

## Article

# Forecasting Industrial Production Using Its Aggregated and Disaggregated Series or a Combination of Both: Evidence from One Emerging Market Economy

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**Abstract:** In this paper, we address whether using a disaggregated series or combining an aggregated and disaggregated series improves the forecasting of the aggregated series compared to using the aggregated series alone. We used econometric techniques, such as the weighted lag adaptive least absolute shrinkage and selection operator, and Exponential Triple Smoothing (ETS), as well as the Autometrics algorithm to forecast industrial production in Brazil one to twelve months ahead. This is the novelty of the work, as is the use of the average multi-horizon Superior Predictive Ability (aSPA) and uniform multi-horizon Superior Predictive Ability (uSPA) tests, used to select the best forecasting model by combining different horizons. Our sample covers the period from January 2002 to February 2020. The disaggregated ETS has a better forecast performance when forecasting horizons that are more than one month ahead using the mean square error, and the aggregated ETS has better forecasting ability for horizons equal to 1 and 2. The aggregated ETS forecast does not contain information that is useful for forecasting industrial production in Brazil beyond the information already found in the disaggregated ETS forecast between two and twelve months ahead.

**Keywords:** industrial production; forecasting; model selection**JEL Classification:** C53; E27; C52

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## 1. Introduction

Economic agents make decisions based on their views on the present state of the economy and their expectations for the future. The general levels of output, employment, interest rates, exchange rates, and inflation are key economic indicators that help to diagnose a country's economic situation. Therefore, the proposition and evaluation concerning the ability of econometric models to forecast a country's economic reality introduce benefits that create better guides for economic agents and policymakers.

One of the main macroeconomic indicators of an economy is the gross domestic product (GDP), which is a proxy for a country's economic performance. We use industrial production as a proxy for the GDP since the monthly industrial production index is of higher frequency than the GDP. Moreover, the industrial production index is released with a lag of one month, which is smaller than that of the GDP, which has a delayed release of more than two months.

We address whether using a disaggregated series or combining an aggregated and disaggregated series improves the forecasting accuracy of the aggregated series compared to using the aggregated series alone for the industrial production in Brazil series. Disaggregated data refer to the decomposition of the main variable into several sub-components, which have different weights for the aggregated series. We obtained a forecast of these

sub-components individually and then we grouped the forecasts of these sub-components to estimate the forecast of the aggregated series. This alternative could increase the accuracy of the forecast; we modeled the sub-components by taking their characteristics into account. We used this alternative in the present work to understand if there was a reduction in the forecast error of the aggregate series by estimating a model for each sub-component.

The literature addresses the accuracy of using disaggregated or aggregated data for forecasting. According to [Lütkepohl \(1987\)](#), the forecast using disaggregation is theoretically optimal if the disaggregated series is uncorrelated; the author suggests using disaggregation if the correlation between the disaggregated series is not strong. Some examples of contributions to the theoretical literature on aggregate or disaggregate forecasting include [Lütkepohl \(1984, 1987\)](#); [Granger \(1987\)](#); [Pesaran et al. \(1989\)](#); [Van Garderen et al. \(2000\)](#); and [Giacomini and Granger \(2004\)](#). The following questions arise: Does aggregating a disaggregated forecast improve the accuracy of the aggregate forecast? One alternative is to estimate using only the lagged aggregate variable to forecast the aggregate series. [Giacomini \(2015\)](#) points out that the results of the empirical literature are mixed, but that disaggregation can improve the forecast accuracy of the aggregate variable. Another alternative is to combine the disaggregate and aggregate series and select the relevant variables to forecast the aggregate series. [Hendry and Hubrich \(2011\)](#) suggest this as a promising direction when using model selection procedures, even though the authors developed a dynamic factor model to consider the disaggregation and did not develop a selection procedure.

Our goal was to determine whether forecasting the disaggregated components of industrial production in Brazil or combining these components with the aggregate series, improve the forecast accuracy of Brazil's aggregate industrial production compared to using only the lagged aggregate variable. We analyzed Brazil as the 9th GDP in dollars based on 2019 World Bank data. In addition, Brazil is an emerging economy, so it has a more volatile business cycle than advanced countries, a stylized fact in the literature as seen in [Aguilar and Gopinath \(2007\)](#), and in [Kohn et al. \(2021\)](#), among others. This higher volatility can lead to difficulty in forecasting Brazilian economic activity, another motivator for our research.

We do not know of any other articles that address the contributions of disaggregated data from the weighted lag adaptive least absolute shrinkage and selection operator (WLadaLASSO) methodology or from exponential triple smoothing (ETS), selecting the most appropriate model or the relevant variables from the combination of a disaggregate and aggregate series to forecast industrial production. Only [Bulligan et al. \(2010\)](#) analyzed the contributions of disaggregated data to forecast industrial production, and we intend to fill this gap. The topic of disaggregation or aggregation in forecasting is most commonly studied for the inflation and GDP series, such as [Espasa et al. \(2002\)](#); [Marcellino et al. \(2003\)](#); [Hubrich \(2005\)](#); [Carlo and Marçal \(2016\)](#); and [Heinisch and Scheufele \(2018\)](#). Additionally, we analyzed the forecast accuracies of the models based on the multi-horizon superior predictive ability method developed by [Quaedvlieg \(2021\)](#) by combining different horizons, which is different from other forecast comparison procedures that focus on the model performances of the models for each horizon separately. [Quaedvlieg \(2021\)](#) developed the average multi-horizon superior predictive ability (aSPA) and uniform multi-horizon superior predictive ability (uSPA) tests to compare a multi-horizon forecast. Using monthly data from January 2002 to February 2020, we selected the best model for a rolling window of 100 fixed observations and evaluated the forecast for industrial production in Brazil one to twelve months ahead. We used 91 rolling windows. We considered the first-order autoregressive model (AR(1)), AR(1) with time-varying parameters (TVP-AR(1)), the thirteenth-order autoregressive model (AR(13)), and the unobserved components with stochastic volatility (UC-SV) estimated based on [Barnett et al. \(2014\)](#) as naive models. We also analyzed the following methods for selecting the best model: ETS based on [Hyndman et al. \(2002, 2008\)](#) and [Hyndman and Khandakar \(2008\)](#), the least absolute shrinkage and selection operator (LASSO), adaptive LASSO (adaLASSO), the WLadaLASSO, and the

Autometrics algorithm. We used the LASSO and its variants to select the lags from the fifteenth-order autoregressive model (AR(15)). Additionally, we considered the Autometrics algorithm that selects the lags from an AR(15) and the dummy variables for outliers or breaks in the sample. In addition, we combined the disaggregated and aggregated series in the model to forecast the general industrial production. To reduce the dimensionality of this model with the combination, we adopted the LASSO and adaLASSO procedures, and the Autometrics algorithm. We compared the forecasting performance between the models based on the mean square error (MSE), the modified [Diebold and Mariano \(1995\)](#) test (henceforth, the MDM test), the model confidence set (MCS) procedure from [Hansen et al. \(2011\)](#), the forecast encompassing test from [Harvey et al. \(1998\)](#), and the multi-horizon superior predictive ability from [Quaedvlieg \(2021\)](#).

Our MSE results point to the ETS model having a better forecasting accuracy for industrial production in Brazil compared to other models. The disaggregated ETS model is the ETS model for each disaggregated series. The disaggregated ETS model leads to the lowest MSE among all of the models for all the forecast horizons, except for those that are one and two months ahead. For the forecasts that are one and two months ahead, the aggregate ETS model has a lower MSE, and there is little difference compared to the disaggregated ETS model. The aggregated ETS model is the ETS model using the lagged aggregated series as covariates. The disaggregated ETS model also has a lower MSE than the forecast of the combination of the aggregated and disaggregated series. This result is similar to that of [Faust and Wright \(2013\)](#), who determined that the combination of the disaggregated and aggregated series does not lead to a better forecast compared to aggregating the disaggregated forecasts; however, their study focused on the United States (US) consumer price index (CPI). Our results are in the opposite direction of the results by [Hendry and Hubrich \(2011\)](#) and [Weber and Zika \(2016\)](#). To analyze whether there was better statistical performance, we used the ETS with disaggregated data as a benchmark in the MDM test. The disaggregated ETS model presents a better forecast performance compared to the naive models (AR(1), AR(13), TVP-AR(1), UC-SV), LASSO, and variants, and the Autometrics algorithm, considering aggregated and disaggregated data (or a combination of both). Only the aggregated ETS model has equal predictive accuracy to the disaggregated ETS model for the forecast horizons of one to five, seven, ten, and twelve months ahead based on the MDM test. The set of “best” models for the most forecast horizons includes only the disaggregated and aggregated ETS models with 90% probability according to the MCS. In 2 of the 12 forecasting horizons, the MCS only has the disaggregated ETS model. We also used the forecast encompassing test. Results showed that the optimal combination forecast only incorporated forecasts from the disaggregated ETS model and the aggregated ETS model. The disaggregated ETS forecast was the only model to be considered in the optimal combination forecast of industrial production for 10 horizons among the 12 analyzed, comparable to the aggregated ETS model. Aggregated ETS does not contain information that is useful for forecasting industrial production in Brazil beyond the information already found in the disaggregated ETS between two and twelve months ahead. When we analyzed the 12 horizons together, we rejected the null hypothesis of equal predictability for all of the models compared to the disaggregated ETS by the uSPA and aSPA tests at 5% statistical significance. In short, we determined that the ETS model presents the best forecast performance comparatively, which is a result similar to that of [Elliott and Timmermann \(2008\)](#). The disaggregated ETS is superior after 6 horizons when compared to the aggregated ETS based on the aSPA test. The aggregated ETS only introduces relevant information to forecast industrial production for one period ahead compared to the disaggregated ETS according to the forecast encompassing test, which indicates the superiority of disaggregated information for industrial production, which is in line with [Bulligan et al. \(2010\)](#).

This article contains five sections in addition to this introduction. Section 2 reviews the literature. Next, we will address the methodologies of the models considered in the paper in Section 3. Section 4 presents our data, the empirical forecasting strategy, the MDM

test, the MCS procedure, the forecast encompassing test, and the aSPA and uSPA tests to compare how the models perform. In Section 5, we will analyze the results of the study. Finally, Section 6 presents the concluding remarks.

## 2. Literature Review

This section discusses the differences in the forecast accuracy in three scenarios—aggregating the disaggregated forecasts, only modeling the aggregate variable, and combining the aggregated and disaggregated series. Bulligan et al. (2010) analyzed the forecasting performance of industrial production models in Italy with forecast horizons that ranged from 1 to 3 months ahead. They determined that disaggregated models have better forecast performance based on the root of MSE. There are not many analyses in the literature that differentiate between the use of the disaggregated and aggregated series to forecast the aggregated series of industrial production. As such, we have to fill in this gap.

Carstensen et al. (2011) compared the ability of indicators to forecast industrial production in the Euro area. The authors were unable to determine any indicator that was dominant as the best predictor of the industrial production because it depends on the forecast horizon and the loss function considered. Additionally, the forecast of the AR(1) model is quite difficult to beat during quiet times based on the fluctuation test by Giacomini and Rossi (2010). Rossi and Sekhposyan (2010) found that the useful predictors for forecasting US industrial production change over time. However, they did not use a disaggregated series of industrial production as Carstensen et al. (2011) did. Kotchoni et al. (2019) analyzed the performance of models selecting factors from 134 monthly macroeconomic and financial indicators to forecast industrial production, and they compared these models to standard time series models. They found that the MCS selected the LASSO model for forecasting during periods of recessions, but did not choose it to forecast the full out-of-sample data.

When addressing the forecast ability of other economic variables, Marcellino et al. (2003) found evidence that the individual estimation of inflation in each Euro area country and the subsequent aggregation of projections increase the forecast accuracy related to forecasting of this variable at the aggregate level. Hubrich (2005) determined that aggregating the forecasts of each component of inflation does not necessarily better predict inflation in the Euro area one year ahead. Espasa et al. (2002) had similar results, indicating that disaggregation leads to better projections for periods longer than one month. Carlo and Marçal (2016) compared forecasts from models for aggregate inflation and those aggregating the forecasts for the components from the Brazilian inflation index. The authors determined that the forecast using disaggregated data increased accuracy, such as Heinisch and Scheufele (2018).

Zellner and Tobias (2000) studied the effects of aggregated and disaggregated models in forecasting the average annual GDP growth rate of 18 countries. In general, disaggregation led to more observations that could be used to estimate the parameters, but the authors obtained better predictions for the aggregate variable. Barhoumi et al. (2010) analyzed the forecasting performance of France's GDP between alternative factor models. They wanted to know whether it was more appropriate to extract factors from aggregate or disaggregated data for forecasting purposes. Rather than using 140 disaggregated series, Barhoumi et al. (2010) showed that the static approach of Stock and Watson (2002) using 20 aggregate series led to better prediction results. In other words, the mentioned articles present favorable evidence for the use of a disaggregated series or to model using an aggregated series only, leaving the question open.

Hendry and Hubrich (2011) proposed an alternative use of a disaggregate variable to forecast the aggregate variable, which was a combination of disaggregated and aggregated variables. This is different from previous literature, which suggested forecasting the disaggregate variables and then aggregating them to obtain the forecast of the aggregate variable, as we discussed earlier in this section. Hendry and Hubrich (2011) determined that including disaggregate variables in the aggregate model improves the forecast accuracy if the disaggregates have different stochastic structures and if the components are interdependent,



according to Monte Carlo simulations. They sought to forecast US inflation by considering the sectorial breakdown of inflation. To reduce the dimension of the disaggregate variables, they used the factor model with the results of using this combination, corroborating those obtained by the Monte Carlo simulations. [Hendry and Hubrich \(2011\)](#) introduced (as a promising direction for procedures) selection of the disaggregated series and their lags together with the lags of the aggregate series to predict the aggregate series.

[Faust and Wright \(2013\)](#) analyzed the forecasting models for the US CPI. They considered the combination idea from [Hendry and Hubrich \(2011\)](#) and compared the use of the aggregated or disaggregated series individually in the model, but did not suggest procedures for variable selection. They determined that the combination model did not lead to a better forecasting performance for the aggregated series according to the root of the MSE when compared to disaggregated or aggregated models. [Weber and Zika \(2016\)](#) sought to forecast general employment in Germany as a function of its lags and disaggregation in different sectors. However, the authors used principal components to summarize information from the sectors. They determined that the disaggregation improved the forecast for general employment when compared to the univariate model for the aggregate series. As such, the contributions of this article include the results of combining the aggregated and disaggregated series and using the variable selection procedure to fill this gap.

Regarding the literature on the methodologies used in this work, [Epprecht et al. \(2021\)](#) conducted a Monte Carlo simulation experiment that considered the data generating process (DGP) to be a linear regression with orthogonal variables and independent data. The authors determined that adaLASSO and the Autometrics algorithms also have similar forecasting performances when there are a small number of relevant variables and when the number of candidate variables is lower than the number of observations. The Autometrics algorithm only performs better when it has a large number of relevant variables (as 15 to 20) because of the bias against the penalization term in adaLASSO. Additionally, [Epprecht et al. \(2021\)](#) determined that adaLASSO performs better than LASSO and the Autometrics algorithm for linear regression with orthogonal variables in terms of model performance. Autometrics is only preferable with small samples. The authors also used genomics data to compare the predictive power to the epidermal thickness in psoriatic patients, in which covariates are not orthogonal. Out-of-sample forecasts with variables that were selected via LASSO, adaLASSO, or Autometrics cannot be statistically differentiated by the MDM test.

[Kock and Teräsvirta \(2014\)](#) used a neural network model with three algorithms to model monthly industrial production and unemployment series from the Group of Seven (G7) countries and Denmark, Finland, Norway, and Sweden. They focused on forecasting during the economic crisis from 2007 to 2009. The authors found that the Autometrics algorithm performs worse with direct forecasts than with recursive forecasts because the model is not a reasonable approximation of reality (as it excludes the most relevant lags).<sup>1</sup> The Autometrics algorithm tends to select a highly parameterized model that does not present competitive forecasts compared to other methodologies in direct forecasting. That is, [Kock and Teräsvirta \(2014\)](#) determined that the Autometrics algorithm may perform worse when there are considerable misspecifications in the general model. In the present work, we used recursive forecasting, in which, according to [Kock and Teräsvirta \(2014\)](#), the Autometrics algorithm does not perform badly. The next section presents the methodology used in this paper.

### 3. Methodology

We considered four naive models to compare our forecasts: UC-SV and an autoregressive model with constant parameters or with time-varying parameters. Our goal was to select the lagging variables that were relevant based on different univariate methodologies. We used LASSO and two of its variants (adaLASSO and WLadaLASSO), the exponential smoothing method, and the Autometrics algorithm. We used the variable  $\Delta y_t$  in the cases of AR(1), AR(13), TVP-AR(1), LASSO and its variants, and the Autometrics algorithm because the series  $y_t$  is non-stationary and  $\Delta y_t$  removes a unit root from the dynamics, where  $\Delta$  is

the first difference operator.<sup>2</sup> In the case of UC-SV and exponential smoothing, we used the variable  $y_t$ .

