

Article

Digital Trade Feature Map: A New Method for Visualization and Analysis of Spatial Patterns in Bilateral Trade

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Abstract: Product bilateral trade features can be organized and expressed in the Cartesian coordinate system by taking imports and exports as X and Y, which is similar to spatial visualization. Hence, geospatial expression and analysis methodologies can be applied in bilateral trade studies. In this paper, we propose a new digital trade feature map (DTFM) method for the visualization of bilateral trade features from a spatial perspective. The implementation process of DTFM can be summarized as feature extraction, visualization, and analysis. China–US bilateral trade data were used in several case studies. As the case studies show, the DTFM has the advantages of clear expression, easy operationalization and is highly extensible. Moreover, this method can provide a broader perspective for the understanding of trade features, i.e., in comprehensively considering the features of a specific product type and its neighbors. Furthermore, we propose an extensible DTFM application framework into which different trade features, different grid generation modes, and numerous spatial analysis models can be readily integrated.

Keywords: geographic information science; international trade; spatial thinking; heavy-tailed distribution; grid; geovisualization

1. Introduction

In the present era of globalization, trade is considered an important catalyst for the growth and development of many nations. Despite the adverse effects of trade barriers and export controls, the development of inter-product and intra-product trade research plays an important role in enhancing the understanding of the trade relationship structure, evolution, and relevant driving factors.

The analysis and visualization of the trade features of numerous different product types at small scales is a challenge for many studies. On the one hand, numerous indexes were proposed from the neo-classical trade theory and the new international trade theory, and widely used in the analysis of international trade relationships and attributions. For instance, [1] used the revealed comparative advantage index (RCAI) [2] to analyze comparative advantage products and their interactions with production structure and product diversification between the European Union (EU-27) and the European Neighborhood Policy countries. [3] used an export dependency index to measure the relative exposure of sectors and countries in Latin America to fluctuations of Chinese

demand. The concentration index and Grubel–Lloyd index have been used to analyze the influence of free trade agreements on the diversification of exports from Latin America [4] and the dynamics of intra-industry trade flows in MENA (Middle Eastern and Northern Africa) countries [5], respectively. The technical complexity index, trade complementarity index, and export similarity index have been comprehensively applied in the comparison of industrial competitive advantages/disadvantages and the analysis of trade structure and its changing trends, as well as to evaluate the national position in the international industrial value chain among multiple economies. However, most of these index-based approaches are appropriate only for a comparison of products or industries of the same type among multiple countries. It is difficult to express the trade features of numerous different product types in small scales. Furthermore, intra-product trade information will be smoothed if we classify thousands of traded products into several industries or broad categories.

On the other hand, complex network analysis methods and complexity theory provide research paradigm for revealing insights into the structure and evolution of trade relationships and interdependencies between trade partners that are not immediately evident in a purely statistical analysis of trade data. For most studies [6–9], networks were constructed by taking countries (or regions) as nodes, trade flows as edges, and trade features (trade volume, RCAI) as weights to express trade relationships, and their driving factors of specific categories of products (e.g., wind renewable energy industry [10,11], iron ore products [12], agricultural products [9,13]) among different countries. For instance, Cristelli [6] quantified export similarity by building distance matrices for products and countries based on the complex network theory and then determining the evolution of competitors' communities. Ermann [7] indicated that trade networks are characterized by being high-nested, which is typical of ecological networks. Given this, he constructed a Google matrix G of the multiproduct world trade between the United Nations (UN) countries to analyze the properties of trade flows [8]. Dong [9] constructed wheat-trading competition networks to analyze the impact of climate change on the global trade flows of wheat by ultimately putting forward a policy framework to promote a stable and healthy wheat-trading environment. The number of products is still a constraint that cannot be ignored for these studies, even though it can be somewhat increased by constructing multilayer networks [14,15]. Some studies developed two-mode network models to express the relationships among numerous categories of products [16–19]. Hildago [17] presents the concept of “product space”, in which products that can be produced in tandem (i.e., products that ‘require similar institutions, infrastructure, physical factors, technology, or some combination thereof’) are closely distributed with each other in the two-mode network. Given that, links of countries and products were integrated into a “product space” network to evaluate the complexity of national productive structures [18,20]. Hausmann takes economic complexity as a measure of society's productive knowledge and thereby expresses each country's adjacent possible or potential new products through the graphical representation of the “product space” [21]. These studies [17,18,20,21] are creative and of great significance for trade features analysis and visualization. However, the network of these hundreds of products is too complicated to identify specific products for visualization, and it is hard to clearly express the differences in trade features among different countries or phases. The same disadvantage also exists in two other widely used product trade pattern analysis models, i.e., the gravity model [22–24] and the clustering model [25].

The above methods significantly influence the understanding and analysis of the trade relationship structures or trade flow characteristics of products (or industries) across multiple countries. However, trade differentiation characteristics and the change processes of thousands of products are difficult to express clearly. Hence, it is of significance to develop methods that can analyze and express bilateral trade patterns and the evolution of many types of products [20]. Over recent years, geographic information science has been used to provide significant theories and methods for the analysis of the spatial differentiation characteristics and spatiotemporal variations of land surface elements [26–28]. The spatial coordinate is important factor for spatial analysis and visualization. Although the bilateral trade data of products has a unique classification system and quantitative expression mode, the trade

volume of product can be organized and expressed in Cartesian coordinate system by taking imports and exports as X and Y , which is similar to spatial visualization of land surface elements. On this basis, spatiotemporal analysis models can be applied to product trade studies.

This study develops a common method with characteristics of high comparability, clear expression, easy operationalization for visualization and analysis of spatial patterns of many types of products. We propose a new digital trade feature map (DTFM) method for the visualization of bilateral trade features from a spatial perspective. China–US bilateral trade data are used in case studies. According to the DTFM method, ‘trade space’ is constructed using product imports and exports as the coordinate axis (unit: dollar). Each type of product is spatially transformed to a points set and expressed in the ‘trade space’ according to annual imports and exports. Then, trade features, including importance level and import–export difference class, are evaluated by spatial statistics and the head/tail breaks method. Lastly, a grid map is generated by the reverse application of the Hilbert curve generation method for the visualization of trade features. As the case studies show, the DTFM method possesses the advantages of clear expression, easy operationalization and is highly extensible. Therefore, we also propose an extensible DTFM application framework in which different trade features, different grid generation modes, and numerous spatial analysis models can be readily integrated.

2. Materials and Methods

2.1. Data

The UN International Trade Statistics Database (UN Comtrade) is the world’s largest and most widely used international trade database with a high degree of authority and uniformity. Its record date can point back to 1962, and its total recorded quantity exceeds 3 billion. Over 200 countries/areas (reporters) provide their annual international trade statistics data detailed by commodities/service categories and partner countries. The data are subsequently transformed into the UN Statistics Division standard format with consistent coding (e.g., HS (Harmonized Product Description and Coding System), SITC (Standard International Trade Classification) and BEC (Classification by Broad Economic Categories)) and valuation in the data loading process. In this paper, a China–US annual bilateral trade dataset was extracted from the database and applied to the development of methods and case studies for the DTFM. The dataset is reported by the Chinese maritime customs and covers 27 years of imports and exports (unit: U.S. dollar) from 1992 to 2018. Product types are classified and encoded in terms of the harmonized product description and coding system (HS) 4-digit coding rule. The HS 4-digit code is generated from further subdivision of the HS 2-digit code (see Table A1 for detailed HS 2-digit coding rule); the total number of product classes is 1256. It is important to note that there is ambiguity in the import and export trade; therefore, to avoid confusion, we stipulate that imports and exports presented in this paper represent China as reporter and USA as partner, respectively.

2.2. Trade Data Spatialization Method

Geospatial expression and analysis methodologies are also appropriate for bilateral trade studies. In this paper, trade space was proposed by using product imports and exports as the coordinate axis (unit: dollar). Then, different types of products were spatially transformed to a points set and expressed in the ‘trade space’ according to their annual imports and exports. For each type of product, the location of a point reflects its trade volume and difference between imports and exports in a certain year, whereas the degree of dispersion of the distribution of points reflects its degree of trade volume change during a certain period of time. China–US annual bilateral trade data from 1992 to 2018 were transformed and expressed as sample points in the ‘trade space’, as shown in Figure 1. Taking product M (gas compressor and fan, HS 4-digit code: 8414) as an example, the trade volume change degree of M (SD_M) can be quantified using Equation (1), wherein $x_{M,i}$ and $y_{M,i}$ present imports and exports, respectively, of M in the i th-year; \bar{x}_M and \bar{y}_M are the mean imports and exports during n years and n is the total number of years. The average trade intensity L_M of M during n years can be calculated

using Equation (2), wherein $I_{M,i}$ represents the annual trade intensity of M in the i th-year. In this way, the changing characteristics of product trade volume and their correlations with each other can be intuitively expressed as spatial migration or spatial aggregation. The value of both exports and imports of different products and the difference between them can be integrated displayed.

