



RI-MFM: A Novel Infrared and Visible Image Registration with Rotation Invariance and Multilevel Feature Matching

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Abstract: In the past ten years, multimodal image registration technology has been continuously developed, and a large number of researchers have paid attention to the problem of infrared and visible image registration. Due to the differences in grayscale distribution, resolution and viewpoint between two images, most of the existing infrared and visible image registration methods are still insufficient in accuracy. To solve such problems, we propose a new robust and accurate infrared and visible image registration method. For the purpose of generating more robust feature descriptors, we propose to generate feature descriptors using a concentric-circle-based feature-description algorithm. The method enhances the description of the main direction of feature points by introducing centroids, and, at the same time, uses concentric circles to ensure the rotation invariance of feature descriptors. To match feature points quickly and accurately, we propose a multi-level feature-matching algorithm using improved offset consistency principle. The comparison experiments with several other state-of-the-art registration methods in CVC and homemade datasets show that our proposed method has significant advantages in both feature-point localization accuracy and correct matching rate.

Keywords: infrared image; image registration; feature matching; robust estimation

1. Introduction

At present, there are more and more types of imaging sensors, and people can obtain images of multiple bands of the same scene for research [1,2]. The images of multiple bands can perform multi-dimensional analysis on the target, and the obtained information is also more comprehensive. One of the most popular topics in vision is multimodal image registration; in particular, infrared and visible image registration is the most studied [3,4]. Since infrared and visible images can provide complementary information, they have wide applications in image fusion [5,6], automatic transform detection [7], and super-resolution reconstruction [8].

In the past decade, researchers have proposed a large number of infrared and visible image registration methods [9,10]. However, since infrared and visible images belong to two wavelength bands, and the resolutions of the two images are different, the registration is difficult. At present, the existing registration methods are mainly divided into two categories, one is a region-based registration method, and the other is a feature-based registration method.

Area-based infrared and visible image registration methods do not require the extraction of salient features. Matching is performed by directly comparing and matching the intensity difference between two images [11]. Specifically, normalized cross-correlation (NCC) [12] and mutual information (MI) [13,14] in region-based registration methods are used to detect the matching accuracy of image pairs. In some cases, this kind of method can obtain higher matching accuracy, but the whole algorithm is computationally difficult and time-consuming. In particular, MI works well for infrared and visible image registration



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Copyright: © 2022 by the authors. Licensee MDPI, Basel, Switzerland. This article is an open access article distributed under the terms and conditions of the Creative Commons Attribution (CC BY) license (https:// creativecommons.org/licenses/by/ 4.0/). because of its statistical dependence between the two images. However, MI is prone to fall into local extrema during optimization iterations, which also reduces its robustness and applicability.

The feature-based infrared and visible image registration method is mainly divided into three steps, namely, feature extraction, feature description and feature matching [15]. Feature extraction means that point, line and area features in infrared and visible images are extracted for subsequent feature description and matching. At present, the more advanced feature-extraction algorithms are SURF [16] and SIFT [17]. Nowadays, there are many scholars who use improved SIFT for feature extraction based on the SIFT algorithm. Ye et al. [18] proposed a real-time adaptive registration algorithm for infrared and visible images using morphological gradients and C_SIFT. Feature description refers to generating a vector of a specific dimension for the extracted feature points. This vector should have sufficiently strong rotation and scale invariance. Xiong et al. [19] proposed a rank-based local self-similarity (RLSS) descriptor. This descriptor is robust to nonlinear radiation differences. Feature matching is performed to establish the correct correspondence between the feature descriptors of two images. There can be a large number of false matching points in the initial matching-point set, and researchers most commonly use random sampling consistency (RANSAC) [20] to eliminate the false matching points. However, there is often a gradient inversion problem in infrared images, which leads to a serious mismatch of the established feature descriptors. Last but not least, the existing image registration methods have high computational complexity, and real-time registration is difficult. This also limits the application of registration algorithms in real-time registration scenarios.

To solve the problems raised above, this paper proposes an infrared and visible imageregistration method with rotation invariance and multi-level feature matching. First, we preprocess the source image. The source images are converted to grayscale and maintain the same resolution. Second, we use the Canny [21] algorithm to detect the edge features of the image. Two sets of the feature points of the infrared and visible images are obtained. Third, we use a feature-description algorithm based on concentric circles to generate feature descriptors corresponding to two sets of feature points. Fourth, we use a multi-level feature-matching algorithm with improved offset consistency to match feature points. We evaluate the registration performance of the proposed method on public and homemade infrared and visible datasets, and compare with several state-of-the-art registration methods. The experimental results show that the registration method proposed by us has great advantages in the localization accuracy and matching accuracy of feature points. The main contributions of this paper are as follows:

- We propose to generate feature descriptors using a concentric circle-based featuredescription algorithm. When the feature descriptor is generated, the description of the main direction of the feature point is enhanced by introducing the centroid, and the rotation invariance is guaranteed by using the concentric circles. This produces more robust feature descriptors and reduces dimensionality, speeding up computation.
- 2. We propose a multi-level feature-matching algorithm with improved offset consistency to match feature points. We use the length and angle of the connection between the correct matching points to be basically the same, and redesign the matching algorithm to achieve a better matching effect. Finally, the matching points with higher positioning accuracy can be obtained by iterative screening using the RANSAC algorithm.
- Experimental results of our proposed infrared and visible image registration method on public and homemade datasets show that it achieves higher localization accuracy and correct matching rate than existing state-of-the-art image registration methods.

2. Related Work

Infrared and visible image registration is a multimodal image registration problem [22,23], since infrared images and visible images provide complementary information, respectively. Therefore, these two kinds of images are heavily used in vision applications (image fusion and image stitching) [24–27]. However, due to the difference in band and resolution between infrared and visible sensors, the two images cannot be directly fused. We need to register the images of both bands and then fuse them. Currently, existing multimodal image registration methods are mainly divided into two categories, namely, regionbased image registration [28,29] and feature-based image registration [30,31]. The two methods are described below.

2.1. Region-Based Methods

Region-based methods utilize the intensity information of images to achieve image registration [32]. Specifically, first, region-based methods find suitable similarity measures in two images. Then, the geometric transformation model is estimated. Finally, iterative optimization is performed on the above similarity measure and transformation parameters are set. However, this method requires a lot of computation. Moreover, it is easy to fall into local minima during the optimization process.

Similarity measurement is an important part in the iterative optimization process of infrared and visible image registration. At present, the similarity measures commonly used by researchers include the sequential similarity detection algorithm [33], mutual information (MI) [13,14,34], normalized cross-correlation (NCC) [12,35], sum of squared differences (SSD) [36] and sum of absolute differences (SAD) [37]. Researchers found that MI is more robust to nonlinear radiation differences and has been used in infrared and visible image-registration methods. Cole-Rhodes et al. [38] improved the joint histogram of MI and proposed a simultaneous perturbation stochastic approximation algorithm for image registration. The algorithm calculates the global optimal value of the local extreme value of the loss function, which greatly speeds up the image-registration speed. To address the problem of insufficient image overlap regions in MI, Xu et al. [39] proposed using Jeffrey divergence can provide a larger search space.

Another important step in region-based image-registration methods is the geometric transformation model. Multimodal images are warped and resampled by estimating the parameters of the transformation model. Finally, the alignment and registration of the multimodal images are completed. Choosing an appropriate transformation model can speed up iteration and optimization while also improving registration accuracy. Currently, most researchers use linear and nonlinear transformation models for image registration [40].

Through the above two steps, the similarity measure and transformation model are determined. Finally, to obtain the best image registration, region-based image-registration methods also need a way to find the optimal transformation in the solution space. The accuracy of image registration is directly determined by the optimization method. Hasan et al. [41] proposed to use partial volume interpolation to optimize the computation of the gradient of the similarity measure. To avoid the iterative optimization process falling into local optima, Yan et al. [42] proposed to use transfer optimization to maximize MI.

2.2. Feature-Based Methods

The feature-based image-registration method performs registration by extracting geometric features in the image. The geometric features include point, line and region features [43].

At this stage, feature-based image-registration methods are mainly divided into three steps, namely, feature extraction, feature description and feature matching. At present, the feature detection and extraction used by researchers mainly focuses on the corners or curves in the image. Commonly used corner and curve feature-detection algorithms are Harris [44], SIFT [17], Canny [22] and Sobel [45]. Moravec et al. [41] developed a Harris corner detector using image gradients and proposed a response function. The Harris corner feature has rotation invariance, and is relatively stable in detecting changes in image contrast and brightness. Lowe et al. [17] proposed the SIFT algorithm. The features extracted by the SIFT algorithm have strong stability in the case of translation, rotation and

scale changes. In order to obtain more useful information, Huang et al. [22] proposed to use the Canny operator to extract edge features in images, and to dilate these edge features.

Between two images, it is difficult to construct the correspondence between features only with the position information of feature points. Therefore, we need to construct a suitable feature descriptor for each feature point, which will be beneficial to the feature-matching process later. In general, the generated feature descriptors are required to be robust to changes in the geometry, appearance, and quality of the image. Moreover, two matching feature descriptors are required to have a close intra-class distance, and two mismatched feature descriptors are required to have a large inter-class distance. At present, for multi-modal images such as infrared and visible, researchers need to make targeted designs and perform optimization according to the characteristics of such images. Chen et al. [46] proposed a multimodal image-registration method based on edge features and scale-invariant PIIFD. They employ the scale-invariant PIIFD algorithm to describe the extracted edge salient features.