### 3.1. Time-Varying Parameters Autoregressive Model of First Order

In this section, we present the methodology of the TVP-AR(1) model. We used this model to obtain a naive forecast and only considered one lag in the model. The methodology using time-varying parameters seeks to contemplate the changes that can occur in the economy over time (Kapetanios et al. 2019). Considering the TVP-AR(1) model, the measurement equation can be written as

$$\Delta y_t = \beta_{0t} + \beta_{1t} \Delta y_{t-1} + \varepsilon_t \quad (1)$$

where  $\varepsilon_t \sim N(0, \sigma^2)$  for  $t = 1, \dots, T$ , and  $\Delta y_0$  is an initial observation. We can write the autoregressive and the constant coefficients  $\beta_t = (\beta_{0t}, \beta_{1t})^\top$  with the following transition equation

$$\beta_t = \beta_{t-1} + u_t \quad (2)$$

where  $u_t \sim N(0, \Omega)$ ,  $\top$  is the transpose of a matrix and the transition equation has the initial value  $\beta_1 \sim N(\beta_0, \Omega_0)$ .

We used the Bayesian estimation according to Kroese et al. (2014). See Appendix A.1 for more details. Next, we will explain the UC-SV model that we used in the present study.

### 3.2. UC with Stochastic Volatility

Stock and Watson (2007) included stochastic volatility in an unobserved component model. The authors showed that UC-SV performed well when forecasting US inflation. The UC-SV model is defined as

$$y_t = \beta_t + \sigma_t^{\frac{1}{2}} v_t \quad (3)$$

$$\beta_t = \beta_{t-1} + \omega_t^{\frac{1}{2}} e_t \quad (4)$$

where  $\ln \sigma_t$  and  $\ln \omega_t$  are the logarithm of the stochastic volatility,  $\beta_t$  is the trend,  $\ln \sigma_t = \ln \sigma_{t-1} + e_{1t}$ , and  $\ln \omega_t = \ln \omega_{t-1} + e_{2t}$ . We allowed the variances of  $e_{1t}$  and  $e_{2t}$  to be distinct following Barnett et al. (2014), which is different from Stock and Watson (2007) who assumed that the variances of the two stochastic volatility processes were equal.<sup>3</sup> The variances of  $e_{1t}$  and  $e_{2t}$  are denoted by  $g_1$  and  $g_2$ , respectively.<sup>4</sup>

We estimated the model using the Markov chain Monte Carlo (MCMC) method with the Gibbs sampling method following Barnett et al. (2014). We describe the MCMC method in Appendix A.2, and we detail the Bayesian estimation and the priors in Appendix A.3.

### 3.3. LASSO-Type Penalties

In this subsection, we present three lasso-type penalties to select the relevant lags for the univariate model from an AR(15): LASSO, adaLASSO, and WLadaLASSO.

#### 3.3.1. LASSO

Tibshirani (1996) proposed the LASSO method based on the following minimization problem

$$\hat{\beta}^{LASSO} = \underset{\beta_0, \beta_1, \dots, \beta_k}{\operatorname{argmin}} \sum_{t=1}^T \left( \Delta y_t - \beta_0 - \sum_{j=1}^k \beta_j \Delta y_{t-j} \right)^2 + \lambda \sum_{j=1}^k |\beta_j| \quad (5)$$

where  $\lambda \geq 0$  is a tuning parameter. LASSO needs a value for  $\lambda$ , which we will explain shortly. The first term is the sum of the square of the residuals and the second term is a shrinkage penalty.  $\sum_{j=1}^k |\beta_j|$  is the  $\ell^1$  norm of a coefficient vector  $\beta$ . The  $\ell^1$  penalty forces

some of the coefficient estimates to be equal to zero when  $\lambda$  is sufficiently large. As such, the LASSO technique can perform the variable selection.

Cross-validation is usually the method choice for obtaining  $\lambda$  value. With the time series data, we used the Bayesian information criterion (BIC) to choose  $\lambda$  according to [Konzen and Ziegelmann \(2016\)](#), based on a grid of  $\lambda$  values. The grid of possible values for  $\lambda$  is (0, 0.5, 1, ..., 10).

### 3.3.2. AdaLASSO

[Zou \(2006\)](#) stated that LASSO can lead to the inconsistent selection of variables that maintain noisy variables for a given  $\lambda$ . Additionally, the author showed that LASSO could lead to correct variable selections using biased estimates for large coefficients, resulting in suboptimal prediction rates.

As such, [Zou \(2006\)](#) introduced adaLASSO, which considers weights  $\omega_j$  that adjust the penalty to be different for each coefficient. The adaLASSO seeks to minimize

$$\hat{\beta}^{adaLASSO} = \underset{\beta_0, \beta_1, \dots, \beta_k}{\operatorname{argmin}} \sum_{t=1}^T \left( \Delta y_t - \beta_0 - \sum_{j=1}^k \beta_j \Delta y_{t-j} \right)^2 + \lambda \sum_{j=1}^k \omega_j |\beta_j| \quad (6)$$

where  $\omega_j = |\hat{\beta}_j^{ridge}|^{-\tau}$ ,  $\tau > 0$ . adaLASSO considers that large (small) coefficients have small (large) weights and small (large) penalties. We used ridge regression estimated coefficients  $\hat{\beta}^{ridge}$  to determine the weight  $\omega_j$ . Ridge regression shrinks the vectors of the coefficients by penalizing the sum of the squares of the residuals:

$$\hat{\beta}^{ridge} = \underset{\beta_0, \beta_1, \dots, \beta_k}{\operatorname{argmin}} \sum_{t=1}^T \left( \Delta y_t - \beta_0 - \sum_{j=1}^k \beta_j \Delta y_{t-j} \right)^2 + \lambda \sum_{j=1}^k \beta_j^2 \quad (7)$$

where the penalty is the  $\ell^2$  norm of the  $\beta$  vector. Ridge regression is not a variable selection method because this regression obtains non-zero estimates for all coefficients.

### 3.3.3. WLadaLASSO

When we used adaLASSO with the time series data, each coefficient was associated with a lagged variable and penalized according to the size of the ridge regression's estimate. The less distant the lag in the variable, the more important the variable must be for the model; therefore, its coefficient should be penalized less (considering the case without seasonality).

[Park and Sakaori \(2013\)](#) proposed different types of penalties for different lags. [Konzen and Ziegelmann \(2016\)](#) denominated the adaLASSO with weighted lags based on those from [Park and Sakaori \(2013\)](#) as WLadaLASSO. The WLadaLASSO method is calculated as:

$$\hat{\beta}^{wladaLASSO} = \underset{\beta_0, \beta_1, \dots, \beta_k}{\operatorname{argmin}} \sum_{t=1}^T \left( \Delta y_t - \beta_0 - \sum_{j=1}^k \beta_j \Delta y_{t-j} \right)^2 + \lambda \sum_{j=1}^k \omega_j^w |\beta_j| \quad (8)$$

where  $\omega_j^w = \left( |\hat{\beta}_j^{ridge}| e^{-\alpha l} \right)^{-\tau}$  is the weight,  $\tau > 0$ ,  $\alpha \geq 0$ ,  $l$  is the order of the variable's lag, and  $e$  is the exponential function. We set the parameter  $\tau$  equal to one for adaLASSO and WLadaLASSO, which was the case in [Konzen and Ziegelmann \(2016\)](#). We considered a grid for  $\alpha$ , where the set of possible values for  $\alpha$  was (0, 0.5, 1, ..., 10). We calculated the optimal  $\lambda$  among those possible for that model with the lowest BIC value for each  $\alpha$  value. We chose the  $\alpha$  value from the model producing the smallest BIC value among all of the possible  $\alpha$  values, following [Konzen and Ziegelmann \(2016\)](#).

### 3.4. Exponential Smoothing

The name exponential smoothing comes from the idea that recent observations are more important to forecasting than older observations and, therefore, have a greater weight to forecast. Exponential smoothing is basically an exponentially weighted sum of past values (to obtain the forecast). We can represent the ETS method as a state space model (Hyndman et al. 2002, 2005; Ord et al. 1997).

We can decompose the economic series into certain components, such as trends (T), cycles (C), seasonality (S), and irregularities or error (E). We used the ETS method to decompose the series into these components. Only the cycle component was not decomposed separately so that it could be modeled along with the trend component following Hyndman and Khandakar (2008) and Hyndman et al. (2008). Thus, we can combine the trend, seasonality, and error components.

Hyndman and Khandakar (2008) and Hyndman et al. (2008) proposed 15 different combinations among the trend and seasonality components. The trend represents the long-term direction of the series. The trend component presents five different possibilities: none, additive, additive damped, multiplicative, and multiplicative damped. The trend component is a combination of the level ( $\ell$ ) and growth ( $b$ ) parameters.  $T_h$  is the forecast trend over the next  $h$  periods, and  $\phi$  is a damping parameter ( $0 < \phi < 1$ ). As such, if there is no trend component,  $T_h = \ell$ . If the trend component is additive,  $T_h = \ell + bh$ . If the trend component is additively damped,  $T_h = \ell + (\phi + \phi^2 + \dots + \phi^h)b$ . If the trend component is multiplicative,  $T_h = \ell b^h$ . If the trend component is multiplicative damped,  $T_h = \ell b^{(\phi + \phi^2 + \dots + \phi^h)}$ . If the growth rate at the end of the series is unlikely to continue, then the damped trend seems to be the most reasonable option.

The next step is to detail the types of seasonal components. There are three types of seasonal components: none, additive, and multiplicative. Additionally, the error component can be additive or multiplicative, but this distinction is not relevant for point forecasting (Hyndman et al. 2008).

As such, we considered the combination of five types of trend components and three types of seasonal components, resulting in 15 types of ETS models, following Hyndman and Khandakar (2008). These 15 possibilities are presented in Table 1 of Hyndman et al. (2008), in which the first entry refers to the trend component and the second refers to the seasonal component.

Basically, the estimation procedure is based on estimating the smoothing parameters and the initial state variables maximizing the likelihood function. The algorithm proposed by Hyndman et al. (2002) also determines which of the 15 ETS models is the most appropriate by selecting the model based on the information criterion. The information criteria used to select the most appropriate model are AIC corrected for small sample bias (AICc), as suggested by Talagala et al. (2018). See Appendix A.4 for more details. We present the Autometrics algorithm in the next subsection.

### 3.5. Autometrics Algorithm

We used the Autometrics algorithm (Castle et al. 2011; Doornik 2008) to address potential instability points and structural changes and to select the lags of the dependent variable that were relevant. The algorithm is based on an approach called the London School of Economics econometric methodology, in which the specification search starts from the General model, and using specification and misspecification tests, the model can be simplified to a Specific model, called GETS. From a general unrestricted model, the algorithm attempts to reduce the unrestricted model through combinations of variables in the general model to evaluate the relevance of these variables to eliminate the irrelevant variables (variables with coefficients that are statistically insignificant). During each step, attempting to reduce the model, the algorithm performs diagnostic tests on the errors to verify the congruence of the models after variables are eliminated.<sup>5</sup> The purpose of this



procedure is to determine the most comprehensive and parsimonious model that is a good representation of the local DGP.

The Autometrics algorithm starts by using a general model in which there are up to 15 lags in the dependent variable for industrial production in Brazil using the following equation

$$\Delta y_t = \sum_{i=1}^{15} \rho_i \Delta y_{t-i} + \sum_{l=1}^T (\alpha_l IIS_l) + \sum_{s=1}^{11} \theta_s Se_s + \varepsilon_t \quad (9)$$

where  $IIS_l$  is an impulse variable that is only equal to one at  $t = l$  and zero otherwise (Pretis et al. 2018).  $Se_s$  is the monthly dummy variable for each month  $s$ .  $\varepsilon_t$  is the error term.

There are two types of models that use Autometrics. The first is the “without outlier” type, which does not consider any type of outlier in the general model. The second type is the “IIS” type, which allows the dummy variables to control for the outlier in the specific model. See Appendix A.5 for more details.

### 3.6. Combination of Aggregated and Disaggregated Series

Hendry and Hubrich (2011) proposed combining a disaggregated and aggregated series to forecast the aggregated series because it could improve the forecast accuracy. However, we considered the combination of the two using the variable selection procedure from the following general model:

$$\Delta y_{g,t} = \sum_{i=1}^{15} (\rho_i \Delta y_{g,t-i}) + \sum_{i=0}^{15} \sum_{j=1}^{24} (\beta_{ji} \Delta y_{j,t-i}) + \varepsilon_t \quad (10)$$

where  $y_{g,t}$  is the general industrial production;  $y_{j,t-i}$  is the industrial production of sector  $j$  and includes a total of 24 sectors—the disaggregated series.

We had 399 parameters—disregarding the constant—to estimate this equation, which was greater than the number of observations for each rolling window—100 observations (defined in Section 4.1). As such, we needed to reduce the dimensionality. We used three methods to select the relevant variables and their lags: LASSO, adaLASSO, and the Autometrics algorithm. Thus, we considered three different methodologies for combining the disaggregated and aggregated series to forecast the general industrial production.

However, we needed the forecast of the disaggregated series to obtain the forecast for the general industry for  $h$  months ahead. For this, we used the forecasts for the disaggregated series that we estimated with each univariate model discussed earlier: the AR(1), TVP-AR(1), UC-SV, ETS; LASSO and its variants; and the Autometrics algorithm and its variant. As such, we had three procedures to select the relevant variables for Equation (10); for each procedure, we used the forecasts for each sector using the 11 models to estimate the forecast for the general industrial production. In this sense, we analyzed 33 different possible combinations. Once again, we used the significance level  $\alpha = 0.1\%$  in the Autometrics algorithm for the combinations.

## 4. Data and Empirical Strategy

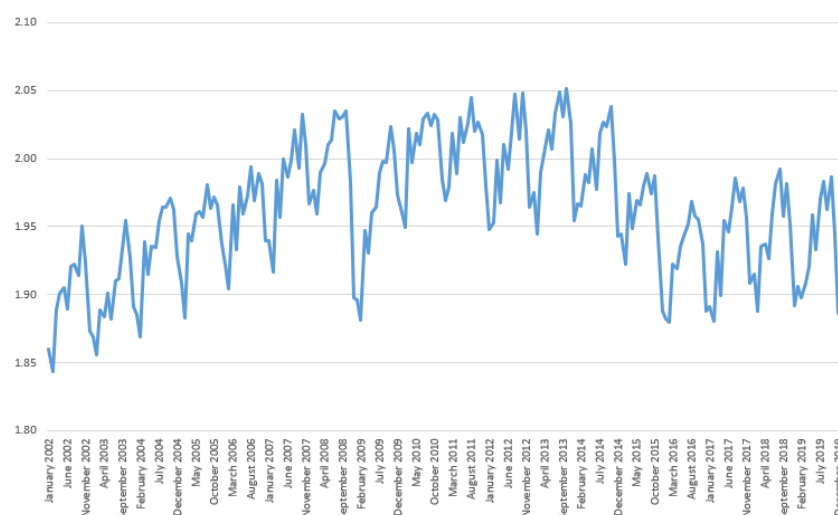
Our data were the logarithm of the industrial production in Brazil index at the general level and its disaggregation by sectors. The data were from the Monthly Industrial Survey of Physical Production (PIM-PF) from the Brazilian Institute of Geography and Statistics (IBGE). We used monthly data from January 2002 to February 2020 and did not make any seasonal adjustments. We did not consider vintage data or past revisions for these series. We removed a unit root from the dynamics using the first difference of the series, with the exception of the UC-SV and ETS models.

The general industry forecast was carried out using a model that only included the lags in this series; we compared this forecast to the forecast for each sector (aggregated according to weight) to obtain the general industry forecast. We used the weights for each

sector according to PIM-PF. According to the IBGE, the weights for each sector have been fixed since 2002, which is our period of analysis.

In addition, we compared the forecast of the aggregate model with the combination of the aggregated and disaggregated series. Thus, we used disaggregated data for the extractive industry and for the 25 sectors of the manufacturing industry. However, two sectors, “printing and reproduction of recordings”, and “maintenance, repair and installation of machines and equipment”, only presented data from January 2012 and, therefore, we did not include these sectors in the estimates.<sup>6</sup> Thus, our disaggregated sample includes the extractive industry category and 23 sectors of the manufacturing industry.

We present the behavior of the logarithm concerning general industrial production in Brazil between January 2002 and February 2020 in Figure 1. There is evidence of seasonality in the series. In addition, the series had an increasing growth rate between 2002 and 2008; between 2009 and 2014 there was no growth in the series. Between 2014 and 2016 there was a fall in industrial production—a period that is noted as being a recession according to the official Brazilian committee for dating business cycles (CODACE).<sup>7</sup> There has been no growth in the series since 2017.



**Figure 1.** Time series of the logarithm of general industrial production in Brazil.

Table A1 in Appendix A.10 reports descriptive statistics for the logarithm of the series analyzed  $y_t$  in the first difference ( $\Delta y_t$ ) and the twelfth difference ( $\Delta_{12}y_t$ ) for comparison. Except for the mean, the other descriptive statistics, such as standard deviation, maximum, minimum, first, and third quantiles, are similar between  $\Delta y_t$  and  $\Delta_{12}y_t$ .  $\Delta_{12}y_t$  has a more right-skewed distribution than  $\Delta y_t$  based on the first and third quantiles.<sup>8</sup> Next, we will detail the empirical strategy and how we compared it with the predictions that were obtained.

#### 4.1. Empirical Strategy and Forecast Comparison

The model that we considered contained 15 lags of the dependent variable. Thus, we used a rolling window of 100 fixed observations for each estimation. We analyzed a recursive forecast horizon that was one to twelve months ahead. We had 91 rolling windows for the general industry forecast series. We re-estimated the model, and we allowed for the best model to be re-specified according to each methodology for each rolling window. We forecasted the production of each sector and used the weight of each sector to obtain the forecasts for the general industry from its components. Our forecast window for analysis ranged from September 2011 to February 2020.

