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Quantitative Analysis of Insulator Degradation in a Single Layer Solenoid by Renormalization of the Transmission Parameter

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Abstract: In this paper, a novel method to quantitatively analyze insulator degradation in a single layer solenoid is proposed. The suggested method employs renormalization of scattering parameters to efficiently detect changes of permittivity in a degraded solenoid. Firstly, a transmission line model, including a locally degraded part in the insulator, was developed, and it was determined that the phase information of the transmission parameter was very informative to check the permittivity change in the transmission line. To check the workability of this idea in a solenoid, a 30-turn single-layer solenoid was designed and fabricated, and 51 degraded states for mimicking insulation deterioration in each turn were introduced by installing additional insulator rings, which increased local relative permittivity. The phase data of the measured transmission parameter turned out to be useful for quantifying changes of the insulator in the solenoid. To maximize the detectability, the measured scattering parameters were renormalized with different reference impedances, which was very useful for detecting degradation in the transmission parameter. In this paper, detailed procedures for quantitatively analyzing degradation of an insulator are proposed and we verify that the suggested renormalization technique is very promising for effectively evaluating the degradation of a solenoid.

Keywords: diagnostic method; single layer solenoid; transmission line theory; scattering parameter renormalization

1. Introduction

Currently, there are 441 nuclear reactors in operation in 30 countries worldwide, which supplied approximately 10.2% of the global electricity in 2017 [1]. According to the International Atomic Energy Agency (IAEA) report, in 2019, 256.3 GW(e) of net capacity, representing more than 65% of power reactors, had been in operation for over 30 years. Long term operation and aging management programs are being implemented to increase nuclear power reactors globally to ensure continued safe and sustainable operations [2]. Each country operates by designating the overhaul period, equipment maintenance, and sensor calibration and replacement according to regulatory standards. However, unnecessary calibration and replacement occurs during the maintenance period due to the absence of a diagnostic model, requiring many human resources. Moreover, economic loss due to risk of malfunction, aging accumulation, and long maintenance periods is enormous [3]. Therefore, diagnostic models for various nuclear power plants (NPP) have been extensively studied [4–8].

The solenoid operated valve (SOV) is one of the elements widely used in nuclear power plants. Although the structure is a simple fundamental element, it is important when operating a nuclear

power plant and, in particular, for controlling the flow rate [9]. The SOV can be divided into electrical parts, including windings and cores, and mechanical parts, including valves and plungers. The electrical parts are particularly essential because the solenoid generates primary power by receiving a signal from the control unit. A severe failure, such as a short circuit between windings, can occur due to a soft failure such as degradation of the winding in the dielectric due to aging. In other words, estimating the deterioration of the insulator in a solenoid is very important to the diagnostics and prognostics of the solenoid valve. To detect and classify the states of soft failure in the winding, both modeling and experimental studies about the aging effect of the solenoid have been conducted. Recently, an experimental analysis reported on the relationship between solenoid impedance and aging effects in insulation coating using an accelerated deterioration [10–12]. The circuit model-based approach can be powerful for estimating operation torque and the corresponding waveform of current; however, it has shortcomings for analyzing and detecting insulator degradation because it uses only equivalent lumped elements.

In this paper, a diagnostic study on the local degradation of an insulator in a single-layered solenoid winding based on measured two-port scattering S -parameters is conducted to overcome the shortcomings of a circuit-based approach. Assuming that a solenoid could be similar to a transmission line, a locally degraded insulator was modeled to derive the formulas so that the phase information of the renormalized transmission parameter could be effectively used to estimate the degradation of the insulator. These formulas were applied to the single-layered solenoid in which additional ring-shaped insulators were installed to mimic the degradation of the insulator. The appropriately renormalized transmission parameter successfully estimated the changes in the permittivity of the solenoid.

The remainder of this paper is organized as follows: In Section 2, the electrical model for a transmission line with local degradation is described, and the approximated formulas for the phase in on the transmission parameter are suggested; in Section 3, the single-layer solenoid is designed and fabricated, and the sheath rubber rings are installed on the bobbin of the solenoid for mimicking the local degradation of the insulator, the whole measurement schemes are presented, and the interface de-embedding process is also described; in Section 4, the results of the quantitative analysis for the local degradation are shown; and finally, the conclusion and summary of the suggested diagnostic method are given.

2. A Transmission Line Model Including a Locally Degraded Part Inside

Figure 1a shows a lumped circuit parameter model for a solenoid where L_s indicates the equivalent series inductance of the solenoid, R_s indicates the conductor's resistance, and C_p and R_i are parallel capacitance and parallel resistance, respectively. This model has been used to estimate reactance [10,13,14], and induced torque with a plunger from measured voltage and current [15] in a low-frequency range. However, it is not suitable for estimating the distributed degradation of the insulator inside a solenoid due to the limit of lumped element modeling itself.

A solenoid can indeed be quite different from a transmission line in that, most importantly, a transmission line repeats the same distributed elements as it travels from port 1 to port 2, as illustrated in Figure 1b, while a solenoid does not. It seems, however, that we could make a rough assumption that changes of permittivity in a solenoid could be estimated in the same way as the changes in a transmission line [16] are estimated using the S -parameters. Note that the signals in a solenoid travel anyway just as the signals in a transmission line travel, including the changes in permittivity inside the solenoid. Furthermore, it is promising to note that the distributed elements in a solenoid, due to the regular winding in the solenoid, are also similarly repeated as the signal travels, similar to the signal in a transmission line. Figure 1b illustrates a distributed model for a transmission line where Z_c is the characteristic impedance of the transmission line, β is a propagation constant, and Z_0 is the reference impedance of the measurement equipment. In the next section, assuming that the permittivity change in a solenoid could be similar to the permittivity change in a transmission line, the S -parameter formulas with a discontinuous parameter in the transmission line, to mimic the deterioration of the insulator inside, is developed.

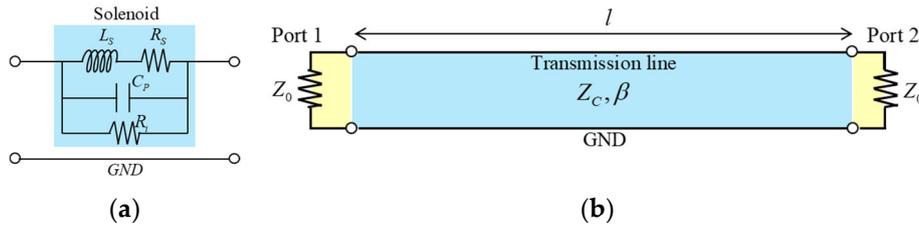


Figure 1. (a) Lumped element model for a solenoid in low frequency range (under the second resonance frequency); (b) Finite length transmission line model emphasizing distribution elements.