Feature matching establishes the correct correspondence between the two sets of extracted feature points. The matching-point pairs of all features include correct matching-point pairs and incorrect matching-point pairs. How to eliminate the wrong matching point pairs is the key to matching. Currently, the most used method by researchers is RANSAC [20], to remove mismatched points. To eliminate the need for artificially set inner point thresholds in RANSAC, Daniel et al. [47] proposed a threshold consistency registration method (MAGSAC). The method proposes the use of an iterative stopping condition based on marginalization. By using threshold consistency, MAGSAC does not require artificially defined interior-point thresholds and can significantly improve the accuracy of robust estimation.

3. Proposed Method

Our proposed infrared and visible image-registration algorithm (RI-MFM) has four key steps, as shown in the flowchart in Figure 1. First, to make the source image more suitable for computer analysis and processing, the use value of the image is improved. We preprocess the source image to enhance edge and texture details in the image. Secondly, in order to extract the robust feature points in the infrared and visible images, we use the Canny algorithm to extract the edge of the preprocessed image, and use the SIFT algorithm to extract the feature-point information in the edge contour. Then, we propose generating feature descriptors using a concentric-circle-based feature-description algorithm. Finally, to achieve more precise matching accuracy and faster matching speed, we propose to use a multi-level feature-matching algorithm with improved offset consistency to match feature points. We will describe each step-in detail, next.

- 1. Image pre-processing: For better robustness and generalization of the proposed registration algorithm, the input infrared and visible images should be pre-processed. First of all, if the device acquires color images, the color images need to be converted to grayscale images. Then, the infrared image is noise-reduced and dynamic range adjusted using an image-enhancement algorithm, which aims to enhance the edge and texture detail information of the image. Finally, the infrared and visible image resolutions are scaled to the same size.
- 2. Feature extraction: At first, the Canny edge-detection algorithm is used to obtain the edge contour maps of infrared and visible images. Additionally, then, the SIFT algorithm is used to detect and localize the edge contour map. Finally, two sets of feature-point sets of infrared and visible images are obtained.
- 3. Feature description based on concentric circles: After obtaining two sets of feature points of infrared and visible images, it is necessary to construct corresponding feature descriptors for each feature point. First, the centroid is calculated using the area-integration method. Then, based on the coordinates of the centroid and the feature point, the principal direction is calculated. Finally, the concentric-ring area is constructed to generate the feature-point descriptors.

4. Multi-level feature matching based on improved offset consistency: The most important feature of feature matching is to search for the most correct matching-point pair in the two images according to the obtained feature descriptor and determine whether it is a feature point in the same scene. Firstly, coarse matching of feature points is performed using Euclidean distance. After that, the feature points are finely matched using an improved offset consistency judgment criterion to further eliminate the incorrect matches. Finally, in order to eliminate the incorrect matching points with insignificant differences among the candidate matching points, the RANSAC algorithm is used for iterative screening to obtain matching points with higher accuracy.

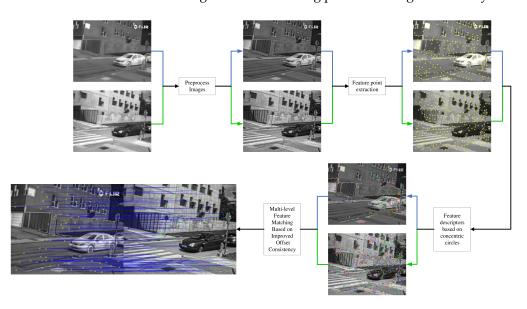
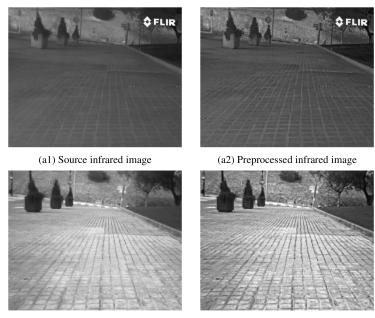


Figure 1. Flowchart of proposed RI-MFM registration method. A pair of corresponding example images are given for each step. The blue arrows in the figure point to the infrared images, and the green arrows point to visible images.

