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A Multiple-Sensor Fault-Tolerant Control of a Single-Phase Pulse-Width Modulated Rectifier Based on MRAS and GPI Observers

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Abstract: Due to their advantages in ensuring low harmonic distortion and high power factors, single-phase Pulse-Width Modulated (PWM) rectifiers are widely employed in several industrial applications. Generally, the conventional control loop of a single-phase PWM rectifier uses both voltage and current sensors. Hence, in case of sensor fault, the performance and the availability of the converter can be seriously compromised. Therefore, diagnosis approaches and fault-tolerant control (FTC) strategies are mandatory to monitor these systems. Accordingly, this paper introduces a novel multiple-sensor FTC scheme for a single-phase PWM rectifier. The proposed fault diagnosis approach relies on joining several Generalized Proportional Integral (GPI) and Model Reference Adaptive System (MRAS) observers with a residual generation technique to detect and isolate sensor faults in a simple and reliable manner. While conventional sensor FTC methods dedicated to PWM rectifiers can only deal with single faults, the suggested approach guarantees a very good effectiveness level of sensor fault detection, isolation (FDI) and FTC of multiple-sensor fault occurrence scenarios. Consequently, the single-phase PWM rectifier can work with only the survivable single sensor with the guarantee of very good performance as in healthy operation mode. The effectiveness of the proposed sensor FDI approach and its control reconfiguration performance are demonstrated through both extensive simulation and experimental results.

Keywords: single-phase pulse-width modulated rectifier; sensor fault detection; fault-tolerant control; observers; GPIO; MRAS



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1. Introduction

In recent years, Pulse-Width Modulation (PWM) Rectifiers have arisen as one of the most important components in various industrial applications such as renewable energy [1–3], EVs [4,5], electric traction [6–8], and so on. They ensure several advantages such as sinusoidal input currents, stable DC-Link voltage and unit power factor [9,10].

For such applications, downtimes caused by different types of failures have a direct impact on the productivity of the system as well as on production costs. Hence, ensuring reliability is becoming an issue of utmost importance. The overall components of the system should be monitored to avoid any possibility of performance degradation due to faults. According to this understanding, fault-tolerant control policies are currently needed more than ever to ensure the system functioning even under fault occurrence.

During the last years, fault diagnosis and fault tolerance of PWM rectifiers have been important research topics that still present challenges, as addressed by several recent publications [11–33]. Apart from failures occurring in the power semiconductors [11–14], a grid-connected voltage source converter is also sensitive to failures in the sensors that

provide vital information used by the main control system. In this context, the continuity of service of the system depends intimately on the availability of reliable measurements.

Regarding sensor FDI and FTC issues in single-phase grid-connected converters, several studies have been conducted. State observers have been investigated for a robust sensor fault-tolerant control of single-phase PWM rectifiers [15–19]. In [15], a Luenberger observer (LO)-based FDI is presented to allow DC-link and grid current sensors fault tolerance. After fault detection and isolation, the fault reconfiguration procedure is based on an open-loop state estimator. The stability and robustness of the observer during parameter variation are verified. Poon et al. [16] addressed a model-based state estimator general FDI approach that can be used to diagnose and identify faults in components and sensors in switching power converters. In [17], an open-loop state estimator is developed for the detection of grid current and DC-link voltage sensors for a single-phase grid-connected PWM rectifier. Scaling and offset and drift fault detection have been investigated. However, the proposed approach may be sensitive to the system's parameters' mismatch. Unknown input observers for sensor fault detection and localization are presented in [18]. A reduced-order observer-based resilient control for single- or multiple-sensor faults for cascaded H-bridge multilevel converters is provided in [19]. Grid current and DC-link voltage sensor faults are considered, and five types of faults for each sensor are investigated.

Xia et al. [20] proposed a sliding-mode observer (SMO)-based algorithm for the fault detection and fault reconfiguration of catenary current and DC-link voltage sensor faults of a single-phase PWM rectifier for electric traction applications considering unipolar and bipolar modulation methods. A similar approach is discussed in [21], where the sliding-mode observer design is improved by considering the DC load current as an unknown input of the observer. In [22], an incipient voltage sensor fault isolation method is developed for a single-phase three-level rectifier. A bank of sliding-mode and adaptive estimators was designed in order to isolate different DC-link voltage sensor fault modes. However, only FDI is discussed, and the FTC is not presented. An interval estimator and a sliding-mode estimator have been designed in [23]. The proposed estimator was used for an incipient sensor fault detection method for a class of nonlinear control systems with observer-unmatched uncertainties. The voltage and current sensor fault-tolerant control of the LC branch in the active power decoupling single-phase PWM converter through SMO are discussed in [24]. In [25], a robust control strategy for a three-phase grid-tied inverter with an LCL filter under grid voltage and grid current sensor faults is presented. A quadrature filter of a dual second-order generalized integrator (DSOGI) architecture is used for the grid current estimation. An internal model-based estimator is proposed for grid voltage estimation. A fault-tolerant space-vector hysteresis current control for a three-phase grid-connected converter is discussed in [26]. The analytical redundancy introduced by the use of three measurements allows the continuous work of the system. The parity space equations and virtual flux estimation have been discussed to ensure grid voltage sensor fault tolerance in [28], whereas a hybrid model-based and data-driven method is proposed for the grid current sensor fault-tolerant control [29].

In addition to residual generation-based FDI approaches, fault estimation (FE)-based approaches have gained more and more interest during the last years [30–32]. A state observer fault estimation to compensate for DC-link voltage and catenary current sensor faults for a single-phase two-level PWM rectifier in a high-speed railway electric traction system has been proposed in [30]. In [31], a grid current sensor fault estimation and compensation for a grid voltage sensorless single-phase grid-connected converter using proportional integral observers is described. A robust grid voltage sensor FE based on an unknown input observer with disturbances decoupling is addressed in [32].

The state-of-the-art review has shown that the research field of sensor FTC in electrical power converters is still very attractive with many challenging issues. Recently, more attention has been paid to the use of data-driven approaches for fault diagnosis purposes. In [33], a just-in-time learning (JITL) and modular Bayesian network (MBN) is proposed to diagnose sensor faults in a high-speed electric railway traction application, whereas

the time series feature patterns of a single-phase PWM rectifier are employed to identify several types of faults such as the following: traction transformer faults, traction converter faults, main grid poor contact or inrush current [34]. Zhu et al. [35] presented an automatic crack damage diagnosis in hydraulic structures by combining computer vision and artificial intelligence. Long short-term memory networks and phase space reconstruction are used for the prediction of a dam deformation [36]. Data-driven-based methods are of great interest for fault diagnosis or predictive maintenance purposes. Nevertheless, they are still not able to handle the fault tolerance step, and the use of estimators/observers is very useful for the continuous operation of the system under sensor faults. In this way, model-based and signal-based methods are still very welcomed to ensure reliable and effective sensor fault tolerance [37].

Moreover, multiple-sensor fault-tolerant control is becoming an attractive research topic but is still limited to three-phase induction motor drives [38] or PMSM drives [39]. The single-phase PWM rectifier's control requires mainly three sensors [15]: one grid voltage sensor, one grid current sensor and a DC-link voltage sensor, as depicted in Figure 1. The state-of-the-art review demonstrates that the previously proposed sensor FTC methods are focused on single-sensor faults only, in particular on the grid current sensor and the DC-link voltage sensor. Indeed, the design of an FTC approach that takes into account the faults in the three sensors has not received much research attention yet. To the best knowledge of the authors, very few contributions have discussed multiple-sensor fault tolerance of a single-phase PWM rectifier [19]. On the other hand, the proposed FTC methods provided by the literature need accurate knowledge of the load current [15,20,30]. Hence, a load current sensor [15] or a load current observer [24] is mandatory, which may increase the system's cost and the FTC algorithm complexity. In this context, a robust sensor FDI and FTC approach focused on the three sensors of the PWM rectifier and able to tolerate multiple-sensor faults is of great significance and may considerably contribute to improving the availability and safety operation of the studied system.

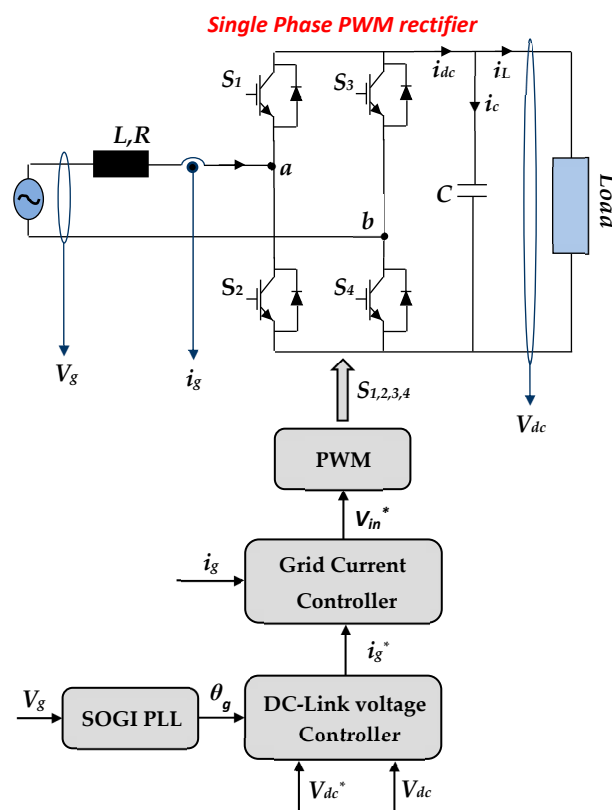


Figure 1. Single-phase PWM rectifier: Converter Topology and its multiloop control scheme.