2.1. Discontinuous Transmission Line Model Mimicking Deterioration of the Insulator

A local permittivity-degraded area in a winding can be modeled by a finite line with different electrical characteristics. Figure 2 shows a transmission line consisting of the following three sectionalized parts: area 1 (length l_1 , characteristic impedance Z_C , and phase constant β) and area 3 (length l_3 , characteristic impedance Z_C and phase constant β) are in a healthy state, and area 2 (length l_2 , characteristic impedance Z'_C and phase constant β') indicates the degraded part. That is, the pink area in the diagram indicates area 2, where the insulator locally deteriorates with the prime symbols. The total ABCD parameter with 't' in the superscript can be calculated by multiplying three ABCD matrices in sequence as Equation (1) [17].

$$\begin{bmatrix} A' & B' \\ C' & D' \end{bmatrix} = \begin{bmatrix} \cos \beta l_1 & jZ_C \sin \beta l_1 \\ j\frac{1}{Z_C} \sin \beta l_1 & \cos \beta l_1 \end{bmatrix} \begin{bmatrix} \cos \beta' l_2 & jZ'_C \sin \beta' l_2 \\ j\frac{1}{Z'_C} \sin \beta' l_2 & \cos \beta' l_2 \end{bmatrix} \begin{bmatrix} \cos \beta l_3 & jZ_C \sin \beta l_3 \\ j\frac{1}{Z_C} \sin \beta l_3 & \cos \beta l_3 \end{bmatrix} \quad (1)$$

Each element in the total ABCD matrix is expressed as Equation (2), and the total S-parameters, S^t , can be represented as Equation (3) [17]. In the next two sections, the effect of area 2 on the total S-parameters is addressed in terms of the total change in permittivity.

$$\begin{aligned} A' &= \cos \beta l_1 \cos \beta' l_2 \cos \beta l_3 \left(1 - \frac{Z_C}{Z'_C} \tan \beta l_1 \tan \beta' l_2 - \frac{Z'_C}{Z_C} \tan \beta' l_2 \tan \beta l_3 - \tan \beta l_1 \tan \beta l_3 \right) \\ B' &= j \cos \beta l_1 \cos \beta' l_2 \cos \beta l_3 \left(Z_C \tan \beta l_1 + Z'_C \tan \beta' l_2 + Z_C \tan \beta l_3 - \frac{Z_C^2}{Z'_C} \tan \beta l_1 \tan \beta' l_2 \tan \beta l_3 \right) \\ C' &= j \cos \beta l_1 \cos \beta' l_2 \cos \beta l_3 \left(\frac{1}{Z_C} \tan \beta l_1 + \frac{1}{Z'_C} \tan \beta' l_2 + \frac{1}{Z_C} \tan \beta l_3 - \frac{Z'_C}{Z_C} \tan \beta l_1 \tan \beta' l_2 \tan \beta l_3 \right) \\ D' &= \cos \beta l_1 \cos \beta' l_2 \cos \beta l_3 \left(1 - \frac{Z'_C}{Z_C} \tan \beta l_1 \tan \beta' l_2 - \frac{Z_C}{Z'_C} \tan \beta' l_2 \tan \beta l_3 - \tan \beta l_1 \tan \beta l_3 \right) \end{aligned} \quad (2)$$

$$S'_{11} = \frac{A' + \frac{B'}{Z_0} - C'Z_0 - D'}{A' + \frac{B'}{Z_0} + C'Z_0 + D'}, S'_{12} = \frac{2(A'D' - B'C')}{A' + \frac{B'}{Z_0} + C'Z_0 + D'}, S'_{21} = \frac{2}{A' + \frac{B'}{Z_0} + C'Z_0 + D'}, S'_{22} = \frac{-A' + \frac{B'}{Z_0} - C'Z_0 + D'}{A' + \frac{B'}{Z_0} + C'Z_0 + D'} \quad (3)$$

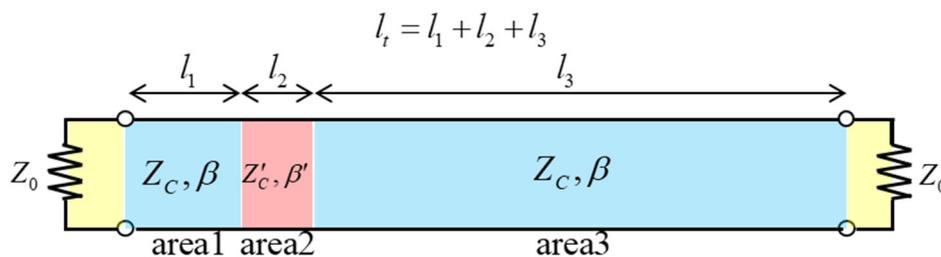


Figure 2. Discontinuous transmission line model. The pink part is introduced for the degraded insulator, and the two sky blue parts are in healthy state.

2.2. Changes in Permittivity of the Transmission Parameter

Equation (4) shows S_{12}^t , which was obtained from Equations (2) and (3) [17]. Assuming Z_C and Z'_C to be real (negligible loss tangent), the phase of S_{12}^t is also described as Equation (5).

$$S_{12}^t = S_{21}^t = \frac{2}{A} \left[\begin{array}{l} \left(2 - \left(\frac{Z_C + Z'_C}{Z'_C + Z_C} \right) \tan \beta l_1 \tan \beta' l_2 - \left(\frac{Z_C + Z'_C}{Z'_C + Z_C} \right) \tan \beta' l_2 \tan \beta l_3 - 2 \tan \beta l_1 \tan \beta l_3 \right) \\ -j \left(\left(\frac{Z_C + Z_0}{Z_0 + Z_C} \right) \tan \beta l_1 + \left(\frac{Z'_C + Z_0}{Z_0 + Z'_C} \right) \tan \beta' l_2 + \left(\frac{Z_C + Z_0}{Z_0 + Z_C} \right) \tan \beta l_3 - \left(\frac{Z_C^2}{Z'_C Z_0} + \frac{Z_0 Z'_C}{Z_C^2} \right) \tan \beta l_1 \tan \beta' l_2 \tan \beta l_3 \right) \end{array} \right] \quad (4)$$

$$\angle S_{12}^t = \arctan \left(\frac{- \left(\left(\frac{Z_C + Z_0}{Z_0 + Z_C} \right) (\tan \beta l_1 + \tan \beta l_3) + \tan \beta' l_2 \left(\left(\frac{Z'_C + Z_0}{Z_0 + Z'_C} \right) - \left(\frac{Z_C^2}{Z'_C Z_0} + \frac{Z_0 Z'_C}{Z_C^2} \right) \tan \beta l_1 \tan \beta l_3 \right) \right)}{2(1 - \tan \beta l_1 \tan \beta l_3) - \left(\frac{Z_C + Z'_C}{Z'_C + Z_C} \right) \tan \beta' l_2 (\tan \beta l_1 + \tan \beta l_3)} \right) \quad (5)$$

