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# Effects of Nb Addition on Microstructures and Mechanical Properties of Nb<sub>x</sub>-CoCrFeMnNi High Entropy Alloy Films

Yu-Hsuan Liang, Chia-Lin Li and Chun-Hway Hsueh \*🝺

Department of Materials Science and Engineering, National Taiwan University, Taipei 10617, Taiwan; r07527005@ntu.edu.tw (Y.-H.L.); chialinli@ntu.edu.tw (C.-L.L.)

\* Correspondence: hsuehc@ntu.edu.tw

**Abstract:** In the present work, Nb<sub>x</sub>-CoCrFeMnNi high entropy alloy films (HEAFs, 0 to 7.2 at.% Nb) were fabricated by radio frequency (RF) magnetron co-sputtering of CoCrFeMnNi alloy and Nb targets. The effects of Nb addition on the microstructures and mechanical properties of HEAFs were systematically investigated. For Nb-free film (0 at.% Nb), the face-centered cubic (FCC) peaks were identified in the X-ray diffraction (XRD) pattern. The addition of Nb resulted in a broadening of diffraction peaks, a decrease in peak intensity, and the vanishment of high-angle peaks. Transmission electron microscope (TEM) images indicated the formation of nanotwins at low Nb concentrations, and a transition from a single phase FCC solid solution to an amorphous phase was observed with the increasing Nb concentration. The films were strengthened with an increase in Nb concentration. Specifically, the hardness characterized by nanoindentation increased from 6.5 to 8.1 GPa. The compressive yield strength and fracture strength measured from micropillar compression tests were improved from 1.08 GPs and 2.56 GPa to 2.70 GPa and 5.76 GPa, respectively, whereas the fracture strain decreased from >29.4% (no fracture) to 15.8%. Additionally, shear banding was observed in the presence of amorphous phase.

**Keywords:** high entropy alloy films; Nb addition; microstructure; mechanical properties; nanoindentation; micro-pillar compression tests

# 1. Introduction

Since high entropy alloys (HEAs) were first reported by Yeh et al. [1] and Cantor et al. [2] in 2004, a great deal of research has been designed to investigate their attractive and versatile properties such as excellent strength and ductility [1,3,4], superior cryogenic fracture toughness [5,6], enhanced corrosion resistance [7,8], high wear resistance [9,10], good irradiation resistance [11], and thermal stability [12], etc. Compared to the traditional designs of alloys, which contain one or, rarely, two base elements, HEAs have been defined as alloys consisting of five or more principal elements with each atomic concentration between 5 and 35 at.% with the configuration entropy  $\Delta S$  higher than 1.5 R where R (=8.314 J/mol/K) is the gas constant [1]. Due to the high-entropy effect, the HEAs are favorable to form simple solid solution phases such as a face-centered cubic (FCC) [2,13,14], body-centered cubic (BCC) [4,15,16], or hexagonal close-packed (HCP) [17,18] structure, rather than the brittle intermetallic compounds. A comprehensive review of the concept, complexity, thermodynamics, stabilization, lattice strains, resulting excellent mechanical properties, and the potential for further optimization and applications was recently performed by Cantor [19]. The equiatomic CoCrFeMnNi HEA (i.e., Cantor alloy [2]), one of the most studied HEAs, crystallizes as a single phase FCC solid solution. It possesses high ductility and strength at cryogenic temperatures but shows a limited strength at room temperature [5,13]. Therefore, the enhancement in strength is of paramount importance in order to use CoCrFeMnNi HEAs in industry applications.