To address the problem of multiple-sensor fault-tolerant control for single-phase PWM rectifiers, this paper proposes a new structure that aims to ensure a simple, reliable and robust single- and multiple-sensor fault detection and fault-tolerant control of a single-phase PWM rectifier. The main features and contributions of this work are:

- (1) The proposed method is capable of tolerating single- or multiple-sensor faults, and the rectifier's control loop can be driven by the single survivable sensor. For this purpose, two multiple-sensor fault-tolerant controls are investigated. In the first scenario, a DC-link voltage sensor fault followed by a grid voltage sensor fault is discussed. In the second scenario, a DC-link voltage sensor fault followed by a grid current sensor fault is investigated.
- (2) For this purpose, a residual generation-based FDI approach is presented. Hence, a bank of two Generalized Proportional Integral Observers (GPIO) and one Model Reference Adaptive System (MRAS) observer are developed in order to accurately estimate the grid voltage, the DC-link voltage and the grid current, respectively. Once the residual exceeds its corresponding threshold, a fault flag switches from 0 to 1 and the faulty sensor is identified. Thereafter, the faulty measurement is substituted by the virtual sensor into the rectifier's control loop, to guarantee the continuous work of the rectifier.
- (3) The proposed FTC approach does not need any additional sensors, in particular load current sensors. Hence, in this work, the load current is considered as an unknown disturbance. It should not have any impact on the performance of the proposed FTC approach, neither in healthy operation nor during sensor post-fault operation of the system. Moreover, the system's parameters' mismatch, including grid-side filter inductor and DC-link capacitance, does not affect the robustness of the proposed method.
- (4) During sensor post-fault operation, the proposed FTC method allows the start-up of the process with the single survivable sensor with good accuracy and the same performance of the closed-loop control as in healthy operation mode.
- (5) The effectiveness of the proposed method is demonstrated through extensive simulation and experimental studies. The proposed FDI/FTC approach can be deployed on the commonly used digital controllers, improving the cost and the performance of real-time control of single-phase PWM converters in several industrial applications.

The paper is organized as follows: First, in Section 2, the single-phase PWM rectifier model and its control strategy are presented. Section 3 is devoted to analyzing the design of the different GPI and MRAS observers. FDI and FTC techniques are discussed in Section 4. Simulation results are carried out in Section 5. The experimental validation of the proposed FDI and FTC algorithm is discussed in Section 6. Finally, the paper is summed up in a conclusion in Section 7.

2. Mathematical Model of the Single-Phase PWM Rectifier and Control Strategy

The system under study and its control strategy are presented in Figure 1. The single-phase PWM rectifier can be modelled using the following equations:

$$\begin{cases} V_g = Ri_g + L \frac{di_g}{dt} + V_{ab} \\ i_c = i_{dc} + i_L = C \frac{dV_{dc}}{dt} \\ V_{ab} = (S_1 - S_3)V_{dc} \\ i_{dc} = (S_1 - S_3)i_g \end{cases} \quad (1)$$

where i_g is the grid current, V_g the grid voltage, V_{ab} is the rectifier input voltage, V_{dc} is the DC-link voltage, i_{dc} is the DC-side output current, i_c is the current in the DC-side capacitor, i_L is the load current and S_1 and S_3 are the binary switching control signal. x^* corresponds to the reference of the variable x . L denotes a filter used for the connection with the grid, R is its internal resistance, and C is the DC-link capacitor. The single-phase PWM rectifier provides a high-energy quality: unity power factor, energy bi-directionality, a sinusoidal

form of the grid current and a continuous and constant DC-link voltage. The loop control of the single-phase PWM rectifier is composed of:

- DC-Link Voltage Control Loop: The main purpose of the DC-link voltage loop is to maintain this voltage at a constant reference value. The voltage control loop is based on a PI controller due to its simplicity, easy implementation and good regulation results of DC quantities.
- PR-Based Grid Current Control: The grid current controller allows i_g to track its reference i_g^* with good accuracy. For this purpose, a proportional resonant (PR) controller is employed [15].
- SOGI-PLL-Based Grid Synchronization: To ensure grid-side unity power factor, the phase angle of the grid current i_g should be synchronized with the grid voltage V_g . Different synchronization techniques are presented in the literature [40]. Among these, the second-order generalized integrator-based phase-locked loop (SOGI-PLL) is an effective approach due to its fast dynamic response and high filtering capacity [15].

3. Design of GPIO and MRAS Observers

In this paper, two generalized proportional integral observers (GPIO) are designed to estimate the grid voltage V_g and the DC-link voltage V_{dc} , respectively. In the same way, a model reference adaptive system (MRAS) observer is employed to estimate the grid current i_g .

From (1), the dynamics of the single-phase PWM rectifier are described by:

$$\begin{cases} \frac{d}{dt} \begin{pmatrix} i_g \\ V_{dc} \end{pmatrix} = \begin{pmatrix} -\frac{R}{L} & -\frac{S_{13}}{L} \\ \frac{S_{13}}{C} & 0 \end{pmatrix} \begin{pmatrix} i_g \\ V_{dc} \end{pmatrix} + \begin{pmatrix} \frac{1}{L} \\ 0 \end{pmatrix} V_g + \begin{pmatrix} 0 \\ \frac{-1}{C} \end{pmatrix} i_L \\ y = \begin{pmatrix} 1 & 0 \\ 0 & 1 \end{pmatrix} \begin{pmatrix} i_g \\ V_{dc} \end{pmatrix} \\ S_{13} = S_1 - S_3 \end{cases} \quad (2)$$

It can be seen from (2) that the state matrix contains the discrete switching control signal S_{13} . For unipolar sinusoidal PWM, S_{13} has three possible states during one switching period: ± 1 and 0. So, changes in S_{13} may affect the performance and the convergence of the observer [19,21]. In order to overcome this issue, the switching control signals S_1 and S_3 may be replaced by their respective duty cycles d_1 and d_3 . During one switching period, the voltage V_{ab} may be expressed as follows:

$$V_{ab}(t) = (d_1 - d_3)V_{dc}(t) = d_{13}V_{dc}(t), kT_s < t \leq (k+1)T_s \quad (3)$$

Since the switching frequency (10 kHz) is much larger than the grid voltage frequency (50 Hz), then the duty cycle d_{13} is considered as a constant in one switching period T_s . Finally, d_{13} is a continuously varying parameter instead of a discrete parameter S_{13} . Furthermore, neglecting high-frequency components, d_{13} may be considered the fundamental component of S_{13} , and V_{ab} can be expressed as:

$$V_{ab}(t) = m_{ab}V_{dc} \sin(\theta_g + \varphi_{ab}) \quad (4)$$

where m_{ab} corresponds to the modulation index, and φ_{ab} is the phase difference with respect to the grid voltage. Finally, a corresponding equivalent circuit of the grid-side loop of Figure 1 is presented in Figure 2.

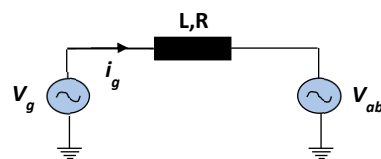


Figure 2. Equivalent Structure of the single-phase PWM rectifier.

The grid current state model is described by:

$$\frac{di_g}{dt} = Ai_g + B(V_g - V_{ab}) \quad (5)$$

where $A = -R/L$ and $B = 1/L$.

3.1. Grid Voltage GPI Observer Design

In this section, a first GPI observer is designed for observing the grid voltage V_g . Generalized proportional integral observers use not only the estimation error information but also the integral of the estimation error, which makes them useful for the estimation of system disturbances and unknown inputs [41,42].

The structure of the GPIO applied to the grid current state Equation (5) is depicted in Figure 3. The variable f_a corresponds to the disturbance and/or unknown input that the GPIO aims to estimate.

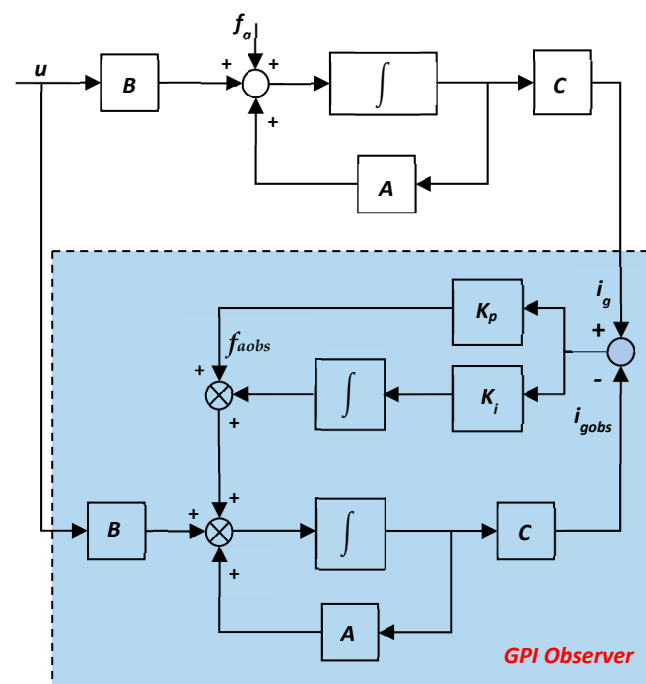


Figure 3. Structure of the GPI Observer.

In order to analyze the system dynamics, the output of the integrator is extended to a new state variable f_a , which denotes the system unknown input and is described by:

$$f_a = \frac{V_g}{L} \quad (6)$$

The structure of the GPIO applied to the grid current state Equation (5) is depicted in Figure 3, where the dynamics of the observer are described by:

$$\frac{d}{dt} \begin{pmatrix} i_{gobs} \\ f_{aobs} \end{pmatrix} = \begin{pmatrix} A & 1 \\ 0 & 0 \end{pmatrix} \begin{pmatrix} i_{gobs} \\ f_{aobs} \end{pmatrix} + \begin{pmatrix} B \\ 0 \end{pmatrix} u + \begin{pmatrix} K_{p1} \\ K_{i1} \end{pmatrix} (i_g - i_{gobs}) \quad (7)$$

where K_{p1} and K_{i1} are the observer's proportional and integral gains, respectively. The variable f_{aobs} is the estimated value of the unknown input f_a , and it corresponds to the integral of the estimation error ($i_g - i_{gobs}$). According to (6) and (7), if the grid voltage is estimated by the GPI observer, $u = -V_{ab}$ and then:

$$f_{aobs} = \frac{V_{gobs}}{L} \quad (8)$$

3.2. Observer Stability Analysis

The error model of the proposed observer is obtained for stability analysis, and the estimation errors of the state variables defined in (7) are given by:

$$e_i = i_g - i_{gobs} \quad \text{and} \quad e_f = f_a - f_{aobs} \quad (9)$$

Consequently, the state error equation is given by the following [43]:

$$\frac{d}{dt} \begin{pmatrix} e_i \\ e_f \end{pmatrix} = \begin{pmatrix} A - K_{p1} & 1 \\ -K_{i1} & 0 \end{pmatrix} \begin{pmatrix} e_i \\ e_f \end{pmatrix} + \begin{pmatrix} 0 \\ \frac{df_a}{dt} \end{pmatrix} \quad (10)$$

From (10), it is observed that the system will be Hurwitz stable if both of the characteristic polynomial's roots in the matrix D_c , i.e., are in the left half-plane [43].

$$F_1(s) = s^2 + \left(\frac{R}{L} + K_{p1} \right) s + K_{i1} \quad (11)$$

In order to simplify the design process, we assume that both observer's poles are located at $-w_0$ and are expressed by:

$$F_1(s) = s^2 + \left(\frac{R}{L} + k_{p1} \right) s + k_{i1} = (s + w_0)^2 \quad (12)$$

Therefore:

$$\left(\frac{R}{L} + K_{p1} \right) = 2w_0 \quad \text{and} \quad k_{i1} = w_0^2$$

From (12), it is shown that the design of $\frac{R}{L} + K_{p1}$ and K_{i1} is related to the GPI observer's bandwidth w_0 . Hence, the key process is the appropriate bandwidth value w_0 selection. The observer's bandwidth is generally selected to be 5–15 times lower than the switching frequency by considering the tradeoff between the fast observation performance and the noise sensitivity immunity [44]. In this paper, the observer bandwidth is selected around 1 kHz, which is 10 times lower than the switching frequency.