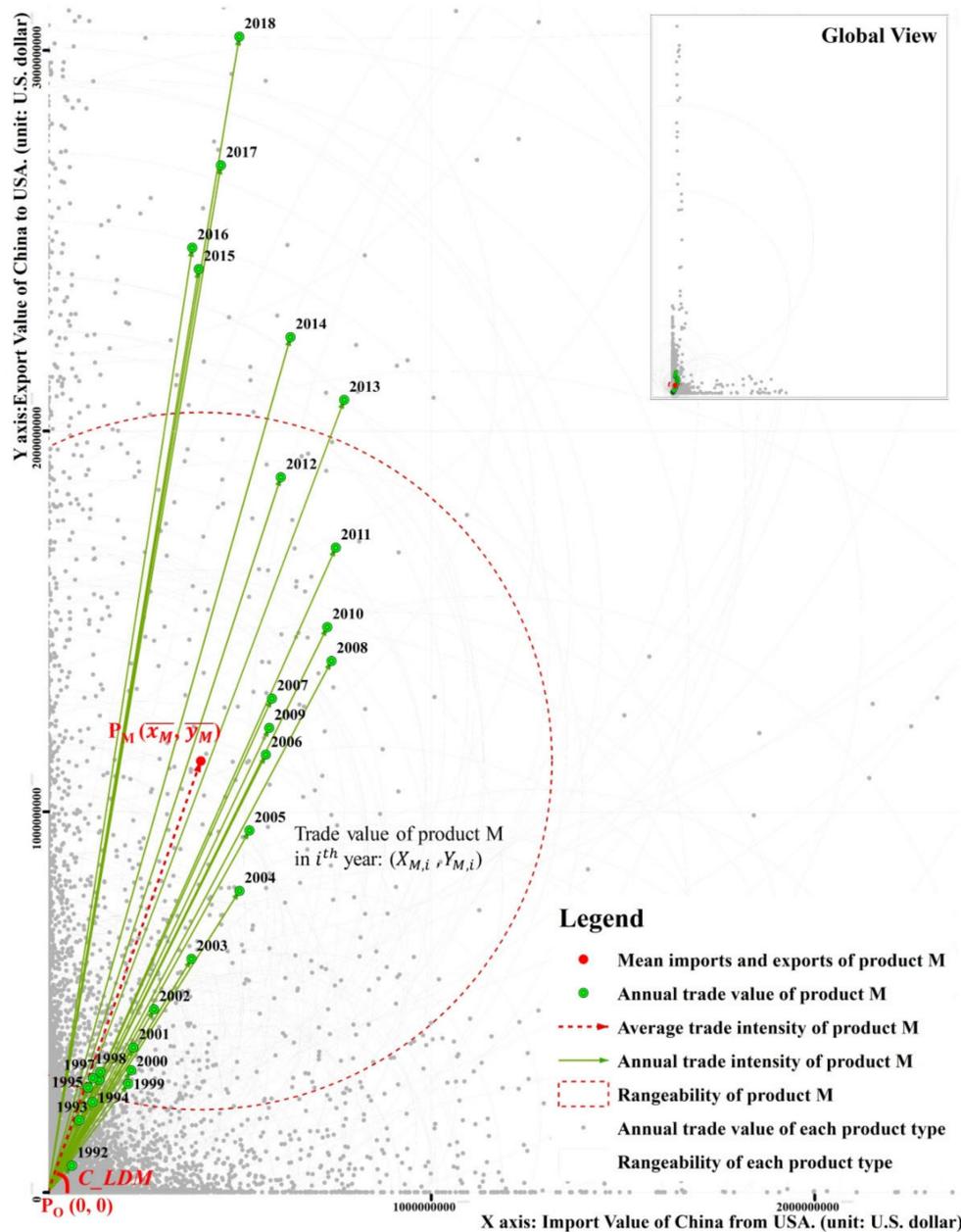


Figure 1. Variation in China–US bilateral trade in ‘trade space’. product M represents ‘Gas compressor and fan’, and its HS 4-digit code is 8414. By creating a line L that connects original point $P_0(0, 0)$ and central point $P_M(\bar{x}_M, \bar{y}_M)$, the length of L indicates the average trade intensity of product M . The Angle C_LDM between the L - and X -axis indicates the import–export difference.

Next, we constructed the rank–size distribution [29] of SD_M and L_M , as shown in Figure 2a,c. The rank–size distributions of SD_M and L_M both express significant characteristics of a heavy tail [30], i.e., products with large values are of low frequency and constitute the ‘head’, whereas products with small values are of high frequency and constitute the ‘tail’. As Figure 2b,d shows, the probability density function (PDF) has a linear distribution when graphed as a double-logarithm plot, i.e., the distributions

of SD_M and L_M can be represented by the power law. A heavy-tailed distribution can also be observed when assessing the PDFs of SD_M and L_M . It should be noted that low-frequency events are present in the head in rank–size distributions but are present in the tail in PDFs. In this article, to avoid confusion, the terms head and tail refer to those of the rank–size distribution rather than those of the PDF.

$$SD_M = \sqrt{\frac{\sum_{i=1}^n (x_{M,i} - \bar{x}_M)^2}{n} + \frac{\sum_{i=1}^n (y_{M,i} - \bar{y}_M)^2}{n}} \quad (1)$$

$$L_M = \frac{\sum_{i=1}^n l_{M,i}}{n}, l_{M,i} = \sqrt{x_{M,i}^2 + y_{M,i}^2} \quad (2)$$

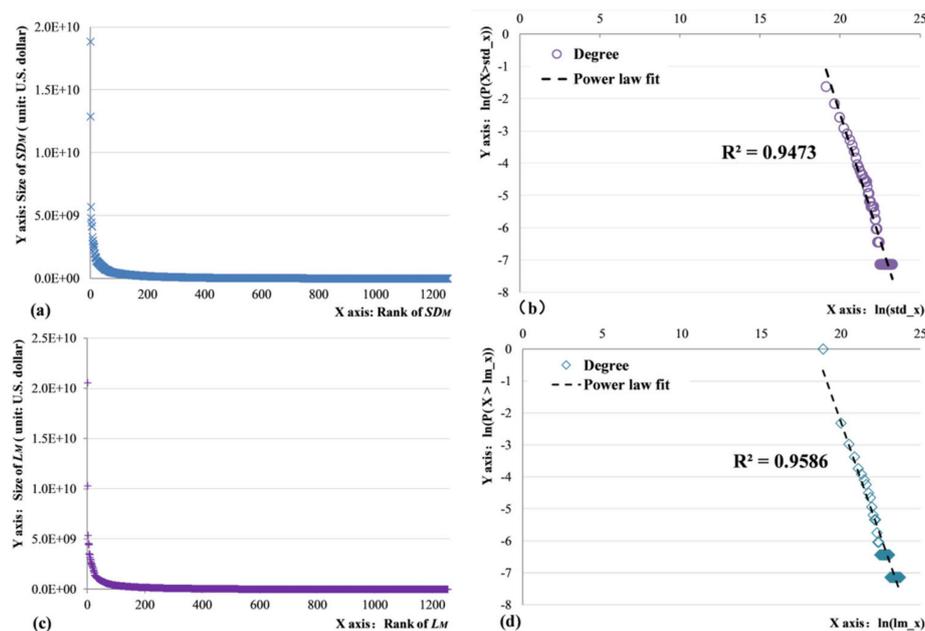


Figure 2. Heavy-tailed distributions of SD_M and L_M . (a) Rank–size distribution of SD_M . (b) Probability density distribution (Log) of SD_M . (c) Rank–size distribution of L_M . (d) Probability density distribution (Log) of L_M .

2.3. Head/Tail Breaks Method

In this study, the heavy-tailed distribution of products' bilateral trade features was considered in the level-classification process. Unlike a normal distribution that has two thin tails that rapidly reach the x -axis, a heavy-tailed distribution, theoretically, has a long tail skewed to the right, approaching but never touching the x -axis. Heavy-tailed distributions have been widely observed for social and natural phenomena [30]. For instance, 10% of the land in Europe is urban, and 90% is countryside; whereas, 80% of people in Europe are urban residents, and 90% of land is owned by 20% of the population, i.e., the smaller area with a large population constitutes the 'head', whereas the 'tail' is composed of the larger area with a small population. Similar phenomena are social wealth distribution and architectural environments [31,32]. Traditional classification methods are dominated by a Gaussian approach [33–35]; they focus on high-frequency events and consider low-frequency events to be separated from high-frequency events [36]. There exist large gaps or breaks between high-frequency and low-frequency values, as well as between different levels of low-frequency values, which constitute the foundation for the natural break classification [37]. However, for a heavy-tailed distribution, low-frequency events contain far more information and tend to be more important than high-frequency events [37]. For instance, there are numerous rare and extreme events in nature, society, and our daily lives that are termed 'black swan events' [38].

For the imbalance of a heavy-tailed distribution, Jiang formulated the head/tail division rule: ‘Given a variable X , if its values follow heavy-tailed distribution, then the mean of the values can divide all the values into two parts: a high percentage in the tail, and a low percentage in the head’ [30]. Under this rule, Jiang proposed the head/tail breaks method for data classification and verified its advantages over the natural break method [39]. The head/tail breaks method partitions the data values into two groups around the arithmetic mean and continues to iteratively partition the values above the mean until the ‘head’ values are no longer heavy-tailed distributed. Therefore, the number of classes and the class intervals are both naturally determined by the fractal nature of the heavy-tailed distribution of the data. The rank–size distribution of SD_M was used as sample data and was classified into five levels according to the head/tail breaks method, as shown in Figure 3, in which a higher level indicates a more important product.

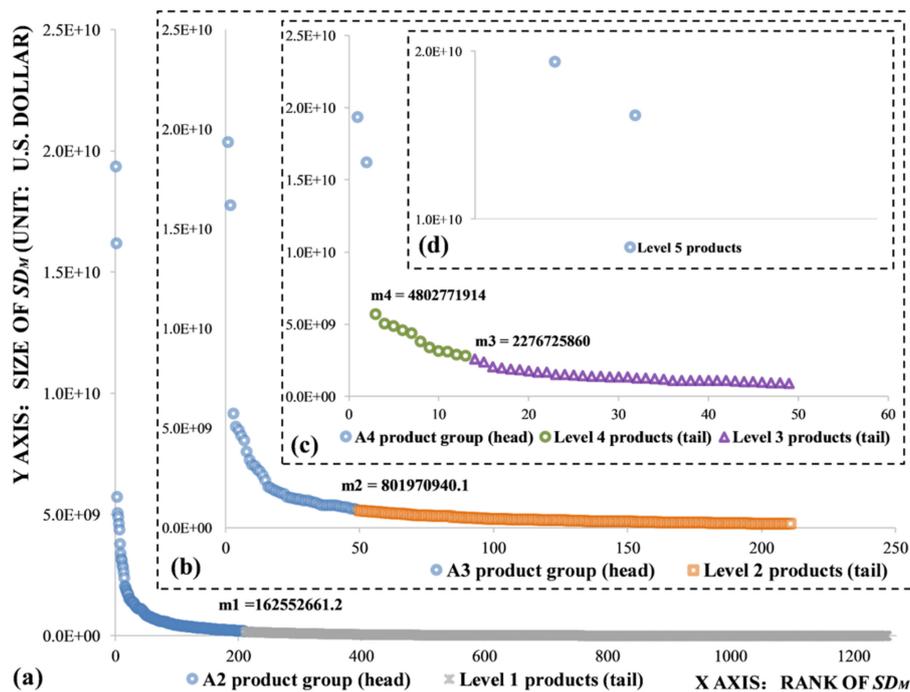


Figure 3. Classification process of the rank–size distribution of SD_M based on the head/tail breaks. (a) Extract Level 1 products— m_1 is the arithmetic mean of all SD_M values; values above m_1 were extracted as an A2 product group (head), and the rest as Level 1 products (tail). (b) Extract Level 2 products— m_2 is the arithmetic mean of A2 values; values above m_2 were extracted as an A3 product group (head), and the rest as Level 2 products (tail). (c) Extract Level 3, 4 products in sequence. (d) Define Level 5 products.