Doping another element in the HEAs with different concentrations has been used as an effective method for microstructure modifications and property regulations. Many



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**Copyright:** © 2021 by the authors. Licensee MDPI, Basel, Switzerland. This article is an open access article distributed under the terms and conditions of the Creative Commons Attribution (CC BY) license (https:// creativecommons.org/licenses/by/ 4.0/). HEAs based on CoCrFeMnNi alloy have been investigated in recent years. For instance, He et al. [20] found that the addition of Al into CoCrFeMnNi alloy resulted in a transition from FCC to BCC and increased strength with a sacrifice in ductility. Stepanov et al. [21] reported that the addition of V into CoCrFeMnNi alloy led to the formation of the intermetallic sigma phase, which enhanced the microhardness and yield strength. Qin et al. [22] claimed that the addition of Ti promoted the growth of the second phases (Laves and sigma phases), which played a positive role in improving the yield strength. Since Nb has a negative enthalpy of mixing with the constituent components in CoCrFeMnNi alloy (the mixing enthalpies of Nb with Co, Cr, Fe, Mn, and Ni atomic pairs are -25, -7, -16, -4, and -30 kJ/mol, respectively, [23]), it would favor the formation of second phases or intermetallic compounds in HEAs. In addition, Nb has a massive size (Nb: 0.143 nm) as compared to the five base elements (0.124 to 0.128 nm), which would result in a large atomic size mismatch and lattice distortion. As a result, the characteristics of Nb have received extensive attention, and some research has proved the improved mechanical properties with the Nb addition. For example, Qin et al. indicated that the volume fraction of second phase in  $(CoCrFeMnNi)_{100-x}Nb_x$  increased with an increase in Nb content (0 to 16 at.%), and the yield strength was improved from 202 to 1010 MPa, whereas the fracture strain was reduced from 60% (no fracture) to 12% [22]. In Braeckman et al.'s work [24,25], Nb<sub>x</sub>-CoCrCuFeNi thin films deposited by magnetron sputtering displayed high hardness. As a result of the formation of nanocomposite in the presence of heavy solute elements such as Nb, the nanocomposite could give rise to an increase in hardness. Other researches, such as CoCrFeNiNb<sub>x</sub> [26,27], AlCoCrFeNb<sub>x</sub>Ni [28], CoFeNi<sub>2</sub>V<sub>0.5</sub>Nb<sub>0.75</sub> [29], and CoCrCuFeNiNb<sub>x</sub> [30], also proved that adequately doping Nb into the base alloy could show its strengthening characteristics. It is worth noting that, by adding rare earth elements (Sm) and refractive elements (Zr, Ti) in the AlCoFeNiSmTiVZr system and using the selective laser melting technique, excellent mechanical and corrosion resistant properties of HEAs could be obtained [31,32].

High entropy alloy films (HEAFs) have also attracted extensive research attention over the last decade due to their unique mechanical properties. The recent research and development of HEAFs, including basic concept, preparation technologies, microstructures, appealing properties, applications and suggested future research work, have been reviewed by Li et al. [33]. Several studies have claimed that the HEAFs have a higher yield strength and hardness compared with their bulk counterparts [33–38]. Apart from the difference in mechanical properties, distinctive phase transformations have also been observed in HEAFs. Different from second phases commonly formed in bulk HEAs, amorphous phases are usually found in HEAFs fabricated by magnetron sputtering when the solute concentration exceeds the certain threshold [37,39]. Braeckman et al. reported that the transformations of  $Ge_x$ -CoCrCuFeNi and  $In_x$ -CoCrCuFeNi HEAFs from FCC to the amorphous phase with an increasing additive concentration were driven by thermodynamic and topological factors, respectively [39].

In this work, a series of Nb<sub>x</sub>-CoCrFeMnNi HEAFs synthesized by radio frequency (RF) magnetron co-sputtering, a PVD process to control the accurate compositions with the homogenous distribution, was designed. In addition, the differences between Nb<sub>x</sub>-CoCrFeMnNi HEAFs and their bulk counterparts were compared. To provide an insight into the influence of Nb addition on the microstructures and mechanical properties of the HEAFs, a systematic investigation was carried out using X-ray diffraction (XRD), scanning electron microscopy (SEM), transmission electron microscope (TEM), and nanoindentation and micro-pillar compression tests.