We compared our forecasts with the estimates of four naive models: the AR(1) model, the AR(13) model, the TVP-AR(1) model, and the UC-SV model. All the models were estimated using the data for the general industry (aggregated forecast), the forecast for the

general industry from the disaggregated data (disaggregated forecast), or the forecast for the general industry obtained from a combination of an aggregated and a disaggregated series (combination). Thus, we obtained three naive predictions using the AR(1) model (aggregated, disaggregated, and the combination).

We analyzed the forecast performance of the models using the MSE, the MDM test (for details, see Appendix A.6), the MCS from Hansen et al. (2011) (for details, see Appendix A.7), the forecast encompassing test using the implementation in Harvey et al. (1998) (for details, see Appendix A.8), and the multi-horizon forecast comparison via the uSPA and aSPA tests from Quaadvlieg (2021), which are a generalization of Hansen (2005) (for details, see Appendix A.9). We wanted to establish if there was a model that could accurately predict the Brazilian general industrial production index for the period considered. We discuss the results in the next section.

## 5. Results

This section presents the forecasts of the naive models—AR(1), AR(13), TVP-AR(1), and UC-SV—for one to twelve months ahead as well as the lag selection resulting from the LASSO and its two variants (adaLASSO and WLadaLASSO), ETS, and Autometrics with and without the inclusion of IIS variables. We used these models to forecast the first difference in the logarithm of the general industrial production from aggregated and disaggregated data and from the combination of both. We compared the results according to five aspects: (i) the MSE, (ii) the MDM test, (iii) the MCS, (iv) the forecasting encompassing test, and (v) the aSPA and uSPA tests to determine the model that provides the most accurate forecast. Table 1 shows the acronyms that we used in this section to describe the models.

Table 2 presents the MSE for the forecast of the first difference in the logarithm of industrial production  $\Delta y_{t+h}$ , one to twelve months ahead for the different models. We multiplied the MSE value by  $10^3$  to improve the visualization of the results reported in Table 2. We also reported the lowest MSE value per forecast horizon (bold). The ETS model resulted in a lower MSE compared to the other models forecasting the first difference in the logarithm of industrial production for all of the forecast horizons. This is not an unprecedented result in the literature. Elliott and Timmermann (2008) determined that ETS led to a lower MSE to forecast US inflation and a value-weighted portfolio of US stocks when disregarding combination forecasts.<sup>9</sup> In general, one can see that the MSE is smaller for the models with disaggregated series compared to the models with aggregated series; this is independent of the forecast horizon, except for TVP-AR(1), UC-SV, and the Autometrics algorithm when considering IIS dummy variables. The model with the lowest MSE for the forecast for one and two months ahead is the aggregated ETS model, but the difference in the MSE is small compared to the disaggregated ETS. Forecasts with the disaggregated ETS present the lowest MSE for all of the other forecast horizons. The TVP-AR(1) model has the worst forecasting performance based on the MSE, regardless of whether the series is aggregated or disaggregated.

**Table 1.** Model Abbreviations.

Abbreviation	Definition
$AR(1)^{dis}$	AR(1) with disaggregated series
$AR(1)^{ag}$	AR(1) with aggregated series
$AR(13)^{dis}$	AR(13) with disaggregated series
$AR(13)^{ag}$	AR(13) with aggregated series
$TVP^{dis}$	TVP-AR(1) with disaggregated series
$TVP^{ag}$	TVP-AR(1) with aggregated series
$UC-SV^{dis}$	UC-SV with disaggregated series
$UC-SV^{ag}$	UC-SV with aggregated series
$ETS^{dis}$	ETS with disaggregated series
$ETS^{ag}$	ETS with aggregated series
$LAS^{dis}$	LASSO with disaggregated series
$LAS^{ag}$	LASSO with aggregated series
$ada^{dis}$	adaLASSO with disaggregated series
$ada^{ag}$	adaLASSO with aggregated series
$WL^{dis}$	WLadaLASSO with disaggregated series
$WL^{ag}$	WLadaLASSO with aggregated series
$Aut\_no^{dis}$	Autometrics without outlier and with disaggregated series
$Aut\_no^{ag}$	Autometrics without outlier and with aggregated series
$Aut\_IIS^{dis}$	Autometrics with IIS dummy variables and with disaggregated series
$Aut\_IIS^{ag}$	Autometrics with IIS dummy variables and with aggregated series
$c\_LAS\_ada$	Combination with LASSO to select and use adaLASSO forecasts
$c\_LAS\_Aut\_no$	Combination with LASSO to select and use $Aut\_no$ forecasts
$c\_LAS\_Aut\_IIS$	Combination with LASSO to select and use $Aut\_IIS$ forecasts
$c\_LAS\_LAS$	Combination with LASSO to select and use LASSO forecasts
$c\_LAS\_TVP$	Combination with LASSO to select and use TVP-AR(1) forecasts
$c\_LAS\_UC-SV$	Combination with LASSO to select and use UC-SV forecasts
$c\_LAS\_WL$	Combination with LASSO to select and use WLadaLASSO forecasts
$c\_LAS\_ETS$	Combination with LASSO to select and use ETS forecasts
$c\_LAS\_AR(1)$	Combination with LASSO to select and use AR(1) forecasts
$c\_ada\_ada$	Combination with adaLASSO to select and use adaLASSO forecasts
$c\_ada\_Aut\_no$	Combination with adaLASSO to select and use $Aut\_no$ forecasts
$c\_ada\_Aut\_IIS$	Combination with adaLASSO to select and use $Aut\_IIS$ forecasts
$c\_ada\_LAS$	Combination with adaLASSO to select and use LASSO forecasts
$c\_ada\_TVP$	Combination with adaLASSO to select and use TVP-AR(1) forecasts
$c\_ada\_UC-SV$	Combination with adaLASSO to select and use UC-SV forecasts
$c\_ada\_WL$	Combination with adaLASSO to select and use WLadaLASSO forecasts
$c\_ada\_ETS$	Combination with adaLASSO to select and use ETS forecasts
$c\_ada\_AR(1)$	Combination with adaLASSO to select and use AR(1) forecasts
$c\_Aut\_ada$	Combination with Autometrics to select and use adaLASSO forecasts
$c\_Aut\_Aut\_no$	Combination with Autometrics to select and use $Aut\_no$ forecasts
$c\_Aut\_Aut\_IIS$	Combination with Autometrics to select and use $Aut\_IIS$ forecasts
$c\_Aut\_LAS$	Combination with Autometrics to select and use LASSO forecasts
$c\_Aut\_TVP$	Combination with Autometrics to select and use TVP-AR(1) forecasts
$c\_Aut\_UC-SV$	Combination with Autometrics to select and use UC-SV forecasts
$c\_Aut\_WL$	Combination with Autometrics to select and use WLadaLASSO forecasts
$c\_Aut\_ETS$	Combination with Autometrics to select and use ETS forecasts
$c\_Aut\_AR(1)$	Combination with Autometrics to select and use AR(1) forecasts

Except for ETS models, the procedure with the smallest MSE is WLadaLASSO with disaggregation for all of the studied forecast horizons—the disaggregated AR(13) model has lower MSE than disaggregated WLadaLASSO only for the forecast (of one month ahead). The combination of the aggregated and disaggregated series with the lowest MSE is the  $c\_LAS\_WL$  model for all of the forecast horizons; this model relies on LASSO to select the most relevant variables in the combination and uses the disaggregated WLadaLASSO forecasts to make predictions. However, this combination leads to a larger MSE than the disaggregated WLadaLASSO does for all the forecast horizons. Even the combination with the lowest MSE has less accurate predictions than the model with the best forecast, excluding the ETS models. Our result—that the combination of the disaggregated and aggregated series does not lead to the best forecast—is similar to the finding by [Faust and Wright \(2013\)](#). However, our result is the opposite of [Hendry and Hubrich \(2011\)](#) and [Weber and Zika \(2016\)](#).

**Table 2.** MSE forecasting results for one to twelve months ahead for different models.

Models	1	2	3	4	5	6	7	8	9	10	11	12
$AR(1)^{dis}$	4.01	4.12	4.22	4.28	4.31	4.33	4.34	4.33	4.32	4.33	4.33	4.33
$AR(1)^{ag}$	4.24	4.26	4.32	4.35	4.37	4.37	4.37	4.36	4.35	4.35	4.35	4.35
$AR(13)^{dis}$	1.21	1.41	1.51	1.59	1.65	1.68	1.70	1.71	1.72	1.72	1.73	1.73
$AR(13)^{ag}$	1.39	1.61	1.70	1.78	1.86	1.90	1.91	1.93	1.94	1.95	1.96	1.96
$TVP^{dis}$	5.27	5.29	5.70	5.96	6.05	6.12	6.11	6.08	5.94	5.74	5.52	5.30
$TVP^{ag}$	5.31	5.31	5.71	5.96	6.03	6.09	6.06	6.01	5.86	5.65	5.44	5.24
$UC-SV^{dis}$	5.02	7.51	8.34	8.81	9.13	9.35	9.50	9.62	9.70	9.73	9.77	9.80
$UC-SV^{ag}$	4.97	7.44	8.29	8.77	9.08	9.31	9.47	9.59	9.66	9.70	9.74	9.77
$ETS^{dis}$	0.16	0.19	<b>0.21</b>	<b>0.21</b>	<b>0.22</b>	<b>0.22</b>	<b>0.22</b>	<b>0.22</b>	<b>0.22</b>	<b>0.22</b>	<b>0.22</b>	<b>0.22</b>
$ETS^{ag}$	<b>0.16</b>	<b>0.19</b>	0.21	0.21	0.22	0.22	0.22	0.22	0.22	0.22	0.23	0.23
$LAS^{dis}$	1.25	1.40	1.49	1.58	1.64	1.67	1.69	1.70	1.71	1.72	1.74	1.75
$LAS^{ag}$	1.58	1.72	1.81	1.92	2.01	2.05	2.06	2.08	2.09	2.09	2.09	2.09
$ada^{dis}$	1.25	1.40	1.49	1.57	1.63	1.66	1.68	1.70	1.71	1.72	1.74	1.75
$ada^{ag}$	1.62	1.74	1.83	1.94	2.01	2.04	2.05	2.08	2.08	2.08	2.09	2.09
$WLa^{dis}$	1.24	1.38	1.47	1.55	1.60	1.63	1.66	1.67	1.69	1.70	1.71	1.72
$WLa^{ag}$	1.59	1.75	1.86	1.97	2.05	2.09	2.11	2.13	2.14	2.14	2.14	2.15
$Aut\_no^{dis}$	1.78	1.76	1.76	1.79	1.81	1.81	1.81	1.81	1.82	1.82	1.82	1.83
$Aut\_no^{ag}$	2.04	2.01	1.93	1.97	1.97	1.99	2.00	1.99	1.98	1.96	1.95	1.94
$Aut\_IIS^{dis}$	2.00	2.06	2.27	2.94	2.72	2.56	2.60	2.51	2.50	2.45	2.45	2.42
$Aut\_IIS^{ag}$	2.16	2.28	2.50	3.19	3.05	2.95	3.05	2.94	2.93	2.92	2.90	2.90
$c\_LAS\_ada$	1.27	1.42	1.51	1.60	1.66	1.70	1.72	1.74	1.76	1.77	1.79	1.81
$c\_LAS\_Aut\_no$	1.84	1.82	1.83	1.86	1.88	1.89	1.89	1.89	1.89	1.90	1.91	1.92
$c\_LAS\_Aut\_IIS$	1.97	2.03	2.26	2.76	2.58	2.46	2.50	2.42	2.41	2.38	2.37	2.35
$c\_LAS\_LAS$	1.27	1.42	1.52	1.61	1.67	1.71	1.73	1.74	1.76	1.77	1.79	1.80
$c\_LAS\_TVP$	4.89	4.93	5.30	5.56	5.64	5.71	5.70	5.67	5.53	5.35	5.15	4.96
$c\_LAS\_UC-SV$	4.74	4.57	4.76	4.92	4.96	5.01	4.98	4.95	4.86	4.72	4.63	4.51
$c\_LAS\_WLa$	1.25	1.40	1.49	1.57	1.63	1.66	1.69	1.71	1.73	1.75	1.77	1.78
$c\_LAS\_ETS$	3.22	2.68	2.52	2.44	2.40	2.36	2.34	2.32	2.31	2.30	2.30	2.29
$c\_LAS\_AR(1)$	3.79	3.92	4.02	4.08	4.12	4.13	4.14	4.14	4.13	4.13	4.14	4.14
$c\_ada\_ada$	1.29	1.44	1.53	1.61	1.67	1.70	1.73	1.75	1.77	1.79	1.81	1.82
$c\_ada\_Aut\_no$	1.92	1.88	1.89	1.91	1.93	1.93	1.92	1.93	1.93	1.94	1.95	1.95
$c\_ada\_Aut\_IIS$	2.05	2.10	2.34	2.86	2.67	2.55	2.59	2.50	2.50	2.46	2.45	2.43
$c\_ada\_LAS$	1.28	1.44	1.53	1.62	1.68	1.72	1.74	1.76	1.77	1.79	1.81	1.82
$c\_ada\_TVP$	4.98	5.03	5.42	5.69	5.78	5.85	5.84	5.81	5.67	5.48	5.28	5.08
$c\_ada\_UC-SV$	4.88	4.71	4.91	5.07	5.12	5.17	5.14	5.11	5.00	4.86	4.76	4.63
$c\_ada\_WLa$	1.27	1.41	1.50	1.57	1.63	1.67	1.69	1.72	1.74	1.76	1.78	1.80
$c\_ada\_ETS$	3.18	2.65	2.49	2.42	2.38	2.34	2.32	2.30	2.29	2.28	2.28	2.27
$c\_ada\_AR(1)$	3.86	4.00	4.11	4.17	4.21	4.22	4.23	4.23	4.22	4.22	4.22	4.22
$c\_Aut\_ada$	1.48	1.63	1.71	1.81	1.94	2.04	2.06	2.07	2.12	2.14	2.12	2.12
$c\_Aut\_Aut\_no$	2.03	1.89	1.93	1.97	2.08	2.15	2.14	2.13	2.15	2.16	2.16	2.17
$c\_Aut\_Aut\_IIS$	1.98	1.90	1.97	2.38	2.32	2.28	2.24	2.19	2.23	2.21	2.24	2.20
$c\_Aut\_LAS$	1.54	1.69	1.76	1.85	1.98	2.07	2.08	2.09	2.14	2.15	2.13	2.13
$c\_Aut\_TVP$	4.63	4.29	4.32	4.37	4.42	4.55	4.53	4.57	4.54	4.40	4.29	4.20
$c\_Aut\_UC-SV$	4.50	4.02	3.92	3.98	3.98	4.11	4.12	4.16	4.18	4.08	4.05	4.00
$c\_Aut\_WLa$	1.47	1.63	1.70	1.80	1.92	2.02	2.03	2.05	2.10	2.11	2.10	2.10
$c\_Aut\_ETS$	3.81	3.22	3.03	2.93	2.85	2.80	2.78	2.75	2.76	2.74	2.73	2.71
$c\_Aut\_AR(1)$	3.55	3.54	3.53	3.55	3.63	3.70	3.68	3.67	3.65	3.64	3.64	3.61

The difference in the MSE between the LASSO models and their variants is small when using disaggregated data; the disaggregated WLadaLASSO performs better than the other disaggregated LASSO-type methods for the different forecast horizons. However, when we estimated the aggregate models, the LASSO model presented better prediction performance compared to its variants until the forecast horizon five months ahead. The aggregated adaLASSO model resulted in a smaller forecast error by the MSE when the forecast horizon was over five months ahead. It would be interesting to find out why WLadaLASSO does not perform better than its variants with aggregate data or why there is this difference in performance between aggregated and disaggregated data. [Konzen and Ziegelmann \(2016\)](#) pointed out that WLadaLASSO forecasts better than LASSO and adaLASSO when the sample is small, and when there is a large number of lags. In the present study, we have a large number of lags; this does not change between using aggregated or disaggregated WLadaLASSO or other LASSO-type methods.



The difference in the MSE does not allow us to state if the forecast from the disaggregated ETS has higher accuracy statistically compared to other methods. Therefore, we analyzed the results of the MDM test. To perform the test, we established the disaggregated ETS as the benchmark model because it has the lowest MSE when the forecast horizon is three to twelve months ahead. We compared the forecast errors of all of the models with those of the benchmark using the MDM test. The null hypothesis of the test is the equal forecast accuracy between the two models. Under the null hypothesis, the disaggregated ETS forecasts performed as well as the analyzed model. The alternative hypothesis indicates that the forecast of the disaggregated ETS is more accurate statistically.

Table A2 in Appendix A.10 presents the MDM statistics and the associated  $p$ -values (below the test statistics and in parentheses) for each model compared to the benchmark. We underline and bold the  $p$ -value when we do not reject the null hypothesis at 10% statistical significance. From the results of the MDM test, the null hypothesis can be rejected for all models except ETS. The disaggregated ETS shows better forecast performance compared to the naive models (AR(1), AR(13), TVP-AR(1), UC-SV), LASSO and its variants, the Autometrics algorithm, or combinations using aggregated and disaggregated data. However, the disaggregated ETS model is only more accurate than the aggregated ETS for forecast horizons that are six, eight, nine, and eleven months ahead at 10% statistical significance based on the MDM test.