Assuming $Z'_C \approx Z_C$, the phase of the transmission parameter could be reduced as Equation (6). Moreover, if $Z_C \approx Z_0$, the phase of S_{21} is linearly decreased as frequency increases as in Equation (7a). For the healthy transmission line only, the phase of S_{21} can be as in Equation (7b). If the characteristic impedance Z_C is not matched to a reference impedance Z_0 , the trace of the phase in S_{21} shows local fluctuations.

$$\angle S_{12}^t = \arctan \left(-\frac{1}{2} \left(\frac{Z_C + Z_0}{Z_0 + Z_C} \right) \tan (\beta l_1 + \beta' l_2 + \beta l_3) \right) \text{ with } Z_0 \ll Z_C \quad (6)$$

$$\angle S_{12}^t = -(\beta l_1 + \beta' l_2 + \beta l_3) \text{ with } Z_0 \approx Z_C \quad (7a)$$

$$\left[\angle S_{12}^t \right]_{\text{healthy}} = -\beta (l_1 + l_2 + l_3) \text{ with } \beta' = \beta \text{ (healthy)} \quad (7b)$$

Equations (7a) and (7b) indicate that phase difference can be monitored with a locally degraded section in the transmission line, which could be used to diagnose the degradation of the solenoid. From the comparison of two phases, the discontinuous factor could be calculated as in Equation (8). Note that we assumed $Z_0 = Z_C$ to calculate the phase difference of the two transmission parameters.

$$\text{phase difference in transmission parameter} = \angle S_{12}^t - \left[\angle S_{12}^t \right]_{\text{healthy}} = -(\beta' - \beta) l_2 \quad (8)$$

2.3. Renormalization Technique of an S-Parameter

From the previous section, we notice that the transmission S-parameter, which is measured with 50 Ω reference impedance, needs to be transformed to the S-parameter referenced for a suitable impedance depending on the device under test. This transformation can be implemented through the renormalization technique, which has been well established in the radio frequency (RF) field, especially for S-parameter reconstruction [18–20].

Figure 3 shows the concept of changing the termination impedance of an S-parameter. Figure 3a shows the S-parameter obtained from the measurement equipment, which is referenced to Z_0 , and Figure 3b shows the renormalized S-parameter when terminated with Z_{new} . Basically, the S-parameter is one of the network parameters, which is dependent on the reference (termination) impedance, but the Z-parameter is not changed by the termination impedance. The relationship between those two parameters is expressed in Equation (9), where G and F are the termination impedance matrix and the real part of them, respectively, and I is the identity matrix. The star is for the conjugate of complex value. In Equation (9a), S is expressed in terms of Z , and Z is expressed in terms of S , in Equation (9b).

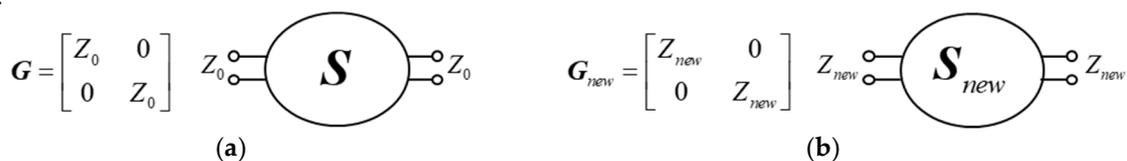


Figure 3. (a) Two-port S-parameter terminated by Z_0 ; (b) The renormalized two-port S-parameter terminated by Z_{new} .

The new S -parameter can also be defined in terms of new G and F as in Equation (10), which comes from Equation (9a). Since the Z -parameter is unique in a given network, Equation (9b) can be plugged into Equation (10), and if we make use of reflection coefficient Γ , Equation (11) can be derived [21].

$$S = F(Z - G^*)(Z + G)^{-1} F^{-1} \quad (9a)$$

$$Z = F^{-1}(I - S)^{-1}(SG + G^*)F, \text{ where } G = \text{diag}\{Z_0\}, \text{ and } F = \text{diag}\left\{\frac{1}{2\sqrt{\text{Re}\{Z_0\}}}\right\} \quad (9b)$$

$$S_{new} = F_{new}(Z - G_{new}^*)(Z + G_{new})^{-1} F_{new}^{-1},$$

where $G_{new} = \text{diag}\{Z_{new}\}$, and $F = \text{diag}\left\{\frac{1}{2\sqrt{\text{Re}\{Z_{new}\}}}\right\}$ (10)

$$S_{new} = F_{new} F^{-1} (I - \Gamma^*)^{-1} (S - \Gamma^*) (I - S)^{-1} (I - S) (I - \Gamma S)^{-1} (I - \Gamma) F F_{new}^{-1},$$

where $\Gamma = (G_{new} - G)(G_{new} + G^*)^{-1}$ (11)

That is, the conversion process of measured S -parameter to the renormalized S -parameter can be obtained using Equation (11). Note that Γ is a diagonal reflection coefficient matrix from Z_0 (G) and Z_{new} (G_{new}). Z_{new} can be selected by the designer as needed. Through this technique, the reference impedance can be matched to the characteristic impedance of the device under test.

3. Fabrication and Measurement Setup for a Prototype of Single-Layered Solenoid

In this chapter, before applying the diagnosis method based on S -parameters for an actual solenoid, a 30-turn single layer solenoid was designed and fabricated. Then, the measurement setup for the prototype solenoid was set, and how to de-embed the interface region between the vector network analyzer (VNA) and the solenoid is described. For mimicking the degraded insulator region in the winding, other additional ring-shaped insulators were introduced between each turn to increase the effective dielectric constant in the solenoid.

3.1. Structure of a Prototype Single-Layered Solenoid

A prototype single-layered solenoid was designed and fabricated to simulate the electrical part of the solenoid valve (winding and metal housing). In order to improve the reproducibility in measurement, a spiral groove was introduced in the bobbin with regular/constant interval so that the shape of the winding could be fixed without moving. The AWG (American wire gauge) 19 magnetic wire (diameter 0.91 mm), which is coated with polyamide-imide (relative permittivity 3.9–5.4, loss tangent 0.05–0.042 at 1 MHz), was used in the winding [22]. The flange and bobbin of the solenoid are made of polyoxymethylene (POM, relative permittivity ~ 3.8 , loss tangent 0.003). The outer structure for the electrical reference and shield was fabricated using aluminum (bulk conductivity 3.8×10^7 Siemens/m).

Detailed geometries of the solenoid with its size are described in Figure 4 and Table 1, respectively. The prototype solenoid has one layer to easily locate the additional ring-type insulators, and the whole solenoid is placed in a metal housing to mimic the real solenoid valve and to also keep the high-frequency signals clean. Figure 4c shows a picture of the manufactured solenoid prototype with RF cables connected at both sides. At both ends of the windings, wires are extended to touch N-type (F) to SMA (F) adaptor, connecting VNA. The yellow dashed lines in Figure 4c indicates the interface part between the solenoid and RF cable, which should be de-embedded for the extraction of solenoid's characteristic from the measurement data.

Table 1. Design parameters of the prototype single-layered solenoid.