2.4. Hilbert Curve-Based Products Grids Generation Method

A Hilbert curve is a continuous curve that has self-similar properties and a zigzag and non-differentiable structure. This type of curve can uninterruptedly traverse each cell of a $2^n \times 2^n$ square grid system. Any two cells traversed sequentially are also adjacent in space. Hence, the Hilbert curve can be used to map elements in a two-dimensional space to a one-dimensional linear space while preserving the proximity among the elements as much as possible. Because of the spatial correlation characteristics of geographical elements, the Hilbert curve has been widely used in geographic data processing and management, e.g., in raster data compression [40–42], spatial indexing [43], and data segmentation [44]. In this paper, a products grid generation method was proposed by the reverse dimension increasing application of the Hilbert curve. A scanning matrix generation method (SMG) [45] was applied for the construction of a Hilbert curve. According to the SMG, an n -order ($2^n \times 2^n$) scanning matrix H_{2^n} can be generated quickly and accurately by a degree elevation iterative algorithm based on

a 1-order ($2^1 \times 2^1$) matrix H_2 , as shown in Equation (3). The Hilbert curve can then be generated by connecting the matrix element values in ascending order, as shown in Figure A1.

$$H_{2^{k+1}} = \begin{cases} \begin{bmatrix} H_{2^k} & 4^k E_{2^k} + H_{2^k}^T \\ (4^k + 1)E_{2^k} - \overline{H_{2^k}} & (3 \times 4^k + 1)E_{2^k} - (\overline{H_{2^k}})^T \end{bmatrix} & \text{k is an even number} \\ \begin{bmatrix} H_{2^k} & (4^{k+1} + 1)E_{2^k} - \overline{H_{2^k}} \\ 4^k E_{2^k} + H_{2^k}^T & (3 \times 4^k + 1)E_{2^k} - (H_{2^k}^T) \end{bmatrix} & \text{k is an odd number} \end{cases}$$

thereunto, $H_2 = \begin{bmatrix} 2 & 3 \\ 1 & 4 \end{bmatrix}$, set $H_m = \begin{bmatrix} a_{1,1} & a_{1,2} & \dots & a_{1,m} \\ a_{2,1} & a_{2,1} & & a_{2,m} \\ \vdots & & \ddots & \vdots \\ a_{m,1} & a_{m,1} & \dots & a_{m,m} \end{bmatrix}$

$$\overline{H_m} = \begin{bmatrix} a_{1,m} & a_{1,m-1} & \dots & a_{1,1} \\ a_{2,m} & a_{2,m-1} & & a_{2,1} \\ \vdots & & \ddots & \vdots \\ a_{m,m} & a_{m,m-1} & \dots & a_{m,1} \end{bmatrix}, \overline{H_m} = \begin{bmatrix} a_{m,1} & a_{m,2} & \dots & a_{m,m} \\ a_{m-1,1} & a_{m-1,2} & & a_{m-1,m} \\ \vdots & & \ddots & \vdots \\ a_{1,1} & a_{1,2} & \dots & a_{1,m} \end{bmatrix} \quad (3)$$

For 1256 types of China–US bilateral trade products, it is hard to comprehensively express the differences in product types, SD_M and L_M , in a one-dimensional space. By the reverse application of SMG, the HS 4-digit codes of products can be mapped to a two-dimensional space and visualized in a grid system. The implementation process is listed as follows.

Step 1: by applying SMG, a 6-order ($2^6 \times 2^6$) scanning matrix H_{2^6} and its corresponding Hilbert curve were generated. Each matrix element can be considered as a node of the Hilbert curve with a unique serial number that is sorted in ascending order starting at one. It means that the initial node and terminal node of the Hilbert curve, respectively, has the minimum (1) and maximum (4096) serial number.

Step 2: construct a vector format-based (*.shp) $2^6 \times 2^6$ grid system V_{2^6} , and create a new field named 'comtrade' for this file.

Step 3: assign the serial number of each matrix element in H_{2^6} to the field 'comtrade' attribute of the corresponding grid with the same row and column number in V_{2^6} by developing an ArcObjects-based application (see V_{2^6} in Supplementary Materials).

Step 4: the 1256 types of products were also sorted in ascending order according to their HS 4-digit codes.

Step 5: the first 1256 grids of V_{2^6} were extracted.

Step 6: for each grid, its field 'comtrade' attribute w ($w = 1, 2 \dots 1256$) was replaced with the HS 4-digit code of the w product in the order. In this way, the HS 4-digit codes of products can be mapped to a two-dimensional space and visualized on a grid system.

As Figure 4 shows, similar types of products are distributed in neighboring grids according to their HS 4-digit codes. Hence, our method provides a broader perspective for understanding and analyzing trade features. We accomplish this by comprehensively considering the features of a specific type of product and its neighbors, which is difficult to achieve using other methods, such as index-based approaches or complex network analysis methods.

We considered that the reverse dimension increasing application of the Hilbert curve has better adaptability than dimension reduction applications. Firstly, the two-dimensional matrix must be organized in the form of $2^n * 2^n$ for dimensionality reduction applications, whereas dimension increasing can be applied on any one-dimensional array. Secondly, neighboring elements in two-dimensional space may become distant from each other through dimension reduction, whereas neighboring relationships can be maintained by dimension increasing. Furthermore, the reverse dimension increasing application

of the Hilbert curve has an advantage of high versatility and will not be restricted by the number of product categories or variation of trade features.

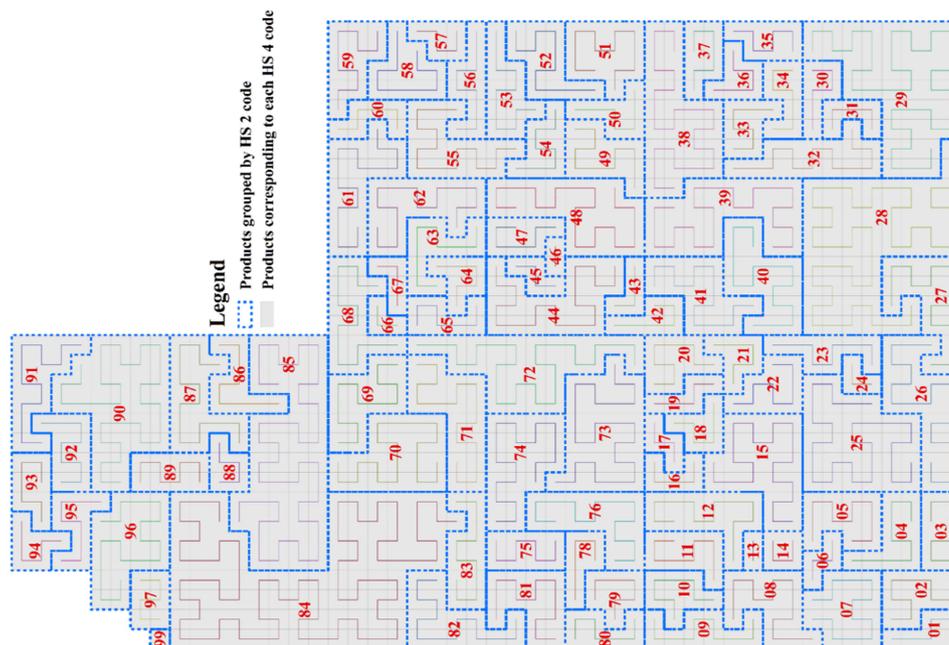


Figure 4. HS 4-digit code grid system. Each type of HS 4-digit code product corresponds to one grid, and the marked number is the HS 2-digit code of the product category to which it belongs. See Figure A2 for details of the HS 6-digit code grid system.

3. Case Studies

3.1. Case Study 1: Spatial Pattern Analysis of Product Importance Level

The spatial pattern of the product importance level in the China–US bilateral trade was calculated using the DTFM method, as shown in Figure 5. The head/tail breaks method was used to classify the rank–size distribution of SD_M and L_M into five levels (Figure 2). High-level product types contain far more information and tend to be more important than low-level product types. The comparison shows that the classification results for SD_M (Figure 3) are nearly in accordance with those of L_M . Hence, for each product type, its importance level was set as the maximum SD_M level and L_M level to maintain the presence of high-level product types as much as possible.

According to Figure 5, nearly 83% of Level 1 product types constitute the ‘tail’, supporting the overall stability of the China–US bilateral trade. The ‘head’ (Levels 2–5) consists of less than 17% of the product types; these types are important in China–US trade relations. Level 5 products are ‘automatic data processing machines (computers)’ (HS 4-digit code: 8471) and ‘electric apparatus for line telephony, telegraphy’ (HS 4-digit code: 8517). Level 3 and 4 products are mainly intensively located in product categories whose HS 2-digit codes are 61–64 (‘textile products’), 87 (‘vehicles, other than railway or tramway rolling stock’), 88 (‘aircraft, spacecraft and parts thereof’), 90 (‘optical, photographic, cinematographic, measuring, checking, medical or surgical instruments and apparatus’) and 94 and 95 (‘furniture, toys, games and sports requisites’). Meanwhile, a few Level 3 and 4 product types show discrete distributions; their corresponding HS 4-digit codes are 1201 (soya beans), 4011 (new pneumatic tires, of rubber), 4707 (waste or scrap of paper or paperboard), 5201 (cotton, not carded or combed), 7108 (gold, unwrought, semi-manufactured, powder form), 7113 (jewelry and parts, containing precious metal), and 7404 (copper, copper alloy, waste, or scrap).