3.1. Image Preprocessing

Image preprocessing can improve the visual effect of images. At the same time, it can be converted into a form more suitable for machine analysis processing. The preprocessed image can significantly improve the use value of the image. As the source image has problems such as too-concentrated grayscale information, an unclear edge texture and weak contrast, we used a weighted guided filtering algorithm to enhance the source image. First, we layered the source image through multi-scale weighted guided filtering with steering kernels to obtain multiple detail-layer images and base-layer images with detailed information. Secondly, the detail layer was enhanced using Markov–Possion-based maximum a posteriori probability algorithm [48] and Gamma [49] correction algorithm. Then, a contrast-limited adaptive histogram equalization algorithm was applied to the base layer for contrast stretching. Finally, linear fusion was performed to obtain the enhanced image. The image after preprocessing was completed as shown in Figure 2.



(b1) Source visible image

(b2) Preprocessed visible image

Figure 2. Comparison of infrared and visible images before and after preprocessing.

The formula of multi-scale weighted guided filtering is defined as:

$$\begin{cases} B = SKWGIF(F) \\ I = F - B \\ I_1 = SKWGIF(I) \\ I_2 = I - I_1 \end{cases}$$
(1)

where *SKWGIF* is a weighted guided filtering algorithm with guided kernel [50], *F* is the input source image, *B* is the base-layer image obtained after filtering, *I* is the detail-layer image obtained by the first filtering, I_1 is the detail-layer image obtained by the second filtering, and I_2 is the second layer of detail image obtained by subtracting I_1 from *I*.

3.2. Feature Detection

Due to the large difference in detail texture between infrared and visible images, features such as grayscale and gradient of a single pixel are not stable between infrared and visible images. However, features such as edges and contours of the target are similar in performance and relatively stable between images. Therefore, we first use the Canny [22] algorithm to extract edge-contour information in infrared and visible images, and then use SIFT [17] to detect and locate feature points on the contour map. The effect after the feature detection is completed is shown in Figure 3. The specific steps are described below.

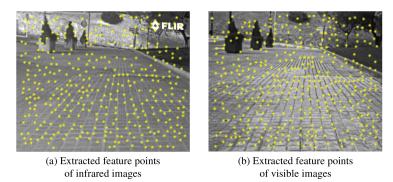


Figure 3. Feature points detected in infrared and visible images, respectively.

First, the image is denoised using Gaussian filtering. Secondly, the Sobel [45] operator is used to calculate the gradient magnitude and argument of the image, and non-maximum suppression is used to eliminate some non-edge points, so that the detection of edge pixel positions is more accurate. Then, the disconnected parts in the thin lines are connected by the double threshold method, which is the required edge-contour feature. Finally, SIFT [17] feature-point detection and localization are performed on the contour map to obtain two sets of feature-point sets of infrared and visible images.

3.3. Feature Description

Between infrared and visible images, it is difficult to construct the correspondence of feature points only by the position information of feature points. Therefore, we need to construct a suitable feature descriptor for each feature point, which is conducive to better matching operations. To improve the accuracy of the descriptors, we introduce centroids and concentric circles in the feature descriptors. At the same time, this can enhance the rotation invariance of the feature descriptor and reduce the algorithm complexity.

First, the centroid is calculated using the area integration method. In the scale space corresponding to feature point $P(x_i, y_i, \sigma)$, each pixel is regarded as a square of 1×1 . Take the feature point $P(x_i, y_i)$ as the center of the circle and 3σ as the radius to make a circular area. Definition: The overlapping area of each pixel and the circular area is the area integration coefficient C_{xy} of the pixel. When the pixel is completely contained within the circular area, the overlap-area value is 1. The corresponding area integration coefficient C_{xy} is 1. The centroid coordinate is the coordinate (x_j, y_j) of the pixel. When there is a partial overlap, the area-integration coefficient C_{xy} of the pixel is the area value of the overlapped part. The centroid coordinate (x_j, y_j) corresponding to the pixel can be obtained through the calculation method of the geometric centroid.

Second, according to the coordinates of the centroid and the feature point, the main direction is calculated. The image moment of feature point P^{mn} can be calculated from the area-integration coefficient and centroid coordinates of each pixel.

$$P^{mn} = \sum C_{xy} x_j^m y_j^n G_{(x,y)} \tag{2}$$

where $G_{(x,y)}$ is the gray value corresponding to (x, y), and m, n is the order corresponding to x, y; the values are, respectively, 0 or 1. Therefore, P^{00} , P^{01} , and P^{10} can be obtained. The brightness centroid coordinates of the circular area of the feature point $P(x_i, y_i)$ is $L(x_k, y_k)$. It is calculated as follows:

$$L(x_k, y_k) = \left(\frac{P^{10}}{P^{00}}, \frac{P^{01}}{P^{00}}\right)$$
(3)