#### 2. Materials and Methods

#### 2.1. Fabrication of Nb<sub>x</sub>-CoCrFeMnNi HEAFs

 $Nb_x$ -CoCrFeMnNi HEAFs were deposited on 0.55 mm thick (111)-oriented silicon substrates by RF magnetron co-sputtering of CoCrFeMnNi alloy and Nb targets. Both targets, with a diameter of 76 mm and thickness of 6 mm, were prepared by vacuum

arc melting with 99.99 wt.% pure elements. Before the deposition process, the silicon substrates were ultrasonically cleaned and rinsed in acetone, ethanol, and deionized water sequentially for 15 min in each step. To reduce any contamination on the surface and to equilibrate the surface composition of the two targets, argon ion bombardment was conducted with 100 W in RF mode for at least 30 min before film deposition. After the high vacuum below  $5 \times 10^{-5}$  Pa was maintained, the 99.9% pure argon gas was introduced at a flow rate of 20 sccm. The working distance and working pressure were fixed at 10 cm and 0.4 Pa, respectively. The rotation speed of the substrate was set at 40 rpm to ensure a homogeneous film thickness and composition. The film composition was regulated by the different powers applied on the target. The power applied on CoCrFeMnNi alloy target was fixed at 400 W, and the different powers applied on the Nb target were regulated, respectively, at 0, 20, 30, 40, and 60 W. All the films were deposited at room temperature for 1 h, and the film thicknesses ranging from 1.8 to 2.0  $\mu$ m were obtained.

#### 2.2. Characterization of Composition and Structure

The chemical composition, surface morphology, and film thickness of the films were determined by a field-emission scanning electron microscope (SEM, NOVA NANO SEM 450, FEI, Hillsboro, OR, USA) with an energy dispersive X-ray spectroscope (EDS, Oxford, UK). The average values of the chemical composition were measured in more than six regions of the films to ensure the reliability of the data. The crystalline structures of the films were examined by a glancing-incidence (1°) X-ray diffraction (XRD, Rigaku TTRAX 3, Tokyo, Japan) with Cu-K $\alpha$  radiation ( $\lambda = 0.15406$  nm), an acceleration voltage of 50 kV, and a working current of 250 mA. The XRD patterns were recorded at room temperature in the angular range (2 $\theta$ ) of 20–100° with the scanning speed of 4°/min. The microstructures of the films were analyzed by transmission electron microscope (TEM, FEI Tecnai G2 F20, Hillsboro, OR, USA) at 200 keV accelerating voltage. Specimens for TEM investigation and micropillar compression tests were prepared by a dual-beam focused ion beam (FIB, FEI Quanta 3D FEG, Hillsboro, OR, OR, OR, OR, Oregon, USA). Before the film was milled, the surface was protected from ion beam damage using deposition of Pt protective layer. The EDS-mapping measurement in TEM was used to confirm the distribution of each element in the films.

## 2.3. Characterization of Mechanical Properties

The hardness and reduced Young's modulus of the films were measured using nanoindentation (Hysitron TI 950 TriboIndenter, Bruker, Billerica, MA, USA) with a Berkovich diamond indenter tip (tip radius of 150 nm). All tests were performed under the displacementcontrolled mode with a rate of 14 nm/s to a depth of 70 nm and a holding time of 5 s between loading and unloading. The penetration depth was less than 1/10 of the film thickness to avoid any influence from the silicon substrate. Each datum was the average from at least seven measurements. The engineering compressive yield strength, fracture strength, fracture strain, and deformation behavior of the films were characterized by the in-situ SEM micro-pillar compression tests. The tests were performed at room temperature under the displacement-rate-controlled mode at a nominal strain rate of  $1 \times 10^{-3}$ /s with the picoindenter (Hysitron PI 85 SEM PicoIndenter, Bruker, Billerica, MA, USA) equipped with a diamond flat-punch tip (tip radius of 2.5 µm). Three micropillars were prepared for each composition. The micropillars with an aspect ratio (the ratio of length to diameter) of ~2.5 and a taper angle of  $<3^{\circ}$  were fabricated. Firstly, a large pillar with a diameter of ~4  $\mu$ m was shaped using coarse FIB milling (Ga<sup>+</sup> ion source at 30 keV voltage and 3 nA current). Then, fine milling was performed with Ga<sup>+</sup> ion voltage of 5 keV and a current of 16 pA to form the micropillar with a diameter ranging from 563 to 708 nm. It is worth noting that an alternative bottom-up method could be used for the pillar formation. Specifically, nano-pillars could be formed by electrochemical deposition on through-hole porous anodic aluminum oxide membranes [40–42].