However, the MCS procedure can also be used to determine which models can be considered the best. Table 3 presents the MCS  $p$ -values for each model. The  $p$ -values of the models are in bold if we determine that the model could be included in the set of “best” models with 90% probability. Only ETS models (with aggregated and disaggregated data) were selected. Only the disaggregated ETS model remains in the MCS for forecast horizons that are nine and eleven months ahead.

Next, we used the forecast encompassing test to study whether the disaggregated ETS model forecasts add information compared to forecasts from the other models. We applied the same approach as in Harvey et al. (1998). Table 4 reports the estimated weights  $\hat{\lambda}_{dis}^h$  and the associated statistical significance of the encompassing analysis considering the disaggregated ETS as the benchmark (presented in bold if we did not reject the null hypothesis that the disaggregated ETS model forecast does not contain information that is useful for forecasting the first difference in industrial production beyond the information already found in the other model at 10% statistical significance). Excluding the aggregated ETS, all of the estimated weights for the disaggregated ETS model are equal to or above one and are statistically significant at 1% for all forecast horizons. All of the models, regardless of whether they used aggregated or disaggregated data or a combination, do not provide significant additional information relative to the forecast of the disaggregated ETS model, except for the aggregated ETS model. In other words, the optimal combination forecast only incorporates information from the disaggregated ETS model at any horizon, except for the aggregated ETS model. The forecasts based on the disaggregated ETS model always encompass the forecasts based on models other than ETS.

Considering the aggregated ETS model as the exception, we analyzed the weights associated with the disaggregated and the aggregated ETS. We estimated a convex combination of the two forecasts as

$$y_{t+h}^h = \lambda_{dis}^h \hat{y}_{dis,t+h}^h + \lambda_{ag}^h \hat{y}_{ag,t+h}^h \quad (11)$$

Table A3 in Appendix A.10 reports the estimated weights of  $\hat{\lambda}_{dis}^h$  and  $\hat{\lambda}_{ag}^h$  and the associated statistical significance of the encompassing analysis that only considers the ETS model. The weight of  $\hat{\lambda}_{dis}^h$  is statistically significant at 10% for all horizons, except for those two and three months ahead. The majority of 1  $\hat{\lambda}_{dis}^h$  is equal to one for forecast horizons greater than four, and the optimal combination forecast provided by (11) only incorporates information from the disaggregated ETS model for these forecast horizons. This points to the disaggregated ETS model having superior informational content compared to the aggregated version of the model. The weight  $\hat{\lambda}_{ag}^h$  is only statistically significant at 5% for

one period ahead. For forecast horizons greater than one, the weight for the aggregated ETS model is statistically zero.

**Table 3.** Model confidence set  $p$ -values for one to twelve months ahead for different models.

Models	1	2	3	4	5	6	7	8	9	10	11	12
$AR(1)^{dis}$	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00
$AR(1)^{ag}$	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00
$AR(13)^{dis}$	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00
$AR(13)^{ag}$	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00
$TVP^{dis}$	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00
$TVP^{ag}$	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00
$UC-SV^{dis}$	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00
$UC-SV^{ag}$	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00
$ETS^{dis}$	<b>0.91</b>	<b>1.00</b>	<b>1.00</b>	<b>1.00</b>	<b>1.00</b>	<b>1.00</b>	<b>1.00</b>	<b>1.00</b>	<b>1.00</b>	<b>1.00</b>	<b>1.00</b>	<b>1.00</b>
$ETS^{ag}$	<b>1.00</b>	<b>0.98</b>	<b>0.89</b>	<b>0.62</b>	<b>0.25</b>	<b>0.28</b>	<b>0.37</b>	<b>0.30</b>	0.09	<b>0.28</b>	0.01	<b>0.50</b>
$LAS^{dis}$	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00
$LAS^{ag}$	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00
$ada^{dis}$	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00
$ada^{ag}$	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00
$WLa^{dis}$	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00
$WLa^{ag}$	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00
$Aut\_no^{dis}$	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00
$Aut\_no^{ag}$	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00
$Aut\_IIS^{dis}$	0.00	0.00	0.00	0.00	0.00	0.00	0.01	0.00	0.00	0.00	0.00	0.00
$Aut\_IIS^{ag}$	0.00	0.00	0.00	0.00	0.00	0.00	0.01	0.00	0.00	0.00	0.00	0.00
$c\_LAS\_ada$	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00
$c\_LAS\_Aut\_no$	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00
$c\_LAS\_Aut\_IIS$	0.00	0.00	0.00	0.00	0.00	0.00	0.02	0.00	0.00	0.00	0.00	0.00
$c\_LAS\_LAS$	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00
$c\_LAS\_TVP$	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00
$c\_LAS\_UC-SV$	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00
$c\_LAS\_WLa$	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00
$c\_LAS\_ETS$	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00
$c\_LAS\_AR(1)$	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00
$c\_ada\_ada$	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00
$c\_ada\_Aut\_no$	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00
$c\_ada\_Aut\_IIS$	0.00	0.00	0.00	0.00	0.00	0.00	0.02	0.00	0.00	0.00	0.00	0.00
$c\_ada\_LAS$	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00
$c\_ada\_TVP$	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00
$c\_ada\_UC-SV$	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00
$c\_ada\_WLa$	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00
$c\_ada\_ETS$	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00
$c\_ada\_AR(1)$	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00
$c\_Aut\_ada$	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00
$c\_Aut\_Aut\_no$	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00
$c\_Aut\_Aut\_IIS$	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.01	0.00	0.00	0.00
$c\_Aut\_LAS$	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00
$c\_Aut\_TVP$	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00
$c\_Aut\_UC-SV$	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00
$c\_Aut\_WLa$	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00
$c\_Aut\_ETS$	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00
$c\_Aut\_AR(1)$	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00

**Table 4.** Forecast encompassing test for one to twelve months ahead for different models using the disaggregated ETS as the benchmark.

Models	$\hat{\lambda}_{dis}^h$																							
	1	2	3	4	5	6	7	8	9	10	11	12	1	2	3	4	5	6	7	8	9	10	11	12
$AR(1)^{dis}$	1.0	***	1.0	***	1.0	***	1.0	***	1.0	***	1.0	***	1.0	***	1.1	***	1.1	***	1.1	***	1.1	***	1.1	***
$AR(1)^{ag}$	1.0	***	1.0	***	1.0	***	1.0	***	1.0	***	1.0	***	1.0	***	1.1	***	1.1	***	1.1	***	1.1	***	1.1	***
$AR(13)^{dis}$	1.2	***	1.2	***	1.2	***	1.2	***	1.2	***	1.2	***	1.2	***	1.2	***	1.2	***	1.2	***	1.2	***	1.2	***
$AR(13)^{ag}$	1.2	***	1.2	***	1.2	***	1.2	***	1.2	***	1.2	***	1.2	***	1.2	***	1.2	***	1.2	***	1.2	***	1.2	***
$TVP^{dis}$	1.0	***	1.0	***	1.0	***	1.0	***	1.0	***	1.0	***	1.0	***	1.0	***	1.0	***	1.0	***	1.1	***	1.1	***
$TVP^{ag}$	1.0	***	1.0	***	1.0	***	1.0	***	1.0	***	1.0	***	1.0	***	1.0	***	1.0	***	1.0	***	1.1	***	1.1	***
$UC-SV^{dis}$	1.0	***	1.0	***	1.0	***	1.0	***	1.0	***	1.0	***	1.0	***	1.0	***	1.0	***	1.0	***	1.0	***	1.0	***
$UC-SV^{ag}$	1.0	***	1.0	***	1.0	***	1.0	***	1.0	***	1.0	***	1.0	***	1.0	***	1.0	***	1.0	***	1.0	***	1.0	***
$ETS^{ag}$	0.5	*	<b>0.5</b>		<b>0.6</b>		0.8	*	1.2	**	1.2	**	1.0	*	1.1	**	1.5	***	1.0	**	2.0	***	0.9	*
$LAS^{dis}$	1.2	***	1.3	***	1.2	***	1.2	***	1.2	***	1.2	***	1.2	***	1.2	***	1.3	***	1.3	***	1.3	***	1.3	***
$LAS^{ag}$	1.2	***	1.2	***	1.2	***	1.2	***	1.2	***	1.2	***	1.2	***	1.2	***	1.2	***	1.3	***	1.3	***	1.3	***
$ada^{dis}$	1.2	***	1.2	***	1.2	***	1.2	***	1.2	***	1.2	***	1.2	***	1.2	***	1.3	***	1.3	***	1.3	***	1.3	***
$ada^{ag}$	1.2	***	1.2	***	1.2	***	1.2	***	1.2	***	1.2	***	1.2	***	1.2	***	1.3	***	1.2	***	1.2	***	1.3	***
$WLa^{dis}$	1.2	***	1.3	***	1.2	***	1.2	***	1.2	***	1.2	***	1.2	***	1.2	***	1.3	***	1.3	***	1.3	***	1.3	***
$WLa^{ag}$	1.2	***	1.2	***	1.2	***	1.2	***	1.2	***	1.2	***	1.2	***	1.2	***	1.2	***	1.2	***	1.2	***	1.2	***
$Aut\_no^{dis}$	1.2	***	1.2	***	1.2	***	1.2	***	1.2	***	1.2	***	1.2	***	1.2	***	1.2	***	1.2	***	1.2	***	1.2	***
$Aut\_no^{ag}$	1.2	***	1.2	***	1.2	***	1.2	***	1.2	***	1.2	***	1.2	***	1.2	***	1.2	***	1.2	***	1.3	***	1.2	***
$Aut\_IIS^{dis}$	1.1	***	1.1	***	1.1	***	1.0	***	1.2	***	1.2	***	1.1	**	1.2	***	1.2	***	1.2	***	1.2	***	1.2	***
$Aut\_IIS^{ag}$	1.1	***	1.1	***	1.1	***	1.0	***	1.2	***	1.2	***	1.1	***	1.2	***	1.1	***	1.2	***	1.2	***	1.2	***
$c\_LAS\_ada$	1.2	***	1.2	***	1.2	***	1.2	***	1.2	***	1.2	***	1.2	***	1.2	***	1.2	***	1.2	***	1.2	***	1.2	***
$c\_LAS\_Aut\_no$	1.1	***	1.2	***	1.2	***	1.2	***	1.2	***	1.2	***	1.2	***	1.2	***	1.2	***	1.2	***	1.2	***	1.2	***
$c\_LAS\_Aut\_IIS$	1.1	***	1.1	***	1.1	***	1.0	***	1.2	***	1.2	***	1.1	**	1.2	***	1.2	***	1.2	***	1.2	***	1.2	***
$c\_LAS\_LAS$	1.2	***	1.2	***	1.2	***	1.2	***	1.2	***	1.2	***	1.2	***	1.2	***	1.2	***	1.2	***	1.2	***	1.2	***
$c\_LAS\_TVP$	1.0	***	1.0	***	1.0	***	1.0	***	1.0	***	1.0	***	1.0	***	1.0	***	1.0	***	1.0	***	1.1	***	1.1	***
$c\_LAS\_UC-SV$	1.0	***	1.0	***	1.0	***	1.0	***	1.0	***	1.0	***	1.1	***	1.0	***	1.1	***	1.1	***	1.1	***	1.1	***
$c\_LAS\_WLa$	1.2	***	1.2	***	1.2	***	1.2	***	1.2	***	1.2	***	1.2	***	1.2	***	1.2	***	1.2	***	1.2	***	1.2	***
$c\_LAS\_ETS$	1.1	***	1.1	***	1.1	***	1.1	***	1.2	***	1.1	***	1.1	***	1.2	***	1.2	***	1.2	***	1.2	***	1.2	***
$c\_LAS\_AR(1)$	1.1	***	1.0	***	1.0	***	1.0	***	1.1	***	1.0	***	1.1	***	1.1	***	1.1	***	1.1	***	1.1	***	1.1	***
$c\_ada\_ada$	1.2	***	1.2	***	1.2	***	1.2	***	1.2	***	1.2	***	1.2	***	1.2	***	1.2	***	1.2	***	1.2	***	1.2	***
$c\_ada\_Aut\_no$	1.1	***	1.2	***	1.2	***	1.2	***	1.2	***	1.2	***	1.2	***	1.2	***	1.2	***	1.2	***	1.2	***	1.2	***
$c\_ada\_Aut\_IIS$	1.1	***	1.1	***	1.1	***	1.0	***	1.2	***	1.2	***	1.1	**	1.2	***	1.2	***	1.2	***	1.2	***	1.2	***
$c\_ada\_LAS$	1.2	***	1.2	***	1.2	***	1.2	***	1.2	***	1.2	***	1.2	***	1.2	***	1.2	***	1.2	***	1.2	***	1.2	***
$c\_ada\_TVP$	1.0	***	1.0	***	1.0	***	1.0	***	1.0	***	1.0	***	1.0	***	1.0	***	1.0	***	1.0	***	1.1	***	1.1	***
$c\_ada\_UC-SV$	1.0	***	1.0	***	1.0	***	1.0	***	1.0	***	1.0	***	1.1	***	1.0	***	1.1	***	1.1	***	1.1	***	1.1	***
$c\_ada\_WLa$	1.2	***	1.2	***	1.2	***	1.2	***	1.2	***	1.2	***	1.2	***	1.2	***	1.2	***	1.2	***	1.2	***	1.2	***
$c\_ada\_ETS$	1.1	***	1.1	***	1.1	***	1.1	***	1.2	***	1.1	***	1.1	***	1.2	***	1.2	***	1.2	***	1.2	***	1.2	***

Table 4. Cont.

Models	$\hat{\lambda}_{dis}^h$																							
	1		2		3		4		5		6		7		8		9		10		11		12	
<i>c_ada_AR(1)</i>	1.0	***	1.0	***	1.0	***	1.0	***	1.1	***	1.0	***	1.0	***	1.1	***	1.1	***	1.1	***	1.1	***	1.1	***
<i>c_Aut_ada</i>	1.2	***	1.2	***	1.2	***	1.2	***	1.2	***	1.2	***	1.2	***	1.2	***	1.2	***	1.2	***	1.3	***	1.2	***
<i>c_Aut_Aut_no</i>	1.1	***	1.2	***	1.2	***	1.2	***	1.2	***	1.2	***	1.2	***	1.2	***	1.2	***	1.2	***	1.2	***	1.2	***
<i>c_Aut_Aut_IIS</i>	1.1	***	1.1	***	1.2	***	1.1	***	1.3	***	1.2	***	1.2	***	1.2	***	1.2	**	1.3	***	1.2	***	1.3	***
<i>c_Aut_LAS</i>	1.2	***	1.2	***	1.2	***	1.2	***	1.2	***	1.2	***	1.2	***	1.2	***	1.2	***	1.2	***	1.3	***	1.2	***
<i>c_Aut_TVP</i>	1.1	***	1.0	***	1.0	***	1.1	***	1.1	***	1.1	***	1.1	***	1.0	***	1.1	***	1.1	***	1.1	***	1.1	***
<i>c_Aut_UC-SV</i>	1.1	***	1.0	***	1.0	***	1.1	***	1.1	***	1.1	***	1.1	***	1.0	***	1.1	***	1.1	***	1.0	***	1.1	***
<i>c_Aut_WLa</i>	1.2	***	1.2	***	1.2	***	1.2	***	1.2	***	1.2	***	1.2	***	1.2	***	1.2	***	1.3	***	1.3	***	1.2	***
<i>c_Aut_ETS</i>	1.1	***	1.1	***	1.1	***	1.1	***	1.1	***	1.1	***	1.1	***	1.1	***	1.1	***	1.1	***	1.1	***	1.1	***
<i>c_Aut_AR(1)</i>	1.1	***	1.1	***	1.1	***	1.1	***	1.1	***	1.1	***	1.1	***	1.1	***	1.1	***	1.1	***	1.1	***	1.1	***

Note: \*, \*\*, \*\*\* denote statistical significance at the 10%, 5%, and 1% levels, respectively.

Finally, we analyzed the forecasts of each model for all of the horizons together using the uSPA and aSPA tests and compared them to the forecast of the ETS model with disaggregated data, which was used as the benchmark. This is different from what we discussed earlier, in which we looked at each time horizon separately. The results of the uSPA and aSPA tests are reported in Table 5. When considering all 12 horizons together, we rejected the null hypothesis of equal predictability for all models for both tests at 1% statistical significance. Together, the multi-horizon results are different from the single-horizon results. Previously, we (i) determined that the ETS model with aggregated data had a lower MSE in the first two-time horizons; (ii) only rejected the null hypothesis of equal predictability between the ETS models with aggregated and disaggregated data using the MDM test for 4 of the 12 horizons; and (iii) determined that the MCS contained the ETS model with aggregated data for 10 of the 12 horizons. However, we determined that the ETS model with disaggregated data was the best compared to all of the other models, according to the uSPA and aSPA tests when considering all 12 horizons together at 1% statistical significance.