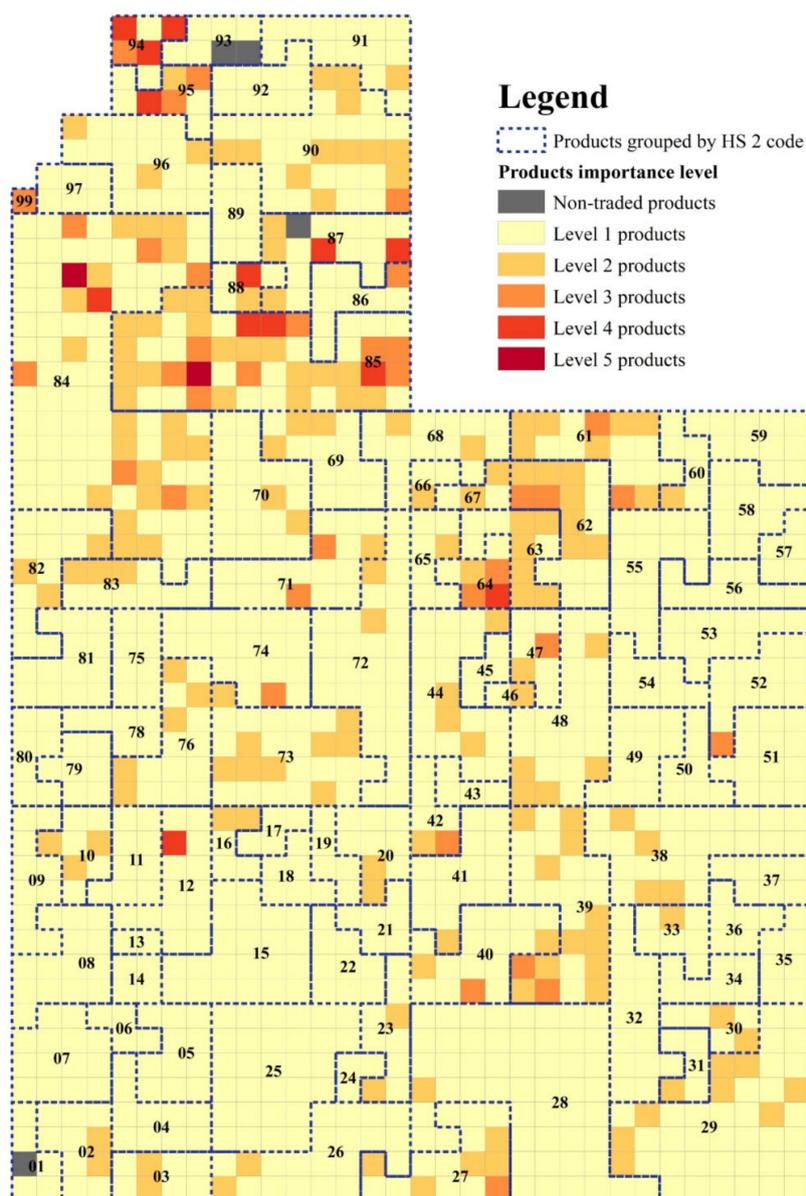


Figure 5. Spatial pattern of product importance level in China–US bilateral trade.

In conclusion, the DTFM provides a uniform and normative grid system for expressing trade features. Bilateral trade features of plentiful different types of products are clearly expressed. The relatively more important product types of the China–US bilateral trade mainly fall into technology-intensive product categories (such as machinery, electrical appliances, aerospace, communications, optics and medicine) and some labor-intensive product categories (such as furniture, toys, and textiles). Product levels in the former type are highly diversified because of significant component assembly and processing in intra-product trade. While for the latter, the highly diverse patterns in products levels are caused by high market demand.

3.2. Case Study 2: Spatial Pattern Analysis of Product Import–Export Difference Class

For each type of product M , its import–export difference C_LDM during n years can be calculated by Equation (4), wherein $x_{M,i}$ and $y_{M,i}$ represent imports and exports, respectively, of M in the i th-year; n is the total number of years. C_LDM is directly proportional to the ratio of total exports to total imports. If total exports of M are equal to its total imports, C_LDM is 45 (unit: degrees). If $C_LDM \in [0, 45)$, total exports of M are less than its total imports. In this instance, the rank–size

distribution of $\cot(C_LDM)$ shows significant characteristics of a heavy tail. Similarly, the rank–size distribution of $\tan(C_LDM)$ can be observed as a heavy-tailed distribution when $C_LDM \in (45, 90]$, as shown in Figure A3. Hence, the ratio of total exports to total imports varies markedly for different intervals of C_LDM . The head/tail breaks method was used with manual amendment to place the rank–size distributions of $\cot(C_LDM)$ and $\tan(C_LDM)$ into five classes, as shown in Table 1. Ultimately, we constructed a color mapping space to synthetically express product importance level and import–export difference class on a grid system, as shown in Figure 6.

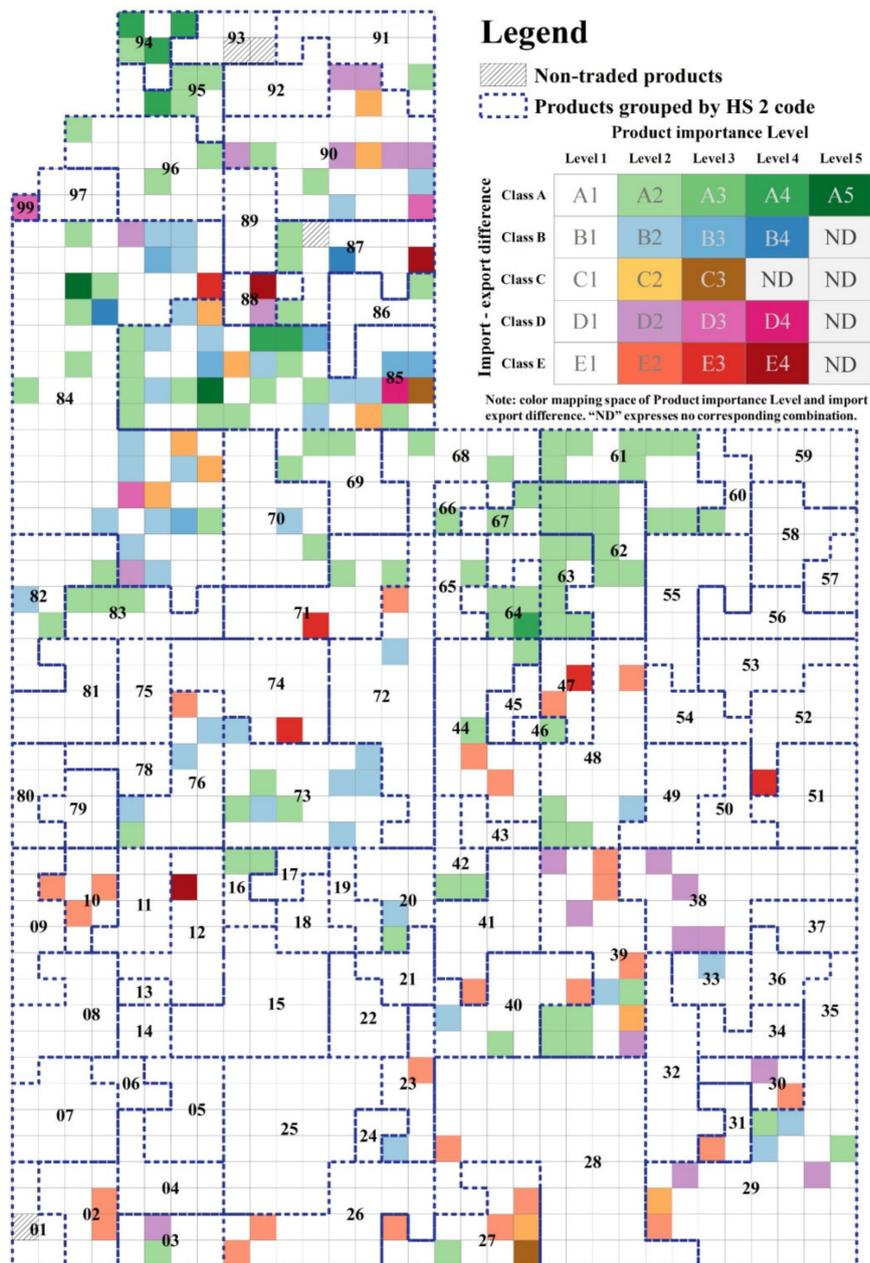


Figure 6. Spatial pattern of product import–export difference class. Only the import–export difference class information about high-level products (importance level > 1) were expressed in this figure. See Figure A4 for detailed information.

For important (Level > 1) products, those with surplus characteristics (Class A/B) are more likely to appear as a local aggregation distribution. These products are intensively located in product categories whose HS 2-digit codes are 61–64, 73, 76, 84, 85, 94, and 95. In ‘machinery and mechanical appliances’

(84) and ‘electrical machinery and equipment’ (85), the distributions of high-level Class A/B products (H-SPs) and high-level Class D/E products (H-DPs) are mixed. H-SPs are manufactured goods at the end of the value chain (low profit), whereas H-DPs are mostly components in the upper region of the value chain. This mixed-status indicates that the trade penalty for these types of products may damage the interests of multiple participating countries in addition to China and the USA. However, H-SPs in ‘furniture, toys, textile products, steel products, aluminum products’ are distributed intensively at the end of the value chain with few neighboring H-DPs and low market access barriers. In the context of a contraction in market demand or where product supply can be taken over by other countries, trade penalties for these H-SPs will occur readily and intensively compromise China’s interests. On the contrary, H-DPs are more likely to appear with a discrete distribution. Most of these H-DPs are raw materials and components in the upstream industrial chain (e.g., ‘soya beans’ (1201), ‘waste or scrap of paper or paperboard’ (4707), ‘cotton, unwrought gold’ (5201) and ‘copper, copper alloy, waste, or scrap’ (7404)). A few H-DPs are manufactured goods, such as ‘motor vehicles for transport of persons (except buses)’ (8703) and ‘aircraft, spacecraft, satellites’ (8802). Raw materials and manufactured goods in these H-DPs have the characteristics of being easy to replace and having a small range of influence.

