



# Article Hierarchical Multi-Scale Coupled Periodical Photonic and Plasmonic Nanopatterns Inscribed by Femtosecond Laser Pulses in Lithium Niobate

Sergey Kudryashov <sup>1,2,\*</sup>, Alexey Rupasov <sup>1</sup>, Mikhail Kosobokov <sup>2</sup>, Andrey Akhmatkhanov <sup>2</sup>, George Krasin <sup>1</sup>, Pavel Danilov <sup>1,2</sup>, Boris Lisjikh <sup>2</sup>, Alexander Abramov <sup>2</sup>, Evgeny Greshnyakov <sup>2</sup>, Evgeny Kuzmin <sup>1</sup>, Michael Kovalev <sup>1,2</sup>, and Vladimir Shur <sup>2</sup>

- <sup>1</sup> Lebedev Physical Institute, 119991 Moscow, Russia
- <sup>2</sup> School of Natural Sciences and Mathematics, Ural Federal University, 620000 Ekaterinburg, Russia
  - Correspondence: kudryashovsi@lebedev.ru

Abstract: The ultrafast interaction of tightly focused femtosecond laser pulses with bulk dielectric media in direct laser writing (inscription) regimes is known to proceed via complex multi-scale light, plasma and material modification nanopatterns, which are challenging for exploration owing to their mesoscopic, transient and buried character. In this study, we report on the first experimental demonstration, analysis and modeling of hierarchical multi-period coupled longitudinal and transverse nanogratings in bulk lithium niobate inscribed in the focal region by 1030 nm, 300 fs laser pulses in the recently proposed sub-filamentary laser inscription regime. The longitudinal Bragg-like topography nanogratings, possessing the laser-intensity-dependent periods  $\approx 400$  nm, consist of transverse birefringent nanogratings, which are perpendicular to the laser polarization and exhibit much smaller periods  $\approx 160$  nm. Our analysis and modeling support the photonic origin of the longitudinal nanogratings, appearing as prompt electromagnetic and corresponding ionization standing waves in the pre-focal region due to interference of the incident and plasma-reflected laser pulse parts. The transverse nanogratings could be assigned to the nanoscale material modification by interfacial plasmons, excited and interfered in the resulting longitudinal array of the plasma sheets in the bulk dielectric material. Our experimental findings provide strong support for our previously proposed mechanism of such hierarchical laser nanopatterning in bulk dielectrics, giving important insights into its crucial parameters and opening the way for directional harnessing of this technology.

**Keywords:** lithium niobate; femtosecond laser; bulk inscription; hierarchical longitudinal and transverse nanogratings; standing electromagnetic and ionization waves; interference of interfacial plasmons

### 1. Introduction

Flexible ultrashort-pulse laser nanopatterning of bulk dielectrics appears as a key enabling technology for next generations of all-dielectric metamaterial platforms made of multiple stacks of different functional metasurfaces. Though these opportunities for versatile nanoscale light control and manipulation are still emerging, various laser nanopatterning modalities have already been developed to produce in dielectric media high-contrast refractive index structures based on atomistic densification [1,2], two-photon polymerization [3], nano-ablation [4,5], periodic nanoscale material self-organization and form-birefringence [6–8] for well-established applications in direct laser writing (inscription) of light waveguides [9] and more complex functional morphologies [2], hollow optical memory bits [4], microfluidic channels [10] and polarizing optical elements and devices [11–13]. Meanwhile, novel promising nanopatterning modalities based on delicate and precise ultrashort-pulse (femtosecond or picosecond, fs/ps) laser inscription in bulk dielectrics are still under intense scientific studies, being highly challenging for accurate fabrication



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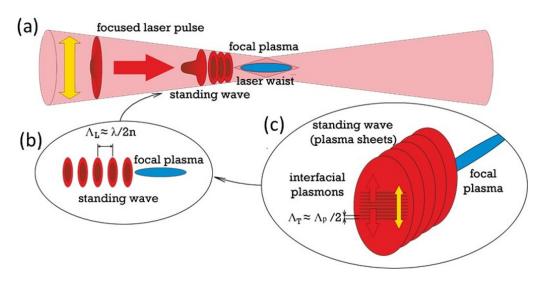
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**Copyright:** © 2022 by the authors. Licensee MDPI, Basel, Switzerland. This article is an open access article distributed under the terms and conditions of the Creative Commons Attribution (CC BY) license (https:// creativecommons.org/licenses/by/ 4.0/). and informative characterization on this dielectric platform because of their mesoscopic, transient and buried character.

