008. Financing Patterns around the World: Are Small Firms Different? *Journal of Financial Economics* 89: 467–87. [CrossRef]
- Berger, Allen N., and Gregory F. Udell. 2006. A more complete conceptual framework for SME finance. *Journal of Banking & Finance* 30: 2945–66. [CrossRef]
- Boldanov, Rustam, Stavros Degiannakis, and George Filis. 2016. Time-varying correlation between oil and stock market volatilities: Evidence from oil-importing and oil-exporting countries. *International Review of Financial Analysis* 48: 209–20. [CrossRef]
- Boubaker, Sabri, Bonnie Buchanan, and Duc Khuong Nguyen. 2016. *Risk Management in Emerging Markets: Issues, Framework, and Modeling*. Bingley: Emerald Group Publishing.
- Campbell, Rachel, Kees Koedijk, and Paul Kofman. 2002. Increased Correlation in Bear Markets. *Financial Analysts Journal* 58: 87–94. [CrossRef]
- Cappiello, Lorenzo, Robert F. Engle, and Kevin Sheppard. 2006. Asymmetric Dynamics in the Correlations of Global Equity and Bond Returns. *Journal of Financial Econometrics* 4: 537–72. [CrossRef]
- Corbet, Shaen, Yang Hou, Yang Hu, Les Oxley, and Danyang Xu. 2021. Pandemic-related financial market volatility spillovers: Evidence from the Chinese COVID-19 epicentre. *International Review of Economics & Finance* 71: 55–81. [CrossRef]
- Cosh, Andy, Douglas Cumming, and Alan Hughes. 2009. Outside Entrepreneurial Capital. *The Economic Journal* 119: 1494–533. [CrossRef]
- Cowling, Marc, Weixi Liu, and Ning Zhang. 2016. Access to bank finance for UK SMEs in the wake of the recent financial crisis. *International Journal of Entrepreneurial Behavior & Research* 22: 903–32. [CrossRef]
- Cumming, Douglas, Marc Deloof, Sophie Manigart, and Mike Wright. 2019. New directions in entrepreneurial finance. *Journal of Banking & Finance* 100: 252–60. [CrossRef]
- D'Amato, Antonio. 2019. Capital Structure, Debt Maturity, and Financial Crisis: Empirical Evidence from SMEs. *Small Business Economics* 55: 919–41. [CrossRef]
- Dickey, David A., and Wayne A. Fuller. 1981. Likelihood Ratio Statistics for Autoregressive Time Series with a Unit Root. *Econometrica* 49: 1057–72. [CrossRef]
- Diebold, Francis X., and Kamil Yilmaz. 2014. On the network topology of variance decompositions: Measuring the connectedness of financial firms. *Journal of Econometrics* 182: 119–34. [CrossRef]
- Ederington, Louis H. 1979. The Hedging Performance of the New Futures Markets. *The Journal of Finance* 34: 157–70. [CrossRef]
- Elsayed, Ahmed H., and Larisa Yarovaya. 2019. Financial stress dynamics in the MENA region: Evidence from the Arab Spring. *Journal of International Financial Markets, Institutions and Money* 62: 20–34. [CrossRef]
- Engle, Robert F. 1982. Autoregressive Conditional Heteroscedasticity with Estimates of the Variance of United Kingdom Inflation. *Econometrica* 50: 987–1007. [CrossRef]
- Engle, Robert F. 2002. Dynamic Conditional Correlation. *Journal of Business & Economic Statistics* 20: 339–50. [CrossRef]
- Engle, Robert F., and Kenneth F. Kroner. 1995. Multivariate Simultaneous Generalized ARCH. *Econometric Theory* 11: 122–50. [CrossRef]
- Enterprise. 2020a. EBRD Could Support Small-Caps Facing New Sponsor Regs. Available online: <https://enterprise.press/stories/2020/09/08/ebrd-could-support-small-caps-facing-new-sponsor-regs-21459/> (accessed on 15 June 2021).
- Enterprise. 2020b. Speed Medical to be the First Jump from Nilex to the EGX. Available online: <https://enterprise.press/stories/2020/12/03/speed-medical-to-be-the-first-jump-from-nilex-to-the-egx-26032/> (accessed on 15 June 2021).