In Figure 4, the root locus of the PI observer with grid inductance L as a variable value is shown. It can be seen that the root locus remains on the left side of the s-plan, and the stability of the observer is guaranteed.

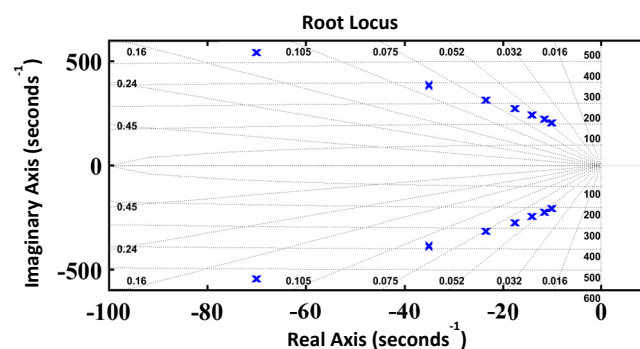


Figure 4. Root locus plot of the grid voltage GPIO with L as a variable value.

3.3. DC-Link Voltage Estimation Based on SOGI-GPIO

Similarly, a second GPIO is used to estimate the DC-link voltage V_{dc} . The DC-link voltage estimation is achieved in two steps. First, the fundamental component of the rectifier's input voltage V_{ab} is estimated through the GPIO. The proposed GPIO structure is similar to the observer used to estimate the grid voltage. Consequently, V_{ab} is considered as an unknown input of the system described by (5) and, therefore, $f_a = -V_{ab}/L$. According

to (7), if V_{ab} is estimated by the GPI observer, $u = V_g$, and the estimated unknown input is expressed as:

$$f_{aobs} = \frac{V_{abobs}}{L} \quad (13)$$

Since the dynamics of the GPIO of V_{ab} are similar to the observer of the grid voltage V_g , then the stability of the observer is guaranteed by the appropriate choice of its proportional and integral parameters K_{p2} and K_{i2} , respectively.

Once the input rectifier voltage is estimated, a SOGI block is used to generate its estimated orthogonal components $V_{ab\alpha-obs}$ and $V_{ab\beta-obs}$ of V_{abobs} , then the estimated value of the DC-link voltage V_{dcobs} is obtained, as presented in Figure 5.

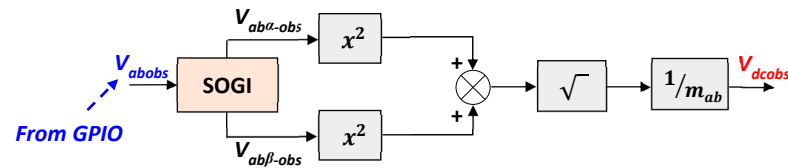


Figure 5. Structure of the SOGI-based DC-Link voltage estimator.

3.4. Virtual Flux MRAS-Based Grid Current Estimation

The MRAS observer main design concept is based on the use of a reference model and an adaptive model. The idea is to use a correction/adaptation mechanism so that the output of the adaptive model is adjusted to the reference model [45].

Recently, the MRAS observer has been successfully used for grid-connected power converters applications to estimate AC voltages [46] or grid-side impedance parameters [47].

The grid current estimation is based on a grid virtual-flux-based MRAS observer. Its structure is depicted in Figure 6a.

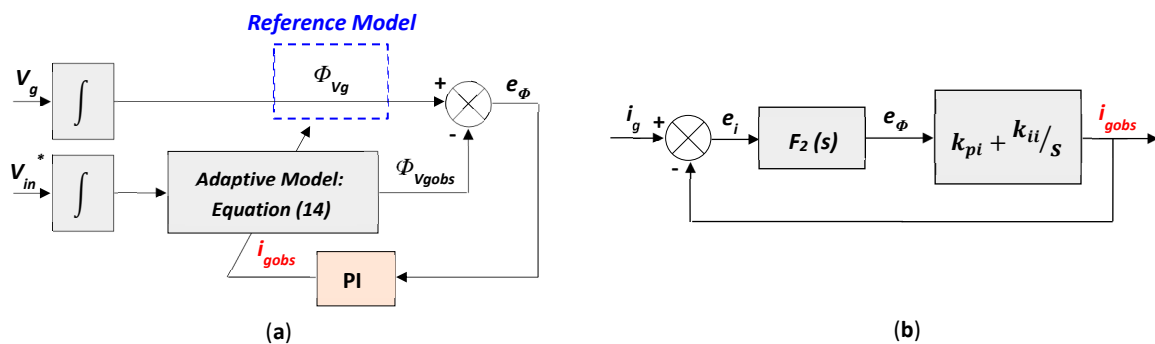


Figure 6. MRAS-based estimator: (a) MRAS-based grid current estimator's structure; (b) Equivalent block diagram of the MRAS estimator.

The reference model of the MRAS observer is the virtual flux Φ_{Vg} , which can be obtained from the grid voltage measurement. The adaptive model aims to generate the estimated virtual flux value Φ_{Vgobs} , expressed as follows:

$$\begin{cases} \phi_{Vg} = \int V_g dt = \int V_{ab} dt + R \int i_g dt + L i_g \\ \phi_{Vgobs} = \int V_{in}^* dt + R \int i_g dt + L i_g \end{cases} \quad (14)$$

The estimation errors are given by:

$$e_\phi = \phi_{Vg} - \phi_{Vgobs} = \left(\frac{R}{s} + L \right) (i_g - i_{gobs}) = \left(\frac{R}{s} + L \right) e_i = F_2(s) e_i \quad (15)$$

The virtual flux estimation error is used to drive a suitable adaptation mechanism which generates the estimated grid current for the adaptive model.

Therefore, a PI corrector is sufficient, and i_{gobs} is given by:

$$i_{gobs} = \left(k_p + \frac{k_i}{s} \right) e_\phi \quad (16)$$

Figure 7 shows the root locus of the closed-loop transfer function, presented in Figure 6b, of the MRAS estimator for the grid current with the grid inductance L filter variations. One can clearly deduce the estimator's stability, since, for all inductance values, the root locus remains on the left side of the s-plan.

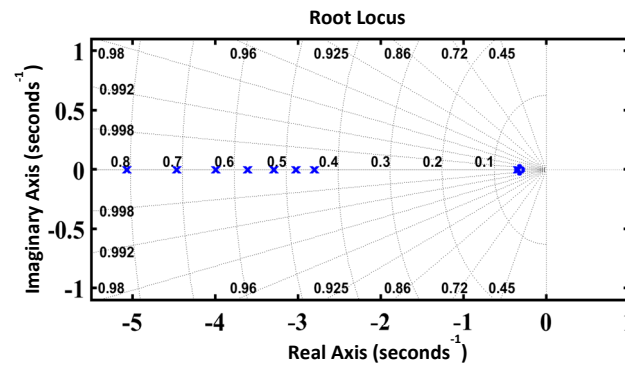


Figure 7. Root locus plot of the grid current MRAS estimator with L as a variable value.

4. Proposed Sensor FDI and FTC Strategy

The control strategy of the single-phase PWM rectifier requires accurate and exact measurements of the grid voltage V_g , the grid current i_g and the DC-link voltage V_{dc} . In case of erroneous measurements, the converter's performance would be seriously perturbed [15]. The overall structure of the proposed multiple-sensor FDI and FTC algorithm is illustrated in Figure 8, while the flowchart of the proposed multiple-sensor fault-tolerant control is depicted in Figure 9. As illustrated by Figure 8a, once the estimated state information is obtained through the GPIOs and MRAS observers, they are compared to the measured information in order to generate the desired residuals. To reduce the impact of the load charge variation and/or system's parameters' mismatch on the fault detection process, all residuals are defined as normalized quantities and expressed as:

$$R_{V_g} = \frac{|V_g - V_{gobs}|}{V_{gnom}}, \quad R_{V_{dc}} = \frac{|V_{dc} - V_{dcobs}|}{V_{dc}^*}, \quad R_{i_g} = \frac{|i_g - i_{gobs}|}{i_{gnom}} \quad (17)$$

where V_{gnom} and i_{gnom} represent the rated values of V_g and i_g , respectively. The detection of the sensor fault is achieved by comparing each residual R_x ($x = i_g, V_{dc}, V_g$) to a corresponding threshold, T_x ($x = i_g, V_{dc}, V_g$). The robustness of the FDI algorithm depends precisely on the residuals' sensitivity to the system's parameters and operating point variations. In healthy mode, all residuals should maintain low values (close to zero) below their corresponding thresholds. However, in faulty operating mode, only the residual corresponding to the faulty sensor exceeds its threshold, while all residuals related to healthy sensors remain below their specified thresholds. Hence, the choice of the thresholds should be carefully made taking into account all system variations to minimize false alarms and increase the FDI algorithm robustness while maintaining a fast detection time. Thus, the fault is detected, and the faulty sensor is isolated when the corresponding fault flag F_x ($x = i_g, V_{dc}, V_g$) is generated:

$$F_x = \begin{cases} 1, & \text{if } R_x > T_x \\ 0, & \text{if } R_x < T_x \end{cases} \quad (18)$$