Recently, a new ultrashort-pulse laser inscription modality was proposed for hierarchical nanopatterning of bulk dielectrics [14,15], via self-organization of birefringent nanograting arrays (Figure 1), utilizing the flexible combinations of laser wavelengths  $\lambda$ , pulsewidths  $\tau$ , pulse energies E, focusing conditions and diverse dielectric materials—fluorite and fused silica [15,16]. Very surprisingly, such birefringent nanopatterns highly extended along the laser beam waist were observed in a linear (sub-filamentary) focusing regime [14–16], rather than along the extended non-linear (filamentary) focus of ultrashort laser pulses, possessing peak powers well above the critical one for Kerr self-focusing [7,17,18]. The self-organized hierarchical nanopatterns—periodical sub-wavelength longitudinal stacks of transverse nanogratings-were assumed to proceed via four schematic main steps: (1) formation of reflective electron-hole plasma of near-critical density in the linear focus (Figure 1a); (2) longitudinal interference of the reflected and incident linearly polarized pulse parts in the pre-focal region, formation of the near-plane standing electromagnetic wave and the corresponding ionization wave (plasma sheets) with the period  $\Lambda_{\rm L} \approx \lambda/(2n)$  (photonic nanostructure) [14,15] (Figure 1a,b); (3) excitation and interference of interfacial (boundary between weakly/strongly photoexcited dielectric layers) sub-wavelength plasmons (wavelength  $\Lambda_{\rm P} \sim \lambda/n^2 \ll \lambda$  [19]), counter-propagating along or normal to the laser polarization [20] in the pre-focal stack of the near-plane plasma sheets separated by the distance  $\Lambda_{\rm L}$  (Figure 1c); (4) periodical structural modification of the dielectric material and the corresponding modulation of the refractive index in the standing electromagnetic/ionization wave of the interfering plasmons (period  $\Lambda_T \approx \Lambda_P/2$ , ultrafine plasmonic sub-structure of the photonic one) [19,21]. Although elaborate and comprehensive visualization of bulk nanoand microscale patterns produced by ultrashort laser pulses in dielectric media has been performed to the date in a limited number of studies [6–8,12,17,18,22], the assignment of patterns to sub-filamentary or filamentary laser focusing regimes, as well as the detailed topographic analysis of the internal structure as a function of laser wavelength, pulse width and energy/intensity/peak power, is still missing, while the visualization results in different studies are quite contradictory in their pulse energy/power trends. Specifically, comprehensive ultrafine visualization was not performed yet for the abovementioned sub-filamentary ultrashort-pulse laser nanopatterning regime to envision the predicted well-ordered hierarchical nanopatterns [14,15]. Moreover, this new ultrashort-pulse laser hierarchical nanopatterning modality is of interest for inscription of functional nanostructures in other, still unexplored dielectric materials (e.g., polymers, ferroelectrics, etc. [23–27]) regarding its relevance and universal performance. Finally, ultrafine visualization analysis could facilitate new emerging functional applications of the predicted hierarchical nanopatterns in nano-optics, quantum and non-linear optics and material science.

In this study, we present for the first time ultrafine comparative experimental visualization, analysis and modeling of multi-scale internal nano-topographies of hierarchical coupled longitudinal photonic and transverse plasmonic nanopatterns in bulk lithium niobate inscribed in the focal region by tightly focused 1030 nm, 300 fs laser pulses in the sub-filamentary laser inscription regime. Our analysis reveals the slight diminishing laser intensity/plasma density effect on the spatial periods of the *photonic* longitudinal nanopatterns accompanying the standing electromagnetic/ionization waves. Likewise, the total height and stripe number of *plasmonic* transverse birefringent nanogratings increase versus laser intensity, ionizing broader beam aperture across and along the optical path in the waist. These findings enable flexible managing of the internal hierarchical nano-topographies by broad tuning of ultrashort-pulse laser parameters for emerging functional applications.