- Ferrando, Annalisa, and Alessandro Ruggieri. 2018. Financial constraints and productivity: Evidence from euro area companies. *International Journal of Finance & Economics* 23: 257–82. [CrossRef]
- Fleming, Jeff, Chris Kirby, and Barbara Ostdiek. 1998. Information and volatility linkages in the stock, bond, and money markets. *Journal of Financial Economics* 49: 111–37. [CrossRef]
- Gharib, C., S. Mefteh-Wali, and S. B. Jabeur. 2021. The Bubble Contagion Effect of COVID-19 Outbreak: Evidence from Crude Oil and Gold Markets. *Finance Research Letters* 38: 101703. [CrossRef]
- Glosten, Lawrence R, Ravi Jagannathan, and David E Runkle. 1993. On the relation between the expected value and the volatility of the nominal excess return on stocks. *J. Finance* 48: 1779–801. [CrossRef]
- Hatemi-J, Abdulnasser. 2012. Asymmetric causality tests with an application. *Empirical Economics* 43: 447–56. [CrossRef]

- Hemche, Omar, Fredj Jawadi, Samir B. Maliki, and Abdoukarim Idi Cheffou. 2016. On the study of contagion in the context of the subprime crisis: A dynamic conditional correlation–multivariate GARCH approach. *Economic Modelling* 52: 292–99. [\[CrossRef\]](#)
- Hou, Yang, and Steven Li. 2016. Information transmission between U.S. and China index futures markets: An asymmetric DCC GARCH approach. *Economic Modelling* 52: 884–97. [\[CrossRef\]](#)
- Hwang, Jae-Kwang. 2014. Spillover effects of the 2008 financial crisis in Latin America stock markets. *International Advances in Economic Research* 20: 311–24. [\[CrossRef\]](#)
- Iglesias-Casal, Ana, María Celia López-Penabad, Carmen López-Andión, and José Manuel Maside-Sanfiz. 2020. Diversification and Optimal Hedges for Socially Responsible Investment in Brazil. *Economic Modelling* 85: 106–18. [\[CrossRef\]](#)
- Jaffee, Dwight M., and Thomas Russell. 1976. Imperfect Information, Uncertainty, and Credit Rationing. *The Quarterly Journal of Economics* 90: 651–66. [\[CrossRef\]](#)
- Jarque, Carlos M., and Anil K. Bera. 1980. Efficient tests for normality, homoscedasticity and serial independence of regression residuals. *Economics Letters* 6: 255–59. [\[CrossRef\]](#)
- Jiang, Yonghong, Yuyuan Fu, and Weihua Ruan. 2019. Risk Spillovers and Portfolio Management between Precious Metal and BRICS Stock Markets. *Physica A: Statistical Mechanics and its Applications* 534: 120993. [\[CrossRef\]](#)
- Jin, Jiayu, Liyan Han, Lei Wu, and Hongchao Zeng. 2020. The hedging effectiveness of global sectors in emerging and developed stock markets. *International Review of Economics & Finance* 66: 92–117. [\[CrossRef\]](#)
- Junttila, Juha, Juho Pesonen, and Juhani Raatikainen. 2018. Commodity market based hedging against stock market risk in times of financial crisis: The case of crude oil and gold. *Journal of International Financial Markets, Institutions and Money* 56: 255–80. [\[CrossRef\]](#)
- Karanasos, Menelaos, Alexandros G. Paraskevopoulos, Faek Menla Ali, Michail Karoglou, and Stavroula Yfanti. 2014. Modelling stock volatilities during financial crises: A time varying coefficient approach. *Journal of Empirical Finance* 29: 113–28. [\[CrossRef\]](#)
- Karmakar, Madhusudan. 2010. Information transmission between small and large stocks in the National Stock Exchange in India: An empirical study. *The Quarterly Review of Economics and Finance* 50: 110–20. [\[CrossRef\]](#)
- Kinateder, Harald, Ross Campbell, and Tonmoy Choudhury. 2021. Safe haven in GFC versus COVID-19: 100 turbulent days in the financial markets. *Finance Research Letters* 43: 101951. [\[CrossRef\]](#)
- Koulakiotis, Athanasios, Vassilios Babalos, and Nicholas Papasyriopoulos. 2016. Financial crisis, liquidity and dynamic linkages between large and small stocks: Evidence from the Athens Stock Exchange. *Journal of International Financial Markets, Institutions and Money* 40: 46–62. [\[CrossRef\]](#)
- Kroner, Kenneth F., and Victor K. Ng. 1998. Modeling Asymmetric Comovements of Asset Returns. *Review of Financial Studies* 11: 817–44. [\[CrossRef\]](#)
- Kroner, Kenneth F., and Jahangir Sultan. 1993. Time-Varying Distributions and Dynamic Hedging with Foreign Currency Futures. *The Journal of Financial and Quantitative Analysis* 28: 535–51. [\[CrossRef\]](#)