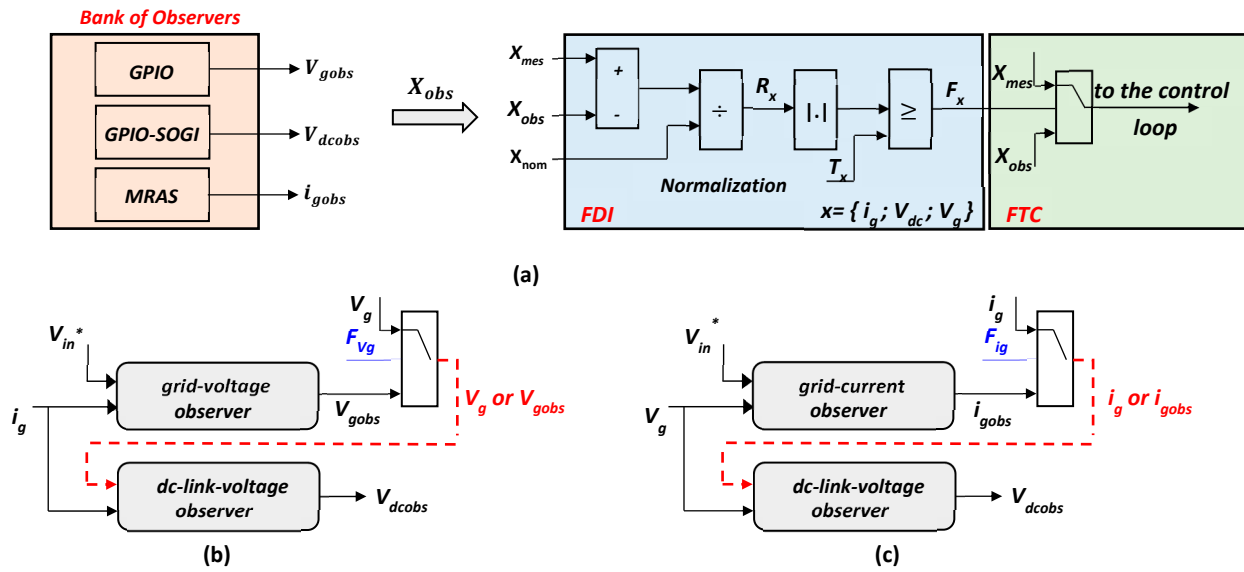


Figure 8. Structure of the proposed multiple-sensor faults FDI and FTC approach: (a) FDI general structure; (b) FTC for case 1: DC-link voltage and grid voltage sensors failure; (c) FTC for case 2: DC-link voltage and grid current sensor failure.

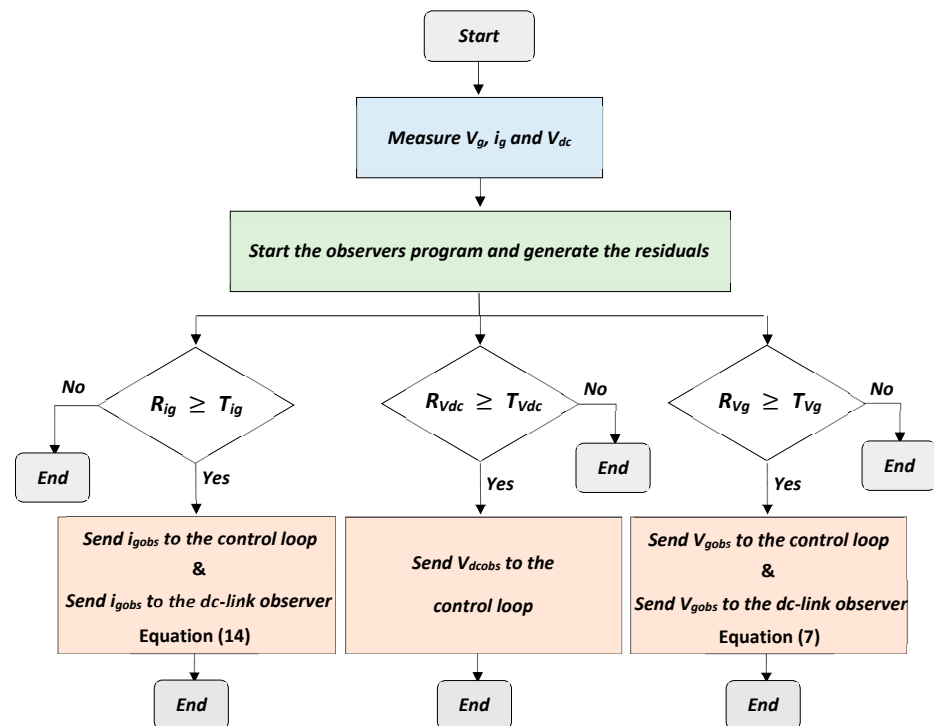


Figure 9. Flowchart of the proposed single- and multiple-sensor fault detection and FTC.

Once the faulty sensor is identified, the fault-tolerant process is initiated. The faulty measurement is substituted by the estimated one in the feedback control loop. It should be noticed that only two multiple-sensor fault scenarios can be treated: DC-link voltage and grid voltage sensors failure and DC-link voltage and grid current sensors failure. The simultaneous failure of the grid voltage sensor and the grid current sensor cannot be handled by the proposed approach. Figure 8a describes the FDI scheme by the residual generation and their evaluation in order to trigger the FTC process due to the switching value of the faulty sensor flag. Figure 8b presents the fault-tolerant control algorithm in case of V_g and V_{dc} multiple-sensor faults, whereas Figure 8c describes the FTC algorithm in case of i_g and V_{dc} multiple-sensor faults.

5. Simulation Results

In order to investigate the performance of the proposed FDI and FTC strategy, the single-phase PWM rectifier model is built in the Matlab-Simulink software R2016b environment. The system parameters used for simulation are presented in Table 1.

Table 1. Parameter values for simulation.

Description	Symbol	Value
RMS voltage supply	V_g	230 V
DC-bus voltage	V_{dc}	400 VDC
Sampling time	T_s	100 μ s
Switching frequency	f_{sw}	10 kHz
Line impedance	L, R	20 mH, 0.2 Ω
DC-Link capacitor	C	1100 μ F
Rated Load resistance	R_L	100 Ω

5.1. Multiple-Sensor Fault-Tolerant Control

The simulation results reported in Figure 10 illustrate the system performance before and after the occurrence of a 100% gain sensor fault of the DC-link voltage sensor at $t = 2$ s followed by an 80% offset fault of the grid voltage sensor which appears at $t = 3$ s. In healthy operating mode, i.e., for $t < 2$ s, all residuals are below the pre-defined fixed thresholds. At the occurrence of the DC-link voltage sensor fault (for $t = 2$ s), the residual $R_{V_{dc}}$ exceeds its fixed threshold $T_{V_{dc}}$, and the fault flag signal $F_{V_{dc}}$ switches from 0 to 1, as presented in Figure 10c,d. This indicates the presence of a DC-link voltage sensor fault. At the same time, both residuals R_{V_g} and R_{i_g} remain below their respective thresholds T_{V_g} and T_{i_g} . Once the DC-link voltage sensor fault is correctly located, the faulty measurement is replaced by its estimated value V_{dcobs} in the converter's control loop. As presented in Figure 10a,b, V_{dcobs} follows its reference value, and the grid current i_g also follows its reference, in phase with the grid voltage. Similarly, at the occurrence of the grid voltage sensor fault (at time $t = 3$ s), the residual R_{V_g} exceeds its fixed threshold T_{V_g} , as shown in Figure 10c,d, and the fault signal F_{V_g} switches from 0 to 1. This indicates the presence of a grid voltage sensor fault. Immediately after, the input of the SOGI-PLL block switches from the measured value of the grid voltage to the estimated value V_{gobs} . After the control reconfiguration, the grid current i_g keeps its sinusoidal shape, in phase with the grid voltage V_g , ensuring a unit power factor.

The simulation results depicted in Figure 11 illustrate the system performance before and after the occurrence of a 100% gain fault of the DC-link voltage sensor at $t = 2$ s followed by a 100% gain fault of the grid current sensor at $t = 3$ s. At the occurrence of a fault (for $t \geq 2$ s), the residual $R_{V_{dc}}$ exceeds its fixed threshold $T_{V_{dc}}$ (Figure 11c), and the fault signal $F_{V_{dc}}$ passes from 0 to 1 (Figure 11d). This indicates the presence of a DC-link voltage sensor fault. At the same time, both residuals R_{V_g} and R_{i_g} remain below their thresholds T_{i_g} and T_{V_g} , the fault signals F_{V_g} and F_{i_g} remain zero and the faulty measurement is replaced by the estimated value of V_{dc} . At $t = 3$ s, residual R_{i_g} exceeds its fixed threshold T_{i_g} , and the fault signal F_{i_g} passes from 0 to 1 (Figure 11d). This indicates the presence of a grid current sensor fault. Once the grid current sensor is correctly located, the faulty measurement is replaced by the estimated value of i_g . One can clearly notice that the grid current i_g keeps its sinusoidal shape and is in phase with the grid voltage V_g , ensuring a unit power factor (Figure 11b), and the system stability is not affected.

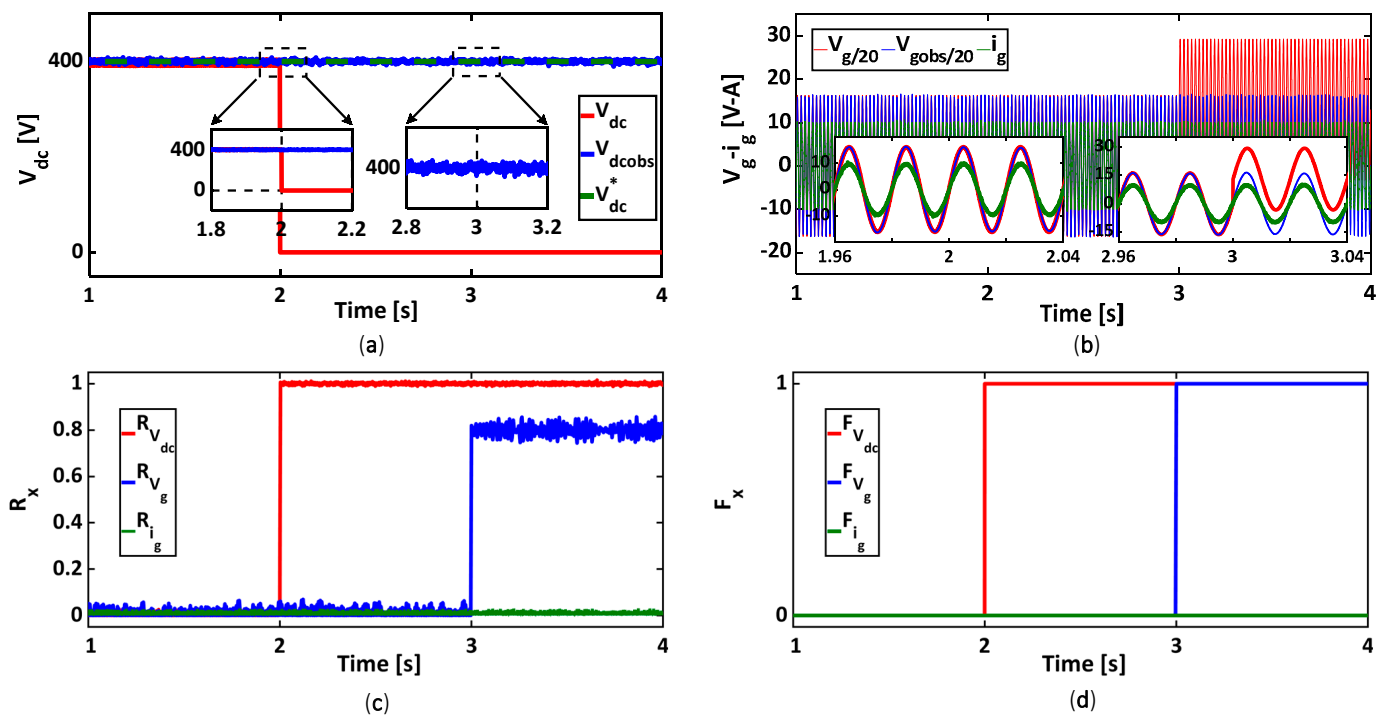


Figure 10. Simulation results for control reconfiguration in case of 100% gain fault of the DC-link voltage sensor and 80% offset fault of the grid voltage sensor, (a) V_{dc} fault tolerant control, (b) V_g fault tolerant control, (c) Residuals evolution, (d) Fault flags variations.