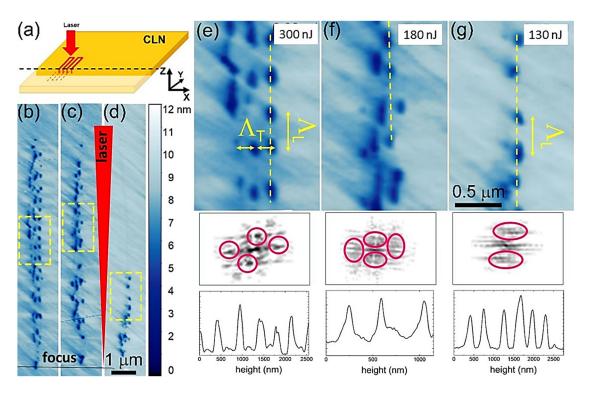


**Figure 1.** (a) Schematic of fs-laser-induced focal plasma and pre-focal electromagnetic/ionization standing waves (yellow arrow—laser polarization direction). (b) Structure of the standing wave of electromagnetic field and plasma sheets. (c) Transverse plasmonic sub-structure of the plasma sheet array.

#### 2. Materials and Methods

In these studies, we used a congruent lithium niobate (CLN) crystalline z-cut plate with its spontaneous polarization parallel to the z-axis (Figure 2a). For laser-induced bulk nanopatterning of the CLN crystal, a 3D-micro/nanostructuring laser workstation based on the femtosecond Yb-doped fiber laser system Satsuma (Amplitude Systemes, France) with the fundamental wavelength  $\lambda = 1030$  nm (TEM<sub>00</sub>), full-width at half-maximum pulse duration  $\tau \approx 300$  fs, variable pulse energy  $E \le 10 \mu$ J and repetition rate f = 0-500 kHz was employed. The laser pulses were focused by a 0.65 NA micro-objective lens into the 1/e-intensity radius  $w_0 = 1.2 \pm 0.1 \mu$ m at the depth ~60 µm inside the lithium niobate crystal. The sample was mounted on a PC-driven high-precision three-dimensional (XYZ) motorized micro-positioning translation stage (Prior Scientific, UK) and scanned at the translation speed of 400 µm/s, enabling inscription at different delivered energies E = 50-300 nJ (peak power  $P \approx 0.17$ –1.0 MW and peak fluence  $F \approx 1$ –8 J/cm<sup>2</sup>) in the sub-filamentary (linear focusing) regime ( $P \le P_{crit} = 0.9 \pm 0.1$  MW for the critical Kerr self-focusing power for z-cut CLN at 1030 nm [23]) 3 mm wide line arrays (series of 3 lines each) with the 3 µm inter-line spacing and the scan direction along the laser polarization.

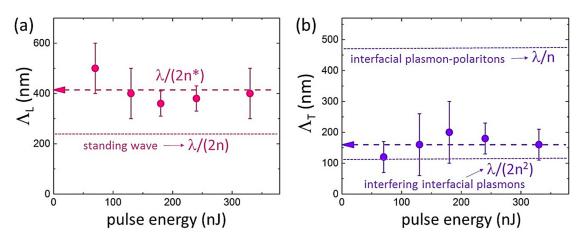
In order to reveal the ultrafine nano-topography of the buried fs-laser nanopatterned CLN regions, the inscribed linear horizontal arrays of vertical nanopatterns in the bulk CLN were saw-cut across the scan lines by an automated precision dicing saw DAD 3220 (DISCO, Japan), using a Disco diamond blade disk Z09-SD3000-Y1-90 55x0.1 A2X40-L (DISCO). The cuts were consequently grinded by Al<sub>2</sub>O<sub>3</sub> powders (grain sizes: 30, 9 and 3 µm) and polished by  $\approx$ 25 nm colloidal SiO<sub>2</sub> nanoparticles on the polishing machine PM5 (Logitech, UK) until optical surface quality. Then, the uncovered topography was characterized by an atomic force microscope NTEGRA Aura (NT-MDT, Russia) in the piezoelectric response mode, using Pt-coated NSC 18 probes (MikroMash, Russia, tip size—30 nm, first resonance frequency—400–500 kHz and stiffness coefficient—2.8 N/m) at the 10-V, 20-kHz probing ac voltage. The acquired surface topographies inscribed at the different fs-laser pulse energies (fluences) are presented in Figure 2b–d along with their two-dimensional (2D) fast Fourier transform (FFT) spectra and longitudinal relief profiles (Figure 2e–g).