- Kyrkilis, Dimitrios, Athanasios Koulakiotis, Vassilios Babalos, and Maria Kyriakou. 2018. Feedback Trading and Short-Term Return Dynamics in Athens Stock Exchange. *International Journal of Managerial Finance* 14: 574–90. [\[CrossRef\]](#)
- Li, Hong. 2007. International linkages of the Chinese stock exchanges: A multivariate GARCH analysis. *Applied Financial Economics* 17: 285–97. [\[CrossRef\]](#)
- Ling, Shiqing, and Michael McAleer. 2003. Asymptotic Theory for a Vector ARMA-GARCH Model. *Econometric Theory* 19: 280–310. [\[CrossRef\]](#)
- Liu, Xueyong, Haizhong An, Shupe Huang, and Shaobo Wen. 2017. The evolution of spillover effects between oil and stock markets across multi-scales using a wavelet-based GARCH-BEKK model. *Physica A: Statistical Mechanics and its Applications* 465: 374–83. [\[CrossRef\]](#)
- Lo, Andrew W., and A. Craig MacKinlay. 1990. When Are Contrarian Profits Due to Stock Market Overreaction? *Review of Financial Studies* 3: 175–205. [\[CrossRef\]](#)
- Majumder, Sayantan Bandhu, and Ranjanendra Narayan Nag. 2018. Shock and volatility spillovers among equity sectors of the national stock exchange in India. *Global Business Review* 19: 227–40. [\[CrossRef\]](#)
- Markwat, Thijs, Erik Kole, and Dick van Dijk. 2009. Contagion as a domino effect in global stock markets. *Journal of Banking & Finance* 33: 1996–2012. [\[CrossRef\]](#)
- McAleer, Michael, Suhejla Hoti, and Felix Chan. 2009. Structure and Asymptotic Theory for Multivariate Asymmetric Conditional Volatility. *Econometric Reviews* 28: 422–40. [\[CrossRef\]](#)
- McIver, Ron P., and Sang Hoon Kang. 2020. Financial crises and the dynamics of the spillovers between the U.S. and BRICS stock markets. *Research in International Business and Finance* 54: 101276. [\[CrossRef\]](#)
- Nassar, Iota Kaousar, and Gert Wehinger. 2016. Opportunities and limitations of public equity markets for SMEs. *OECD Journal: Financial Market Trends* 2015: 49–84.
- Nguyen, Duc Khuong, Ricardo M. Sousa, and Gazi Salah Uddin. 2015. Testing for asymmetric causality between U.S. equity returns and commodity futures returns. *Finance Research Letters* 12: 38–47. [\[CrossRef\]](#)
- Nguyen, Trang, Taha Chaiechi, Lynne Eagle, and David Low. 2020. Dynamic transmissions between main stock markets and SME stock markets: Evidence from tropical economies. *The Quarterly Review of Economics and Finance* 75: 308–24. [\[CrossRef\]](#)
- Nikkinen, Jussi, Vanja Piljak, and Timo Rothovius. 2020. Impact of the 2008–2009 financial crisis on the external and internal linkages of European frontier stock markets. *Global Finance Journal* 46: 100481. [\[CrossRef\]](#)

- Papadamou, Stephanos, Athanasios P. Fassas, Dimitris Kenourgios, and Dimitrios Dimitriou. 2021. Flight-to-quality between global stock and bond markets in the COVID era. *Finance Research Letters* 38: 101852. [CrossRef]
- Phillips, Peter C. B., and Pierre Perron. 1988. Testing for a Unit Root in Time Series Regression. *Biometrika* 75: 335–46. [CrossRef]
- Rose, Andrew K., and Mark M. Spiegel. 2010. Cross-country causes and consequences of the 2008 crisis: International linkages and American exposure. *Pacific Economic Review* 15: 340–63. [CrossRef]
- Salisu, Afees A., and Tirimisiyu F. Oloko. 2015. Modeling oil price–US stock nexus: A VARMA–BEKK–AGARCH approach. *Energy Economics* 50: 1–12. [CrossRef]
- Salisu, Afees, Xuan Vinh Vo, and Adedoyin Isola Lawal. 2021. Hedging Oil Price Risk with Gold during COVID-19 Pandemic. *Resources Policy* 70: 101897. [CrossRef]
- Samarakoon, Lalith P. 2011. Stock market interdependence, contagion, and the U.S. financial crisis: The case of emerging and frontier markets. *Journal of International Financial Markets, Institutions and Money* 21: 724–42. [CrossRef]
- Samitas, Aristeidis, Dimitris Kenourgios, and Nick Konstantopoulos. 2006. The small business capital market behavior in Athens Stock Exchange. *Small Business Economics* 27: 409–17. [CrossRef]
- Singhal, Shelly, and Sajal Ghosh. 2016. Returns and volatility linkages between international crude oil price, metal and other stock indices in India: Evidence from VAR-DCC-GARCH models. *Resources Policy* 50: 276–88. [CrossRef]
- Stiglitz, Joseph E., and Andrew Weiss. 1981. Credit Rationing in Markets with Imperfect Information. *The American Economic Review* 71: 393–410.