Design Parameter	Length (mm)	Description	Design Parameter	Length (mm)	Description
f_h	64.5	flange height	h_h	68.5	housing height
f_w	64.5	flange width	h_w	68.5	housing width
f_t	10	flange thickness	h_l	132	housing length
b_l	64	bobbin length	h_t	2	housing thickness
b_d	40	bobbin diameter	i_l	20	interface length
p	2	pitch of winding	-	-	-

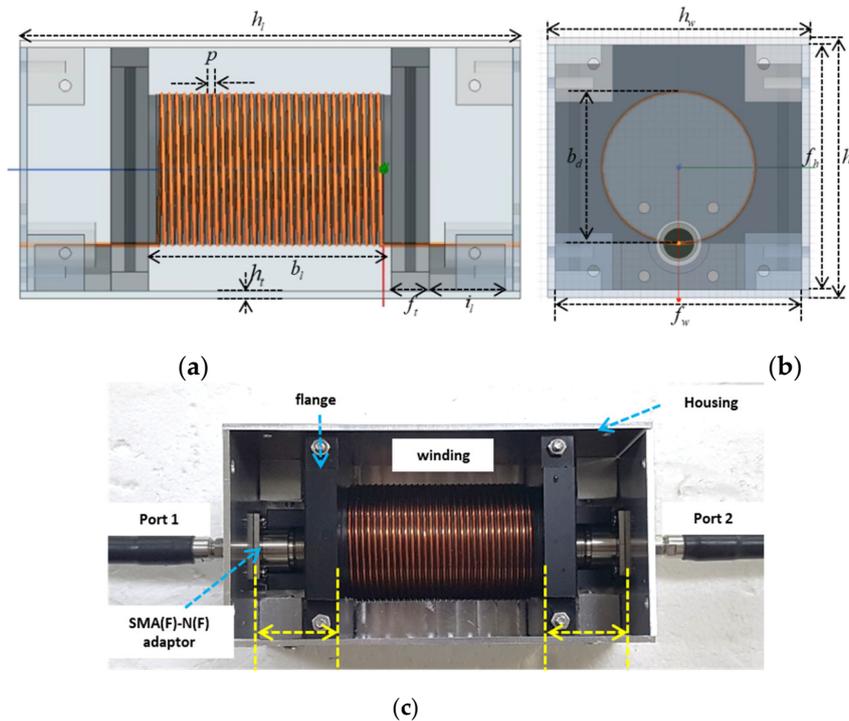


Figure 4. Structure of prototype 30-turn single-layered solenoid. (a) Drawing in front view; (b) Drawing in port side view; (c) A picture from above with radio frequency (RF) cables connected and with upper housing removed.

3.2. Setup for Experimental Measurement and De-Embedding Interfaces

Figure 5a shows the experimental setup for the measurement of S -parameters of the prototype solenoid. The two red dashed lines indicate the electrical reference plane where the VNA is calibrated, and the two-port SOLT (short-open-load-thru) calibration was used for this measurement. The first interface from the solenoid was simplified to be modeled as a single wire above a conducting plane. The second interface to the VNA was modeled as a coaxial cable, as described in Figure 5b. The characteristic impedance of a single wire and coaxial cable can be effectively approximated as in Equations (12) and (13), respectively [23].

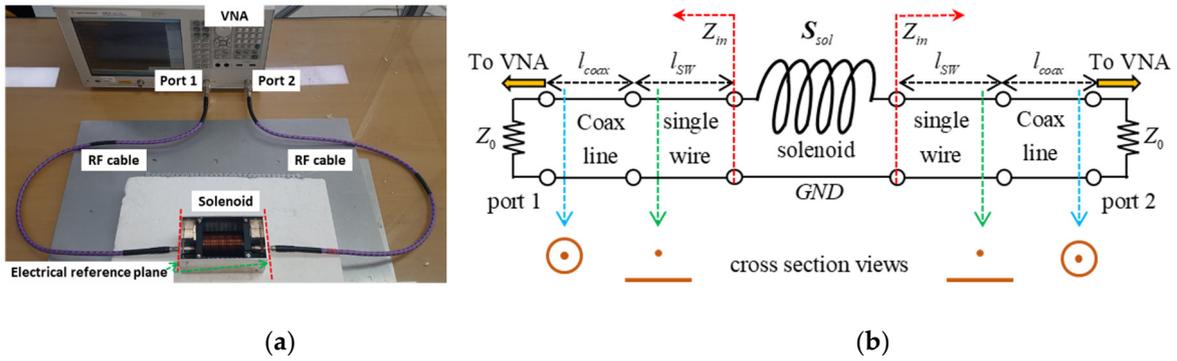


Figure 5. Measurement for prototype solenoid. (a) A picture of the two-port measurement setup with the vector network analyzer (VNA); (b) Interfacing parts to the VNA and its cross-sectional views.

$$Z_{C,SW} = \frac{276}{\sqrt{\epsilon_{eff,SW}}} \log_{10} \frac{2h}{r_{in}} = 231.24\Omega \quad (12)$$

$$Z_{C,coax} = \frac{138}{\sqrt{\epsilon_{eff,coax}}} \log_{10} \frac{r_{out}}{r_{in}} \approx 118.25\Omega \quad (13)$$

where SW represents a single wire on a plane, ϵ_{eff} is the effective permittivity in the background, and h is the height from the reference plane. Applying the physical data ($r_{in} = 0.57$ mm, $r_{out} = 4.1$ mm, $h = 12.25$ mm, $\epsilon_{eff,coax} = 1$, and $\epsilon_{eff,SW} = 2.3$), the characteristic impedance of each part can be calculated. Furthermore, the input impedance toward the VNA, as in Figure 5b [17], can be calculated as in Equation (14).

$$Z_{in} = Z_{C,SW} \frac{Z_0 (Z_{C,coax} - Z_{C,SW} \tan \beta_{SW} l_{SW} \tan \beta_{coax} l_{coax}) + jZ_{C,coax} (Z_{C,coax} \tan \beta_{coax} l_{coax} + Z_{C,SW} \tan \beta_{SW} l_{SW})}{Z_{C,coax} (Z_{C,SW} - Z_{C,coax} \tan \beta_{SW} l_{SW} \tan \beta_{coax} l_{coax}) + jZ_0 (Z_{C,SW} \tan \beta_{coax} l_{coax} + Z_{C,coax} \tan \beta_{SW} l_{SW})} \quad (14)$$

Since the Z_0 in Equation (14) is the reference impedance in the VNA (50Ω), the input impedance Z_{in} can be calculated, of course, and reversely the Z_0 can be calculated for a given input impedance value. If we need to convert Z_{in} into the solenoid impedance, that is, if we need the input impedance Z_{in} to be matched to the solenoid impedance, the new Z_0 can be calculated using Equation (14). Since the measured S -parameter is based on the reference impedance of 50Ω , it can be converted into new S -parameter based on the new Z_0 , which is calculated using Equation (14). In the equation, l_{coax} is 18 mm, and l_{sw} is 14 mm, respectively, and if $Z_{C,coax} = Z_{C,SW} = Z_0$, then we have $Z_{in} = Z_0$, as expected. S_{sol} in Figure 5b represents the de-embedded S -parameter of the solenoid using Equation (14). Keysight’s E5061B model of the vector network analyzer was used for the two-port measurement, and the measurement was performed with 1601 points from 1 kHz to 250 MHz on a linear scale. When measuring the solenoid's S -parameter, the solenoid was enclosed by six sides of the aluminum harness plane for shielding, reducing interference from the outer electromagnetic environment.