**Figure 2.** (a) Optical layout of fs-laser inscription, CLN sample arrangement and its cross cut for AFM characterization. (b–d) Panoramic AFM images of the uncovered longitudinal (vertical) and transverse (horizontal) nanopatterned relief topographies, inscribed at different fs-laser pulse energies of 130, 180 and 300 nJ, respectively. (e–g) (top) Magnified views of the characteristic transverse nanopattern topographies highlighted in (b–d) by yellow dashed frames; (bottom) their 2D FFT spectra and longitudinal relief profiles along the yellow dashed lines in (e–g).

## 3. Experimental Results and Discussion

These hierarchical well-organized buried nanopattern topographies, observed for the first time in comparison to laser-inscribed single periodical nano- or micropatterns [6-8,12,17,18,22], exhibit the ultrafine periodical longitudinal pre-focal structure, composed by the periodical transverse one, with the typical nanorelief height  $\sim 10$  nm (Figure 2b–d). In the linear focusing regime, at the higher fs-laser pulse energies the length, L, of the ablatively nanopatterned regions appears larger (the larger pre-focal high-intensity/fluence region above the local ablation threshold) with the larger number of longitudinal nanopatterns N, but with the almost constant sub-wavelength period  $\Lambda_L = L/N \approx 400$  nm (Figures 2a and 3a). Likewise, the number of the transverse nanopatterns increases versus increasing *E* (Figure 2b–f), exhibiting also the almost constant but even smaller sub-wavelength period  $\Lambda_{\rm T} \approx 160$  nm (Figures 2b and 3b). For the same reason, the longitudinal nanopatterns become sharper (less transverse nanopatterns) when farther from the laser focus, with some nano-features less pronounced or stacking faults in the transverse nanopatterns between the neighboring longitudinal stripes. These trends are perfectly consistent with the threshold appearance of the ablative nanopatterns at the fs-laser pulse energies, exceeding the overall ablation threshold pulse energy value  $\approx 50$  nJ (fluence—1.2 J/cm<sup>2</sup>). Furthermore, similar to other sub-filamentary fs-laser-inscribed birefringent nanopatterns in dielectrics [14–16], the nanopatterned regions in CLN exhibit high pulse-energy tunable retardance magnitudes up to  $\lambda/5$ , measured by a birefringence imaging system Thorlabs LCC7201B (not shown).



**Figure 3.** (a) Periods of longitudinal ( $\Lambda_L$ , violet symbols) and (b) transverse ( $\Lambda_T$ , pink symbols) nanopatterns versus fs-laser pulse energy. The corresponding colored dashed lines indicate the average  $\Lambda_L$  and  $\Lambda_T$  magnitudes, while dotted lines indicate the expected longitudinal nanopattern period  $\lambda/(2n) \approx 235$  nm in (a), and the expected transverse nanopattern periods for interfacial plasmon-polaritons  $\lambda/n \approx 470$  nm and for interfering interfacial plasmons  $\lambda/(2n^2) \approx 110$  nm in (b).