The import–export difference class information of some high-level products (Level > 2) is listed in Table 2. First, the distribution of these products is unbalanced; the quantity of H-SPs is significantly greater than that of H-DPs, which is directly shown as the trade surplus between China and the USA. Second, in the context of economic globalization, the China–US bilateral trade is closely intertwined and mutually influenced, with a clear division of complementary types. H-SPs are mainly manufactured goods with a strong dependence on market demand, whereas H-DPs are mainly raw materials and components with resource barriers or technical barriers. This phenomenon indicates that the USA can be regarded as China’s product sales market and origin of raw materials; therefore, taken as a whole, China does not have a market advantage in China–US trade conflicts. Furthermore, there are only two types of high-level Class C products. This indicates that product trade competitiveness is weak between these two countries. Furthermore, we visualized the different aggregation characteristics of products and their relationship with trade features from a broader perspective.

$$C_LDM = \arctan\left(\frac{\sum_{i=1}^n y_{M,i}}{\sum_{i=1}^n x_{M,i}}\right) \quad (4)$$

Table 1. Head/Tail Breaks intervals of C_LDM .

| No. | Class | C_LDM Intervals | Illustration |
|-----|---------|--------------------|--|
| 1 | Class A | [85, 90] | $S_{exp}^1 \gg S_{imp}^2, S_{exp} / S_{imp} > 11.43$ |
| 2 | Class B | (60, 85) | $S_{exp} > S_{imp}, S_{exp} / S_{imp} \in (1.73, 11.43]$ |
| 3 | Class C | [30, 60] | $S_{exp} \approx S_{imp}, S_{exp} / S_{imp} \text{ or } S_{imp} / S_{exp} \in [1, 1.73]$ |
| 4 | Class D | (5, 30) | $S_{exp} < S_{imp}, S_{imp} / S_{exp} \in (1.73, 11.43]$ |
| 5 | Class E | [0, 5] | $S_{exp} \ll S_{imp}, S_{imp} / S_{exp} > 11.43$ |

¹ total exports, ² total imports

Table 2. Import–export difference class information of some high-level products (Level > 2).

| HS 4 Code | Type of Product | Class, Level | HS 4 Code | Type of Product | Class, Level |
|-----------------------|--|------------------|-----------------------|---------------------------------------|------------------|
| Surplus (Class A / B) | | | Deficit (Class D / E) | | |
| 3924 | Plastic table, kitchen, household, toilet articles | Class A, Level 3 | 1201 | Soya beans | Class E, Level 4 |
| 3926 | Plastic articles nes | Class A, Level 3 | 4707 | Waste or scrap of paper or paperboard | Class E, Level 3 |
| 4011 | New pneumatic tires, of rubber | Class A, Level 3 | 5201 | Cotton, not carded or combed | Class E, Level 3 |

Table 2. Cont.

| HS 4 Code | Type of Product | Class, Level | HS 4 Code | Type of Product | Class, Level |
|-----------|--|------------------|-----------|---|------------------|
| 4202 | Trunks, suitcases, camera cases, handbags, etc | Class A, Level 3 | 7108 | Gold, unwrought, semi-manufactured, powder form | Class E, Level 3 |
| 6104 | Women's, girl's suit, dress, skirt, etc, knit or crochet | Class A, Level 3 | 7404 | Copper, copper alloy, waste or scrap | Class E, Level 3 |
| 6110 | Jerseys, pullovers, cardigans, etc, knit or crochet | Class A, Level 3 | 8411 | Turbo-jets, turbo-propellers/other gas turbine engine | Class D, Level 3 |
| 6203 | Men's or boy's suits, jackets, trousers etc not knit | Class A, Level 3 | 8486 | Machines and apparatus of a kind used solely or principally for the manufacture of semiconductor boules or wafers, semiconductor devices, electronic integrated circuits or flat panel displays; machines and apparatus specified in Note 9 (C) of this Chapter | Class E, Level 3 |
| 6204 | Women's, girl's suits, jacket, dress, skirt, etc, woven | Class A, Level 3 | | | |
| 6402 | Footwear nes, with outer sole, upper rubber or plastic | Class A, Level 3 | | | |
| 6403 | Footwear with uppers of leather | Class A, Level 4 | 8542 | Electronic integrated circuits and microassemblies | Class D, Level 4 |
| 6404 | Footwear with uppers of textile materials | Class A, Level 3 | 8703 | Motor vehicles for transport of persons (except buses | Class E, Level 4 |
| 7113 | Jewelry and parts, containing precious metal | Class A, Level 3 | 8802 | Aircraft, spacecraft, satellites | Class E, Level 4 |
| 8414 | Air, vacuum pumps, compressors, ventilating fans, etc | Class B, Level 3 | 9018 | Instruments etc for medical, surgical, dental, etc us | Class D, Level 3 |
| 8443 | Printing and ancillary machinery | Class A, Level 3 | | | |
| 8467 | Tools for working in the hand, non-electric motor | Class A, Level 3 | 8541 | Diodes, transistors, semi-conductors, etc | Class C, Level 3 |
| 8471 | Automatic data processing machines (computers) | Class A, Level 5 | 2709 | Petroleum oils, oils from bituminous minerals, crude | Class C, Level 3 |
| 8473 | Parts, accessories, except covers, for office machine | Class B, Level 4 | | | |
| 8481 | Taps, cocks, valves for pipes, tanks, boilers, etc | Class B, Level 3 | 8544 | Insulated wire and cable, optical fiber cable | Class B, Level 3 |
| 8504 | Electric transformers, static converters and rectifier | Class B, Level 3 | 8609 | Cargo containers designed for carriage of goods | Class A, Level 3 |
| 8516 | Electric equipment with heating element, domestic etc | Class A, Level 3 | 8708 | Parts and accessories for motor vehicles | Class B, Level 4 |
| 8517 | Electric apparatus for line telephony, telegraphy | Class A, Level 5 | 9401 | Seats (except dentist, barber, etc chairs) | Class A, Level 4 |
| 8518 | Audio-electronic equipment, except recording devices | Class A, Level 3 | 9405 | Lamps and lighting fittings, illuminated signs, etc | Class A, Level 4 |
| 8521 | Video recording and reproducing apparatus | Class A, Level 3 | 9404 | Mattress supports, mattresses, bedding | Class A, Level 3 |
| 8525 | Radio and TV transmitters, television cameras | Class A, Level 4 | 9403 | Other furniture and parts thereof | Class A, Level 4 |

Table 2. Cont.

| HS 4 Code | Type of Product | Class, Level | HS 4 Code | Type of Product | Class, Level |
|-----------|---|------------------|-----------|---|------------------|
| 8528 | Television receivers, video monitors, projectors | Class A, Level 4 | 9503 | Other toys, scale models, puzzles, etc | Class A, Level 4 |
| 8529 | Parts for radio, TV transmission, receive equipment | Class B, Level 3 | 9504 | Articles for funfairs, table and parlor games | Class A, Level 3 |
| 8543 | Electrical machinery and apparatus, nes | Class B, Level 3 | 9506 | Equipment for gymnastics, sports, outdoor games nes | Class A, Level 3 |

4. Discussion: Extensible DTFM Application Framework and Development Path

In the second metrological revolution, spatiotemporal analysis methodology was widely used in the study of geography. This study is a preliminary attempt to apply spatiotemporal analysis methods to the study of international trade. The case studies focus on applying the DTFM on trade features visualization, and trade data processing is simplified without considering inflation, re-export/re-import and bilateral asymmetries. For one trade feature map, relevant country numbers are limited to one reporter and one partner.

As shown by the case studies, the DTFM has the advantages of clear expression, easy operationalization and is highly extensible. Trade features of thousands of products and their relationships in the China–US bilateral trade can be overall displayed in one map. It provides a proper way of expressing index-based [1–5] trade features calculation results. Moreover, this method can provide a broader perspective for understanding and analyzing trade features by comprehensively considering the features of a specific type of product and its neighbors. Different aggregation characteristics of products on trade features can be expressed. Hildago’s “product space” [17,18,20,45] proposes a creative method to evaluate and express the complexity of national productive structures. Our DTFM can be used as an alternative method of two-mode network models for expressing “product space”, by which economic complexity among different reporter-partner groups can be expressed clearly with higher comparability.

The DTFM is not limited by the specific case studies, but can be widely used in different forms of bilateral trade structure, variation and relationship analysis by modifying the application process and integrating additional spatiotemporal analysis models. Hence, we propose an extensible DTFM application framework, as shown in Figure 7. In the feature extraction process (Stage 1), the trade data specialization method and head/tail breaks model were applied to evaluate trade importance level and import–export difference class. Other features of trade products, such as the RCAI (revealed comparative advantage index), export similarity index and technical complexity index, are also appropriate for calculation and expression by DTFM. In Stage 2, the Hilbert curve generation method can be extended to construct different types of grid map, depending on actual product type coding strategies. The DTFM can be used as a replacement option of the two-mode network for clear expression of “product space” [17,18]. For Stage 3, the DTFM proposes a spatial expression mode similar to raster data; hence, numerous spatial analysis models (e.g., the change detection model, spatiotemporal clustering model, spatial autocorrelation model and k-means model) can be easily integrated to analyze product trade structure characteristics and their changes. Furthermore, image compression technology, spatial index technology and multi-band data organization model can be applied in DTFM to optimize trade data organization, storage, and management.

Paths for developing DTFM theories, methods and applications can be summarized as two parts. On the one hand, a trade data specialization method can simultaneously express imports and exports of bilateral trade products with different periods. On that basis, it is interesting to develop a path tracking method to describe the various characteristics of trade relations, identify product types with drastic change and, thereby, explore the driving factors of mutation in bilateral trade. On the other hand, DTFM can express the static features of numerous types of products, and the spatial visualization

process is unrestricted by the number of product types. In the next step, relevant works could focus on developing a coupling model to analyze the dynamic interactions of trade flows among multiple countries or groups.

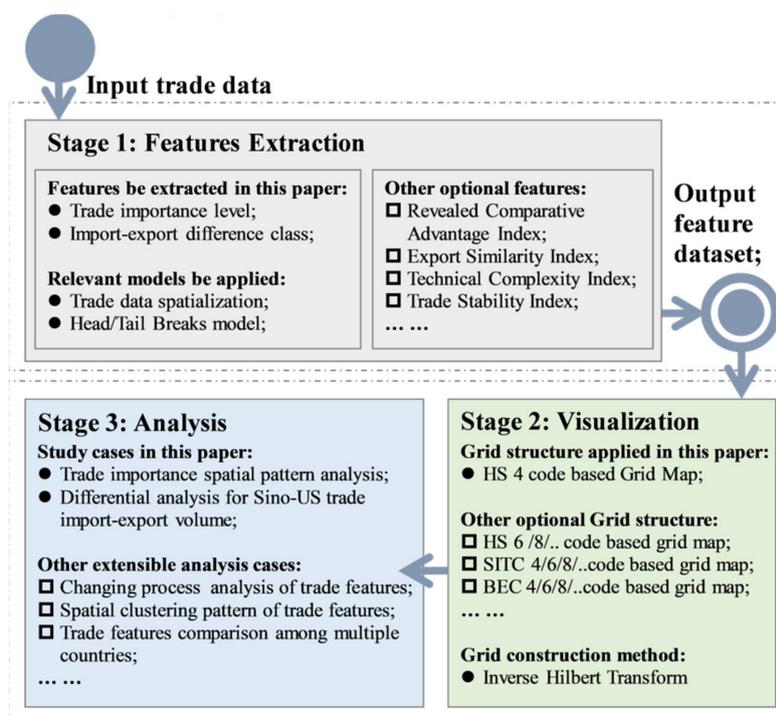


Figure 7. Extensible DTFM application framework.