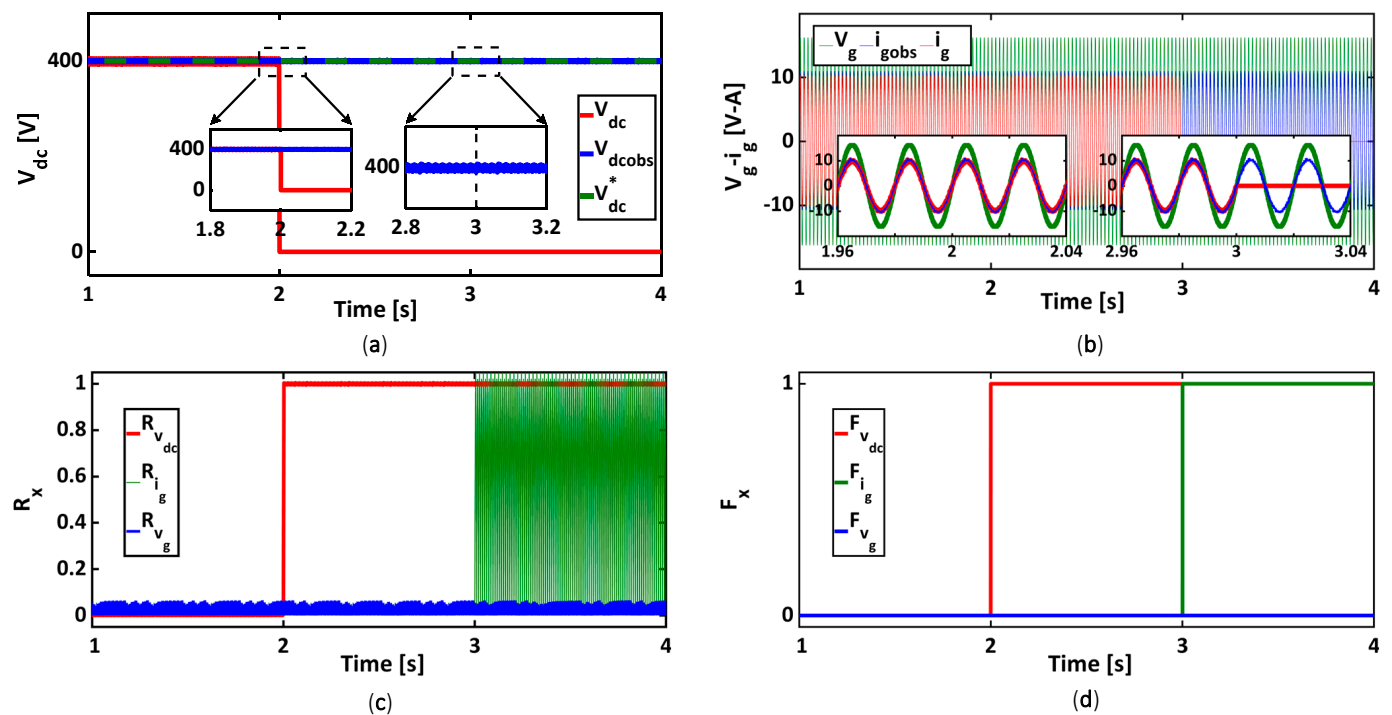


Figure 11. Simulation results for control reconfiguration in case of 100% gain fault of the DC-link voltage sensor and 100% gain fault of the grid current sensor. (a) V_{dc} fault tolerant control, (b) i_g fault tolerant control, (c) Residuals evolution, (d) Fault flags variations.

5.2. Post-Fault System Restart with the Single Survivable Sensor

The effectiveness of the proposed FTC approach has been investigated in the previous section by means of simulation. Nevertheless, and since the converter is not continuously working (the converter may be switched off by the user), it is important to investigate the capability of the proposed FTC algorithm to start up the converter using only the single survivable sensor.

Figure 12a–c present the simulation results regarding the start-up of the converter without DC-Link voltage and grid voltage sensors under 50% and 120% variation of nominal values of L and C as well as the operating point variation. As can be seen, all of the observed variables are accurately estimated under different operating conditions. More precisely, when the converter controller is activated, the DC-link estimated voltage reaches its reference value and is equal to the actual DC-link voltage. Moreover, it takes about 40 ms for the estimated grid voltage to reach the actual value. In addition, the resultant grid current presents a highly sinusoidal waveform with a unity power factor operation even with 100% variation of the output load resistance introduced at time $t = 1$ s (see Figure 12c).

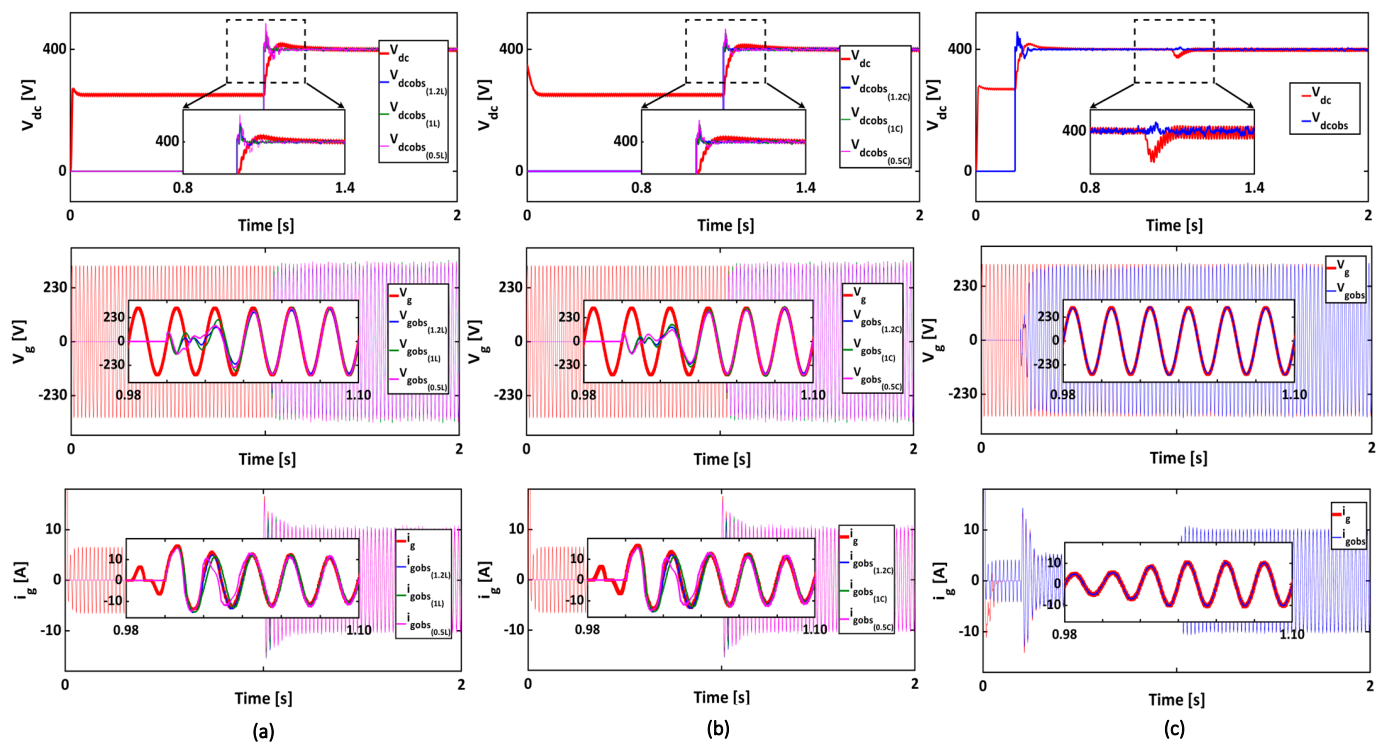


Figure 12. Simulation results for converter's start-up without DC-link voltage and grid voltage sensors considering parameter mismatches: (a) grid inductance mismatches; (b) DC-link capacitance mismatches; (c) DC load variation.

A second test for the start-up of the converter closed-loop operation without DC-link voltage and grid current sensors was performed (Figure 13a–c). It can be observed that the estimated DC-Link voltage follows its reference and actual values. Similarly, the estimated grid current perfectly follows the actual current under L , C and DC load variation. Moreover, the estimated grid voltage follows the actual grid voltage with accuracy even under extreme conditions and parameter uncertainties.