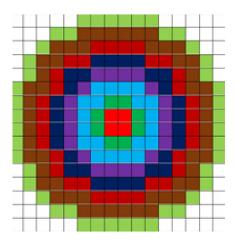
Definition: The angle θ_1 between the direction vector OL of the circular area and the *X* axis is the main direction of the feature point. θ is calculated as follows:

$$\theta = \arctan\left(\frac{y_k - y_i}{x_k - x_i}\right) \tag{4}$$

Third, concentric annular regions are constructed and feature-point descriptors generated. Taking the feature point $P(x_i, y_i)$ as the center of the circle, the coordinate axis was rotated to coincide with the main direction. A concentric annular region of radius 8 was constructed, as shown in Figure 4. The gradient magnitude and argument for each pixel were calculated using the following equations.

$$A(x,y) = \sqrt{(M(x+1,y) - M(x-1,y))^2 + (M(x,y+1) - M(x,y-1))^2}$$
(5)

$$\theta_2 = \arctan\left(\frac{M(x, y+1) - M(x, y-1)}{M(x+1, y) - M(x-1, y)}\right)$$
(6)



where A(x, y), θ_2 and $M_{x,y}$ represent the magnitude of the gradient, the argument direction of the pixel point and the gray value of the pixel point, respectively.

Figure 4. Schematic diagram of feature-descriptor concentric circles.

Each feature point corresponds to a concentric annular region. The rings of each color form a sub-area. First, the gradient values of all pixels within the first annular region are calculated. The accumulated gradient values are counted in 8 directions ($0^{\circ} \sim 360^{\circ}$ is evenly divided into 8 intervals) to generate an 8-dimensional vector. Then, to make the gradient accumulation with the largest value as the head of the feature vector, the gradient accumulation value is processed by using the maximum value circular shift. We can obtain the 1st to 8th vectors of the feature descriptor. Finally, the gradient-accumulation values in each direction are obtained by calculating the other regions of each circle separately using the above approach. A total of $8 \times 8 = 64$ -dimensional vectors are generated as descriptors of feature points. The use of concentric rings to compute the descriptors of feature points ensures that the relative information remains unchanged when the vectors are rotated, and also facilitates the subsequent computation of feature matching.

3.4. Feature Matching

In point-based registration methods, feature matching is the most important step, which directly determines the accuracy of image registration. Feature matching is to establish the correct correspondence between two sets of feature points. Due to the difference in band and resolution between the infrared image and the visible image, there is a certain deviation in the position of the extracted feature points. Therefore, in order to obtain matching points with higher localization accuracy, we propose the RI-MFM feature-matching method.

Suppose the set of feature-point coordinates extracted from the infrared image is $I = (i_1, \dots, i_K)^T$, and this set is a $K \times 2$ -dimensional matrix. The set of feature-point coordinates extracted from the visible image is $V = (v_1, \dots, v_L)^T$, and this set is a $L \times 2$ -dimensional matrix; K and L are not necessarily equal. The feature points extracted from the two images have their own feature descriptors.

First, the Euclidean distance between each pair of feature descriptors is calculated and the ratio between the nearest neighbor and the next neighbor Euclidean distance is compared with the set threshold to determine whether it is a valid matching pair. The feature point whose coordinates are i_K is selected, and the Euclidean distance between all the feature points in the point set V and the given point calculated. The closest point is recorded as v_{m1} , and the distance of the feature point is recorded as d_{m1} . The next closest point is recorded as v_{m2} , and the distance between feature points is recorded as d_{m2} . The distance ratio between the closest and the next closest feature points is defined as:

$$R = \frac{d_{m1}}{d_{m2}} \tag{7}$$

Obviously, $R \le 1$. The smaller the value of R, the greater the difference between the nearest neighbor distance and the second neighbor distance.

Therefore, it can be shown that the similarity between feature points i_K and v_{m1} is very high, and the possibility of correct matching is high. On the contrary, it means that the similarity between the feature points x_K and v_{m1} is not high, and it is most likely not a valid match. Firstly, whether it is a valid match is judged by setting a reasonable threshold. We set the threshold *R* to 0.8.

Then, the improved offset consistency theory is introduced. Suppose two pairs of IR and visible image matching points are given, $I_1(x_1, y_1), I_2(x_2, y_2)$ and $V_1(m_1, n_1), V_2(m_2, n_2)$, respectively. If the following equation is satisfied, the two pairs of matching points are considered as correct matching points.