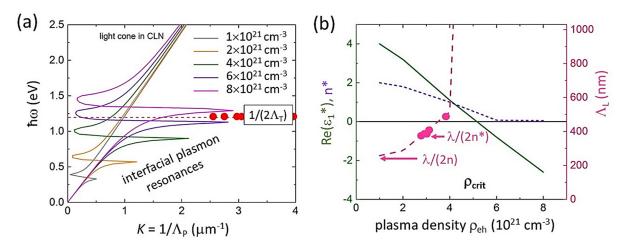
Surprisingly, both the measured longitudinal photonic and transverse plasmonic nanopattern periods  $\Lambda_L$ ,  $\Lambda_T$  exhibit deeply sub-wavelength scales, while the former quantity ( $\approx$ 400 nm) considerably differs from the expected magnitude  $\lambda/(2n) \approx 235$  nm (where  $n \approx 2.15$  is the ordinary wave refractive index value at the 1030 nm wavelength in CLN [28]) for the standing electromagnetic wave in the bulk dielectric. This effect could be associated with the spatially continuous prompt electron-hole plasma (EHP) diminishing of the real part of the dielectric function in the photoexcited CLN, Re[ $\epsilon^*$ ] (and the corresponding refractive index value n\*), along the pre-focal laser interference region. To obtain insight into the intriguing sub-wavelength scales of the longitudinal and transverse nanopattern periods,  $\Lambda_L$  and  $\Lambda_T$ , respectively, the prompt dielectric function of the photoexcited CLN was modeled as a function of EHP density  $\rho_{eh}$  and optical frequency  $\Omega$  in the following form [29]:

$$\varepsilon^*(\Omega, \rho_{eh}) = \varepsilon(\Omega) \left( 1 - \frac{\rho_{eh}}{\rho_{sat}} \right) - \frac{\Omega_{PL}^2(\rho_{eh})}{\Omega^2 + \nu(\rho_{eh})^2} \left( 1 - \frac{i\nu(\rho_{eh})}{\Omega} \right) \tag{1}$$

where the EHP frequency  $\Omega_{PL}(\rho_{eh})$  and scattering rate  $\nu(\rho_{eh})$  were evaluated as follows [21]:

$$\Omega_{PL}^{2}(\rho_{eh}) = \frac{\rho_{eh}e^{2}}{\varepsilon_{0}\varepsilon_{hf}(\rho_{eh})m_{opt}^{*}}, \ \nu(\Omega,\rho_{eh}) = \left(\frac{\pi^{2}\sqrt{3}}{128E_{F}^{2}}\right)\frac{(\pi k_{B}T_{e})^{2} + (\hbar\Omega)^{2}}{1 + \exp\left(\frac{-\hbar\Omega}{k_{B}T_{e}}\right)}\Omega_{PL}(\rho_{eh}) \propto C\Omega_{PL}(\rho_{eh})^{\prime}$$
(2)

accounting for the effective optical EHP mass  $m_{\text{opt}}^*$ , the high-frequency dielectric constant  $\varepsilon_{\text{hf}}(\rho_{\text{eh}})$  due to EHP screening tending to 1 at near-critical EHP densities  $\rho_{\text{eh}} \sim \rho_{\text{crit}} (\rho_{\text{crit}} \approx 5 \times 10^{21} \text{ cm}^{-3}$  in CLN at 1030-nm wavelength, Figure 4b), defined from Equation (1) as  $\Omega_{\text{PL}}(\rho_{\text{crit}}) = \sqrt{\varepsilon(\Omega)} \Omega$ , EHP saturation density for interband transitions  $\rho_{\text{sat}}$ , temperature  $T_{\text{e}}$  and Fermi level  $E_{\text{F}}$  and the numerical factor  $C \sim 10$  in different dielectrics [15,19,21,30]. See the other calculation details in Supplementary Materials.



**Figure 4.** (a) Color dispersion curves  $\hbar\omega$ -K of interfacial plasmons in CLN at different e-h plasma densities in the range of (1–8) × 10<sup>21</sup> cm<sup>-3</sup> and mapping of the plasmon resonance at 1030 nm (1.2 eV), using the experimental 1/(2 $\Lambda$ <sub>T</sub>) values (red circles). (b) Left axis: dependences of Re( $\varepsilon$ \*) (green curve) and n\* (violet dot curve) at 1030 nm on  $\rho_{eh}$ ; right axis: calculated periods  $\lambda/(2n^*)$  (pink dashed curve) in comparison to experimental values  $\Lambda_L$  (pink circles) versus  $\rho_{eh}$ .