**Table 5.** aSPA and uSPA tests for a multi-horizon forecast comparison with all 12 horizons together.

Models	uSPA		aSPA	
	t Statistics	p-Value	t Statistics	p-Value
AR(1) <sup>dis</sup>	7.724	0.000	29.404	0.000
AR(1) <sup>ag</sup>	7.758	0.000	29.522	0.000
AR(13) <sup>dis</sup>	4.810	0.000	11.127	0.000
AR(13) <sup>ag</sup>	4.768	0.000	9.783	0.001
TVP <sup>dis</sup>	7.539	0.000	28.050	0.000
TVP <sup>ag</sup>	7.431	0.000	28.734	0.000
UC-SV <sup>dis</sup>	7.189	0.000	16.878	0.000
UC-SV <sup>ag</sup>	7.127	0.000	17.065	0.000
ETS <sup>ag</sup>	−0.124	0.003	2.722	0.009
LAS <sup>dis</sup>	4.731	0.000	11.025	0.000
LAS <sup>ag</sup>	4.159	0.000	9.134	0.001
ada <sup>dis</sup>	4.830	0.000	11.240	0.001
ada <sup>ag</sup>	4.778	0.000	10.155	0.000
WLa <sup>dis</sup>	4.773	0.000	11.284	0.000
WLa <sup>ag</sup>	4.761	0.000	9.746	0.001
Aut_no <sup>dis</sup>	6.549	0.000	14.215	0.000
Aut_no <sup>ag</sup>	5.637	0.000	10.512	0.001
Aut_IIS <sup>dis</sup>	2.455	0.000	4.659	0.002
Aut_IIS <sup>ag</sup>	2.940	0.000	5.151	0.002
c_LAS_ada	5.077	0.000	11.562	0.000
c_LAS_Aut_no	6.715	0.000	14.349	0.000
c_LAS_Aut_IIS	2.576	0.000	5.090	0.001
c_LAS_LAS	4.962	0.000	11.308	0.001
c_LAS_TVP	7.518	0.000	28.717	0.000
c_LAS_UC-SV	7.502	0.000	28.987	0.000
c_LAS_WLa	4.993	0.000	11.635	0.000
c_LAS_ETS	6.934	0.000	20.147	0.000
c_LAS_AR(1)	7.856	0.000	27.967	0.000
c_ada_ada	5.229	0.000	11.606	0.000
c_ada_Aut_no	6.705	0.000	13.912	0.000
c_ada_Aut_IIS	2.556	0.000	5.033	0.001
c_ada_LAS	5.229	0.000	11.606	0.000
c_ada_TVP	7.510	0.000	29.496	0.000
c_ada_UC-SV	7.549	0.000	29.223	0.000
c_ada_WLa	5.127	0.000	11.658	0.000
c_ada_ETS	6.917	0.000	20.114	0.000
c_ada_AR(1)	7.846	0.000	29.007	0.000
c_Aut_ada	3.805	0.000	10.468	0.000
c_Aut_Aut_no	4.854	0.000	11.488	0.000
c_Aut_Aut_IIS	3.103	0.000	6.388	0.001
c_Aut_LAS	3.805	0.000	10.468	0.000
c_Aut_TVP	5.941	0.000	15.168	0.000
c_Aut_UC-SV	4.469	0.000	11.117	0.000
c_Aut_WLa	3.754	0.000	10.347	0.000
c_Aut_ETS	6.832	0.000	19.809	0.000
c_Aut_AR(1)	5.903	0.000	16.763	0.000

By considering the multi-horizon together, we can determine the horizon at which the ETS model with disaggregated data becomes the best model to forecast when comparing only with the aggregated ETS—because it is the model with the most accurate forecasts by



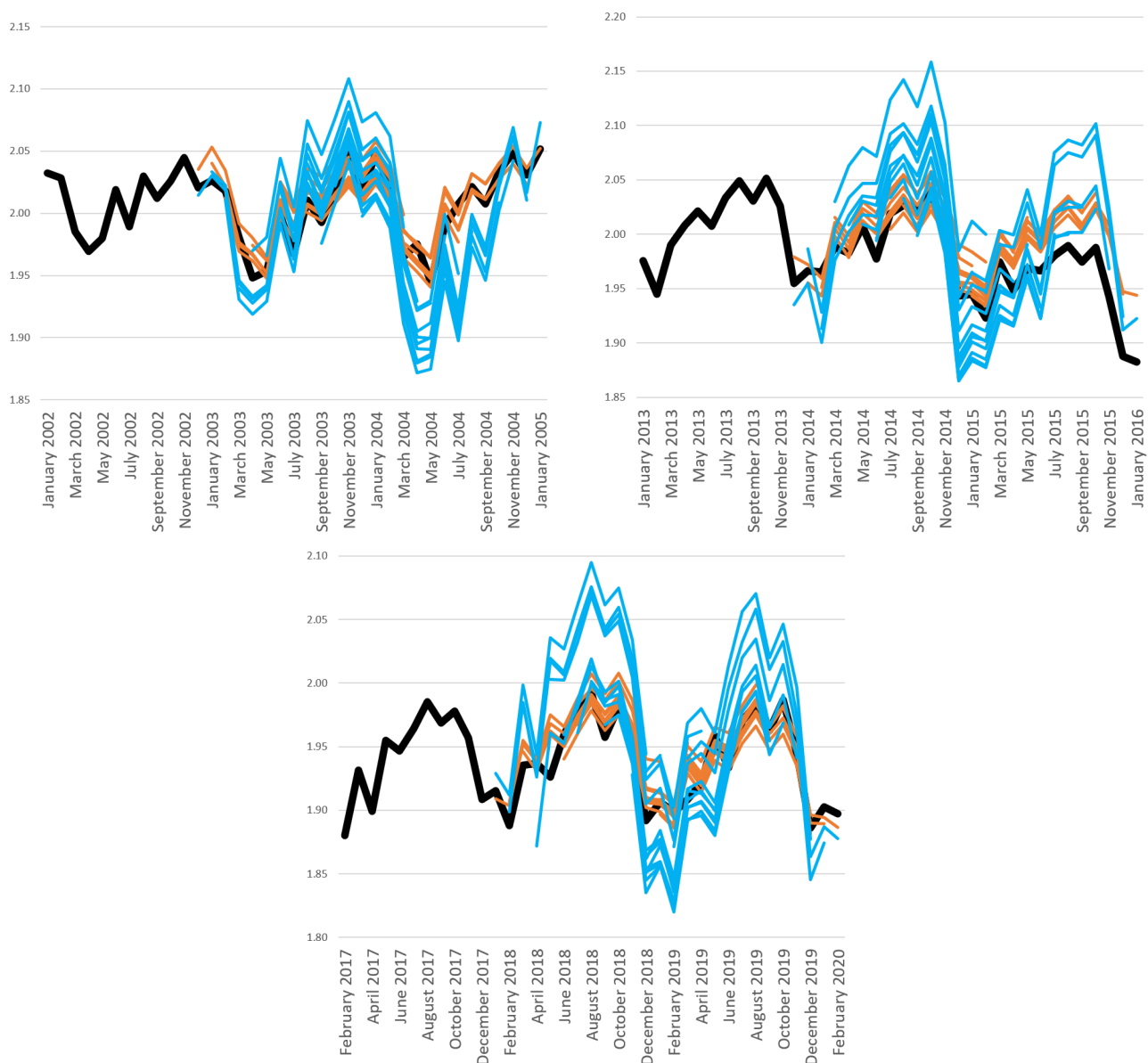
the MSE in addition to the disaggregated ETS itself. For this, we conducted the aSPA and uSPA tests recursively by considering the horizons together. For example, we first analyzed the tests for  $h = 1$  only, and then reported the tests with  $h = 1$  and  $h = 2$  together, and so on. We report the results of the uSPA and aSPA tests comparing the ETS models using aggregated and disaggregated data while considering the horizons together in Table 6, in which rejection at 10% statistical significance is in bold. At 10% statistical significance, we can say that the ETS model with disaggregated data becomes the best model after six forecast horizons (jointly with the uSPA test) or after seven forecast horizons (jointly with the aSPA test). It is important to remember that we rejected the null hypothesis of equal predictability between the ETS models using aggregated and disaggregated data after six horizons in the MDM test results in Table A2 at 10% statistical significance. Based on the aSPA test, we can say that the forecast provided by the ETS model disaggregated over the longer forecast horizons—for example, six and seven horizons—compensates for worse performances over the shorter forecast horizons—for example, one and two horizons—considering a total of seven horizons.

**Table 6.** Comparison between ETS models with aggregated and disaggregated data with a multi-horizon analysis.

Horizons	uSPA		aSPA	
	t-Statistics	p-Value	t-Statistics	p-Value
1	−0.124	0.612	−0.124	0.617
1,2	−0.124	0.407	−0.073	0.574
1,2,3	−0.124	0.280	0.014	0.488
1,2,3,4	−0.124	0.196	0.171	0.361
1,...,5	−0.124	0.153	0.506	0.165
1,...,6	−0.124	<b>0.088</b>	0.783	0.101
1,...,7	−0.124	<b>0.065</b>	0.912	<b>0.081</b>
1,...,8	−0.124	<b>0.028</b>	1.189	<b>0.049</b>
1,...,9	−0.124	<b>0.016</b>	1.715	<b>0.025</b>
1,...,10	−0.124	<b>0.010</b>	2.003	<b>0.019</b>
1,...,11	−0.124	<b>0.005</b>	2.727	<b>0.009</b>
1,...,12	−0.124	<b>0.003</b>	2.722	<b>0.009</b>

#### *Comparing the Forecast of the Disaggregated ETS Model with That of the Disaggregated WLadaLASSO*

In this subsection, we want to determine why the ETS model performs better in forecasting industrial production in Brazil.<sup>10</sup> In Figure 2, we compare the forecasts for one to twelve months made by the disaggregated ETS model (orange line) and the disaggregated WLadaLASSO (light blue line) model, which was determined to be the best model according to MSE apart from the ETS model. Fifteen orange lines represent the disaggregated ETS forecast for one to twelve months because each line represents forecasts, i.e., one step, two steps, etc., up to twelve steps ahead for the disaggregated ETS model for one rolling window. For example, the upper left figure considers the period from January 2002 to January 2005 and reports the forecasts of 15 rolling windows for the disaggregated ETS. In addition, the thick black line presents the realization of the logarithm for general industrial production in Brazil. We divided it into three periods to improve the visualization of results.



**Figure 2.** Comparison of the forecast provided by the disaggregated WLadaLASSO while considering three periods. The thick line is the realization, the light blue line is the disaggregated WLadaLASSO forecast, and the orange line is the disaggregated ETS forecast. The upper left and upper right figures cover the period between January 2002 and January 2005 and between January 2013 and January 2016, respectively, and the lower figure covers the period between February 2017 and February 2020.

In Figure 2, we can see that the forecast of the ETS model follows the trend and seasonality of the logarithm of industrial production more closely. In addition, the WLadaLASSO forecasts tend to indicate a stronger increase (decrease) in the series than in the observed series over the three periods. The comparison of the model forecasts with the observed series does not lead to many changes in the three periods, showing the superiority of the forecast provided by the ETS model. The ETS model is an adaptive scheme, and the other methods are not. Additionally, we can see a change in the series pattern in the upper right figure with the forecast period being 2012 because there was a break in 2014, the beginning of the recession in Brazil, and there was another recession in 2016, the impeachment of President Dilma Rousseff, where there was a break in the trend (no-trend).

## 6. Conclusions

The present work sought to analyze two points regarding how to forecast industrial production in Brazil. First, we compared different univariate models to select the lags using LASSO and two of its variants, ETS models, and the Autometrics algorithm. Among these models, we studied which model was best able to forecast industrial production in Brazil. Second, we considered whether aggregated or disaggregated data or the combination of the two led to better forecasting accuracy for general industrial production.

Our results indicated that the ETS model was able to provide a better forecast. This model was also the best for forecasting US inflation and the US stock portfolio in [Elliott and Timmermann \(2008\)](#) if we disregarded the combination of forecasts. The ETS with disaggregated data had the smallest MSE across all of the forecast horizons, with the exception of one and two months ahead. We used the ETS model with disaggregated data as the benchmark for the MDM test. We rejected the null hypothesis of forecast accuracy equality for all of the models except for the aggregated ETS model based on the MDM test result. The disaggregated ETS model only demonstrated the same forecasting performance as the aggregated ETS for forecast horizons of one to five, seven, ten, and twelve months ahead. Our results indicate the importance of modeling the series separately when forecasting industrial production in Brazil.

In addition, the ETS with the disaggregated series was included in the set of “best” models with 90% probability for all forecast horizons based on the MCS. This was also the case for the ETS model using the aggregate series for all the forecast horizons, except for those nine and eleven months ahead. These were the only two models included in the MCS. The MCS also included the ETS model using the aggregate series even when the modified [Diebold and Mariano \(1995\)](#) test indicated that it performed worse compared to the disaggregated ETS, such as in the case with forecast horizons that were six and eight months ahead.

The combination of the aggregated and disaggregated series did not lead to a better forecast than when only the disaggregated series was considered by the ETS model. This is in contrast to [Hendry and Hubrich \(2011\)](#) and [Weber and Zika \(2016\)](#), but similar to [Faust and Wright \(2013\)](#).

[Epprecht et al. \(2021\)](#) obtained different results than we did and determined that adaLASSO and the Autometrics algorithm demonstrated similar forecasting performance with a small number of relevant variables and when the candidate variables were lower than the number of observations. In our case, the LASSO models and variants performed better than the Autometrics algorithm in general, even when the number of candidate variables was lower than the number of observations. In addition, we used a recursive forecast, in which the Autometrics algorithm presented better results compared to those obtained by [Kock and Teräsvirta \(2014\)](#).

We investigated the forecasts of each model for all of the horizons together by using the uSPA and aSPA tests differently than we did before. We rejected the null hypothesis of equal predictability between the disaggregated ETS model and all of the other models for both tests at 1% statistical significance while considering all 12 horizons together. These multi-horizon results were different from what we were able to obtain with just one horizon. We can say that the ETS model with disaggregated data is the best model to forecast horizons from six or seven periods onward, together, depending on the test compared to the aggregated ETS. This is because we do not reject the null hypothesis of equal predictability between aggregated and disaggregated ETS models at 10% statistical significance in case we consider up to the sixth forecast horizon together (or the seventh, depending on the test version).

We also analyzed forecast encompassing tests to investigate whether the other models reported relevant information in their forecasts for the optimal combination forecasts compared to the disaggregated ETS model. Except for the aggregated ETS model, the optimal combination forecast only incorporated information from the disaggregated ETS model compared to models other than ETS. In such cases, the optimal combination forecast

was simply the forecast of the disaggregated ETS model, except when we considered the aggregated ETS model, because the disaggregated ETS model forecast contains all the information that is useful for forecasting the first difference in industrial production compared to the other models. The aggregated ETS forecasts add relevant information that is statistically significant at 5% for only one period ahead compared to the disaggregated ETS model. For one period ahead only, the optimal combination forecast includes the aggregated ETS forecasts with positive weight. The disaggregated ETS introduced information for forecasting industrial production for six horizons among the 12 that were analyzed compared to the aggregated ETS model at 5% statistical significance. Additionally, the estimated weight for the disaggregated ETS model was close to or greater than one in nine of the twelve horizons analyzed compared to the aggregated ETS model. That is, the optimal combination forecast included only the forecast of the disaggregated ETS model in these forecast horizons. We can say that disaggregated ETS model forecasts are informationally superior.

As an extension of the present work, we will compare these results with the robust forecasting<sup>11</sup> devices described by [Castle et al. \(2015\)](#) and the smoothed robust forecasting techniques found in [Martinez et al. \(2022\)](#). According to these studies, the use of the ETS would not be the best option. Additionally, we will consider the Card procedure proposed by [Doornik et al. \(2020\)](#), which performed better than ETS in [Makridakis et al. \(2020\)](#), to determine if this improves the forecast accuracies of our models. However, this comparison will only be possible when the new version of OxMetrics™ ([Doornik and Hendry \(2022\)](#)) is released.

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## Appendix A. Appendices—Supplementary Materials for the Paper Forecasting Industrial Production Using Aggregated and Disaggregated Series or a Combination of Both—Evidence from One Emerging Market Economy

These supplementary materials present additional information for the estimation of some models; explanations of the ETS models, MDM test, MCS procedure, and forecast encompassing test, and tables containing descriptive statistics from the MDM test and the forecast encompassing test.

### Appendix A.1. Detailing the Bayesian Estimation

Following [Kroese et al. \(2014\)](#), we stacked the observations over all the times  $t$  from the matrix notation of Equation (1). So, we have

$$\Delta y = \Delta X\beta + \varepsilon \quad (\text{A1})$$

where  $\Delta y = (\Delta y_1, \dots, \Delta y_T)^\top$ ,  $\beta = (\beta_1^\top, \dots, \beta_T^\top)^\top$ ,  $\varepsilon = (\varepsilon_1, \dots, \varepsilon_T)^\top \sim N(0, \sigma^2 I)$ ,  $\Delta x_t^\top = (1, \Delta y_{t-1})$ , and  $\Delta X = \begin{pmatrix} \Delta x_1^\top & 0 & \dots & 0 \\ 0 & \Delta x_2^\top & \dots & 0 \\ \vdots & \vdots & \ddots & \vdots \\ 0 & 0 & \dots & \Delta x_T^\top \end{pmatrix}$ . The logarithm of the joint density function of  $\Delta y$  (omitting the initial observation  $\Delta y_0$ ) is

$$\ln f(\Delta y | \beta, \sigma^2) = -\frac{T}{2} \ln \sigma^2 - \frac{1}{2\sigma^2} (\Delta y - \Delta X \beta)^\top (\Delta y - \Delta X \beta) + \text{const} \quad (\text{A2})$$

where *const* is the constant term. Now, we can stack the transition equation, Equation (2), over time  $t$ .  $\beta_0 = 0$  for simplification. The transition equation, Equation (2), can be written in the matrix form as

$$H\beta = u \quad (\text{A3})$$

where  $u \sim N(0, S)$ ,  $u = (u_1, \dots, u_T)^\top$ ,  $H = \begin{pmatrix} I & 0 & \dots & 0 & 0 \\ -I & I & \dots & 0 & 0 \\ \vdots & \vdots & \ddots & \vdots & \vdots \\ 0 & 0 & 0 & -I & I \end{pmatrix}$ ,

$S = \begin{pmatrix} \Omega_0 & 0 & \dots & 0 \\ 0 & \Omega & \dots & 0 \\ \vdots & \vdots & \ddots & \vdots \\ 0 & 0 & \dots & \Omega \end{pmatrix}$ ,  $I$  is the identity matrix, and  $\Omega$  is the covariance matrix.