- The World Federation of Exchanges. 2015. WFE Report on SME Exchanges. Available online: https://www.world-exchanges.org/storage/app/media/research/Studies_Reports/WFE%20Report%20on%20SME%20Exchanges.pdf (accessed on 27 February 2021).
- The World Federation of Exchanges. 2018. An Overview of WFE SME Markets. Available online: <https://www.world-exchanges.org/news/articles/world-federation-exchanges-publishes-report-global-sme-markets> (accessed on 27 February 2021).
- Tiwari, Aviral Kumar, and Claudiu Tiberiu Albuлесcu. 2016. Oil price and exchange rate in India: Fresh evidence from continuous wavelet approach and asymmetric, multi-horizon Granger-causality tests. *Applied Energy* 179: 272–83. [CrossRef]
- Tiwari, Aviral Kumar, Ibrahim Dolapo Raheem, and Sang Hoon Kang. 2019. Time-varying dynamic conditional correlation between stock and cryptocurrency markets using the copula-ADCC-EGARCH model. *Physica A: Statistical Mechanics and its Applications* 535: 122295. [CrossRef]
- Umar, Zaghun, Youssef Manel, Yasir Riaz, and Mariya Gubareva. 2021. Return and volatility transmission between emerging markets and US debt throughout the pandemic crisis. *Pacific-Basin Finance Journal* 67: 101563. [CrossRef]
- Vardar, Gülin, Yener Coşkun, and Tezer Yelkenci. 2018. Shock transmission and volatility spillover in stock and commodity markets: Evidence from advanced and emerging markets. *Eurasian Economic Review* 8: 231–88. [CrossRef]
- Vismara, Silvio, Stefano Paleari, and Jay R. Ritter. 2012. Europe's Second Markets for Small Companies. *European Financial Management* 18: 352–88. [CrossRef]
- Vrieze, Scott I. 2012. Model Selection and Psychological Theory: A Discussion of the Differences between the Akaike Information Criterion (AIC) and the Bayesian Information Criterion (BIC). *Psychol Methods* 17: 228–43. [CrossRef] [PubMed]
- Wang, Gang Jin, Chi Xie, Zhi Qiang Jiang, and H. Eugene Stanley. 2016. Extreme Risk Spillover Effects in World Gold Markets and The Global Financial Crisis. *International Review of Economics & Finance* 46: 55–77. [CrossRef]
- Wang, Gang Jin, Chi Xie, Min Lin, and H. Eugene Stanley. 2017. Stock Market Contagion during the Global Financial Crisis: A Multiscale Approach. *Finance Research Letters* 22: 163–68. [CrossRef]
- Wen, Xiaoqian, Yanfeng Guo, Yu Wei, and Dengshi Huang. 2014. How do the stock prices of new energy and fossil fuel companies correlate? Evidence from China. *Energy Economics* 41: 63–75. [CrossRef]
- Wen, Danyan, Yudong Wang, Chaoqun Ma, and Yaojie Zhang. 2020. Information transmission between gold and financial assets: Mean, volatility, or risk spillovers? *Resources Policy* 69: 101871. [CrossRef]
- WHO. 2020. Novel Coronavirus (2019-nCoV) Situation Report-1. Available online: https://www.who.int/docs/default-source/coronaviruse/situation-reports/20200121-sitrep-1-2019-ncov.pdf?sfvrsn=20a99c10_4 (accessed on 10 March 2021).
- Wu, Fei, Dayong Zhang, and Zhiwei Zhang. 2019. Connectedness and risk spillovers in China's stock market: A sectoral analysis. *Economic Systems* 43: 100718. [CrossRef]
- Xu, Haifeng, and Shigeyuki Hamori. 2012. Dynamic Linkages of Stock Prices between the BRICs and the United States: Effects of the 2008–09 Financial Crisis. *Journal of Asian Economics* 23: 344–52. [CrossRef]
- Xu, Weiju, Feng Ma, Wang Chen, and Bing Zhang. 2019. Asymmetric volatility spillovers between oil and stock markets: Evidence from China and the United States. *Energy Economics* 80: 310–20. [CrossRef]
- Yarovaya, Larisa, and Marco Chi Keung Lau. 2016. Stock market comovements around the Global Financial Crisis: Evidence from the UK, BRICS and MIST markets. *Research in International Business and Finance* 37: 605–19. [CrossRef]
- Yu, Lean, Rui Zha, Dimitrios Stafylas, Kaijian He, and Jia Liu. 2020. Dependences and volatility spillovers between the oil and stock markets: New evidence from the copula and VAR-BEKK-GARCH models. *International Review of Financial Analysis* 68: 101280. [CrossRef]
- Zhang, Wenting, and Shigeyuki Hamori. 2021. Crude oil market and stock markets during the COVID-19 pandemic: Evidence from the US, Japan, and Germany. *International Review of Financial Analysis* 74: 101702. [CrossRef]