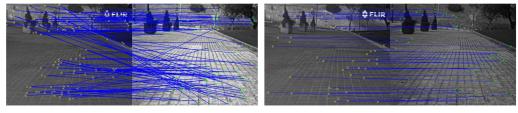
$$\left[\left|\theta_{I_2,V_2} - \theta_{I_1,V_1}\right| \times \left(d_{I_2,V_2} - d_{I_1,V_1}\right)\right] \le T$$
(8)

where *T* is a manually set threshold constant, $\{\theta_{I_i,V_i}, i = 1, 2\}$ and $\{d_{I_i,V_i}, i = 1, 2\}$ are calculated as follows.

$$\theta_{I_i,V_i} = \arctan\left(\frac{n_i - y_i}{m_i - x_i}\right), i = 1, 2$$
(9)

$$d_{I_i,V_i} = \sqrt{(m_i - x_i)^2 + (n_i - y_i)^2}, i = 1, 2$$
(10)

Finally, the matching points with higher positioning accuracy can be obtained by iterative screening using the RANSAC algorithm. After the above two steps, most of the erroneous matching points in the candidate matching can be removed. However, a few erroneous matching points with insignificant differences still remain. This part of the wrong matching points accounts for a small proportion of the total matching points. However, to pursue higher matching-point positioning accuracy, we use the RANSAC algorithm for iterative screening to obtain matching points with higher positioning accuracy. The results of the initial matching are shown in Figure 5a. Figure 5b shows the result after optimization by our proposed matching algorithm.



(a) Initial matching result

(b) Final matching result

Figure 5. Schematic diagram of the initial and final lines connecting a set of infrared and visible image matching points. After the optimization of our proposed feature-point matching algorithm, most of the wrong matching points were eliminated.

4. Experimental Analysis

To verify the effectiveness of our proposed registration method, we compare it with three other state-of-the-art infrared and visible image-registration methods. The three methods are: EG-SURF [51], LPM [52] and SI-PIIFD [53]. All comparative experiments were run on the same computer, and the experimental environment was as follows: CPU Intel i7-7820X, RAM 16GB, Windows 10 system.

4.1. Dataset

In experiments, we qualitatively and quantitatively compare four infrared and visible image-registration methods using the CVC Multimodal Stereo Dataset [54] and a home-made dataset. Among them, the CVC Multimodal Stereo Dataset contains 100 pairs of long-wave infrared and visible images with an image resolution of 506×408 , mainly taken in urban streets. The visible camera model used in the homemade dataset is: MER-031-

300GM/C, the resolution is 640×480 , the focal length is 12 mm, and the HFOV is 22° . The model of the infrared camera is LTWN640, the resolution is 640×480 , the focal length is 13 mm, and the HFOV is 36° . The homemade dataset contains 50 pairs of long-wave infrared and visible images, which are mainly captured in campus scenes. Figure 6 shows samples from both datasets, where the first three columns are from the CVC Multimodal Stereo Dataset and the last two columns are from the homemade dataset.



Figure 6. Samples of CVC and homemade datasets. The first row is the infrared image and the second row is the visible image.

4.2. Evaluation Metrics

To quantitatively evaluate RI-MLM and three other infrared and visible image-registration methods, we used three evaluation metrics, namely, root mean square error (RMSE) [55], correct match rate (CMR) [56] and average runtime (ART) [57].

1. RMSE

The RMSE is to detect the positioning accuracy of feature points, and RMSE is defined as:

$$RMSE = \sqrt{\frac{\sum_{i=1}^{N} \|(x_i - x_i^T) + (y_i - y_i^T)\|_2}{N}}$$
(11)

where (x_i, y_i) is the infrared image feature-point coordinates, (x_i^T, y_i^T) is the corresponding visible image theoretical matching point coordinates, and *N* is the number of matching points.

To distinguish the location of each pair of matching points in the alignment results, $\|(x_i - x_i^T) + (y_i - y_i^T)\|_2 \le 8$ is defined as the correct matching point. The rest are false match points.

2. CMR

To quantitatively evaluate the matching accuracy of the matching method, the CMR evaluation index is introduced. CMR is defined as follows:

$$CMR = \frac{N_{Correct}}{N_{Total}}$$
(12)

where $N_{Correct}$ is the number of correctly matched feature-point pairs, and N_{Total} is the number of all detected feature-point pairs.

3. ART

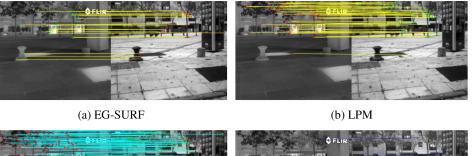
The efficiency of each method is judged by counting the average running time of different infrared and visible image-registration methods on the same experimental platform.

4.3. Experiments on the CVC Dataset

To demonstrate the superiority of our proposed infrared and visible image-registration method, we qualitatively and quantitatively compare the registration performance of the four methods.