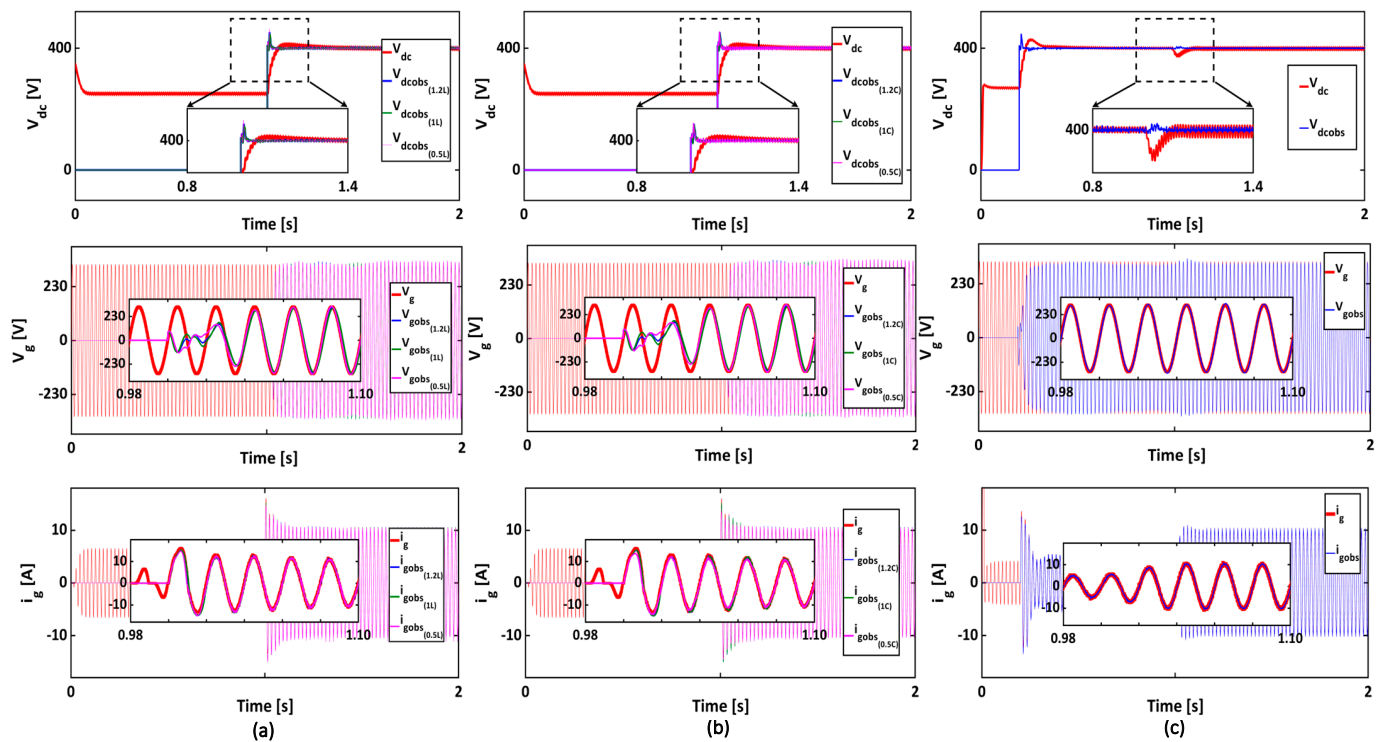


Figure 13. Simulation results for converter's start-up without DC-link voltage and current voltage sensors considering parameter mismatches: (a) grid inductance mismatches; (b) DC-link capacitance mismatches; (c) DC load variation.

These different case studies prove the robustness of the proposed observation approach considering different operation conditions.

6. Experimental Results

To demonstrate the feasibility and effectiveness of the proposed FTC method, experimental results, based on a reduced-scale experimental setup, are carried out. The structure of the experimental setup is presented in Figure 14. It comprises one Semikron SKiiP voltage source converter used as a single PWM rectifier, an input filter (20 mH, 0.2 Ω), a DC-bus capacitor bank of 1100 μ F and a variable resistive load. The rectifier's PWM frequency is set to 10 kHz. A current sensor (LEM PR 30) is used to measure the grid current i_g . The DC-link voltage and the grid voltage are measured by two Tektronix p5200 voltage sensors. A 48 V/230 V single-phase transformer is used for the converter's grid connection. The FTC algorithm is implemented through the Matlab-Simulink environment into the dSPACE DS1104 digital controller board using a sampling time of 100 μ s. All experimental setup parameters are reported in Table 2. The values of the different proportional and integral observers' gains K_p and K_i used in simulations and experiments are listed in Table 3.

Table 2. Laboratory prototype system parameters.

Description	Symbol	Value
RMS voltage supply	V_g	230/48 V
DC-Link voltage	V_{dc}	80 VDC
Sampling time	T_s	100 μ s
Switching frequency	f_{sw}	10 kHz
Line impedance	L, R	20 mH, 0.2 Ω
DC-Link capacitor	C	1100 μ F
Rated Load resistance	R_L	36 Ω

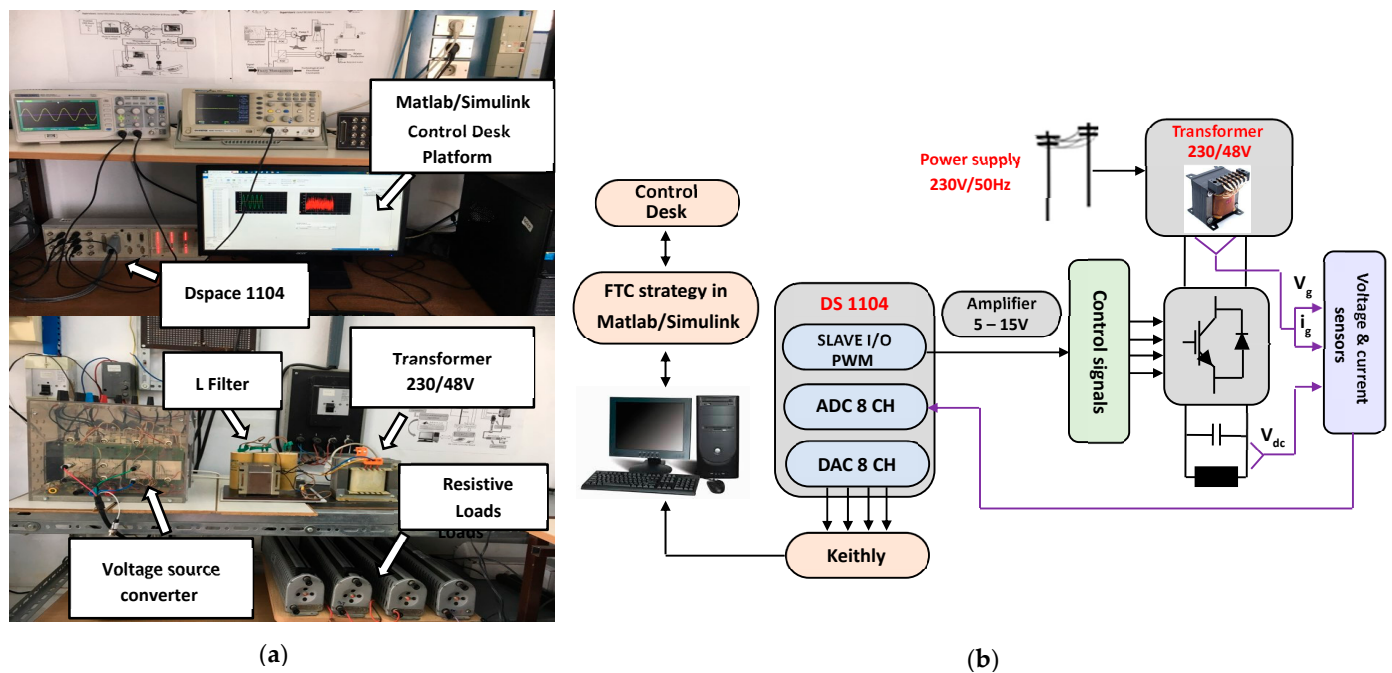


Figure 14. Experimental implementation of the proposed FDI and FTC: (a) experimental test bench; (b) descriptive diagram of the experimental implementation.

Table 3. GPI and MRAS observers' gains.

Estimator	Simulations		Experiments	
	k_p	k_i	k_p	k_i
V_g estimator	2.5×10^3	8×10^6	100	1×10^5
V_{dc} estimator	10	1×10^4	500	5×10^5
i_g estimator	0.7×10^3	5×10^2	31	10

6.1. Residual Robustness Analysis and Threshold Selection

The robustness of the FDI algorithm under healthy operation depends on the residuals' sensitivity to the system parameters' variations and to the operating point variations. In Figure 15a, the experimental results regarding the variations of the three residuals under load variations are reported. The load resistance is shifted from 60 to 40 Ω at time $t = 1.70$ s and again from 40 to 60 Ω at time $t = 3.10$ s. It can be seen that during resistance load variations, all residuals maintain low values below 0.08. In Figure 15b, the residuals' evolution under a DC-link voltage variation from 80 V to 100 V is detailed. All residuals present small variations, always below 0.08. Finally, the sensitivity of the proposed fault diagnosis approach is tested under a system parameter variation, namely the L filter inductance variation. The filter inductance was first changed from 30 mH to 20 mH and then to 14 mH. As can be seen, slight variations of the three residuals occurred; however, such variations are still low, around 0.05.

Therefore, the behavior of the three residuals following these different tests showed that their oscillations are still very small, close to zero. The thresholds should be carefully selected in order to guarantee the proposed method high immunity under healthy operation, as well as an accurate/fast detection and localization of the faulty sensor [15]. As presented in Figure 15, the defined fault detection residuals variations under healthy operation are small and always below 0.08. Under faulty operation mode, the variations of the residuals correspond to the measurement error. According to this, thresholds $T_{V_{dc}}$, T_{V_g} and T_{i_g} may have the same value, fixed at 0.1.

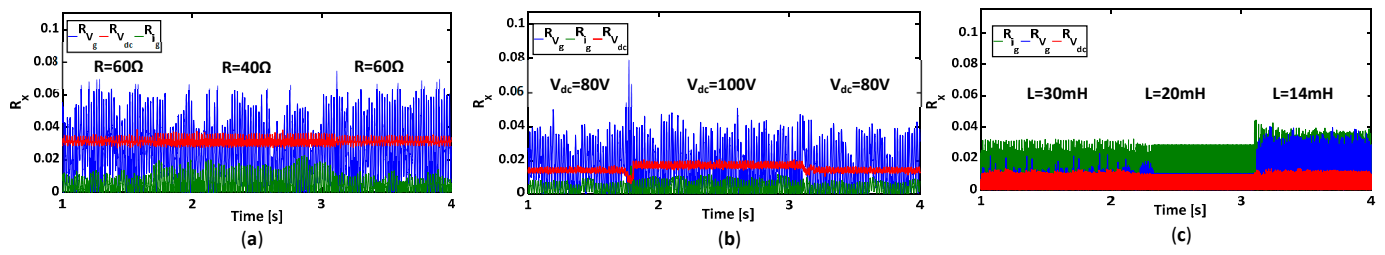


Figure 15. Experimental results regarding residuals evolution under: (a) DC load variation, (b) DC-link voltage variations, (c) grid filter inductance variations.