Given that  $|H| = 1$  and  $|S| = |\Omega_0| |\Omega|^{T-1}$ , the logarithm of the joint density function of  $\beta$  is given by

$$\ln f(\beta | \Omega) = -\frac{T-1}{2} \ln |\Omega| - \frac{1}{2} \beta^\top H^\top S^{-1} H \beta + \text{const} \quad (\text{A4})$$

We can reduce the number of parameters by assuming that  $\Omega$  is diagonal. Consider  $\omega^2 = (\omega_0^2, \omega_1^2)^\top$  as the vector of diagonal elements of  $\Omega$ .

We can obtain the posterior density by specifying the prior value for  $\sigma^2$  and  $\omega^2$ . Assume an independent prior  $f(\sigma^2, \omega^2) = f(\sigma^2) f(\omega^2)$ , where  $\sigma^2 \sim IG(\alpha_{\sigma^2}, \lambda_{\sigma^2})$ ,  $\omega_i^2 \sim IG(\alpha_{\omega_i^2}, \lambda_{\omega_i^2})$  with  $i = 0, 1$  and  $IG$  is the inverse-gamma distribution. We specify the constants  $\alpha_{\sigma^2}$ ,  $\lambda_{\sigma^2}$ ,  $\alpha_{\omega_i^2}$ , and  $\lambda_{\omega_i^2}$ .

The posterior density function is given by

$$f(\beta, \sigma^2, \omega^2 | \Delta y) \propto f(\Delta y | \beta, \sigma^2) f(\beta | \omega^2) f(\sigma^2) f(\omega^2) \quad (\text{A5})$$

where  $\ln f(\Delta y | \beta, \sigma^2)$  and  $\ln f(\beta | \omega^2)$  are described in (A2) and (A4), respectively. We can obtain posterior draws using the Gibbs sampler, which is explained in the next subsection. We draw from  $f(\beta | y, \sigma^2, \omega^2)$  followed by drawing from  $f(\sigma^2, \omega^2 | \Delta y, \beta)$ . As  $f(\beta | \Delta y, \sigma^2, \omega^2)$  is a normal density, if we determine the mean vector and the precision matrix, we can apply the algorithm described below to obtain a draw from it efficiently. Using (A2) and (A4), we write

$$\ln f(\beta | \Delta y, \sigma^2, \omega^2) = \ln f(\Delta y | \beta, \sigma^2) + \ln f(\beta | \omega^2) + \text{const} \quad (\text{A6})$$

as

$$\ln f(\beta | \Delta y, \sigma^2, \omega^2) = -\frac{1}{2} (\beta - \hat{\beta})^\top K_\beta (\beta - \hat{\beta}) + \text{const} \quad (\text{A7})$$

where  $K_\beta = \frac{1}{\sigma^2} X^\top X + H^\top S^{-1} H$  and  $\hat{\beta} = K_\beta^{-1} \left( \frac{1}{\sigma^2} X^\top \right)$ . This means that  $\beta | \Delta y, \sigma^2, \omega^2 \sim N(\hat{\beta}, K_\beta^{-1})$ . Then, we can draw  $f(\beta | \Delta y, \sigma^2, \omega^2)$  with the algorithm that will be described below.



The algorithm generates multivariate normal vector generation using the precision matrix. The algorithm obtains  $N$  independent draws from  $N(\mu, \Lambda^{-1})$  with  $n$  dimensions using the following steps:

1. We obtain the lower Cholesky factorization  $\Lambda = DD^\top$ .
2. We draw  $Z_1, \dots, Z_n \sim N(0, 1)$ .
3. We determine  $\Delta Y$  from  $Z = D^\top \Delta Y$ .
4. We obtain  $W = \mu + \Delta Y$ .
5. We repeat steps 2–4 independently  $N$  times.

The next point is to be able to draw  $f(\sigma^2, \omega^2 | \Delta y, \beta)$ . Given  $\Delta y$  and  $\beta$ ,  $\sigma^2$  and  $\omega^2$  are conditionally independent. From (A5), we have  $f(\sigma^2 | \Delta y, \beta) \propto f(\Delta y | \beta, \sigma^2) f(\sigma^2)$  and  $f(\omega^2 | \Delta y, \beta) \propto f(\beta | \omega^2) f(\omega^2)$ . Both conditional densities are IG densities, for which

$$\sigma^2 | \Delta y, \beta \sim IG\left(\alpha_{\sigma^2} + \frac{T}{2}, \lambda_{\sigma^2} + \frac{1}{2}(\Delta y - \Delta X\beta)(y - \Delta X\beta)^\top\right) \quad (\text{A8})$$

and

$$\omega_i^2 | \Delta y, \beta \sim IG\left(\alpha_{\omega_i^2} + \frac{T-1}{2}, \lambda_{\omega_i^2} + \frac{1}{2} \sum_{t=2}^T (\beta_{it} - \beta_{it-1})^2\right) \quad (\text{A9})$$

Following Kroese et al. (2014), we set small values for the shape parameter of the IG distribution so that the prior value is more non-informative. That is,  $\alpha_{\sigma^2} = \alpha_{\omega_i^2} = 5$ ,  $i = 0, 1$ . Moreover, we set the prior value as  $\lambda_{\sigma^2} = (\alpha_{\sigma^2} - 1)$ ,  $\lambda_{\omega_0^2} = 0.5^2(\alpha_{\omega_0^2} - 1)$ , and  $\lambda_{\omega_1^2} = 0.1^2(\alpha_{\omega_1^2} - 1)$ . Finally, we set the covariance matrix  $\Omega_0$  to be diagonal with diagonal elements to be equal to five, in line with Kroese et al. (2014).

#### Appendix A.2. Markov Chain Monte Carlo Method

The MCMC method is used to summarize the posterior distribution according to Albert (2009). A Markov Chain describes a probabilistic transition between states. This enables the probability to change from one state to another and the probability to keep its own state. We only need the current state, and we have each probability of transitioning to a new (or staying in the current) state.

We use Gibbs sampling as an MCMC algorithm. The idea of Gibbs sampling is that we can approximate the joint posterior distribution by simulating individual parameters from the set of conditional distributions (Albert 2009). Considering  $\Xi$  as all  $l$  parameters, our interest is in the parameter vector  $\Xi = (\Xi_1, \Xi_2, \dots, \Xi_l)$ . We may have a joint posterior distribution  $g(\Xi | y_t)$  that is difficult to summarize. As such, we can focus on the conditional distributions of the individual parameters. We can define the set of conditional distributions  $g(\Xi_1 | \Xi_2, \dots, \Xi_l, y_t)$ ,  $g(\Xi_2 | \Xi_1, \Xi_3, \dots, \Xi_l, y_t)$ , ...,  $g(\Xi_l | \Xi_1, \dots, \Xi_{l-1}, y_t)$ . The draws from this simulation algorithm for each individual parameter converge to the joint posterior distribution of interest under general conditions (Albert 2009).

We can implement the Gibbs sampling algorithm if we know the form of the conditional distributions  $g(\Xi_i | \Xi_{-i}, y_t)$  and  $\Xi_{-i}$  includes all the elements of  $\Xi$  except for  $\Xi_i$ . As such, we can take random draws from these conditional distributions (Blake and Mumtaz 2017).

First-iteration Gibbs sampling follows the steps outlined below:

- (1) We set the starting values  $\Xi_1^0, \dots, \Xi_l^0$  for  $\Xi_1, \dots, \Xi_l$ , where the superscript 0 represents the starting values.
- (2) We take draws and obtain a sample  $\Xi_1^1$  from the distribution of the  $\Xi_1$  conditional on the current values of  $\Xi_2, \dots, \Xi_l$ :  $g(\Xi_1^1 | \Xi_2^0, \dots, \Xi_l^0, y_t)$
- (3) We take draws obtaining a sample  $\Xi_2^1$  from the distribution of  $\Xi_2$  conditional on the current values of  $\Xi_1, \Xi_3, \dots, \Xi_l$ :  $g(\Xi_2^1 | \Xi_1^1, \Xi_3^0, \dots, \Xi_l^0, y_t)$

In (l), we take samples  $\Xi_l^1$  from the distribution of  $\Xi_l$ , which is conditional on current values of  $\Xi_1, \dots, \Xi_{l-1}$ :  $g(\Xi_l^1 | \Xi_1^1, \dots, \Xi_{l-1}^1, y_t)$

This completes the first iteration of the Gibbs sampling algorithm. We repeat the Gibbs iteration 10,000 times and we keep the last 1000 draws of  $\Xi_i$ . As such, we estimate the mean of the marginal posterior distribution for  $\Xi_i$  as the sample means of the 1000 retained draws. The same applies to the estimate of the variance of the marginal posterior distribution (Blake and Mumtaz 2017).

### Appendix A.3. Detailing the Bayesian Estimation of UC-SV

Our first step is to establish the priors and starting values. We define the prior for the initial value of the  $\ln\sigma_t$  as  $\ln\sigma_0 \sim N(\mu_0, 10)$  where  $\mu_0$  is the variance of  $y_{t_0} - \beta_{t_0}$  and  $t_0$  refers to the training sample of 40 observations and  $\beta_{t_0}$  is an initial estimate for the trend from the Hodrick–Prescott filter. Similarly,  $\ln\omega_0 \sim N(\omega_0, 10)$  where  $\omega_0 = \Delta\beta_{t_0}$ . We use the priors for  $g_1$  and  $g_2$  from an IG and we set the prior scale parameters to equal 0.01 and 0.0001, respectively, with one degree of freedom as Barnett et al. (2014). As such, we use non-informative priors.

The next step is to simulate the posterior distributions. We draw the  $\sigma_t$  and  $\omega_t$  conditional on the  $g_1$  and  $g_2$  with the Metropolis algorithm according to Jacquier et al. (2002). We draw  $\beta_t$  using the Carter and Kohn (1994) algorithm. We generate the sample for  $g_1$  and  $g_2$  based on the IG distribution. We consider 10,000 replications of the MCMC algorithm and keep the last 1000 replications for inference.

Below, we detail how we calculate the marginal likelihood. We use a particle filter to calculate the log-likelihood function for the UC-SV. We define  $\Xi = (g_1, g_2, \sigma_0, \omega_0)$  as all of the model parameters. Based on Chib (1995), we consider the log marginal likelihood to be:

$$\ln p(y_t) = \ln f(y_t|\hat{\Xi}) + \ln p(\hat{\Xi}) - \ln g(\hat{\Xi}|y_t) \quad (\text{A10})$$

where  $\ln p(y_t)$  is the log marginal likelihood that we want to calculate,  $\ln f(y_t|\hat{\Xi})$  is the log-likelihood function,  $\ln p(\hat{\Xi})$  is the log prior density, and  $\ln g(\hat{\Xi}|y_t)$  is the log posterior density of the model parameters. The three elements on the right-hand side of (A10) are evaluated at the posterior mean for the model parameters  $\hat{\Xi}$ .

We calculate the log-likelihood function for this model using a particle filter following Barnett et al. (2014). The posterior density in the equation for the marginal likelihood is  $g(\hat{\Xi}|y_t) = g(\hat{g}_1, \hat{g}_2, \hat{\sigma}_0, \hat{\omega}_0)$  and we drop the dependence on  $y_t$  to simplify the notation. The factorization of this density can be described by

$$g(\hat{g}_1, \hat{g}_2, \hat{\sigma}_0, \hat{\omega}_0) = h(\hat{g}_1|\hat{g}_2, \hat{\sigma}_0, \hat{\omega}_0)h(\hat{g}_2|\hat{\sigma}_0, \hat{\omega}_0)h(\hat{\sigma}_0|\hat{\omega}_0)h(\hat{\omega}_0) \quad (\text{A11})$$

We use additional Gibbs runs to approximate the first three terms, and we conduct the main Gibbs run to approximate the final term. We will detail this in the sequence by considering each term on the right-hand side of this equation.

We can express the term  $h(\hat{g}_1|\hat{g}_2, \hat{\sigma}_0, \hat{\omega}_0)$  as

$$\int h(\hat{g}_1|\hat{g}_2, \hat{\sigma}_0, \hat{\omega}_0, \Theta)h(\Theta|\hat{g}_2, \hat{\sigma}_0, \hat{\omega}_0)d\Theta \quad (\text{A12})$$

where  $\Theta = \{\beta_t, \sigma_t, \omega_t\}$  represents the state variables. We can approximate  $h(\hat{g}_1|\hat{g}_2, \hat{\sigma}_0, \hat{\omega}_0, \Theta)$  using an additional Gibbs run, in which we obtain  $\Theta_j|\hat{g}_1, \hat{g}_2, \hat{\sigma}_0, \hat{\omega}_0$ , and then draw from the density  $g_{1j}|\hat{g}_2, \hat{\sigma}_0, \hat{\omega}_0, \Theta_j$ , and we evaluate the IG density  $h(\hat{g}_1|\hat{g}_2, \hat{\sigma}_0, \hat{\omega}_0, \Theta_j)$ .  $h(\hat{g}_1|\hat{g}_2, \hat{\sigma}_0, \hat{\omega}_0)$  is approximated by  $\frac{1}{J} \sum_{j=1}^J h(\hat{g}_1|\hat{g}_2, \hat{\sigma}_0, \hat{\omega}_0, \Theta_j)$ , where  $J$  is the number of retained Gibbs draws.

Similarly, we can approximate  $h(\hat{g}_2|\hat{\sigma}_0, \hat{\omega}_0)$  through a Gibbs run that samples the following conditional densities: (i)  $g_{2j}|\hat{\sigma}_0, \hat{\omega}_0, g_{1j}, \Theta_j$ , (ii)  $g_{1j}|\hat{\sigma}_0, \hat{\omega}_0, g_{2j}, \Theta_j$ , and (iii)  $\Theta_j|\hat{\sigma}_0, \hat{\omega}_0, g_{2j}, g_{1j}$ . Similarly,  $h(\hat{g}_2|\hat{\sigma}_0, \hat{\omega}_0)$  is approximated by  $\frac{1}{J} \sum_{j=1}^J h(\hat{g}_2|\hat{\sigma}_0, \hat{\omega}_0, g_{1j}, \Theta_j)$ , where  $h(\hat{g}_2|\hat{\sigma}_0, \hat{\omega}_0, g_{1j}, \Theta_j)$  is the IG density.

The term  $h(\hat{\sigma}_0|\hat{\omega}_0)$  is approximated using an additional Gibbs sampler that samples from (i)  $g_{2j}|g_{1j}, \hat{\sigma}_0, \hat{\omega}_0, \Theta_j$ , (ii)  $g_{1j}|\hat{\sigma}_0, \hat{\omega}_0, g_{2j}, \Theta_j$ , and (iii)  $\sigma_0|\Theta_j, g_{1j}, g_{2j}, \hat{\omega}_0$ .  $h(\hat{\sigma}_0|\hat{\omega}_0)$  is approximated by  $\frac{1}{J} \sum_{j=1}^J h(\sigma_0|\Theta_j, g_{1j}, g_{2j}, \hat{\omega}_0)$  where  $h(\sigma_0|\Theta_j, g_{1j}, g_{2j}, \hat{\omega}_0)$  is a normal density.

Finally, the final term  $h(\hat{\omega}_0)$  on the right-hand side of Equation (A11) is approximated by  $\frac{1}{J} \sum_{j=1}^J h(\hat{\omega}_0 | g_{1j}, g_{2j}, \sigma_{0j}, \Theta_j)$ . We use the draws on the right-hand side of the original Gibbs sampler. Following Barnett et al. (2014), we use 10,000 replications in additional Gibbs runs, leaving the last 3000 remaining.

#### Appendix A.4. Explanation of the 15 Types of ETS Models

Some of the exponential smoothing methods in Table 1 are known by other names. For example, in cell  $N, N$  represents the simple exponential smoothing method; in cell  $A, N$  refers to Holt's linear method; and in cell  $A_d, N$  is associated with the damped trend method. In cell  $A, A$  describes the additive Holt–Winter method, and in cell  $A, M$  refers to the multiplicative Holt–Winter method.

We consider 1 of the 15 types of ETS models to understand each of the components of the models that can be combined. For example, consider Holt's linear method (cell  $A, N$ ), which can be described as

$$\ell_t = \alpha y_t + (1 - \alpha)(\ell_{t-1} + b_{t-1}) \quad (\text{A13})$$

$$b_t = \beta^*(\ell_t - \ell_{t-1}) + (1 - \beta^*)b_{t-1} \quad (\text{A14})$$

$$\hat{y}_{t+h|t} = \ell_t + b_t h \quad (\text{A15})$$

where Equation (A13) shows the model at the level of the series at time  $t$   $\ell_t$ . Equation (A14) describes the growth rate (slope estimate) of the series at time  $t$   $b_t$ .  $b_t$  is a weighted average of the growth estimate obtained by the difference between successive levels and previous growth  $b_{t-1}$ . Finally, the Equation (A15) presents the prediction for the variable  $y$   $h$  periods ahead using the information that is available at time  $t$ . This equation describes how the forecast for the  $h$  periods ahead is provided based on the current time  $\ell_t$  by adding the growth  $b_t$  for the  $h$  periods.  $\alpha$  is the smoothing parameter for the level with  $0 < \alpha < 1$ , and  $\beta^*$  is the smoothing parameter for the trend with  $0 < \beta^* < 1$ .