# 3. Results and Discussion

## 3.1. Compositions and Structures

The chemical compositions (at.%) of the CoCrFeMnNi alloy target measured by EDS were  $20.1\% \pm 1.1\%$  of Co,  $19.6\% \pm 0.9\%$  of Cr,  $19.9\% \pm 1.4\%$  of Fe,  $22.0\% \pm 0.7\%$  of Mn, and  $18.4\% \pm 0.8\%$  of Ni. The molar ratio of each element was close to equimolar. The Nb concentrations (0 to 7.2 at.%) of the Nb<sub>x</sub>-CoCrFeMnNi HEAFs were regulated by the different powers applied on the Nb target, and their chemical compositions measured by EDS are listed in Table 1. The concentration of Nb increased with the increasing power applied on the Nb target.

**Table 1.** Chemical compositions of  $Nb_x$ -CoCrFeMnNi HEAFs with different powers applied on the Nb target.

Power on	Power on	Chemical Composition (at.%)					
Target (W)	Target (W)	Nb	Со	Cr	Fe	Mn	Ni
	0	0	$\begin{array}{c} 21.7 \\ \pm \ 0.2 \end{array}$	$\begin{array}{c} 18.1 \\ \pm \ 0.1 \end{array}$	$\begin{array}{c} 20.9 \\ \pm \ 0.1 \end{array}$	$\begin{array}{c} 18.0 \\ \pm \ 0.2 \end{array}$	$\begin{array}{c} 21.3 \\ \pm \ 0.1 \end{array}$
400	20	$\begin{array}{c} 0.6 \\ \pm \ 0.1 \end{array}$	$\begin{array}{c} 19.5 \\ \pm \ 0.1 \end{array}$	$\begin{array}{c} 18.7 \\ \pm \ 0.1 \end{array}$	$\begin{array}{c} 20.0 \\ \pm \ 0.2 \end{array}$	$\begin{array}{c} 21.6 \\ \pm \ 0.2 \end{array}$	$\begin{array}{c} 19.7 \\ \pm \ 0.3 \end{array}$
	30	$\begin{array}{c} 1.8 \\ \pm \ 0.1 \end{array}$	$\begin{array}{c} 20.1 \\ \pm 1.1 \end{array}$	$\begin{array}{c} 18.6 \\ \pm \ 0.5 \end{array}$	$\begin{array}{c} 21.1 \\ \pm 1.0 \end{array}$	$\begin{array}{c} 19.2 \\ \pm \ 0.8 \end{array}$	$\begin{array}{c} 19.2 \\ \pm \ 0.7 \end{array}$
	40	$\begin{array}{c} 4.1 \\ \pm \ 0.0 \end{array}$	$\begin{array}{c} 19.3 \\ \pm \ 0.5 \end{array}$	$\begin{array}{c} 19.4 \\ \pm \ 0.3 \end{array}$	$\begin{array}{c} 20.5 \\ \pm \ 0.1 \end{array}$	$\begin{array}{c} 17.9 \\ \pm \ 0.2 \end{array}$	$\begin{array}{c} 18.9 \\ \pm \ 0.3 \end{array}$
	60	$\begin{array}{c} 7.2 \\ \pm \ 0.0 \end{array}$	$\begin{array}{c} 18.8 \\ \pm \ 0.2 \end{array}$	$\begin{array}{c} 17.9 \\ \pm \ 0.3 \end{array}$	$\begin{array}{c} 19.7 \\ \pm \ 0.2 \end{array}$	$\begin{array}{c} 17.2 \\ \pm \ 0.7 \end{array}$	$\begin{array}{c} 19.1 \\ \pm \ 0.4 \end{array}$