4.3.1. Qualitative Evaluation

We show the feature-point matching results of the four registration methods in Figures 7 and 8. The two pairs of images are from the 11th and 30th pairs of images in the CVC dataset, respectively. The left side of each subplot shows the infrared image and the right side shows the visible image. Figures 7a and 8a are from EG-SURF. It can be seen from the figure that there are fewer feature points obtained by EG-SURF, and most of them are concentrated in the upper part of the image. The matching results of feature points extracted by LPM are shown in Figures 7b and 8b. Compared with EG-SURF, LPM obtains more matching feature points. Figures 7c and 8c are the matching results of SI-PIIFD. SI-PIIFD obtains more matching points, but the distribution of matching points is relatively concentrated, which is not conducive to image alignment. In Figures 7d and 8d, our proposed method obtains the most matching points, and the distribution is relatively uniform. It is more convenient in image-alignment work, and the alignment accuracy of images is higher. As we fully consider the overall difference between infrared image and visible image in the process of feature extraction, the extracted feature points are distributed more and more uniformly in the graph. By using the feature-description method based on concentric circles, the rotation invariance and robustness of feature points are improved. As can be seen from Figures 7d and 8d, the matched feature points correspond strictly.





(c) SI-PIIFD

(d) Ours

Figure 7. Feature-matching results on the 11th pair of images in CVC dataset with different methods.

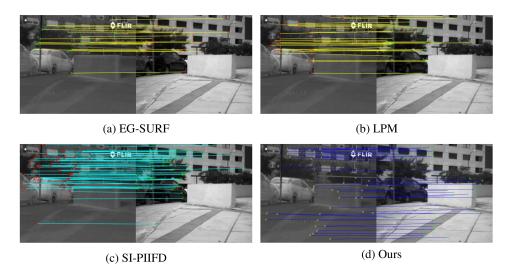


Figure 8. Feature matching results on the 30th pair of images in CVC dataset with different methods.

4.3.2. Quantitative Evaluation

In Figure 9, four registration methods were quantitatively analyzed using RMSE and CMR. Twenty pairs of infrared and visible images were randomly selected from the CVC dataset for analysis. In Figure 9a, we can see that the RMSE values obtained by EG-SURF and LPM are larger, implying lower accuracy of these two registration methods. The RMSE values obtained by SI-PIIFD and our proposed method are relatively close on some image pairs. However, the average RMSE obtained by our proposed method is smaller than that of SI-PIIFD. Therefore, it has higher registration accuracy as we use the feature-description method based on concentric circles to generate robust feature descriptors and improve feature-point location accuracy.

In Figure 9b, the CMR values obtained for EG-SURF, LPM and SI-PIIFD are relatively close, with an average correct match rate close to 50%. However, since we use a multi-level feature-matching method with improved offset consistency, the incorrect matching points are quickly eliminated. As a result, our proposed registration method obtains the highest correct matching rate. It is demonstrated by RMSE and CMR that the accuracy of our proposed registration method is significantly better than the other three.

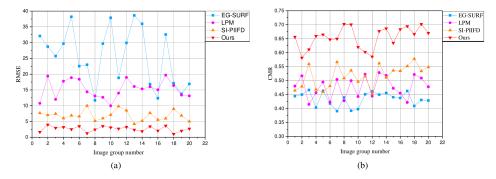


Figure 9. Quantitative comparison of our proposed and other three registration methods on the CVC dataset. (a) RMSE is the root mean square error, which is used to detect the localization accuracy of feature points. The smaller the RMSE value, the higher the localization accuracy of the registration method. (b) CMR is the correct matching rate, which is used to quantitatively evaluate the matching accuracy of the matching method. The larger the CMR value, the better the matching accuracy of the matching method.

The average running times (the average time to complete the registration of 20 pairs of images) of the four registration methods are shown in Table 1. The average running time of EG-SURF is the smallest, indicating that this method has the highest registration efficiency. The average running times of LPM, SI-PIIFD and our proposed method are not very different, and the running efficiency of the registration methods is still lacking.

Table 1. Comparison of the average running time of our proposed and three other registration methods (average time to complete the registration of 20 pairs of images). The smaller the ART, the higher the efficiency of the registration method.