Then, the dielectric function  $\varepsilon^*(\Omega, \rho_{eh})$  was used to evaluate the wavenumber  $K = 1/\Lambda_P$  of plasmons, propagating at the "weakly/strongly photoexcited CLN" interface of the plasma sheets in the pre-focal region, through the common dispersion relationship for surface (here—interfacial, IPP) plasmon-polaritons [31]:

$$K = \Re e \left( \frac{1}{\lambda} \sqrt{\frac{\varepsilon * \varepsilon}{\varepsilon * + \varepsilon}} \right)$$
(3)

where the complex dielectric functions of the photoexcited and unexcited CLN are  $\varepsilon^*(\Omega, \rho_{eh})$ and  $\varepsilon(\Omega)$ , respectively. The results of our calculations of IPP dispersion curves, utilizing the complete form of Equation (3) [32], which was previously successfully applied in SPP simulations for different metals, semiconductors and dielectrics immersed in various dielectric media [15,19,33], are given in Figure 4a.

The calculated dispersion curves demonstrate a series of the interfacial plasmon resonances, raising in their energy versus the increasing EHP density  $\rho_{eh} = (1-8) \times 10^{21} \text{ cm}^{-3}$  (Figure 4a). Particularly, the plasmon resonance approaches 1.2-eV energy (laser wavelength—1030 nm) at the densities  $(6-8) \times 10^{21} \text{ cm}^{-3}$ , where  $\varepsilon^*(1.2 \text{ eV}, \rho_{eh} > \rho_{crit}) \approx -\varepsilon(1.2 \text{ eV})$  as the basic requirement for the interfacial plasmonic resonance [31]. The experimental data values  $1/(2\Lambda_T)$  are reasonably mapping the IPP resonances in Figure 4a; moreover, these experimental values  $\Lambda_T$  are also reasonably consistent with the transverse nanopattern periods, the expected periods for interfering undamped interfacial plasmons  $\lambda/(2n^2) \approx 110 \text{ nm}$  [19] (Figure 3b), rather than for interfacial plasmon-polaritons  $\lambda/n \approx 470 \text{ nm}$ .

Finally, these simulations enable to evaluate the quasi-continuous component of the EHP density in the pre-focal laser interference region, which decreases the local Re( $\epsilon^*$ ) and n\* magnitudes to result in the longitudinal nanopattern periods  $\lambda/(2n^*) \approx 400$  nm, rather than  $\lambda/(2n) \approx 235$  nm (Figures 3a and 4b). The evaluated EHP density (Figure 4b) is reasonably subcritical,  $\rho_{eh} \approx 3 \times 10^{21}$  cm<sup>-3</sup> <  $\rho_{crit}$ , to enable microscale laser penetration and interference in the plasma.

## 4. Conclusions

In this study, hierarchical nanopatterning by ultrashort laser pulses was for the first time observed in the bulk dielectric material (crystalline lithium niobate) in the linear focusing (sub-filamentary) regime, exhibiting the longitudinal *photonic* nanopatterns with the period of  $\approx$  400 nm, consisting of transverse *plasmonic* nanopatterns with the period

of  $\approx$  160 nm. The related analysis and modeling indicate the interference (standing wave) photonic origin of the longitudinal nanopatterns in the pre-focal sub-critical electron-hole plasma, while in the interference maxima plasma density approaches near-critical magnitudes, supporting excitation of deeply sub-wavelength interfacial plasmons at the dielectric/plasma interfaces. These results provide important insights into our previously proposed mechanism of such hierarchical sub-filamentary laser nanopatterning in bulk dielectrics and uncover novel opportunities of its advanced applications in nano-optics, quantum and non-linear optics and material science.

**Supplementary Materials:** The following supporting information can be downloaded at: https://www.mdpi.com/article/10.3390/nano12234303/s1, References [34–39] are cited in the Supplementary Materials.

**Author Contributions:** Conceptualization, S.K. and V.S.; methodology, M.K. (Mikhail Kosobokov); formal analysis, E.K.; validation, A.A. (Andrey Akhmatkhanov); investigation, A.R., G.K. and P.D.; writing—original draft preparation, S.K.; writing—review and editing, S.K., M.K. (Mikhail Kosobokov), A.A. (Andrey Akhmatkhanov) and V.S.; visualization, B.L., A.A. (Alexander Abramov) and E.G.; supervision, M.K. (Michael Kovalev); project administration, A.A. (Andrey Akhmatkhanov); funding acquisition, V.S. All authors have read and agreed to the published version of the manuscript.

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