The cross-sections of the films were examined using FE-SEM to observe the morphology and to measure the film thickness, as shown in Figure 1a–e. An extremely thin layer resulting from the scraping and break separation process of the specimen was observed on the top surface of each film, and it was also observed previously in the cross-sections of ZrNi films on Si substrates prepared by notching and breaking [43]. All the films showed good bonding with substrates. Figure 1a reveals that the fracture surface of the Nb-free film (0 at.% Nb) was composed of three layers. Region 1 showed dimples on the fracture surface, signifying ductile fracture, while regions 2 and 3 displayed a relatively smooth and crack-free morphology. The detailed microstructure evolution of the film during sputter deposition has been studied elsewhere [44,45]. Specifically, Wang et al. [44] also observed the three-layer structure from the TEM images and selected area diffraction patterns of the CoCrFeMnNi HEAF with a thickness of 1400 nm. In their case, region 3 consisted of an amorphous structure with a small amount of nanocrystals, region 2 had the single crystal structure with nanotwins, and region 1 consisted of nanotwinned columnar grains perpendicular to the substrate surface with a preferred (111) orientation. In the present study, as the Nb atoms were added in the film, the large atoms of Nb promoted the pinning effect [46]. The Nb atoms pinned on the substrate favored the formation of clusters with the same lattice orientation [44,46], forming only a single layer in the films (Figure 1b–e). Figure 1b revealed that the film with 0.6 at.% Nb had a nanosized columnar morphology. Figure 1c-e revealed that the films with higher Nb concentrations (1.8, 4.1 and 7.2 at.% Nb) transformed to a relatively dense and smooth morphology.

(a)

 $1 \mu m$ 

(d)

Film

thickness

1\_μm

1821 nm

Si substrate



Figure 1. FE-SEM cross-section micrographs of the Nb<sub>x</sub>-CoCrFeMnNi HEAFs with various Nb concentrations: (a) 0, (b) 0.6, (c) 1.8, (d) 4.1, and (e) 7.2 at.%. (f) The deposition rate as a function of the sputtering power applied on the Nb target.

1837 nm

Si substrate

Film

thickness

1 μm

The deposition rate could be calculated from the measured thickness divided by the deposition time, and the deposition rate as a function of the sputtering power applied on the Nb target is shown in Figure 1f. Basically, a higher sputtering power would lead to a higher sputtering yield to generate more atoms from the target and give rise to an increase in film thickness. However, the highest deposition rate of 33.1 nm/min occurred in the Nb-free film, and it decreased to ~30.6 nm/min as the power applied on the Nb target increased from 0 to 60 W, which may be explained by the following. An increase in the power applied on the Nb target would raise the production of the Nb atoms in the chamber, resulting in a decrease in the mean free path of the gas molecules. Additionally, the big atomic size of Nb atoms increased the chance of atom collisions, which would hinder the arrival of atoms on the substrate and retard the deposition of the film [47,48].

20 30 40 60 100 140

Power on Nb target (W)

Figure 2 shows the XRD patterns of  $Nb_x$ -CoCrFeMnNi HEAFs (0 to 7.2 at.%). The crystal structure of the Nb-free film was a single phase FCC solid solution associated with the sharp and strong (111) peak and high-angle weak (200), (220), and (311) peaks because of the high-entropy effect. It was clear that the addition of Nb resulted in the broadening of the diffraction peak, a decrease in the (111) peak intensity, and the vanishment of the higher angle diffraction peaks. Compared with the bulk  $Nb_x$ -CoCrFeMnNi HEA [22], the films in the present study were prepared by magnetron sputtering process, which is a rapid quenching method to limit the diffusion of elements and inhibit the grain growth to obtain the smaller grain sizes and produce the metastable solid solution without the presence of Laves phase or any precipitates. The full width at half maximum (FWHM) of the diffraction peak significantly increased from  $0.47^{\circ}$  to  $4.72^{\circ}$  with the initial addition of Nb (0.6 at.% Nb), and then slightly increased to 5.02° with the further increase in Nb concentration (7.2 at.% Nb) resulting from the formation of amorphous phase. Moreover, the great difference in atomic size between Nb and CoCrFeMnNi alloy tended to induce severe lattice distortion and caused the instability of crystalline structures.