5. Conclusions

The trade space has many features similar to geographical space, such as abstract expression of elements, space coordinates, spatial correlation and spatiotemporal variation. We believe that these features are of great significance in studying the trade structures and relations of numerous types of products. These features are difficult to express and analyze when traditional statistical methods or complex network methods are used.

In this paper, we proposed a new DTFM method for the visualization of bilateral trade features from a spatial perspective. The implementation process of DTFM can be summarized as feature extraction (Stage 1), visualization (Stage 2), and analysis (Stage 3). The China–US bilateral trade data were used in case studies. In Stage 1, ‘trade space’ was constructed using product imports and exports as the coordinate axis. Each type of product can be spatially transformed to a points set and expressed in the ‘trade space’ according to its annual imports and exports. Next, the trade features, including importance level and import–export difference class, were evaluated by spatial statistics and the head/tail breaks method. In Stage 2, a grid map was generated by the reverse application of the Hilbert curve generation method for visualization of the trade features. In Stage 3, the spatial pattern of the trade features was analyzed. In this way, bilateral trade features of plentiful different types of products are expressed with the advantages of clear expression, easy operationalization, good comparability, and high extensibility. Trade features aggregation characteristics of different products can also be expressed from a broader perspective. Furthermore, we propose an extensible DTFM application framework into which different trade features, different grid generation modes and numerous spatial analysis models can be readily integrated. In the future, we should develop methods for spatially understanding international trade systems.

Supplementary Materials: The following are available online at <http://www.mdpi.com/2220-9964/9/6/363/s1>.

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Conflicts of Interest: The authors declare no conflict of interest.

Appendix A. —HS 2-Digit Coding Rule

Table A1. Mapping table of HS 2-digit code and product type.

| HS 2-Digit Code | Product Type | HS 2-Digit Code | Product Type | HS 2-Digit Code | Product Type |
|-----------------|--|-----------------|---|-----------------|---|
| 01 | Animals; live | 34 | Soap, organic surface-active agents; washing, lubricating, polishing or scouring preparations; artificial or prepared waxes, candles and similar articles, modelling pastes, dental waxes and dental preparations with a basis of plaster | 67 | Feathers and down, prepared; and articles made of feather or of down; artificial flowers; articles of human hair |
| 02 | Meat and edible meat offal | 35 | Albuminoidal substances; modified starches; glues; enzymes | 68 | Stone, plaster, cement, asbestos, mica or similar materials; articles thereof |
| 03 | Fish and crustaceans, mollusks and other aquatic invertebrates | 36 | Explosives; pyrotechnic products; matches; pyrophoric alloys; certain combustible preparations | 69 | Ceramic products |
| 04 | Dairy produce; birds' eggs; natural honey; edible products of animal origin, not elsewhere specified or included | 37 | Photographic or cinematographic goods | 70 | Glass and glassware |
| 05 | Animal originated products; not elsewhere specified or included | 38 | Chemical products n.e.c. | 71 | Natural, cultured pearls; precious, semi-precious stones; precious metals, metals clad with precious metal, and articles thereof; imitation jewelry; coin |
| 06 | Trees and other plants, live; bulbs, roots and the like; cut flowers and ornamental foliage | 39 | Plastics and articles thereof | 72 | Iron and steel |

Table A1. Cont.

| HS 2-Digit Code | Product Type | HS 2-Digit Code | Product Type | HS 2-Digit Code | Product Type |
|-----------------|--|-----------------|---|-----------------|---|
| 07 | Vegetables and certain roots and tubers; edible | 40 | Rubber and articles thereof | 73 | Iron or steel articles |
| 08 | Fruit and nuts, edible; peel of citrus fruit or melons | 41 | Raw hides and skins (other than furskins) and leather | 74 | Copper and articles thereof |
| 09 | Coffee, tea, mate and spices | 42 | Articles of leather; saddlery and harness; travel goods, handbags and similar containers; articles of animal gut (other than silk-worm gut) | 75 | Nickel and articles thereof |
| 10 | Cereals | 43 | Furskins and artificial fur; manufactures thereof | 76 | Aluminum and articles thereof |
| 11 | Products of the milling industry; malt, starches, inulin, wheat gluten | 44 | Wood and articles of wood; wood charcoal | 78 | Lead and articles thereof |
| 12 | Oil seeds and oleaginous fruits; miscellaneous grains, seeds and fruit, industrial or medicinal plants; straw and fodder | 45 | Cork and articles of cork | 79 | Zinc and articles thereof |
| 13 | Lac; gums, resins and other vegetable saps and extracts | 46 | Manufactures of straw, esparto or other plaiting materials; basketware and wickerwork | 80 | Tin; articles thereof |
| 14 | Vegetable plaiting materials; vegetable products not elsewhere specified or included | 47 | Pulp of wood or other fibrous cellulosic material; recovered (waste and scrap) paper or paperboard | 81 | Metals; n.e.c., cermets and articles thereof |
| 15 | Animal or vegetable fats and oils and their cleavage products; prepared animal fats; animal or vegetable waxes | 48 | Paper and paperboard; articles of paper pulp, of paper or paperboard | 82 | Tools, implements, cutlery, spoons and forks, of base metal; parts thereof, of base metal |
| 16 | Meat, fish or crustaceans; mollusks or other aquatic invertebrates; preparations thereof | 49 | Printed books, newspapers, pictures and other products of the printing industry; manuscripts, typescripts and plans | 83 | Metal; miscellaneous products of base metal |

Table A1. Cont.

| HS 2-Digit Code | Product Type | HS 2-Digit Code | Product Type | HS 2-Digit Code | Product Type |
|-----------------|---|-----------------|--|-----------------|---|
| 17 | Sugars and sugar confectionery | 50 | Silk | 84 | Nuclear reactors, boilers, machinery and mechanical appliances; parts thereof |
| 18 | Cocoa and cocoa preparations | 51 | Wool, fine or coarse animal hair; horsehair yarn and woven fabric | 85 | Electrical machinery and equipment and parts thereof; sound recorders and reproducers; television image and sound recorders and reproducers, parts and accessories of such articles |
| 19 | Preparations of cereals, flour, starch or milk; pastrycooks' products | 52 | Cotton | 86 | Railway, tramway locomotives, rolling-stock and parts thereof; railway or tramway track fixtures and fittings and parts thereof; mechanical (including electro-mechanical) traffic signaling equipment of all kinds |
| 20 | Preparations of vegetables, fruit, nuts or other parts of plants | 53 | Vegetable textile fibers; paper yarn and woven fabrics of paper yarn | 87 | Vehicles; other than railway or tramway rolling stock, and parts and accessories thereof |
| 21 | Miscellaneous edible preparations | 54 | Man-made filaments; strip and the like of man-made textile materials | 88 | Aircraft, spacecraft and parts thereof |
| 22 | Beverages, spirits and vinegar | 55 | Man-made staple fibers | 89 | Ships, boats and floating structures |
| 23 | Food industries, residues and wastes thereof; prepared animal fodder | 56 | Wadding, felt and nonwovens, special yarns; twine, cordage, ropes and cables and articles thereof | 90 | Optical, photographic, cinematographic, measuring, checking, medical or surgical instruments and apparatus; parts and accessories |
| 24 | Tobacco and manufactured tobacco substitutes | 57 | Carpets and other textile floor coverings | 91 | Clocks and watches and parts thereof |
| 25 | Salt; sulfur; earths, stone; plastering materials, lime and cement | 58 | Fabrics; special woven fabrics, tufted textile fabrics, lace, tapestries, trimmings, embroidery | 92 | Musical instruments; parts and accessories of such articles |
| 26 | Ores, slag, and ash | 59 | Textile fabrics; impregnated, coated, covered or laminated; textile articles of a kind suitable for industrial use | 93 | Arms and ammunition; parts and accessories thereof |

Table A1. Cont.

| HS 2-Digit Code | Product Type | HS 2-Digit Code | Product Type | HS 2-Digit Code | Product Type |
|-----------------|--|-----------------|---|-----------------|--|
| 27 | Mineral fuels, mineral oils and products of their distillation; bituminous substances; mineral waxes | 60 | Fabrics; knitted or crocheted | 94 | Furniture; bedding, mattresses, mattress supports, cushions and similar stuffed furnishings; lamps and lighting fittings, n.e.c.; illuminated signs, illuminated name-plates and the like; prefabricated buildings |
| 28 | Inorganic chemicals; organic and inorganic compounds of precious metals; of rare earth metals, of radio-active elements and of isotopes | 61 | Apparel and clothing accessories; knitted or crocheted | 95 | Toys, games and sports requisites; parts and accessories thereof |
| 29 | Organic chemicals | 62 | Apparel and clothing accessories; not knitted or crocheted | 96 | Miscellaneous manufactured articles |
| 30 | Pharmaceutical products | 63 | Textiles, made up articles; sets; worn clothing and worn textile articles; rags | 97 | Works of art; collectors' pieces and antiques |
| 31 | Fertilizers | 64 | Footwear; gaiters and the like; parts of such articles | 99 | Commodities not specified according to kind |
| 32 | Tanning or dyeing extracts; tannins and their derivatives; dyes, pigments and other coloring matter; paints, varnishes; putty, other mastics; inks | 65 | Headgear and parts thereof | | |
| 33 | Essential oils and resinoids; perfumery, cosmetic or toilet preparations | 66 | Umbrellas, sun umbrellas, walking-sticks, seat sticks, whips, riding crops; and parts thereof | | |