3.3. Setup for Mimicking Degraded Insulator in the Prototype Solenoid

It is well known that most of the aging effect of a solenoid comes from dielectric degradation, which leads to an increase of permittivity, loss tangent, and leakage current [24–27]. The exact measurement of a loss tangent and a leakage current, however, usually requires the rated voltage and current at the nominal condition, and the rated voltage and current are large in amplitude, which could damage the electrical device. In this paper, we focus only on how to detect effective permittivity change to diagnose an aging effect in the insulator of a solenoid. One of the advantages of using S -parameter could be to use a few milliwatts in power, which would never damage the solenoid valve.

With a real physically degraded solenoid, one cannot know the exact location and the degree of degradation of the solenoid, which would be necessary to know to check the effectiveness of the

proposed methodology. In this paper, ring-type insulators are installed to increase the effective permittivity of the insulator in which we know a priori the locations and the degree of permittivity change.

In the fabricated solenoid, sheath rubber rings with relative permittivity of 2–3 were employed between the turns in the prototype solenoid. Table 2 shows the number of rings and their locations on the solenoid. For one ring, all of the 31 locations were used one by one, and for two rings, location r_{3-4} , r_{9-10} , r_{15-16} , r_{21-22} , r_{27-28} , $r_{3,29}$ were used for installation, and so on. Note that the last one ($r_{3,29}$) indicates the two rings are separately located at r_3 and r_{29} (the red color in Table 2), while the others are consecutively installed. The number of rings and their locations in Table 2 imply both the level of effective permittivity and the scatteredness of the degradation in the insulator.

Figure 6a shows the cross-sectional views of a solenoid for a healthy condition (left side) and with installed ring-type insulators (right side). And Figure 6b,c shows the two pictures for the ring installation at r_{21} , and r_{20-22} , respectively.

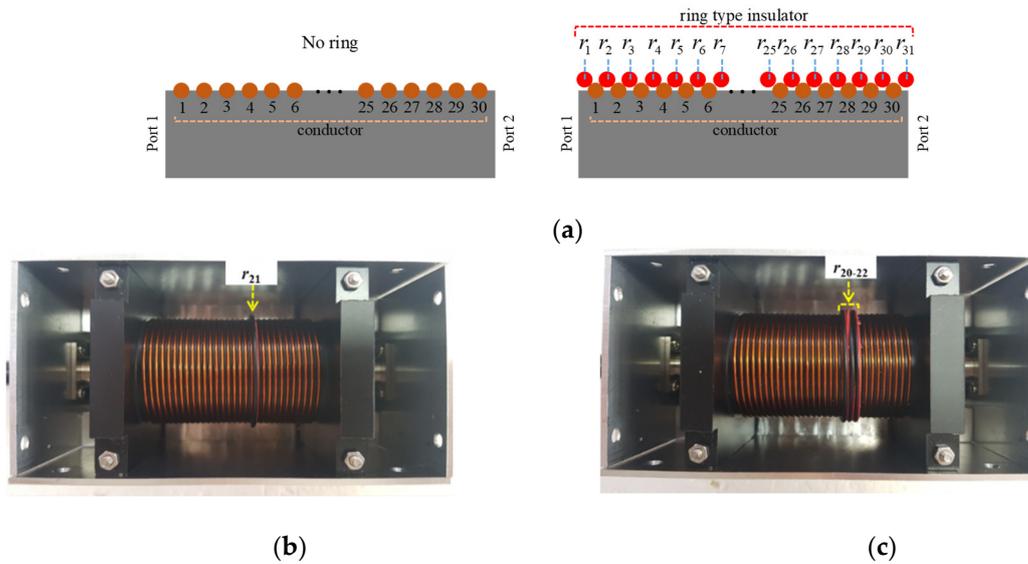


Figure 6. Installation of ring-type insulators on the solenoid. (a) 30 conductor turns and 31-ring insulators are numbered from left and to right. (b) A picture of the solenoid when the 21st ring is installed, (c) A picture of the solenoid when three rings from the 20th to 22nd ring are installed, consecutively.

Table 2. Number and location of sheath rubber rings installed on the solenoid. Rings are separated on the bobbin for the red-colored rings.

No. of Rings	Ring Location	No. of Rings	Ring Location
0	None (healthy)	3	r_{3-5} , r_{9-11} , r_{15-17} , r_{21-23} , r_{27-29} , $r_{3,16,29}$
1	$r_1, r_2, \dots, r_{30}, r_{31}$	4	r_{2-5} , r_{8-11} , r_{14-17} , r_{20-23} , r_{26-29} , $r_{3,11,20,29}$
2	r_{3-4} , r_{9-10} , r_{15-16} , r_{21-22} , r_{27-28} , $r_{3,29}$	5	r_{1-5} , r_{7-11} , r_{13-17} , r_{19-23} , r_{25-29} , $r_{3,8,16,23,29}$

4. Detection of Insulator Degradation in Solenoid Using S-Parameters

In this chapter, we describe how to detect the degradation of the insulator in a solenoid based on the theory in Section 2. The formulas in Section 2 suggest that to transform the reference impedance of the measured S-parameters to the characteristic impedance of the solenoid (if any), and then the phase difference between the S-parameters of the degraded solenoid and the S-parameters of the healthy solenoid could be used to detect the insulator degradation in a solenoid, i.e., Equation (8) for S_{21}/S_{12} .

Since the solenoid is not a transmission line, its characteristic impedance could not be clearly defined but could be represented by a two-port impedance network, as described in Figure 5. To use Equation (8) for detecting the insulator degradation, one needs to find out an appropriate Z_{in} , which

most effectively transfers the signal. Figure 7 describes how to determine the appropriate Z_{in} for the analysis.

Firstly, Z_{in} is set, and then the measured S -parameters are converted with reference to the new $Z_0(Z_{in})$, and the solenoid S -parameters are checked if $S_{sol,12}$ is high enough in the low-frequency range. If $S_{sol,12}$ is high enough, then the final $Z_0(Z_{in})$ to be used is determined.