Figure 2. XRD patterns of the Nb<sub>x</sub>-CoCrFeMnNi HEAFs.

### 3.2. Microstructures

The microstructures of the cross-sections of Nb<sub>x</sub>-CoCrFeMnNi HEAFs and the corresponding selected area electron diffraction (SAED) patterns were characterized by TEM, as shown in Figure 3. Nano-sized columnar grains with the similar orientation and the single phase FCC solid solution were observed in the Nb-free film (Figure 3a), and the columnar growth direction was perpendicular to the substrate surface during the sputtering process. In Figure 3b, the nanotwins were observed in the film with 0.6 at.% Nb. The formation of nanotwins was mainly due to the atomic peening effect [49,50]. Since Nb atom was two times heavier than Ar atom, the atomic peening effect was highly enhanced. More backscattered Ar atoms were introduced with the increasing power applied on the Nb target [25]. These energetic particles stroke the substrate and caused bombardments on the film, leading to an increase in compressive stress and the formation of defects in the film and inducing the formation of nanotwins [51,52]. The HRTEM image of the film with 0.6 at.% Nb and the corresponding fast Fourier transform (FFT) image are shown in Figure 4, confirming the thin nanotwins (~4 nm) in the FCC matrix.



**Figure 3.** Cross-section bright field TEM images and the corresponding SAED patterns of the Nb<sub>x</sub>-CoCrFeMnNi HEAFs with the Nb concentrations of (**a**) 0, (**b**) 0.6, (**c**) 1.8, (**d**) 4.1, and (**e**) 7.2 at.%. (m: matrix, t: twin).



**Figure 4.** The HRTEM image of the film with 0.6 at.% Nb with the corresponding FFT image in the inset. (m: matrix, t: twin).

With the further addition of Nb, the amount of nanotwins decreased and the amorphous phase became dominant. The nanocrystallites embedded in the amorphous matrix could be observed in the films with 1.8 and 4.1 at.% Nb (Figure 3c,d), and the corresponding SAED patterns indicated the decreasing crystalline structure (FCC phase and nanotwins) and the appearance of halo rings. No crystallites were detected in the film with 7.2 at.% Nb, and this film was fully amorphous (Figure 3e). Hence, with the increasing Nb concentration in the film, the microstructures of the films transformed from a single FCC phase (Figure 3a,b) to a mixture of FCC phase and amorphous phase (Figure 3c,d), and to a totally amorphous phase (Figure 3e).

The molar ratio of each element was close to equimolar. The Nb concentrations (0 to 7.2 at.%) of the Nb<sub>x</sub>-CoCrFeMnNi HEAFs were regulated by the different powers applied on the Nb target, and their chemical compositions measured by EDS are listed in Table 1.

The concentration of Nb increased with the increasing power applied on the Nb target. The tendency of crystalline-to-amorphous configuration could be attributed to two factors. First is the atomic size mismatch ( $\delta$ ) of the film, defined as [53,54]:

$$\delta = \sqrt{\sum_{i=1}^{N} c_i \left(1 - \frac{r_i}{\sum_{j=1}^{N} c_j r_j}\right)^2} \tag{1}$$

where *N* is the number of constituent elements in the HEA,  $c_i$  and  $r_i$  are the atomic fraction and radius of element *i*, respectively. Since Nb has a massive size (Nb: 0.143 nm) as compared to the five base elements (0.124 to 0.128 nm), the addition of Nb would lead to an increase in atomic size mismatch from 1.11% (for 0 at.% Nb) to 3.62% (for 7.2 at.% Nb), as listed in Table 2. The significant atomic size mismatch and the fast cooling rate during film deposition could validate the topological instability and promote the formation of the amorphous phase. Second, on the basis of Braeckman et al.'s study [39], the large negative mixing enthalpies of Nb–TM (TM = transition metals) atomic pairs, as listed in Table 3, stabilize the amorphous phase. The TEM results also agreed with the XRD experimental results, both showing a transition from a single phase FCC solid solution to an amorphous phase with an increasing Nb concentration in Nb<sub>x</sub>-CoCrFeMnNi HEAFs.