Table 2 of Hyndman and Khandakar (2008) presents the equations for the level, growth, seasonality ( $s_t$ ), and forecast of the series of  $h$  periods ahead for the 15 cases considered. Some of the values for the exponential smoothing parameters lead to interesting specific cases. Some examples of this are how the level remains constant over time if  $\alpha = 0$ , the slope is constant over time if  $\beta^* = 0$ , and the seasonal behavior is the same over time if  $\gamma = 0$ . Finally, the specifications  $A$  and  $M$  for the trend component are particular cases of  $A_d$  and  $M_d$  with  $\phi = 1$ . Additionally, the way Hyndman and Khandakar (2008) define the seasonal component when the smooth parameter  $\gamma$  is equal to zero is  $s_t = s_{t-m}$ , which is equivalent to  $(1 - L^m)s_t = (1 - L)(1 + L + L^2 + \dots + L^{m-1})s_t$ . As such, the seasonal component is obtained by extracting the trend  $(1 - L)$  and the seasonal part of the model  $(1 + L + L^2 + \dots + L^{m-1})$ .

Essentially, the estimation procedure is based on estimating the smoothing parameters  $\alpha, \beta, \gamma, \phi$  and the initial state variables  $\ell_0, b_0, s_0, s_{-1}, \dots, s_{-m+1}$  maximizing the likelihood function.

#### Appendix A.5. Autometrics

According to Hendry and Nielsen (2007), a model is congruent when it satisfies specification error tests for (i) heteroskedasticity, autocorrelation, and non-normality, (ii) failure of the weak exogeneity hypothesis, and (iii) has constant parameters over time. The algorithm allows the number of variables to be greater than the number of observations, and it deals with the perfect collinearity generated by the saturation dummy variables that we mention below.

We adopt the Autometrics algorithm with the significance level  $\alpha \leq 1/N$ , where  $N$  is the number of variables that we have in the general model following Castle et al. (2011). As such, we use  $\alpha = 0.1\%$  in all cases based on the number of variables we have. We also consider the block method with the inclusion of impulse indicator saturation (IIS) variables.

All of these variables are added at each point in time in the regression to analyze whether they are relevant using the Autometrics algorithm. That is—if we have a regression with 100 observations over time, the algorithm analyzes the relevance of 100 possibilities for the IIS dummy variables. The IIS is a set of dummy variables, in which a dummy variable is only equal to one at a given point in time and zero otherwise.

#### Appendix A.6. Test of Forecast Accuracy Between Models

We present the Modified Diebold-Mariano Test (MDM) in details. Consider the difference between the actual value of the series and the estimated value as the forecasting error. The MSE is the average of this difference squared for the forecast sample.

The MDM test verifies if there is any model that has a statistically more accurate prediction for Brazilian general industrial production during the study period. Assuming two models (1 and 2), in which the forecasting errors  $\hat{\varepsilon}_{t+h|t,j}$  for  $j = 1, 2$  and  $h$  periods ahead are  $\hat{\varepsilon}_{t+h|t,1} = y_{t+h} - \hat{y}_{t+h|t,1}$  and  $\hat{\varepsilon}_{t+h|t,2} = y_{t+h} - \hat{y}_{t+h|t,2}$ , where  $\hat{y}_{t+h|t,j}$  is the forecast from model  $j = 1, 2$  for  $h$  periods ahead. The MDM test is based on the difference between the forecasting error of the models.

The null hypothesis of the test is the equal forecast accuracy between the two models. On the other hand, the alternative hypothesis (one-sided test) defines that the forecast of the benchmark model is more accurate than that of the other model. We need to establish the forecasts of one of the models as a benchmark for the test, which is possible by choosing the model with the lowest MSE value. Consider a loss function  $g$  based on forecasting errors, in which  $g$  is a quadratic loss function. Following Harvey et al. (1997), the MDM test is

$$S = \left( \frac{P + 1 - 2h + P^{-1}h(h-1)}{P} \right)^{1/2} \frac{\bar{d}}{\sqrt{\widehat{var}(\bar{d})}} \quad (A16)$$

where  $P$  is the sample size of the forecasts for a given forecast horizon,  $\bar{d} = \frac{1}{P} \sum_{t=1}^P d_t$ ,  $d_t = g(\hat{\varepsilon}_{t+h|t,1}) - g(\hat{\varepsilon}_{t+h|t,2})$ , and  $\widehat{var}(\bar{d})$  are the estimated long-run variances in series  $d_t$ . Thus, the  $S$  statistic follows a Student's  $t$ -distribution and has a  $P - 1$  degree of freedom.

#### Appendix A.7. Model Confidence Set—MCS

Hansen et al. (2011) proposed the MCS, which has an interpretation similar to that of a confidence interval. The advantage of this procedure is that we do not have to impose a benchmark. This procedure allows a set of models that contains the best model with a certain confidence level to be established.  $MCS_{1-\alpha}$  considers the best model to be the one with  $100(1 - \alpha)\%$  confidence. The set will contain more models if we decrease  $\alpha$ .

MCS requires a loss function to create the test statistics. We use squared errors as the loss function. The MCS procedure estimates  $p$ -values for all of the models from these statistics, and the variance is calculated by the bootstrap estimation. The null hypothesis of MCS is the equal predictive ability between the models of the set.

Consider the loss statistics  $\bar{d}_{ij} = P^{-1} \sum_{t=1}^P d_{ij,t}$ , and  $d_{ij,t} = g(\hat{\varepsilon}_{t+h|t,i}) - g(\hat{\varepsilon}_{t+h|t,j})$ ,  $g$  is a quadratic function.  $\bar{d}_{ij}$  is the relative loss between the  $i$ -th and  $j$ -th models and  $\bar{d}_i = m^{-1} \sum_{j \in \mathcal{M}} \bar{d}_{ij}$ , where  $\bar{d}_i$  is the loss of the  $i$ -th model relative to the average across  $m$  models in  $\mathcal{M}$ .

We obtain sets of models until the null hypothesis is no longer rejected for the  $\alpha$  that we established. Hansen et al. (2011) presented two different statistics:  $T_{max,\mathcal{M}}$  and  $T_{R,\mathcal{M}}$ . We consider the first statistic because it is simple and easy to compute.<sup>12</sup> We have the statistics

$$t_i = \frac{\bar{d}_i}{\sqrt{\widehat{var}(\bar{d}_i)}} \quad (A17)$$

Note that  $\hat{var}(\bar{d}_i)$  is the bootstrapped estimate of  $var(\bar{d}_i)$ .  $T_{max, \mathcal{M}} = \max_{i \in \mathcal{M}} t_i$ , where  $t_i$  is the statistics for the sample loss between  $i$  and across models in  $\mathcal{M}$ . The asymptotic distribution of this statistic is nonstandard and Hansen et al. (2011) propose the use of bootstrap methods.

Then, the algorithm is a sequential procedure and it starts by considering the total models as the set of models; that is,  $\mathcal{M} = \mathcal{M}^0$  in the first step. The second step is to test the null hypothesis at level  $\alpha$ . The third step takes place if we do not reject the null hypothesis, resulting in the final set being  $\mathcal{M} = \mathcal{M}^0$ ; otherwise, we eliminate the model with the lowest p-value from  $\mathcal{M}$  and we repeat the procedure by considering  $\mathcal{M} = \mathcal{M}^1$ , where  $\mathcal{M}^1$  is  $\mathcal{M}^0$  and does not contain the value with the worst the p-value. We use 10,000 bootstrap re-samples.

#### Appendix A.8. Forecast Encompassing Test

If we establish that one method is superior in making predictions, then it can be used as a benchmark. The other models still contain useful information to predict the variable that is not contained in the benchmark forecast. We investigated this with the forecast encompassing test, which was initially proposed by Chong and Hendry (1986) and could also be seen in Ericsson (1992) and in Clements and Hendry (1993).

We followed Rapach et al. (2016) and Borup and Schütte (2020) and used the approach implemented in Harvey et al. (1998). Consider the convex combination of the two forecasts as

$$y_{t+h}^h = \lambda_b^h \hat{y}_{b,t+h}^h + \lambda_{mod}^h \hat{y}_{mod,t+h}^h \quad (\text{A18})$$

where  $\hat{y}_{b,t+h}^h$  and  $\hat{y}_{mod,t+h}^h$  are the forecasts from the benchmark and one of the models, respectively.  $\lambda_b^h + \lambda_{mod}^h = 1$  and  $0 \leq \lambda_b^h \leq 1$ .  $\lambda_b^h$  and  $\lambda_{mod}^h$  are the weights associated with the benchmark and one of the models, respectively. If  $\lambda_b^h = 0$ , the *mod* forecasts encompass the benchmark forecasts and the benchmark forecasts do not provide relevant information to forecast industrial production beyond the information already found in the forecast of one of the models (*mod*). If  $\lambda_b^h > 0$ , the benchmark forecasts contain useful information in addition to the *mod* forecasts.

We test the null hypothesis of  $\lambda_b^h = 0$  against the one-sided alternative hypothesis of  $\lambda_b^h > 0$ . Consider  $\hat{\varepsilon}_{t+h|t,j}^h$  where  $j = \{b, mod\}$ . Now, let  $\hat{d}_{t+h} = (\hat{\varepsilon}_{t+h|t,mod}^h - \hat{\varepsilon}_{t+h|t,b}^h) \hat{\varepsilon}_{t+h|t,mod}^h$  to obtain the test statistic  $HLN^h = \bar{d}(\hat{var}(\bar{d}))^{-1/2}$  and  $\hat{var}(\bar{d})$  are similar to the MDM test with  $\bar{d} = P^{-1} \sum_{t=1}^P \hat{d}_{t+h}$ . We use a heteroskedasticity and autocorrelation consistent (HAC) estimator for the variance in  $\bar{d}$  with a Bartlett kernel and bandwidth with a length of  $h - 1$ . We employ the modified  $HLN^h$  test, which has the same expression as (A16), but while considering the definition of  $\bar{d}$  for forecast encompassing. Additionally, this statistic has the same distribution and degrees of freedom. We estimate the weights as

$$\lambda_b^h = \frac{\sum_{t=1}^P \hat{d}_{t+h}}{\sum_{t=1}^P (\hat{\varepsilon}_{t+h|t,mod}^h - \hat{\varepsilon}_{t+h|t,b}^h)^2} \quad (\text{A19})$$

#### Appendix A.9. Multi-Horizon Forecast Comparison through Uniform and Average Superior Predictive Ability (SPA)

The standard approach is to compare models that consider different forecast horizons independently. This can lead to conclusions that are worthy of attention. We determined that the first model is better for forecasting two and four horizons ahead and that the second model is better for predicting three horizons ahead, but the difference in forecasting performance is not statistically significant for all of the other horizons. In finite samples, we were able to determine that a population model would perform worse than a misspecified model at one of the horizons. If we consider all of the horizons together, this problem can be avoided.



We evaluated the multi-horizon forecast comparison using two bootstrap-based test statistics from [Quaedvlieg \(2021\)](#), which generalized the test proposed by [Hansen \(2005\)](#). The two statistics are the uSPA and aSPA. The first statistic is based on the idea that a superior model should be able to make a better forecast at each horizon. The second statistic allows for a worse performance at some horizons to be compensated by a better performance at other horizons. This means that the definition for uSPA is more stringent than that of aSPA. Both tests reduce to the [Diebold and Mariano \(1995\)](#) test if we only have one horizon.

[Quaedvlieg \(2021\)](#) defined null hypotheses based on the expected loss differentials  $E(d_{ij,t}^h)$ , where  $d_{ij,t}^h = g(\hat{\varepsilon}_{t+h|t,i}) - g(\hat{\varepsilon}_{t+h|t,j})$ . Consider  $E(d_{ij,t}^h) = \mu_{ij}^h$  so that the null hypotheses of both tests are

$$H_0^{uSPA} : \mu_{ij}^h = 0 \quad (\text{A20})$$

and

$$H_0^{aSPA} : \sum_{h=1}^H w_h \mu_{ij}^h = 0 \quad (\text{A21})$$

for all  $i$ , and  $i \neq j$ .  $w_h$  are predetermined weights where  $\sum_{h=1}^H w_h = 1$ . We used the same weights on the forecast horizons as [Quaedvlieg \(2021\)](#). This means that each forecast horizon has the same weight; that is,  $w_h = \frac{1}{H}$ . If we establish different weights, this would correspond to different forecasters having different utility functions.

The alternative uSPA and aSPA hypotheses are  $\mu_{ij}^h > 0$  and  $\sum_{h=1}^H w_h \mu_{ij}^h > 0$  respectively. We chose model  $j$  as the benchmark, which means that the alternative hypothesis is that model  $j$  is the best model. The uSPA statistic considers the minimum value of the [Diebold and Mariano \(1995\)](#) statistics for the different horizons:

$$t_{uSPA,ij} = \min_h \frac{\sqrt{P} \bar{d}_{ij}^h}{\sqrt{\hat{v}ar(\bar{d}_{ij}^h)}} \quad (\text{A22})$$

In the case of aSPA statistics, we have the following form

$$t_{aSPA,ij} = \min_h \frac{\sqrt{P} \bar{d}_{aSPA,ij}}{\sqrt{\hat{v}ar(\bar{d}_{aSPA,ij})}} \quad (\text{A23})$$

where  $\bar{d}_{ij}^h = \frac{1}{P} \sum d_{ij,t}^h$  and  $\bar{d}_{aSPA,ij} = \sum_{h=1}^H w_h \bar{d}_{ij}^h$ . We can estimate the variances in the denominators of both statistics using the HAC estimator from [Andrews \(1991\)](#). We calculated critical values using the moving block bootstrap method according to [Quaedvlieg \(2021\)](#). We considered 10,000 bootstrap re-samples for blocks with lengths of three.

#### Appendix A.10. Tables Showing Descriptive Statistics and the Results for Forecast Accuracy Between Models

**Table A1.** Descriptive statistics in the first difference ( $\Delta y_t$ ) and  $\Delta_{12}y_t$ .

	$\Delta y_t$	$\Delta_{12}y_t$
Mean	0.0002	0.0023
Standard deviation	0.0283	0.0281
Maximum	0.0722	0.0754
Minimum	−0.0850	−0.0808
First quartile	−0.0186	−0.0134
Third quartile	0.0196	0.0201

**Table A2.** Test for prediction accuracy between models with test statistics and  $p$ -values for one to twelve months ahead for different models.