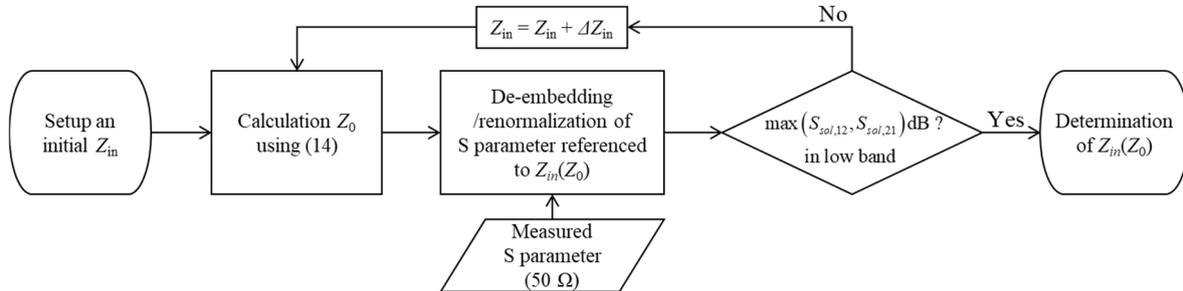


Figure 7. Flow chart for determining $Z_0(Z_{in})$ to effectively renormalize scattering S -parameter for the diagnosis of insulator degradation.

4.1. Quantitative Detection of Insulator Degradation Using Renormalized S -parameters

Figure 8 shows the magnitude and phase of the transmission S -parameter, $S_{sol,12}$, of the single-layered solenoid. One can find that the transmission characteristic has been significantly enhanced with 1500Ω reference impedance as compared with 50Ω reference impedance; for $S_{sol,12}$ with 1500Ω reference impedance, the magnitude increases significantly in the low-frequency range up to ~ 100 MHz, and the phase decreases more linearly than $S_{sol,12}$ with 50Ω reference impedance. This could suggest that the characteristic impedance of the single-layered solenoid would be close to 1500Ω , not to 50Ω in this specific frequency range up to 100 MHz. After ~ 100 MHz, the magnitude of $S_{sol,12}$ decreases more, but the phase keeps linearity up to ~ 250 MHz, as seen in Figure 8b. The $S_{sol,12}$ signals with degraded insulator (51 1–5 rings) are also shown in Figure 8 with 1500Ω reference in various colors. Nevertheless, it is observed that the $S_{sol,12}$ signals are overlapped and become a thick trace, where it is not easy to identify each line. To identify the traces more clearly, the phase difference in $S_{sol,12}$, between the healthy and degraded solenoids, was calculated using Equation (8). Figure 9a shows the phase of $S_{sol,12}$ with 1500Ω reference impedance, which has been wrapped between $-\pi$ and π , and the nine points for the multiples of $-\pi$ are indicated as sky blue colored squares. It can be seen that the curves get thicker as the frequency increases, which means that the differences are getting larger as the frequency increases.

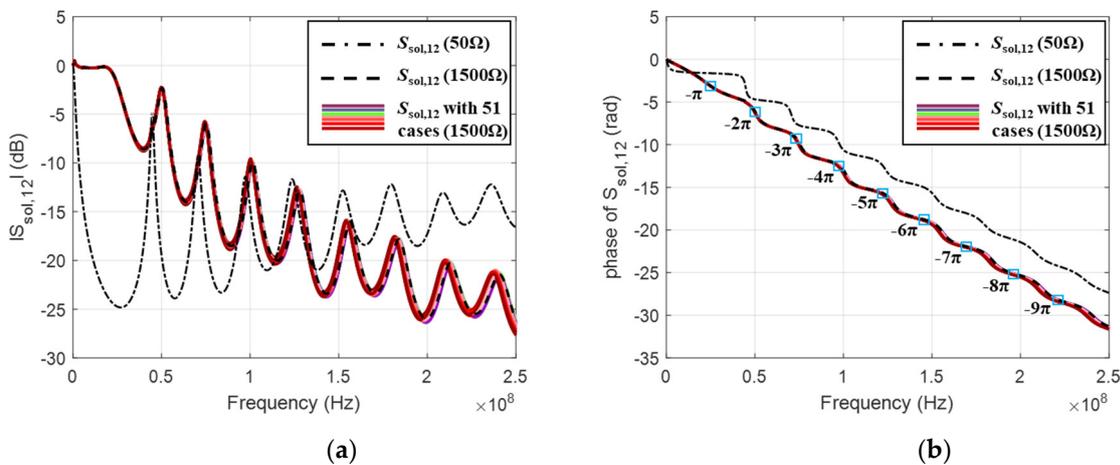


Figure 8. Transmission parameter of one-layered solenoid, $S_{sol,12}$, referenced to 1500Ω and 50Ω . (a) Magnitude; (b) Phase characteristics. Colored traces are for 55 $S_{sol,12}$ data with 1–5 rings installed in the solenoid.

Figure 9b shows an enlargement of the red-dotted box in Figure 9a, and it is clear that with more rings installed, the larger the phase difference becomes. Shown in Figure 9c is the simple difference between the two normalized phases for the healthy and degraded solenoids using Equation (15). Note that the phase has been normalized with respect to ω to minimize the frequency dependence.

$$\text{Normalized } \Delta \angle S_{sol,21} = -\frac{(\beta' - \beta)l_2}{\omega} = -\left(\frac{1}{v'_p} - \frac{1}{v_p}\right)l_2 = -(t'_d - t_d) \quad (s) \quad (15)$$

where v_p is phase velocity, and t_d is delay time due to the degraded section in the solenoid. One can see that the phase differences in Figure 9c are fluctuating even though they are normalized with respect to the frequency, especially at the local nine least peak frequencies. The local nine least peaks actually correspond to the nine sky-blue small boxes in Figures 9a and 8b.

Figure 9d shows an enlargement of the red-colored box in Figure 9c. It is satisfactory to see that the thirty-one one-ring signals do not overlap with the six two-ring signals, which do not again overlap with the six 3-ring signals, which do not again overlap with six four-ring signals, which do not finally overlap with six five-ring signals. Note also that the dotted curves in Figure 9d are for the cases in which the rings are installed on the bobbin in separate turns, not consecutively, as described in Table 2. One can find that each dotted line can be grouped into the appropriate region where the total number of rings are the same. For example, the dotted curve for the two-rings (bright pink dotted curve) is grouped into the region where the five two-rings are located without overlapping with other regions. This means that the insulator degradation in a solenoid can be identified quantitatively by checking the phase difference of the solenoid transmission S-parameter with appropriate renormalization.