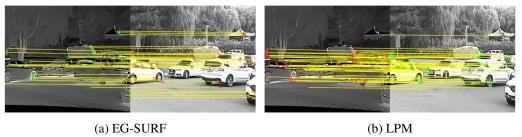
Methods	EG-SURF	LPM	SI-PIIFD	Ours
ART(s)	5.5982	16.2643	15.2845	18.5826

4.4. Experiments on Homemade Datasets

4.4.1. Qualitative Evaluation

In Figures 10 and 11, the registration results of the four registration methods on our homemade dataset are shown, respectively. The two pairs of images are from the 5th and 32nd pairs of images in the homemade dataset, respectively. The left side of each subplot shows the infrared image and the right side shows the visible image. Figures 10d and 11d show the matching results of our proposed registration method. Figures 10a–c and 11a–c

show the matching results of the other three methods, respectively. It can be seen from Figures 10 and 11 that EG-SURF and LPM obtain fewer matching points than the other two methods. In addition, the matching points are densely concentrated in the middle of the image, which is more difficult for the subsequent image-registration process. The matching points of SI-PIIFD and our proposed method are more numerous. However, the matching points of our proposed registration method are more evenly distributed throughout the whole image and most of them are located at critical positions in the image. We propose to match feature points using a multi-level feature-matching algorithm with improved offset consistency. The redesigned matching algorithm achieves a better matching effect. As can be seen from Figures 10d and 11d, our proposed registration method performs better on the homemade dataset.

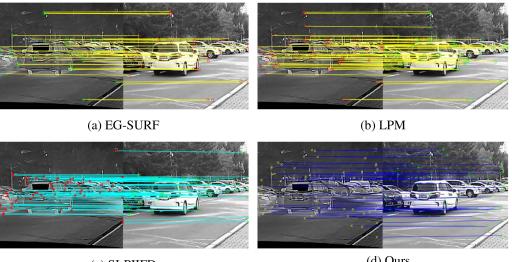




(c) SI-PIIFD

(d) Ours

Figure 10. Feature-matching results on the 5th pair of images in homemade dataset with different methods.



(c) SI-PIIFD

(d) Ours

Figure 11. Feature matching results on the 32nd pair of images in homemade dataset with different methods.

4.4.2. Quantitative Evaluation

Figure 12a,b are the qualitative evaluation results of the four registration methods on the homemade dataset. Figure 12a shows the RMSE values of 10 randomly selected pairs of image-matching points in the homemade dataset. As can be seen from the line Figure 12a, our proposed registration method has a smaller RMSE value compared to the other three registration methods. This also means that the registration point positioning points obtained by our proposed method are more accurate.

The CMR values of the four registration methods are shown in Figure 12b. The CMR value of EG-SURF is the smallest. The CMR values of LPM and SI-PIIFD are relatively close in most cases. It is obvious from Figure 12b that the CMR values of our proposed registration method are significantly improved compared to the other methods. Combining the RMSE and CMR values obtained by the four registration methods, it can be seen that our proposed registration method achieves a better level of localization accuracy and correct matching rate.

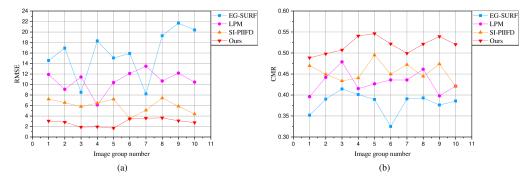


Figure 12. Quantitative comparison of our proposed and other three registration methods on the homemade dataset. (**a**) RMSE is the root mean square error, which is used to detect the localization accuracy of feature points. The smaller the RMSE value, the higher the localization accuracy of the registration method. (**b**) CMR is the correct matching rate, which is used to quantitatively evaluate the matching accuracy of the matching method. The larger the CMR value, the better the matching accuracy of the matching method.

Table 2 shows the average running time of the four registration methods to complete the 10-pair image registration on the homemade dataset. The ART value of EG-SURF is the smallest. Therefore, EG-SURF has the highest running efficiency. The ART values of the other three methods are three times larger than the ART values of EG-SURF. Therefore, the other three methods have lower running efficiency and there is more room for optimization.

Table 2. Comparison of the average running time of our proposed and three other registration methods (average time to complete the registration of 10 pairs of images). The smaller the ART, the higher the efficiency of the registration method.

Methods	EG-SURF	LPM	SI-PIIFD	Ours
ART(s)	3.6854	14.2961	12.5884	13.2691

5. Conclusions

The RI-MFM method proposed in this paper significantly improves the registration accuracy of infrared and visible images. While there are differences in gray distribution and resolution in the source image, the method can accurately and quickly match the extracted effective feature points as we used a concentric-circle-based feature-description algorithm to generate robust feature descriptors. At the same time, a multi-level feature-matching algorithm with improved offset consistency was used in the feature-matching process, which optimizes the positioning accuracy and correct matching rate of matching points. Qualitative and quantitative experimental results on CVC and homemade datasets show that our proposed method performs better than state-of-the-art registration methods.

In the future, we will continue to optimize the computational complexity of the algorithm, speed up the registration speed, and strive to achieve real-time registration as

soon as possible. Meanwhile, the RI-MFM method also needs to achieve more complex work in other aspects of multimodal image registration, such as medical and remote-sensing image registration.

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