**Table 2.** The atomic size mismatch ( $\delta$ ) of Nb<sub>x</sub>-CoCrFeMnNi HEAFs with different Nb concentrations.

Nb Concentration (at.%)	Atomic Size Mismatch ( $\delta$ )
0	1.11%
0.6	1.52%
1.8	2.10%
4.1	2.87%
7.2	3.62%

	Table 3. Mixing	enthalpies	of different atom	pairs $\Delta H_{AB}^{mix}$	(kJ/mol)	[23]
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Element (Atomic Size, Young's Modulus)	Со	Cr	Fe	Mn	Ni	Nb
Co (0.125 nm, 211 GPa)	-	-4	-1	-5	0	-25
Cr (0.128 nm, 279 GPa)		-	-1	2	-7	-7
Fe (0.126 nm, 208 GPa)			-	0	-2	-16
Mn (0.127 nm, 191 GPa)				-	-8	-4
Ni (0.124 nm, 200 GPa)					-	-30
Nb (0.143 nm, 105 GPa)						-

Figure 5a shows the cross-section bright field TEM image of the film with 1.8 at.% Nb, and Figure 5b shows the elemental distributions of Co, Cr, Fe, Mn, Ni, and Nb in the framed area in Figure 5a. As evidently observed from these images, the constituent elements were uniformly distributed without the presence of any second phase or precipitate.



**Figure 5.** (**a**) The cross-section bright field TEM image of the film with 1.8 at.% Nb and (**b**) elemental distributions of Co, Cr, Fe, Mn, Ni, and Nb in the framed area in (**a**).

## 3.3. Mechanical Properties

The hardness and reduced Young's modulus of the Nb<sub>x</sub>-CoCrFeMnNi HEAFs were measured by nanoindentation based on the Oliver and Pharr method [55], and the results are presented in Figure 6a,b as functions of the power applied on Nb target and the Nb concentration, respectively. The hardness increased from 6.5 to 8.1 GPa when the Nb concentration increased from 0 to 7.2 at.%. Strengthening of Nb<sub>x</sub>-CoCrFeMnNi HEAFs shown in the present study could be attributed to the following:

- Grain boundary strengthening (Hall–Petch relation): The tendency of forming smaller grains in the films with Nb addition could be observed in the XRD results. According to the classical Hall–Petch relation, the grain boundary strengthening increased with the decreasing grain size [35];
- (ii) Solid solution strengthening: The solid solution strengthening was introduced by the lattice distortion which was relevant to the atomic size mismatch [35,56]. Since Nb had a large atomic radius, doping Nb into CoCrFeMnNi HEAFs contributed to the increase in atomic size mismatch (see Table 2) that enhanced the solid solution effect.



**Figure 6.** The hardness (*H*) and reduced Young's modulus ( $E_r$ ) of Nb<sub>x</sub>-CoCrFeMnNi HEAFs as functions of (**a**) the power applied on Nb target and (**b**) Nb concentration.

The Young's moduli of the constituent elements in Nb<sub>x</sub>-CoCrFeMnNi are also listed in Table 3. Since Nb exhibited the lowest Young's modulus of the six constituents [57], the reduced Young's modulus decreased with the addition of Nb in the film.

To further characterize the mechanical properties of Nb<sub>x</sub>-CoCrFeMnNi HEAFs, in-situ micropillar compression tests were performed. Figure 7a–e shows the SEM images of as-compressed micropillars with different Nb concentrations from 0 to 7.2 at.%. As shown in Figure 7, except for the micropillars of the films with 0 and 0.6 at.% Nb, the other films (1.8, 4.1, and 7.2 at.% Nb) showed the increasing shear bands with the increasing Nb

concentration after compression. This was attributed to the differences in microstructures in these micropillars. During the plastic deformation, the amorphous phase, not having well-defined defects as the crystalline structure, would lead to the formation of shear bands [58–60].