6.2. Multiple-Sensor Fault-Tolerant Control

The experimental results shown in Figure 16 present the performance of the proposed FDI and FTC in the case of DC-link voltage and grid voltage sensor faults. At time $t = 3.90$ s, the DC-link voltage fault is introduced (Figure 16a). In healthy operation mode, $V_{dc} = 80$ V; thus, the output of the DC-link voltage sensor value is set to 0. While grid voltage and current residuals remain at small values below their respective thresholds, the DC-link voltage R_{vdc} exceeds its threshold T_{vdc} . The fault flag F_{vdc} is set to 1, which indicates that the V_{dc} sensor is faulty. Immediately, the fault tolerance process is triggered, and the virtual sensor V_{dcobs} is sent to the control loop of the system. Then, an 80% offset fault of the grid voltage sensor is applied at time $t = 10.05$ s, as illustrated in Figure 16b. As a result, the grid voltage residual exceeds its threshold, and its corresponding fault flag is then set to 1 (Figure 16d,e). Furthermore, when the grid voltage sensor's detection is achieved, the input of the SOGI-PLL block switches from the measured grid voltage to the estimated grid voltage obtained from the GPIO. Now, the converter's control loop is employing only the single survivable grid current sensor. The DC-link voltage control loop, as well as the grid current reference generation, are based on the estimated voltages values V_{dcobs} and V_{gobs} , respectively. The single-phase PWM rectifier can still operate normally after the DC-link and grid voltage sensors malfunction. It can be seen in the zoomed parts of Figure 16a–c that the DC-link voltage is well regulated at 80 V, the grid current is sinusoidal with low harmonic distortion and the grid power factor is equal to 1.

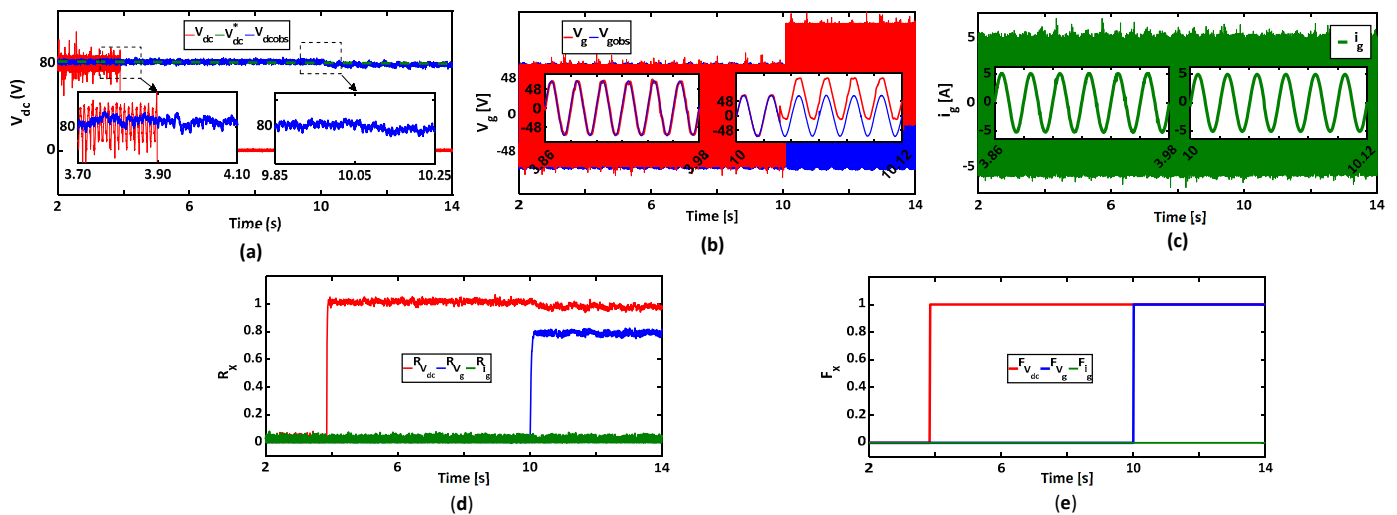


Figure 16. Experimental results for the fault-tolerant control in case of 100% gain fault of the DC-link voltage sensor and 80% offset fault of the grid voltage sensor. (a) V_{dc} fault tolerant control, (b) V_g fault tolerant control, (c) grid current i_g , (d) Residuals evolution, (e) Fault flags variations.

The experimental results concerning the control reconfiguration for the single-phase converter in case of 100% gain fault of the grid current sensor fault and 100% gain fault of the DC-link voltage sensor are detailed in Figure 17. When the DC-link voltage sensor fault is introduced at time $t = 5.32$ s, the residual R_{vdc} exceeds its fixed threshold T_{vdc} , and therefore, the fault flag F_{vdc} is equal to 1. Consequently, V_{dcest} substitutes the erroneous measurement in the loop control. It can be seen from Figure 17a–c that the DC-link voltage sensor fault tolerance is successfully achieved, and the system maintains its performance. At time $t = 10.193$ s, the output of the grid current sensor is forced to 0. As a consequence, as indicated in Figure 17d, the grid current residual exceeds its threshold, and the fault flag F_{ig} is set to 1. Once the grid current sensor is correctly located, the faulty measurement is replaced by the estimated value of i_{gobs} . After the control reconfiguration of the grid current sensor fault, only the grid voltage sensor survives. The zooms of Figure 17a–c clearly show that V_{dcobs} and i_{gobs} are following their respective reference values, ensuring a unit power factor, and that the converter stability is not affected.

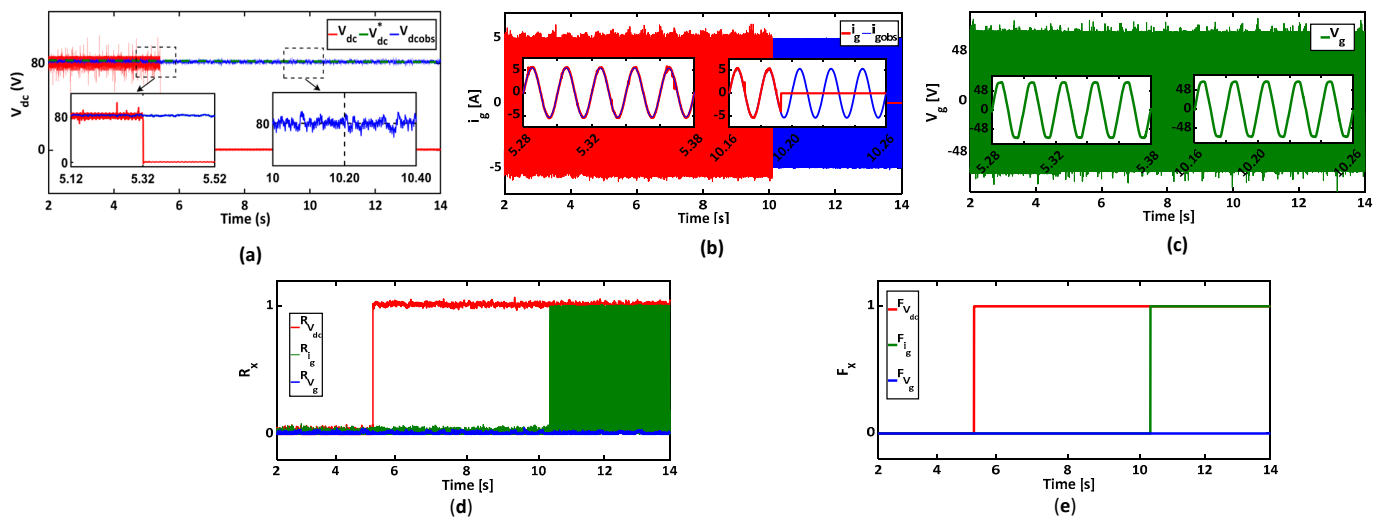


Figure 17. Experimental results for the fault-tolerant control in case of 100% gain fault of the DC-link voltage sensor and 100% gain fault of the grid current sensor. (a) V_{dc} fault tolerant control, (b) i_g fault tolerant control, (c) grid voltage V_g , (d) Residuals evolution, (e) Fault flags variations.

6.3. Post-Fault System Restart with the Single Survivable Sensor

Figure 18 presents the experimental results in the case of DC-link and grid voltages sensorless operation of the converter. Hence, the rectifier's control loop is only driven by the grid current sensor. Initially, the converter is operating as a diode full bridge. At time $t = 1.88$ s, the feedback control is activated. Figure 18a shows the variation of the observed quantity V_{dcobs} and of the actual voltage V_{dc} . It can be seen that the observed DC-link voltage, as well as the actual DC-link voltage, are correctly reaching their reference value. Figure 18b,c show the variations of the estimated grid voltage V_{gobs} , the actual grid voltage V_g and the grid current i_g . The estimated grid voltage follows the measured one, and the grid current i_g has a sinusoidal waveform in phase with the grid voltage. Moreover, at time $t = 8.25$ s, the load is changed from 100 Ω to 36 Ω . It can be observed that the proposed control strategy keeps its good performance. The estimated values V_{dcobs} and V_{gobs} are following their respective actual values while ensuring a unit power factor, and the converter stability is not affected.

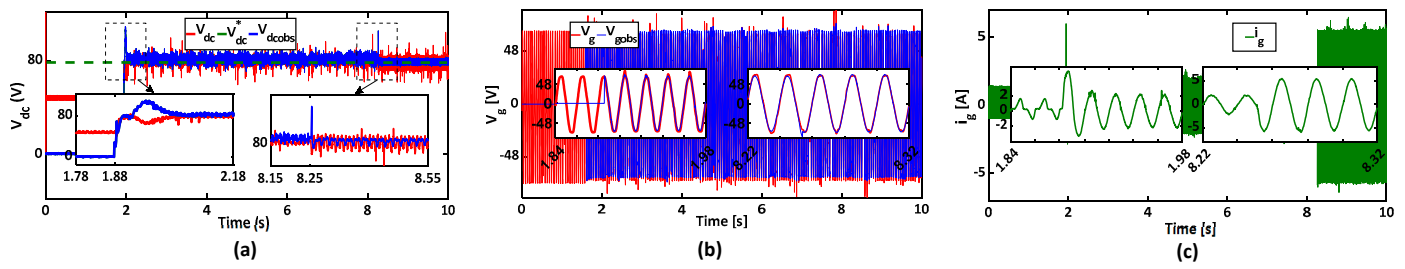


Figure 18. Experimental results for the system's start-up without DC-link voltage and grid voltage sensors. (a) dc-link voltage, (b) Grid voltage, (c) Grid current.