Models	1	2	3	4	5	6	7	8	9	10	11	12
$AR(1)^{dis}$	−6.32 (0.00)	−7.32 (0.00)	−9.68 (0.00)	−8.53 (0.00)	−11.28 (0.00)	−12.42 (0.00)	−49.47 (0.00)	−7.32 (0.00)	−7.29 (0.00)	−7.31 (0.00)	−7.26 (0.00)	−7.16 (0.00)
$AR(1)^{ag}$	−6.31 (0.00)	−7.36 (0.00)	−9.69 (0.00)	−8.60 (0.00)	−11.36 (0.00)	−12.43 (0.00)	−48.81 (0.00)	−7.32 (0.00)	−7.29 (0.00)	−7.30 (0.00)	−7.26 (0.00)	−7.15 (0.00)
$AR(13)^{dis}$	−6.51 (0.00)	−5.41 (0.00)	−5.30 (0.00)	−4.72 (0.00)	−4.87 (0.00)	−5.07 (0.00)	−5.68 (0.00)	−6.68 (0.00)	−7.33 (0.00)	−9.77 (0.00)	−11.81 (0.00)	−14.62 (0.00)
$AR(13)^{ag}$	−6.03 (0.00)	−5.31 (0.00)	−4.88 (0.00)	−3.81 (0.00)	−3.94 (0.00)	−4.07 (0.00)	−4.72 (0.00)	−5.55 (0.00)	−6.58 (0.00)	−10.42 (0.00)	−11.00 (0.00)	−13.60 (0.00)
$TVP^{dis}$	−7.28 (0.00)	−7.27 (0.00)	−10.90 (0.00)	−10.47 (0.00)	−7.26 (0.00)	−16.76 (0.00)	−7.41 (0.00)	−8.37 (0.00)	−6.89 (0.00)	−16.22 (0.00)	−11.66 (0.00)	−8.55 (0.00)
$TVP^{ag}$	−6.86 (0.00)	−7.30 (0.00)	−11.08 (0.00)	−10.44 (0.00)	−7.38 (0.00)	−14.97 (0.00)	−7.46 (0.00)	−8.39 (0.00)	−6.97 (0.00)	−15.83 (0.00)	−11.91 (0.00)	−8.47 (0.00)
$UC-SV^{dis}$	−8.00 (0.00)	−7.10 (0.00)	−6.56 (0.00)	−7.56 (0.00)	−8.41 (0.00)	−8.93 (0.00)	−8.65 (0.00)	−10.07 (0.00)	−13.25 (0.00)	−14.08 (0.00)	−10.11 (0.00)	−14.24 (0.00)
$UC-SV^{ag}$	−7.41 (0.00)	−7.02 (0.00)	−6.51 (0.00)	−7.57 (0.00)	−8.57 (0.00)	−9.17 (0.00)	−8.63 (0.00)	−10.14 (0.00)	−12.72 (0.00)	−14.43 (0.00)	−10.12 (0.00)	−15.82 (0.00)
$ETS^{ag}$	0.11 (0.54)	−0.02 (0.49)	−0.13 (0.45)	−0.72 (0.24)	−1.01 (0.16)	−1.51 (0.07)	−0.87 (0.19)	−1.44 (0.08)	−1.77 (0.04)	−0.95 (0.17)	−4.75 (0.00)	−0.54 (0.29)
$LAS^{dis}$	−6.51 (0.00)	−5.01 (0.00)	−4.85 (0.00)	−4.66 (0.00)	−4.80 (0.00)	−5.01 (0.00)	−5.48 (0.00)	−6.31 (0.00)	−6.79 (0.00)	−7.47 (0.00)	−7.99 (0.00)	−9.27 (0.00)
$LAS^{ag}$	−6.76 (0.00)	−4.85 (0.00)	−4.71 (0.00)	−4.08 (0.00)	−3.97 (0.00)	−4.03 (0.00)	−4.83 (0.00)	−5.14 (0.00)	−5.84 (0.00)	−8.97 (0.00)	−8.53 (0.00)	−8.04 (0.00)
$ada^{dis}$	−6.44 (0.00)	−5.14 (0.00)	−4.97 (0.00)	−4.65 (0.00)	−4.84 (0.00)	−5.05 (0.00)	−5.66 (0.00)	−6.57 (0.00)	−7.51 (0.00)	−8.48 (0.00)	−9.40 (0.00)	−11.93 (0.00)
$ada^{ag}$	−6.35 (0.00)	−4.93 (0.00)	−4.84 (0.00)	−4.54 (0.00)	−4.62 (0.00)	−4.81 (0.00)	−5.27 (0.00)	−6.05 (0.00)	−8.88 (0.00)	−14.46 (0.00)	−12.65 (0.00)	−8.70 (0.00)
$WLa^{dis}$	−6.33 (0.00)	−5.08 (0.00)	−5.10 (0.00)	−4.62 (0.00)	−4.67 (0.00)	−5.11 (0.00)	−5.58 (0.00)	−6.44 (0.00)	−7.23 (0.00)	−7.85 (0.00)	−9.13 (0.00)	−12.64 (0.00)
$WLa^{ag}$	−6.46 (0.00)	−5.06 (0.00)	−4.96 (0.00)	−4.54 (0.00)	−4.53 (0.00)	−4.71 (0.00)	−5.11 (0.00)	−5.98 (0.00)	−8.86 (0.00)	−13.08 (0.00)	−11.52 (0.00)	−9.12 (0.00)
$Aut\_no^{dis}$	−7.21 (0.00)	−6.59 (0.00)	−6.92 (0.00)	−7.05 (0.00)	−7.11 (0.00)	−7.70 (0.00)	−7.61 (0.00)	−8.24 (0.00)	−7.83 (0.00)	−6.76 (0.00)	−6.08 (0.00)	−6.52 (0.00)
$Aut\_no^{ag}$	−5.82 (0.00)	−6.48 (0.00)	−6.90 (0.00)	−5.76 (0.00)	−5.39 (0.00)	−5.26 (0.00)	−5.71 (0.00)	−4.88 (0.00)	−5.67 (0.00)	−5.13 (0.00)	−4.41 (0.00)	−4.95 (0.00)
$Aut\_IIS^{dis}$	−5.50 (0.00)	−5.04 (0.00)	−5.44 (0.00)	−2.51 (0.01)	−4.84 (0.00)	−3.40 (0.00)	−1.78 (0.04)	−2.61 (0.01)	−2.23 (0.01)	−2.32 (0.01)	−2.24 (0.01)	−2.43 (0.01)
$Aut\_IIS^{ag}$	−6.03 (0.00)	−4.43 (0.00)	−4.93 (0.00)	−2.49 (0.01)	−4.09 (0.00)	−4.30 (0.00)	−2.11 (0.02)	−3.03 (0.00)	−2.44 (0.01)	−2.94 (0.00)	−2.94 (0.00)	−2.93 (0.00)
$c\_LAS\_ada$	−6.51 (0.00)	−5.45 (0.00)	−5.28 (0.00)	−4.98 (0.00)	−5.19 (0.00)	−5.26 (0.00)	−5.83 (0.00)	−6.52 (0.00)	−7.20 (0.00)	−7.94 (0.00)	−9.09 (0.00)	−12.92 (0.00)
$c\_LAS\_Aut\_no$	−7.27 (0.00)	−6.68 (0.00)	−7.11 (0.00)	−7.35 (0.00)	−7.42 (0.00)	−7.62 (0.00)	−7.50 (0.00)	−7.82 (0.00)	−7.26 (0.00)	−6.52 (0.00)	−6.06 (0.00)	−6.16 (0.00)
$c\_LAS\_Aut\_IIS$	−5.80 (0.00)	−5.51 (0.00)	−5.80 (0.00)	−2.81 (0.00)	−5.09 (0.00)	−3.41 (0.00)	−1.87 (0.03)	−2.92 (0.00)	−2.34 (0.01)	−2.43 (0.01)	−2.42 (0.01)	−2.62 (0.01)
$c\_LAS\_LAS$	−6.64 (0.00)	−5.35 (0.00)	−5.18 (0.00)	−4.95 (0.00)	−5.11 (0.00)	−5.22 (0.00)	−5.60 (0.00)	−6.26 (0.00)	−6.57 (0.00)	−7.17 (0.00)	−7.81 (0.00)	−10.14 (0.00)
$c\_LAS\_TVP$	−7.25 (0.00)	−7.49 (0.00)	−10.72 (0.00)	−10.59 (0.00)	−7.37 (0.00)	−15.25 (0.00)	−7.52 (0.00)	−8.37 (0.00)	−6.97 (0.00)	−14.25 (0.00)	−10.91 (0.00)	−46.46 (0.00)
$c\_LAS\_UC-SV$	−8.05 (0.00)	−7.68 (0.00)	−10.41 (0.00)	−8.92 (0.00)	−7.17 (0.00)	−12.03 (0.00)	−7.38 (0.00)	−98.73 (0.00)	−6.88 (0.00)	−36.35 (0.00)	−15.21 (0.00)	−7.59 (0.00)
$c\_LAS\_WLa$	−6.45 (0.00)	−5.38 (0.00)	−5.38 (0.00)	−4.93 (0.00)	−5.01 (0.00)	−5.32 (0.00)	−5.79 (0.00)	−6.42 (0.00)	−6.94 (0.00)	−7.37 (0.00)	−8.69 (0.00)	−13.89 (0.00)
$c\_LAS\_ETS$	−8.72 (0.00)	−6.76 (0.00)	−8.05 (0.00)	−8.56 (0.00)	−9.75 (0.00)	−10.65 (0.00)	−11.82 (0.00)	−10.42 (0.00)	−17.75 (0.00)	−27.30 (0.00)	−7.47 (0.00)	−7.35 (0.00)
$c\_LAS\_AR(1)$	−6.41 (0.00)	−7.42 (0.00)	−9.53 (0.00)	−8.64 (0.00)	−11.23 (0.00)	−12.03 (0.00)	−27.44 (0.00)	−39.87 (0.00)	−7.40 (0.00)	−7.40 (0.00)	−7.33 (0.00)	−7.24 (0.00)
$c\_ada\_ada$	−6.52 (0.00)	−5.57 (0.00)	−5.38 (0.00)	−5.15 (0.00)	−5.31 (0.00)	−5.33 (0.00)	−5.85 (0.00)	−6.50 (0.00)	−6.89 (0.00)	−7.28 (0.00)	−8.07 (0.00)	−10.05 (0.00)
$c\_ada\_Aut\_no$	−7.30 (0.00)	−6.79 (0.00)	−7.17 (0.00)	−7.39 (0.00)	−7.36 (0.00)	−7.41 (0.00)	−7.19 (0.00)	−7.36 (0.00)	−6.80 (0.00)	−6.25 (0.00)	−5.73 (0.00)	−5.77 (0.00)
$c\_ada\_Aut\_IIS$	−5.62 (0.00)	−5.51 (0.00)	−5.84 (0.00)	−2.83 (0.00)	−5.00 (0.00)	−3.29 (0.00)	−1.86 (0.00)	−2.93 (0.00)	−2.27 (0.00)	−2.39 (0.00)	−2.38 (0.00)	−2.58 (0.00)

Table A2. Cont.

Models	1	2	3	4	5	6	7	8	9	10	11	12
<i>c_ada_LAS</i>	(0.00) −6.62	(0.00) −5.47	(0.00) −5.26	(0.00) −5.13	(0.00) −5.25	(0.00) −5.31	(0.03) −5.57	(0.00) −6.21	(0.01) −6.31	(0.01) −6.61	(0.01) −7.07	(0.01) −8.56
<i>c_ada_TVP</i>	(0.00) −7.19	(0.00) −7.50	(0.00) −10.90	(0.00) −10.53	(0.00) −7.41	(0.00) −15.82	(0.00) −7.50	(0.00) −8.36	(0.00) −6.99	(0.00) −15.29	(0.00) −11.05	(0.00) −33.03
<i>c_ada_UC-SV</i>	(0.00) −8.02	(0.00) −7.73	(0.00) −10.41	(0.00) −8.87	(0.00) −7.15	(0.00) −12.00	(0.00) −7.36	(0.00) −8.15	(0.00) −6.90	(0.00) −56.69	(0.00) −15.26	(0.00) −7.55
<i>c_ada_WLa</i>	(0.00) −6.47	(0.00) −5.48	(0.00) −5.47	(0.00) −5.09	(0.00) −5.12	(0.00) −5.37	(0.00) −5.79	(0.00) −6.38	(0.00) −6.65	(0.00) −6.81	(0.00) −7.74	(0.00) −10.51
<i>c_ada_ETS</i>	(0.00) −8.73	(0.00) −6.77	(0.00) −8.05	(0.00) −8.49	(0.00) −9.81	(0.00) −10.73	(0.00) −11.90	(0.00) −10.48	(0.00) −18.05	(0.00) −24.88	(0.00) −7.45	(0.00) −7.33
<i>c_ada_AR(1)</i>	(0.00) −6.39	(0.00) −7.45	(0.00) −9.65	(0.00) −8.63	(0.00) −11.27	(0.00) −12.35	(0.00) −36.83	(0.00) −7.41	(0.00) −7.38	(0.00) −7.36	(0.00) −7.31	(0.00) −7.24
<i>c_Aut_ada</i>	(0.00) −6.03	(0.00) −5.12	(0.00) −5.64	(0.00) −5.02	(0.00) −4.61	(0.00) −4.01	(0.00) −5.15	(0.00) −3.78	(0.00) −4.58	(0.00) −8.13	(0.00) −9.89	(0.00) −6.13
<i>c_Aut_Aut_no</i>	(0.00) −6.22	(0.00) −4.68	(0.00) −5.37	(0.00) −6.21	(0.00) −4.71	(0.00) −4.53	(0.00) −5.62	(0.00) −4.41	(0.00) −6.58	(0.00) −5.69	(0.00) −6.00	(0.00) −5.82
<i>c_Aut_Aut_IIS</i>	(0.00) −5.28	(0.00) −4.97	(0.00) −5.11	(0.00) −3.57	(0.00) −3.97	(0.00) −3.48	(0.00) −2.54	(0.01) −2.38	(0.01) −2.16	(0.02) −3.32	(0.00) −2.78	(0.00) −4.01
<i>c_Aut_LAS</i>	(0.00) −6.32	(0.00) −4.67	(0.00) −5.38	(0.00) −4.96	(0.00) −4.71	(0.00) −3.90	(0.00) −5.53	(0.00) −4.11	(0.00) −4.43	(0.00) −7.57	(0.00) −6.83	(0.00) −143.16
<i>c_Aut_TVP</i>	(0.00) −6.81	(0.00) −5.82	(0.00) −6.27	(0.00) −8.09	(0.00) −8.86	(0.00) −5.51	(0.00) −17.62	(0.00) −17.02	(0.00) −10.96	(0.00) −16.10	(0.00) −7.21	(0.00) −7.43
<i>c_Aut_UC-SV</i>	(0.00) −7.44	(0.00) −5.95	(0.00) −5.73	(0.00) −7.26	(0.00) −8.31	(0.00) −4.80	(0.00) −6.17	(0.00) −9.62	(0.00) −5.81	(0.00) −9.47	(0.00) −6.99	(0.00) −5.14
<i>c_Aut_WLa</i>	(0.00) −6.03	(0.00) −5.18	(0.00) −5.76	(0.00) −5.08	(0.00) −4.60	(0.00) −3.98	(0.00) −5.05	(0.00) −3.78	(0.00) −4.53	(0.00) −7.87	(0.00) −10.42	(0.00) −29.62
<i>c_Aut_ETS</i>	(0.00) −8.81	(0.00) −6.38	(0.00) −7.76	(0.00) −7.98	(0.00) −8.62	(0.00) −8.05	(0.00) −11.81	(0.00) −23.83	(0.00) −6.83	(0.00) −7.60	(0.00) −7.16	(0.00) −7.60
<i>c_Aut_AR(1)</i>	(0.00) −5.99	(0.00) −5.53	(0.00) −6.22	(0.00) −7.49	(0.00) −6.49	(0.00) −6.25	(0.00) −15.61	(0.00) −10.31	(0.00) −9.35	(0.00) −8.58	(0.00) −13.28	(0.00) −16.32

Note: *p*-values are in parentheses.Table A3. Forecast encompassing tests between aggregated and disaggregated ETS with  $\hat{\lambda}_{dis}^h$  ( $\hat{\lambda}_{ag}^h$ ) and the disaggregated (aggregated) ETS weights.

Horizon	$\hat{\lambda}_{ag}^h$	$\hat{\lambda}_{dis}^h$
1	0.53 **	0.47 *
2	0.48	0.52
3	0.41	0.59
4	0.22	0.78 *
5	−0.25	1.25 **
6	−0.17	1.17 **
7	0.02	0.98 *
8	−0.08	1.08 **
9	−0.51	1.51 ***
10	−0.01	1.01 **
11	−0.97	1.97 ***
12	0.09	0.91 *

Note: \*, \*\*, \*\*\* denote statistical significance at 10%, 5%, and 1% levels, respectively.

## Notes

<sup>1</sup> Direct forecasts require estimating a separate time series model for each forecasting horizon; the only change between each model is the number of horizons ahead for the dependent variable. The recursive forecast is defined if we re-estimate the model for each period in the forecast evaluation sample and if we compute forecasts with the recursively estimated parameters. See pages 30 and 31 of Ghysels and Marcellino (2018) for a definition of a recursive forecast.

<sup>2</sup> We considered an AR(13) model to approximate a multiplicative seasonality in which the non-seasonal part was the first-order autoregressive and the seasonal part was dependent on the previous year.

- 3 Stock and Watson (2007) assumed that  $(e_{1t}, e_{2t}) \sim N(0, \gamma * I_2)$ , and that  $(v_t, e_t) \sim N(0, I_2)$ , or a mixture of two normal distributions, with  $N(0, 0.1 * I_2)$  with a probability 0.95 and  $N(0, 0.5 * I_2)$  with a probability 0.05.  $I_2$  is the identity matrix of order 2,  $\gamma$  is a scalar parameter and controls the smoothness of the stochastic volatility process.
- 4 For comparison, Stock and Watson (2007) called the models (3) and (4) UC-SV, but the DGP for the SV was a random walk instead of the AR(1) model with a non-zero mean. This is the Stock and Watson (2007) formulation for UC-SV, which is unconventional. Their model implies that when the distribution of  $(v_t, e_t)$  is a mixture of normal distributions, there is a heavy tail that is a characteristic of SV models. We think they used this model because they only estimated one parameter  $\gamma$  instead of six for two SVs: two constants in AR(1), two autoregressive parameters, and two variances.
- 5 In general, a model being congruent means not having a problem in the specifications based on tests of heteroskedasticity, autocorrelation, and normality, among others. A more detailed discussion is in the Appendix A.5.
- 6 These two sectors together have a 2.3% share in the industrial production index.
- 7 Getulio Vargas Foundation created the CODACE in 2008. According to Picchetti (2018), this committee follows practices similar to those of the dating committee of the US National Bureau of Economic Research (NBER).
- 8 The standard deviation of  $\Delta y_t$  for industrial production in Brazil is about four times the standard deviation for the first difference in the logarithm of the non-seasonally adjusted US industrial production series for comparison.
- 9 A value-weighted portfolio means that the weight of a specific stock in a value-weighted portfolio is proportional to the market capitalization of this stock (Bhattacharya and Galpin 2011).
- 10 We compared the specifications of the selected ETS model that we obtained with the one from Hyndman et al. (2002). We considered the aggregated ETS model for simplification. Regarding the aggregated ETS model chosen for each of the 91 rolling windows, we determined that additive seasonality is more common, which differs from Hyndman et al. (2002), who found that most monthly series had multiplicative seasonality. Additive and additive dampened trends represent, respectively, 44% and 35% of the selected specifications in the 91 rolling windows. Hyndman et al. (2002) obtained a similar proportion of monthly series (with additive or additive dampened trends), which does not differ from what we obtained for the 91 rolling windows. So, we obtained a specification of the trend component for our case that was similar to the pattern reported by Hyndman et al. (2002), but our pattern differs in the case of the seasonality component (in relation to the authors).
- 11 We would like to acknowledge the comments by one of the referees
- 12 The second statistic compares all of the models in pairs to obtain a set, but the computational process is more intense.

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