Appendix B. —Hilbert Curve in Different Grid System

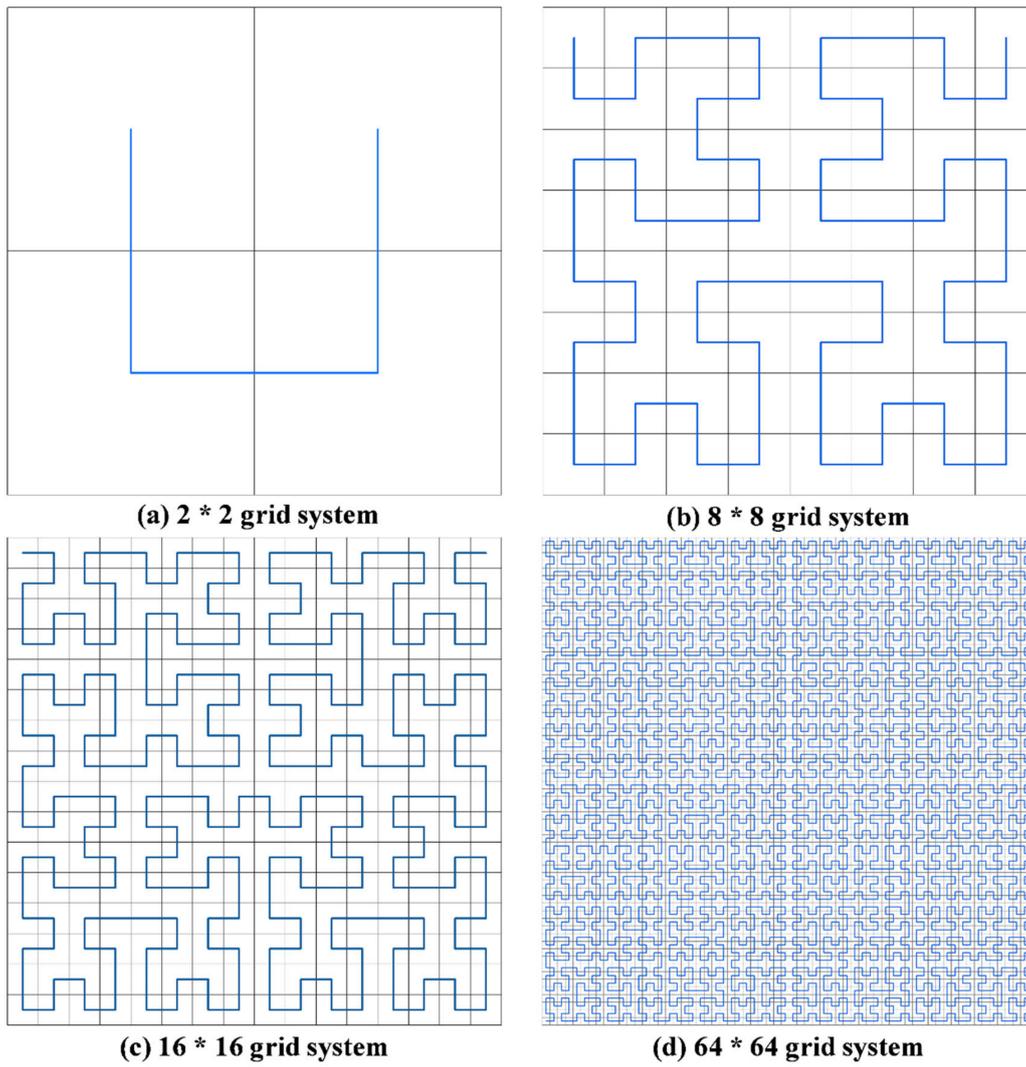


Figure A1. Hilbert curve in different grid system.

Appendix C. —Hilbert Curve in Different Grid System

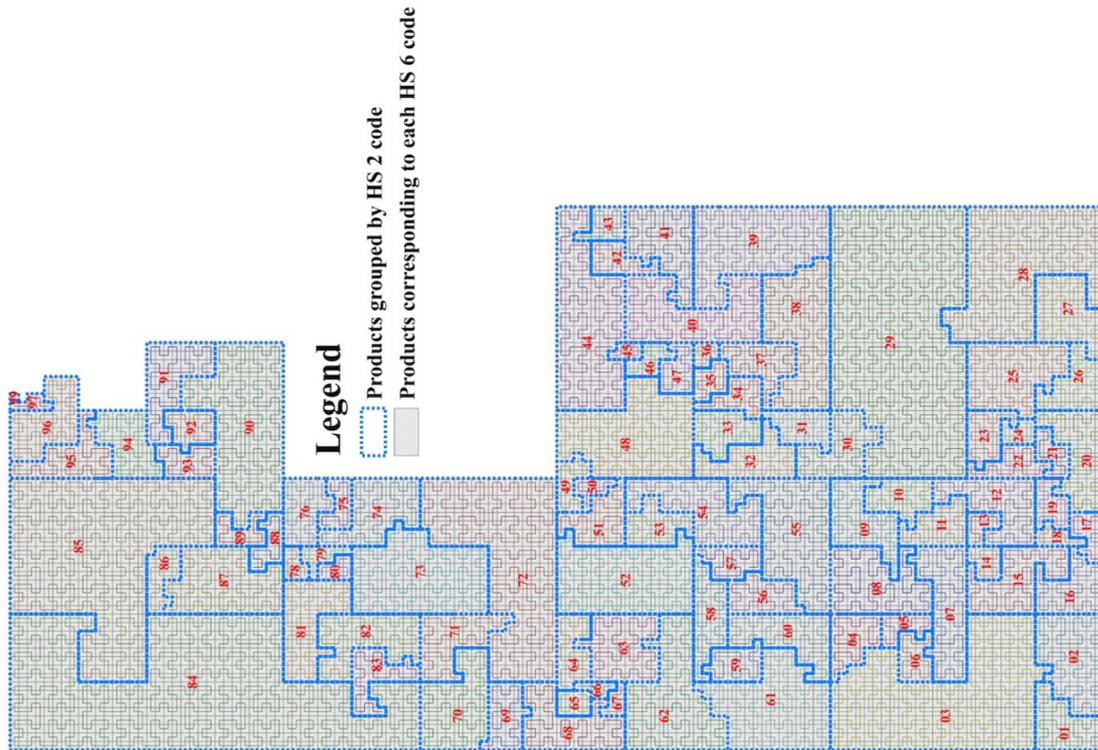


Figure A2. HS 6-digit code grid system (each type of HS 6-digit code product corresponds to one grid, and the marked number is HS 2-digit code of the product category it belongs to).

Appendix D. —Heavy-Tailed Distribution of $\cot(c_ldm)$ and $\tan(c_ldm)$

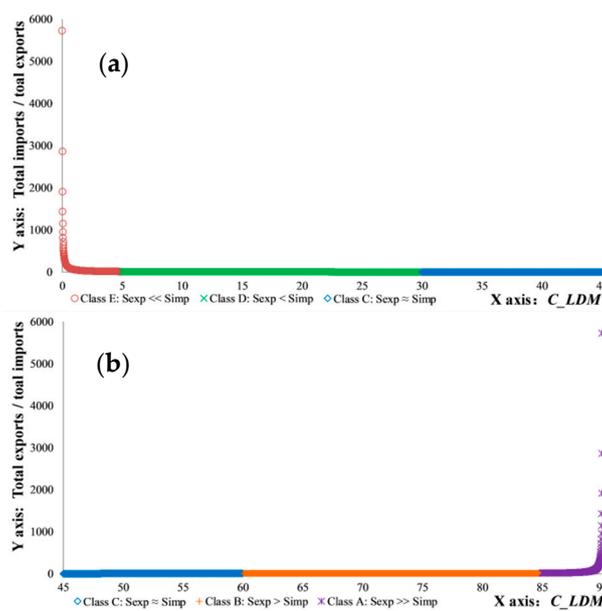


Figure A3. Heavy-tailed distribution of $\cot(C_LDM)$ and $\tan(C_LDM)$. (a) Heavy-tailed distribution of $\cot(C_LDM)$. (b) Heavy-tailed distribution of $\tan(C_LDM)$. In rank of C_LDM (unit: degree), we take 0.01 as the step size for sampling.

Appendix E. —Detailed Information for Spatial Pattern Of Products Import–Export Difference Class

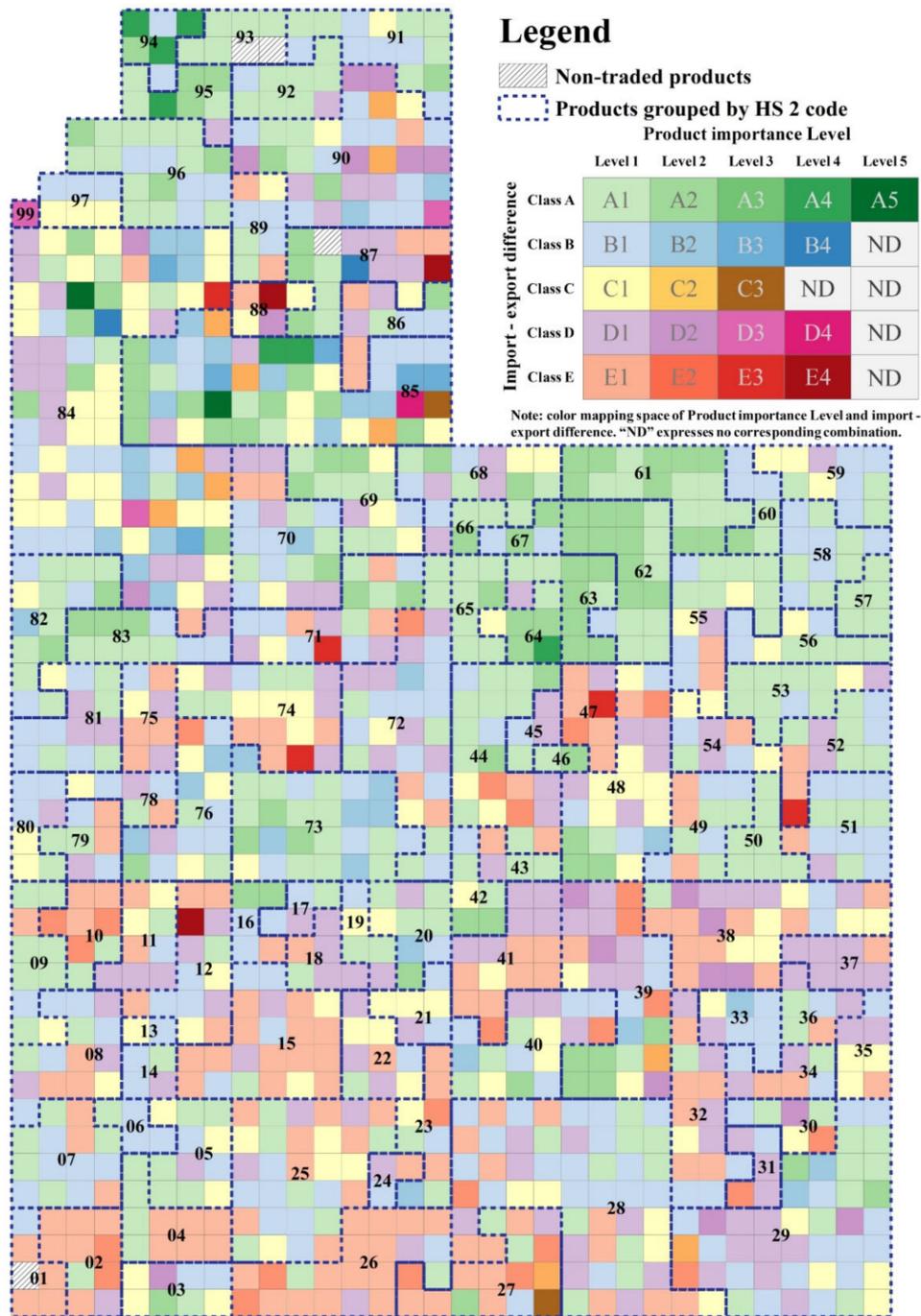


Figure A4. Detailed information for spatial pattern of products import–export difference class.