Figure 7. SEM images of as-compressed micropillars for (a) 0, (b) 0.6, (c) 1.8, (d) 4.1, and (e) 7.2 at.% Nb.

The engineering compressive stress-strain curves of Nb<sub>x</sub>-CoCrFeMnNi HEAFs subjected to micropillar compression tests are plotted in Figure 8. Distinct from typical curves, slight serrations were observed in micropillar with 1.8 at.% Nb and heavy serrations were observed in micropillars with 4.1 and 7.2 at.% Nb. Each strain burst in serrated curves indicated a shear band propagation, and this result agreed with the SEM images shown in Figure 7. The compressive yield strength values in these micropillars were evaluated using the 0.2% offset method. The fracture strength and the fracture strain were obtained, respectively, from the maximum load and the corresponding strain of the stress-strain curve. All the measured values are listed in Table 4. As shown in Figure 8, a tendency of the increasing yield strength and fracture strength was observed with the increasing Nb concentration in the films. The yield strength and fracture strength were improved from 1.08 GPa and 2.56 GPa for 0 at.% Nb to 2.70 GPa and 5.76 GPa for 7.2 at.% Nb, respectively. However, suffering from the strength–ductility trade-off, the fracture strain reduced from >29.4% (no fracture) for 0 at.% Nb to 15.8% for 7.2 at.% Nb. For the bulk materials in Qin et al.'s study [22], the yield strength of  $(CoCrFeMnNi)_{100-x}Nb_x$  HEA was improved with the increasing Nb concentration (0.2 GPa at 0 at.% Nb to 1.01 GPa at 16 at.% Nb). It could be seen that the films possessed a much higher yield strength than their bulk counterparts.





**Table 4.** The compressive yield strength ( $\sigma_y$ ), fracture strength ( $\sigma_f$ ), and fracture strain ( $\varepsilon_f$ ) of Nb<sub>x</sub>-CoCrFeMnNi HEAFs.

Thin Films (at.% Nb)	$\sigma_y$ (GPa)	σ <sub>f</sub> (GPa)	ε <sub>f</sub> (%)
0	1.08	2.56	>29.4
0.6	1.15	3.69	>35
1.8	2.25	4.36	32.3
4.1	2.08	4.33	24.8
7.2	2.70	5.76	15.8

# 4. Conclusions

The Nb<sub>x</sub>-CoCrFeMnNi HEAFs were successfully prepared by magnetron co-sputtering. The effects of Nb addition on the microstructures and mechanical properties of HEAFs were systematically investigated, and the following conclusions could be drawn:

- (1) The structure transferred from a single phase FCC solid solution to an amorphous phase with an increasing Nb concentration in the films. The Nb-free film was a single phase FCC solid solution phase. The films with 1.8 and 4.1 at.% Nb showed nanocrystals embedded in amorphous matrix, while the films with 7.2 at.% Nb completely transferred to an amorphous phase;
- (2) Nanotwins were first found in the film with 0.6 at.% Nb, and the disappearance of nanotwins was observed with the further increase in Nb concentration as the amorphous phase became dominant;
- (3) The nanoindentation results showed an increase in the hardness of the film with an increasing Nb concentration. The hardness increased from 6.5 GPa to 8.1 GPa as the Nb concentration increased from 0 to 7.2 at.%;
- (4) The micropillar compression tests indicated the strengthening of the films with the increasing Nb concentration. From 0 to 7.2 at.% Nb, the compressive yield strength and fracture strength increased from 1.08 GPa and 2.56 GPa to 2.70 GPa and 5.76 GPa, respectively. However, the fracture strain reduced from >29.4% (no fracture) to 15.8% due to the strength–ductility trade-off. Additionally, shear bands were observed in the presence of the amorphous phase.

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