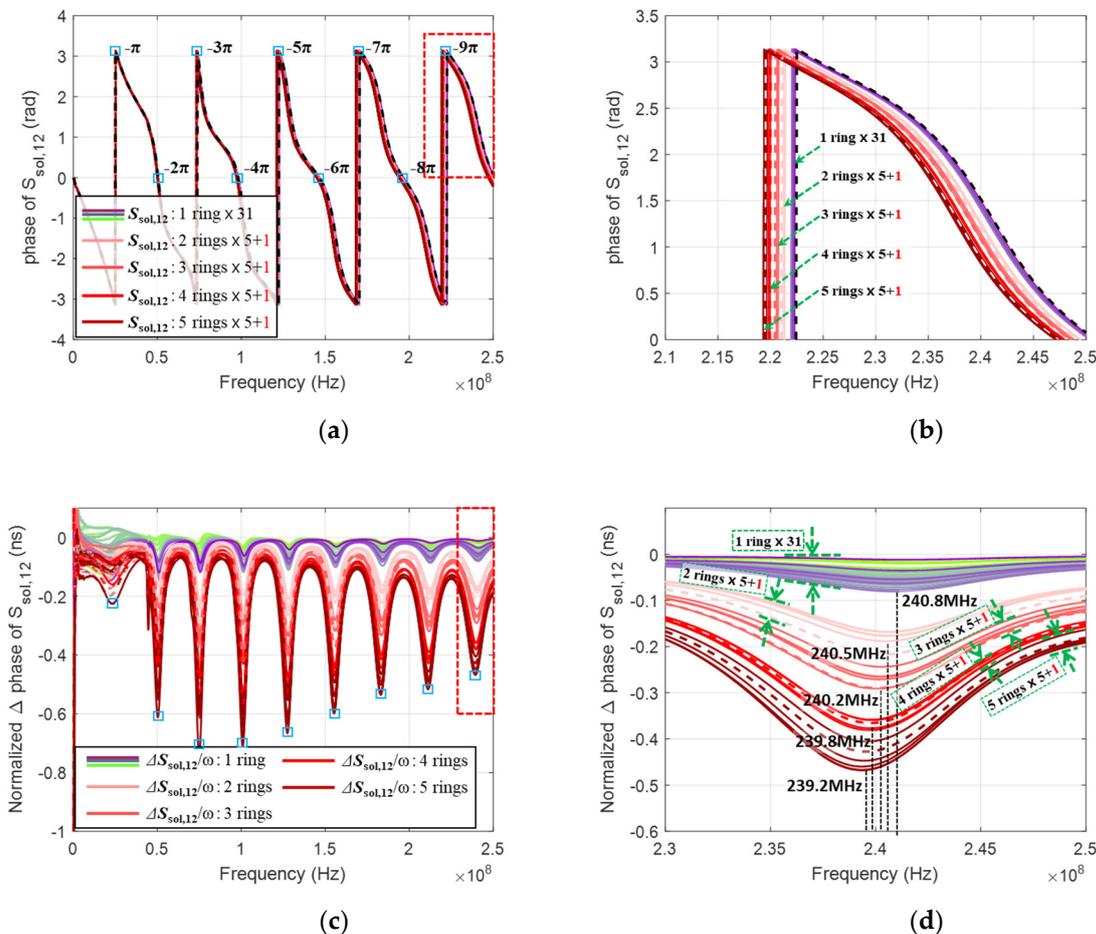


Figure 9. (a) Phase of $S_{sol,12}$ with 1500 Ω reference impedance which has been wrapped between $-\pi$ and π ; (b) An enlargement of the red-dotted box in (a); (c) Normalized phase difference with respect to angular frequency using Equation (15); (d) An enlargement of the red-dotted box in (c).

Note, however, that the least peak frequencies in Figure 9d are different from each other, due to the coefficient term in front of the tangent function in Equation (6). If $Z_c = Z_0$ in front of the tangent function in Equation (6), the least peak frequencies in Figure 9d could have the same values as Equation (6) predicts. Since we are using the measured S-parameters, which are converted into S-parameters with another reference impedance, the coefficient term in front of the tangent function in Equation (6) cannot be deleted in principle. However, we can try to use the phase information only without the coefficient term in front of the tangent function in Equation (6) if we pick up the phase data at multiples of π ($-\pi$: $n = 1-9$). That is, if we make use of the phase data at multiples of π only, the phase of Equation (6) will be zero anyway regardless of the coefficient term in front of the tangent function in Equation (6). It is known that the phase data can be used to calculate the effective permittivity of the insulator, and the effective permittivity in the solenoid can be calculated as Equation (16).

$$\beta l = \sqrt{\epsilon_{eff}} \frac{2\pi f}{c} l, \quad \epsilon_{eff} = \left(\frac{1}{-\angle S_{sol,21}} \frac{c}{2\pi fl} \right)^2 \tag{16}$$

Figure 10a shows averaged effective permittivity data for each group of rings vs. frequency, and the variation seems to be too large to be physically meaningful. To pick up the meaningful data only, we need to use the data at the multiples of π only at the small sky-blue boxes in Figure 10a. The calculated results are summarized in Table 3, and Figure 10b illustrates the calculated effective permittivity at different frequencies, as in the small box inside. The permittivity data can be meaningful, noticing that the effective permittivity increases as the number of rings increases, but still, the data shows some dependence on frequency. The values of the effective permittivity are around 2.6–2.75 after 100 MHz.

The difference of the effective permittivity is shown in Figure 10c as n increases from 1 to 9, and the same data is shown in Figure 10d as the number rings increases. It is good to see that the increment of effective permittivity looks approximately proportional to the number of rings after the 3π . These graphs suggest that the insulator degradation of a solenoid could be quantitatively estimated using the proposed method in this paper. Note that in Figure 10d, n starts from 3, discarding $n = 1$ and 2 data, because of the obscure raw data in the low frequency region, as in Figure 9c.

Table 3. Estimated effective permittivity at the multiples of π as the number of rings increases.

No. of Rings	0 (Healthy)	1	2	3	4	5
ϵ_{eff} at π , f (MHz)	2.503, (25.16)	2.512, (25.16)	2.517, (25.00)	2.519, (25.00)	2.528, (25.00)	2.530, (25.00)
ϵ_{eff} at 2π , f (MHz)	2.484, (50.47)	2.506, (50.47)	2.505, (50.31)	2.527, (50.31)	2.523, (50.16)	2.544, (50.16)
ϵ_{eff} at 3π , f (MHz)	2.608, (73.91)	2.609, (73.75)	2.623, (73.59)	2.630, (73.44)	2.641, (73.28)	2.662, (73.28)
ϵ_{eff} at 4π , f (MHz)	2.625, (98.13)	2.636, (98.13)	2.649, (97.81)	2.661, (97.66)	2.672, (97.34)	2.680, (97.19)
ϵ_{eff} at 5π , f (MHz)	2.643, (122.3)	2.649, (122.2)	2.666, (121.9)	2.678, (121.6)	2.692, (121.3)	2.701, (121.1)
ϵ_{eff} at 6π , f (MHz)	2.654, (146.6)	2.663, (146.3)	2.676, (145.9)	2.688, (145.6)	2.704, (145.2)	2.716, (144.8)
ϵ_{eff} at 7π , f (MHz)	2.673, (170.3)	2.679, (170.2)	2.694, (169.7)	2.709, (169.2)	2.724, (168.8)	2.738, (168.3)
ϵ_{eff} at 8π , f (MHz)	2.622, (196.6)	2.630, (196.3)	2.650, (195.5)	2.658, (195.0)	2.681, (194.4)	2.694, (193.9)
ϵ_{eff} at 9π , f (MHz)	2.590, (222.5)	2.598, (222.2)	2.619, (221.3)	2.634, (220.6)	2.653, (219.8)	2.665, (219.4)