References

1. Boschma, R.; Capone, G. Relatedness and diversification in the European Union (EU-27) and European Neighbourhood Policy countries. *Environ. Plan. C* **2016**, *34*, 617–637. [[CrossRef](#)]
2. Balassa, B. Trade liberalization and revealed comparative advantage. *Manch. Sch. Econ. Soc. Stud.* **1965**, *33*, 99–123. [[CrossRef](#)]

3. Casanova, C.; Xia, L.; Ferreira, R. Measuring Latin America's export dependency on China. *JCEFTS* **2016**, *9*, 213–233. [[CrossRef](#)]
4. Dingemans, A.; Ross, C. Free trade agreements in Latin America since 1990: An evaluation of export diversification. *CEPAL Rev.* **2012**, *108*, 27–48. [[CrossRef](#)]
5. Haddou, A.; Young, J. Comparative Intra-industry trade analysis on the asymmetric effects of the FTA: Korea and MENA Countries. *J. Int. Trade Commer.* **2018**, *14*, 49–62. [[CrossRef](#)]
6. Cristelli, M.; Tacchella, A.; Gabrielli, A.; Pietronero, L.; Scala, A.; Caldarelli, G. Competitors' communities and taxonomy of products according to export fluxes. *EPJST* **2012**, *212*, 115–120. [[CrossRef](#)]
7. Ermann, L.; Shepelyansky, D. Ecological analysis of world trade. *Phys. Lett. A* **2013**, *377*, 3–4. [[CrossRef](#)]
8. Ermann, L.; Shepelyansky, D. Google matrix analysis of the multiproduct world trade network. *EPJB* **2015**, *88*, 84. [[CrossRef](#)]
9. Dong, C.; Yin, Q.; Lane, K.; Yan, Z.; Shi, T.; Liu, Y.; Bell, M.L. Competition and transmission evolution of global food trade: A case study of wheat. *Phys. A* **2018**, *509*, 998–1008. [[CrossRef](#)]
10. Basso, F.; Geciane, P.; Kannebley, J. International Trade Relations of Products for Wind Energy Production: A Study from the Dynamic Social Network Analysis (DSNA). In Proceedings of the 2017 Portland International Conference on Management of Engineering and Technology, Portland, OR, USA, 9–13 July 2017; pp. 1–18.
11. Fu, X.; Yang, Y.; Dong, W.; Wang, C.; Liu, Y. Spatial structure, inequality and trading community of renewable energy networks: A comparative study of solar and hydro energy product trades. *Energy Policy* **2017**, *106*, 22–31. [[CrossRef](#)]
12. Hao, X.; An, H.; Sun, X.; Zhong, W. The import competition relationship and intensity in the international iron ore trade: From network perspective. *Resour. Policy* **2018**, *57*, 45–54. [[CrossRef](#)]
13. Pappalardo, G.; Allegra, V.; Zarba, A. The effects of the bsec on regional trade flows of agri-food products. In Proceedings of the SGEM 2014 Scientific Subconference on Political Sciences, Law, Finance, Economics and Tourism, Sofia, Bulgaria, 3–9 September 2014; Volume 4.
14. Kivel, M.; Arenas, A.; Barthelemy, M.; Gleeson, J.; Moreno, Y.; Porter, M. Multilayer networks. *J. Complex Netw.* **2014**, *2*, 203–271. [[CrossRef](#)]
15. Liu, X.; Stanley, H.; Gao, J. Breakdown of interdependent directed networks. *Proc. Natl. Acad. Sci. USA* **2016**, *113*, 1138–1143. [[CrossRef](#)]
16. Latapy, M.; Magnien, C.; Vecchio, N. Basic notions for the analysis of large two-mode networks. *Soc. Netw.* **2008**, *30*, 31–48. [[CrossRef](#)]
17. Hidalgo, C.; Klinger, B.; Barabási, A.; Hausmann, R. The product space conditions the development of nations. *Science* **2007**, *317*, 482–487. [[CrossRef](#)] [[PubMed](#)]
18. Hidalgo, C.; Hausmann, R. The building blocks of economic complexity. *Proc. Natl. Acad. Sci. USA* **2009**, *106*, 10570–10575. [[CrossRef](#)] [[PubMed](#)]
19. Vidmer, A.; Zeng, A.; Medo, M.; Zhang, Y.-C. Prediction in complex systems: The case of the international trade network. *Phys. A* **2015**, *436*, 188–199. [[CrossRef](#)]
20. Mealy, P.; Farmer, J.; Teytelboym, A. Interpreting economic complexity. *Sci. Adv.* **2019**, *51*, 1705. [[CrossRef](#)]
21. Hausmann, R.; Hidalgo, C. *The Atlas of Economic Complexity: Mapping Paths to Prosperity*; MIT Press Books; The MIT Press: Cambridge, UK, 2014; Volume 1.
22. Fadeyi, O.; Bahta, T.; Ogundeji, A.; Willemse, B.J. Impacts of the SADC Free Trade Agreement on South African agricultural trade. *Int. J. Entrep. Innov.* **2014**, *15*, 53–59. [[CrossRef](#)]
23. Mupela, E.; Szirmai, A. Communication costs and trade in sub Saharan Africa: A gravity approach. In e-Infrastructure and e-Services for Developing Countries. In *AFRICOMM 2013. Lecture Notes of the Institute for Computer Sciences, Social Informatics and Telecommunications Engineering*; Bissyandé, T., van Stam, G., Eds.; Springer: Cham, Switzerland, 2013; p. 135.
24. Matkovski, B.; Radovanov, B.; Zekic, S. The effects of Foreign agri-food trade liberalization in South East Europe. *Ekonomicky Casopis* **2018**, *66*, 945–966.
25. De, F.; De, S.; Vleira, J. Evaluation of logistic performance indexes of brazil in the international trade. *RAM. Rev. Admin. Mackenzie* **2015**, *16*, 213–235.
26. Goodchild, M. Geographical information-science. *IJGIS* **1992**, *6*, 31–45. [[CrossRef](#)]
27. Goodchild, M.; Haining, R.; Wise, S. Integrating GIS and spatial data analysis: Problems and possibilities. *IJGIS* **1992**, *6*, 407–423. [[CrossRef](#)]

28. Goodchild, M.; Yuan, M.; Cova, T. Towards a general theory of geographic representation in GIS. *IJGIS* **2007**, *21*, 239–260. [[CrossRef](#)]
29. Zipf, G.K. *Human Behaviour and the Principles of Least Effort*; AddisonWesley: Cambridge, MA, USA, 1949.
30. Jiang, B.; Liu, X. Scaling of geographic space from the perspective of city and field blocks and using volunteered geographic information. *IJGIS* **2012**, *26*, 215–229. [[CrossRef](#)]
31. Jiang, B. A topological pattern of urban street networks: Universality and peculiarity. *Phys. A* **2007**, *384*, 647–655. [[CrossRef](#)]
32. Jiang, B. Street hierarchies: A minority of streets account for a majority of traffic flow. *IJGIS* **2009**, *23*, 1033–1048. [[CrossRef](#)]
33. Fisher, W.D. On grouping for maximum homogeneity. *J. ASA* **1958**, *53*, 789–798. [[CrossRef](#)]
34. Jenks, G.F. Generalization in statistical mapping. *Ann. AAG* **1963**, *53*, 15–26. [[CrossRef](#)]
35. Wang, J.F.; Li, X.H.; Christakos, G.; Liao, Y.; Zhang, T.; Gu, X.; Zheng, X. Geographical detectors-based health risk assessment and its application in the neural tube defects study of the Heshun region, China. *IJGIS* **2010**, *24*, 107–127. [[CrossRef](#)]
36. Jiang, B.; Ma, D. How complex is a fractal? Head/tail breaks and fractional hierarchy. *J. Geovisualization Spat. Anal.* **2018**, *2*, 1–6. [[CrossRef](#)]
37. Jiang, B.; Yin, J. Ht-Index for quantifying the fractal or scaling structure of geographic features. *Ann. AAG* **2014**, *104*, 530–540. [[CrossRef](#)]
38. Taleb, N.N. *The Black Swan: The Impact of the Highly Improbable*; Allen Lane: London, UK, 2007.
39. Jiang, B. Head/Tail Breaks: A new classification scheme for data with a heavy-tailed distribution. *Prof. Geogr.* **2012**, *65*, 482–494. [[CrossRef](#)]
40. Ye, S.J.; Zhang, C.; Wang, Y.; Liu, D.; Du, Z.; Zhu, D. Design and implementation of automatic orthorectification system based on GF-1 big data. *TCSAE* **2017**, *33*, 266–273.
41. Ye, S.J. Research on application of Remote Sensing Tupu-take monitoring of meteorological disaster for example. *AGCS* **2018**, *47*, 892. (In Chinese with English abstract)
42. Ye, S.; Liu, D.; Yao, X.; Tang, H.; Xiong, Q.; Zhuo, W.; Du, Z.; Huang, J.; Su, W.; Shen, S.; et al. RDCRMG: A raster dataset clean & reconstitution multi-grid architecture for remote sensing monitoring of vegetation dryness. *Remote Sens.* **2018**, *10*, 1376.
43. Yao, X.; Mokbel, M.; AlArabi, L.; Eldawy, A.; Yang, J.; Yun, W.; Li, L.; Ye, S.; Zhu, D. Spatial coding-based approach for partitioning big spatial data in Hadoop. *Comput. Geosci.* **2017**, *106*, 60–67. [[CrossRef](#)]
44. Ye, S.J.; Yan, T.L.; Yue, Y.-L.; Lin, W.-Y.; Li, L.; Yao, X.; Mu, Q.-Y.; Li, Y.-Q.; Zhu, D.-H. Developing a reversible rapid coordinate transformation model for the cylindrical projection. *Comput. Geosci.* **2016**, *89*, 44–56. [[CrossRef](#)]
45. Wang, S.; Xu, X. A new algorithm of hilbert scanning matrix and its MATLAB program. *J. Image Graph.* **2006**, *1*, 119–122.