The start-up of the PWM rectifier operation without DC-link voltage and grid current sensors is illustrated in Figure 19. The closed-loop control is initiated at time $t = 4.25$ s. Similarly to the simulation results, the observed voltage V_{dcobs} and the actual voltage V_{dc} are correctly reaching their reference value. As shown in Figure 19c, the estimated grid current i_{gobs} is following the actual grid current i_g .

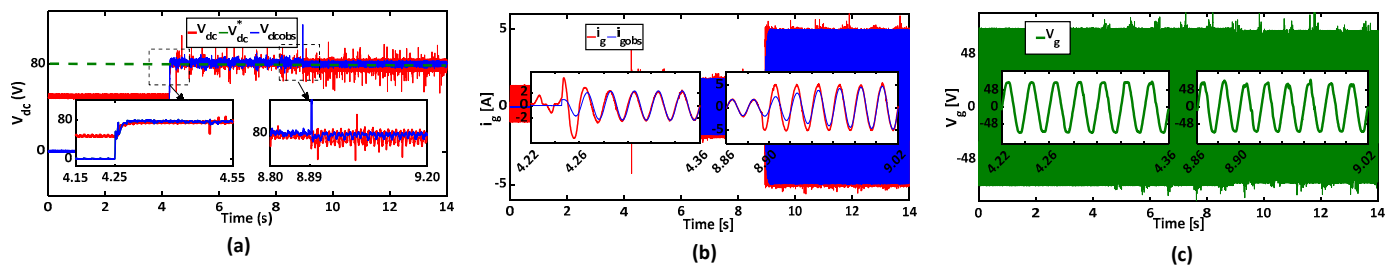


Figure 19. Experimental results for the system's start-up without DC-link voltage and grid current sensors. (a) dc-link voltage, (b) Grid current, (c) Grid voltage.

Moreover, the grid unity power factor is guaranteed according to Figure 19b,c, where the grid current is in phase with the grid voltage. At $t = 8.89$ s, the load is changed from 100Ω to 40Ω . It can be observed from Figure 19a that the proposed control strategy keeps its good performance. The estimated values V_{dcobs} and i_{gobs} are following their respective reference values while ensuring a unit power factor, and the converter stability is not affected.

6.4. Comparative Study with Previously Proposed Methods

To better highlight the benefits of the proposed multiple-sensor fault diagnosis algorithm, its performance is compared with some previously reported approaches, as summarized in Table 4. It can be seen that the proposed approach has similar sensor fault detection and sensor FTC performance to those discussed by [15,17,21,25,30]. Nevertheless, the abovementioned methods cannot handle multiple-sensor failures. Moreover, they need the use of an additional DC load current sensor [15,25,30], which increases the system's cost.

The approach presented by [27] ensures a multiple-sensor fault-tolerant control for a three-phase grid-connected inverter fed by PV arrays. It has focused on the three grid-side AC current sensor faults and DC-link voltage sensor faults. The proposed sensor fault detection and isolation decision logic can guarantee the detection of a single- or multiple-AC-sensor fault; however, if the DC-link voltage sensor is faulty, it violates one or more analytical redundancy relations on the AC side. In order to overcome this issue, when both AC and DC sensor faults occur, the isolation high priority is given to the DC sensor, while the AC sensors are given low-priority fault isolation signals.

Table 4. Fault detection and FTC performance comparison for different methods.

Fault Diagnosis Method	Fault Modes	Single- and Multiple-Sensor Fault Tolerance	Detection Time	Need of Additional Sensor	Algorithm Accuracy	Algorithm Complexity
Luenberger observer [15]	Current and DC-link voltage sensor faults	Single-sensor FTC	$<0.02 T_f$	Yes	Robust against variations	Medium
Open-loop estimator [17]	Current and DC-link voltage sensor faults	Single-sensor FTC	$<0.2 T_f$	No	Affected by parameters' variations	Medium
Sliding-mode observer [21]	Current and DC-link voltage sensor faults	Single-sensor FTC	$\approx 0.05 T_f$	No	Robust against variations	Medium
Fault estimation [30]	Current and DC-link voltage sensor faults	Single-sensor FTC	---	Yes	Robust against variations	Medium
DSOGI estimator [25]	Current and AC voltage sensor faults	Single-sensor FTC	---	Yes	Robust against variations	Medium
State estimator [27]	Current and DC-link voltage sensor faults	Single- and multiple-sensor FTCs	$\approx 0.05 T_f$	Yes	Robust against variations	Medium
Reduced-order observer [19]	Current and DC-link voltage sensor faults	Single- and multiple-sensor FTCs	$<0.015 T_f$	Yes	Robust against variations	Medium
Proposed approach	Current, DC-link voltage and AC voltage sensor faults	Single- and multiple-sensor FTCs	$\approx 0.05 T_f$	No	Robust against variations	Medium

In the proposed FTC approach, it has been shown that an AC sensor fault can be discriminated from a DC sensor fault without any constraints. When DC and AC sensor faults occur, the proposed FTC method can easily handle both of them.

The method discussed by [19] ensures multiple-sensor fault-tolerant control in cascaded H-bridge multilevel converters and can identify the fault type (open-circuit fault, stuck fault, gain fault, offset fault, and abnormal noise). However, only one multiple-sensor FTC scenario has been discussed, which involves the grid current sensor and the DC-link voltage sensor. In our work, two scenarios have been presented: in the first scenario, a DC-link voltage sensor fault followed by a grid voltage sensor and, in the second scenario, a DC-link voltage sensor fault followed by a grid current sensor fault. It is important to highlight that for the multiple-grid current sensor and DC-link voltage sensor faults, the extreme case with 100% gain faults for both sensors has been discussed.

Both work in [19,27] and our work address multiple-sensor faults, but the proposed work emphasizes a novel approach that simplifies the system by not requiring additional sensors, which represents an improvement in terms of system complexity and cost.

Finally, none of these methods has proposed a unified sensor fault detection approach for the main three sensors used in the closed-loop control of the single-phase PWM rectifier without any extra hardware. The extensive experimental results demonstrated that the proposed method can be easily implemented into a real-time digital controller, which may improve the cost and the performance of a single-phase PWM converter in several industrial applications such as EVs, electric traction systems, and so on.

Likewise, the proposed method has some limitations. It cannot identify the sensor fault type (scaling, offset, open-circuit, and so on). Additional features should be extracted in order to enhance its performance in that sense. Moreover, open-circuit faults would change the rectifier's input voltage, which results in high estimation errors and may lead to a sensor false alarm. Hence, in future work, an effective algorithm that can diagnose and discriminate sensor faults from power semiconductor faults in a single-phase PWM converter will be considered.

7. Conclusions

This paper proposes a novel, simple, and fast unified sensor fault detection and isolation without extra hardware and sensor fault-tolerant control of a single-phase pulse PWM rectifier based on residual generation through a robust bank of GPI and MRAS observers. Compared with the previous published methods, the proposed approach offers some benefits:

- (1) The proposed approach is a unified sensor fault detection method for the main three sensors used in the closed-loop control of the single-phase PWM rectifier without any extra hardware.

- (2) In addition to single-sensor fault detection, the proposed approach is able to diagnose multiple-sensor faults and ensure a post-fault operation of the PWM rectifier with the single survivable sensor.
- (3) It has the capability to guarantee the start-up of the single-phase PWM rectifier with a single survivable sensor and with the same performance as in healthy operation, even under DC-link load variations or system's parameters' mismatch.

In particular, if compared with other methods addressing multiple-sensor faults, the proposed method relies on a novel approach that does not require additional sensors, with a moderate mathematical complexity, based on a clear mechanism for fault detection and isolation. Additionally, it is characterized by robustness and practical viability, which are important features in real-world applications.

Several simulations and experimental results have been discussed to demonstrate the robustness and effectiveness of the proposed approach under distinct simultaneous faulty scenarios and to show the very good performance of the post-fault operation of the single-phase PWM rectifier in terms of DC-link voltage regulation and grid-side power quality.

In future work, some improvements to the proposed method should be introduced in order to identify the sensor fault type and to discriminate sensor faults from power semiconductor faults. In this way, the combination of model-based approaches with data-driven approaches is of great benefit.

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Nomenclature

ADC	Analogue to Digital Converter
C	DC-link capacitor
d_1, d_3	Duty Cycle
DAC	Digital to Analogue Converter
DSOGI	Dual Second-Order Generalized Integrator
EVs	Electric Vehicles
f_a	Disturbance and/or unknown input
f_{aobs}	Observed value of the disturbance and/or unknown input
FDI	Fault Detection and Isolation
FE	Fault Estimation
FTC	Fault-Tolerant Control
f_{sw}	Switching frequency
F_x	Fault Flag, $x = \{i_g, V_g, V_{dc}\}$
GPIO	Generalized Proportional Integral Observer
i_c	Current in the DC-side capacitor
i_{dc}	DC-side output current
i_g	Grid current
i_{gobs}	Observed value of the grid current
i_g^*	Reference value of the grid current
i_{gnom}	Nominal value of the grid current
i_L	Load current

T_f	Grid current fundamental period
K_i	Integral Gain
K_p	Proportional Gain
L	Line inductance
LO	Luenberger observer
m_{ab}	Modulation index
MRAS	Model Reference Adaptive System
PI	Proportional Integral
PR	Proportional Resonant
PWM	Pulse-Width Modulated
R	Line resistance
R_L	Rated Load resistance
R_x	Residual, $x = \{i_g, V_g, V_{dc}\}$
SMO	Sliding-Mode Observer
SOGI	Second-Order Generalized Integrator
SOGI-PLL	Second-Order Generalized Integrator Phase-Locked Loop
S_1, S_3	Binary Switching Control Signal
T_s	Sampling Time
T_x	Threshold, $x = \{i_g, V_g, V_{dc}\}$
V_{ab}	Rectifier input voltage
V_{abobs}	Estimated value of the rectifier input voltage
$V_{abobs\alpha}, V_{abobs\beta}$	Estimated orthogonal components of the rectifier input voltage
V_{dc}	DC-link voltage
V_{dc}^*	Reference value of the DC-link voltage
V_{dcobs}	Observed value of the DC-link voltage
V_{in}^*	Reference value of the rectifier voltage
V_g	Grid voltage
V_{gnom}	Nominal value of the grid voltage
V_{gobs}	Observed value of the grid voltage
θ_g	Phase angle
ϕ_g	Grid virtual flux
ϕ_{gobs}	Observed value of the grid virtual flux
φ_{ab}	Phase difference

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