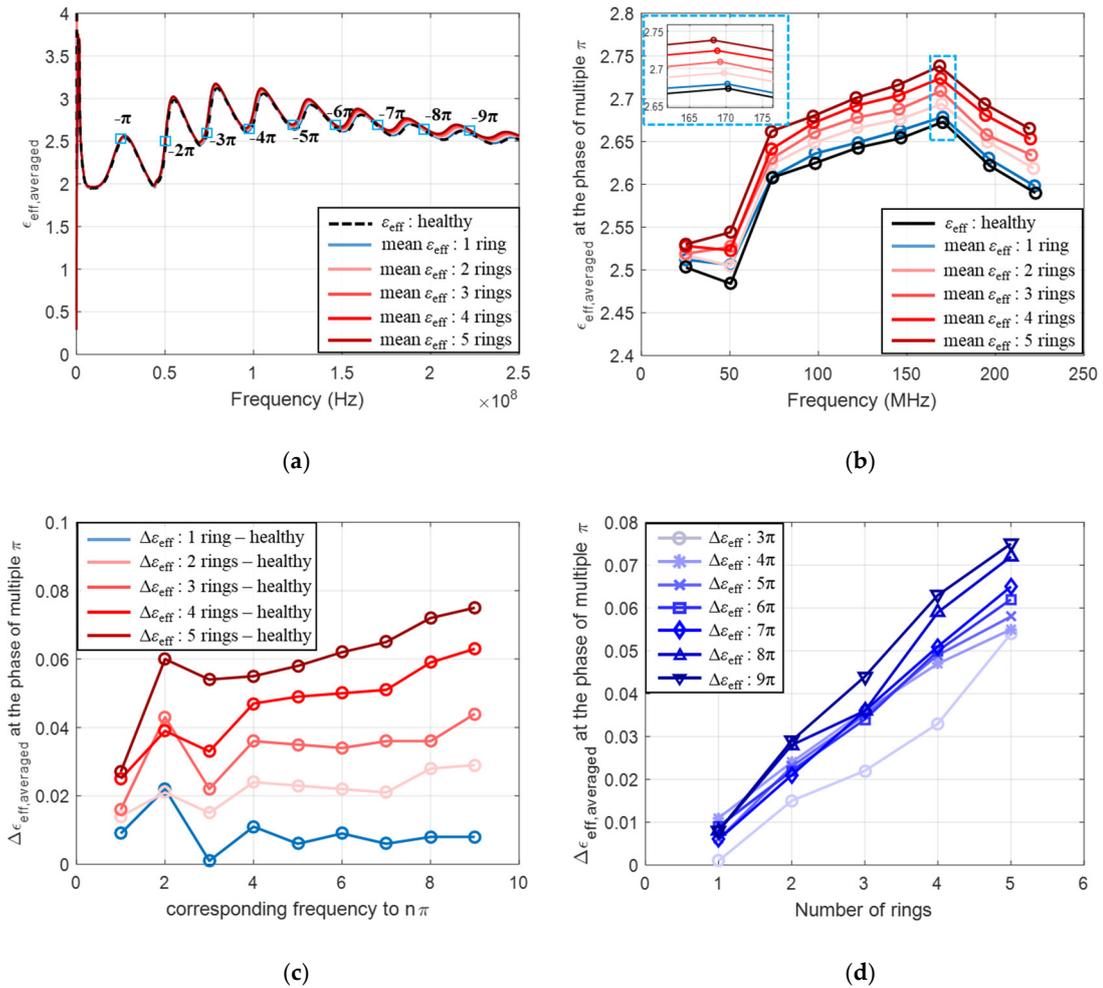


Figure 10. (a) Calculated average effective permittivity for healthy and 1–5 rings installed using Equation (16); (b) Calculated average effective permittivity at the multiples of π ; (c) Incremental (difference) average effective permittivity at the multiples of π ; (d) Incremental (difference) average effective permittivity as the number of rings increases.

5. Conclusions

In this paper, a novel method for quantitative diagnosis of insulator degradation in a solenoid is presented. First, a transmission line with a locally degraded insulator was introduced to estimate the local insulator degradation quantitatively, and it was found in the formulas that the transmission parameter (S_{21}), especially the phase of S_{21} , could be very useful to quantify the degradation in the insulator if the S -parameters are converted into other S -parameters with appropriate reference impedance using a renormalization technique.

For validation of a suggested idea, a single-layer solenoid with thirty turns was designed and fabricated. This prototype simulated the electrical part of a solenoid valve in the winding and housing as well. A two-port S -parameter measurement was set up, and additional sheath rubber rings were introduced to mimic the insulator degradation in the winding. The interface between measurement equipment and prototype solenoid was de-embedded, and the renormalization of S -parameters was conducted by choosing an appropriate reference impedance, which was about 1500 Ω in this specific case.

The phase difference of the renormalized S_{21} between healthy and degraded (with rings installed) solenoids showed clear classification into five groups (one–five rings), demonstrating the usefulness of the proposed method to quantify the degradation of the insulator. Furthermore, the increment of

effective permittivity data (the difference from the healthy solenoid and the solenoid with rings installed) at multiple π clearly showed proportionality as the number of the rings increased.

This paper verified that the changes of an electrical characteristic caused by insulator degradation in a solenoid could be successfully quantified by the normalized phase difference and by the increment of effective permittivity of a solenoid using the renormalized transmission parameter (S_{21}). We believe that the proposed method can be used for any solenoid valve to evaluate the degradation in the insulator part, including SOVs in NPP in an overhaul period. For the next step, the proposed method needs to be repeated for physically degraded solenoids. It is concluded that the suggested method would be very promising to quantitatively diagnose future degradation of a solenoid.

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Abbreviations

AWG	American Wire Gauge
GW(e)	Gigawatt electrical
IAEA	International Atomic Energy Agency
NPP	Nuclear power plant
RF	Radio frequency
S-parameters	Scattering parameters
S_{11} parameters	Input port voltage reflection coefficient in two-port network
S_{12} parameters	Reverse voltage gain in two-port network
S_{21} parameters	Forward voltage gain in two-port network
S_{22} parameters	Output port voltage reflection coefficient in two-port network
SOLT	Short-open-load-thru
SOV	Solenoid operated valve
VNA	Vector network analyzer
Z_c	Characteristic impedance of the transmission line
Z_0	Reference impedance of the ports
Z_{in}	Input impedance from the end of solenoid to port
β	Propagation constant of the transmission line
ϵ_{eff}	Effective permittivity
Γ	Matrix of the reflection coefficient from each port
t_d	Delay time
v_p	Phase velocity

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