## Article

## Supplementary

## Control of Lateral Composition Distribution in Partitioned Dual-Beam Pulsed Laser Deposition

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## Model for Simulation



Figure S1: Coordinate system used for the simulation of trajectories of ejected particles from a single target. The point of coordinate $(X, Y)=(0,0)$ represents the laser spot on the target surface. $(0,50)$ corresponds to the center of the substrate.

In order to figure out the thickness distribution obtained in the single target ablation experiment of $\mathrm{CeO}_{2}$ (Section 3.1), the trajectories of particles ablated from a single target to reach the substrate surface under various conditions (pressure $p_{\mathrm{O} 2}$ and gap $G$ ) were simulated by a Monte Carlo method. Figure S1 shows the coordinate system used for the calculation. Expecting qualitative results, we constructed a primitive model to represent the ablation process on the basis of assumptions described below.

1) In the two-dimensional $(X, Y)$ space (Figure S1), the particles ejected from the point $(0,0)$ on the target surface repeatedly experience elastic collisions with the ambient gas molecules until reaching the substrate surface $(Y=X / 5+50)$.
2) The path length between collisions, $L_{n}$, and the change in the direction caused by the collision, $\theta_{n}$, obey normal distributions [S1]. Here, the subscript $n$ indicates the number of collision, except $n=0$ that denotes the ejection from the target.
3) The path length between the ejecting point $(0,0)$ to the first collision point, $L$, is 1.5 mm in average [S2]. The standard deviation for $L_{n}$ is $L_{n} / 5$ for all $n$ including 0 .
4) The distribution of the ejection angle $\theta_{0}$ is centered on the target normal, with a standard deviation $\sigma_{\theta 0}$ of $11.4^{\circ}$ [S3].
5) After the first collision ( $n \geq 1$ ), collisions with ambient gas molecules dominate the movement of the particles. Mean free path in air is adopted as the averaged path length between collisions, $L_{n}(n \geq 1) . L_{n}$ (in mm) is obtained from the pressure $p_{02}$ (in Torr) using

$$
\begin{equation*}
\log L_{n}=a \log p_{\mathrm{O} 2}+b \tag{1}
\end{equation*}
$$

where $a$ and $b$ were taken as -1 and -1.3 [S4].
6) The distribution of $\theta_{n}(n \geq 1)$ is with the mean of $0^{\circ}$ and the standard deviation $\sigma_{\theta n}$ of $6^{\circ}$ [S5].
7) For the particle that falls behind the target surface or that collides with the partition, the calculation is stopped at that moment and is not counted into the results.
The $X$ coordinate of each particle at the instant it arrived at the substrate's surface was recorded. For each combination of $p_{02}$ and $G$, the calculation was done for $6 \times 10^{6}$ ejected particles to obtain the thickness distribution.

## References

1 A number of studies have reported that the thickness distribution of conventional PLD processes (without partition) is fitted with $\cos ^{N} \theta[\mathrm{~S} 6-\mathrm{S} 8]$. In the present simulation, however, $\cos ^{N} \theta$ is approximated by normal distribution in order to simplify the calculation.
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3 A previous study on the film thickness distribution in ablation from an oxide $\mathrm{MO}_{x}(\mathrm{M}: \mathrm{Al}, \mathrm{Hf}, \mathrm{Y})$ target has revealed that $N$ depends on the pressure $p$, the atomic weight $m$ of the metallic element M , and the direction of distribution (whether it is in parallel or perpendicular to the longitudinal axis of the laser spot) [S8]. In the case of $\mathrm{Ce}(m=140 \mathrm{u})$, in parallel with the longitudinal axis of the laser spot, and $p$ of zero, we estimate $N$ to be 25 on the basis of the results in ref.[S8]. The normal distribution with $\sigma \theta 0$ of 11.4 gives the same full width at half maximum as $\cos ^{25} \theta$.

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5 The $\sigma \theta n$ of $6^{\circ}$ is estimated from the maximum scattering angle of a Ce atom ( 140 u ) that elastically collides with a stationary $\mathrm{O}_{2}$ molecule ( 32 u ), which is calculated to be $13.2^{\circ}$.
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