

## Supplementary Material

# Investigation of the Stability and Hydrogen Evolution Activity of Dual-Atom Catalysts on Nitrogen-Doped Graphene

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## Methodologies

We calculated the formation energy of two types of vacancy sites in graphene substrate structures to determine their stability ( $E_f$ ) [54]:

$$E_f = E_{sub} + x\mu_C - E_G - y\mu_N \quad (1)$$

In the formula,  $E_{sub}$  is the total energy of SVGN<sub>3</sub> or 4N-doped double-vacancies graphene (DVG<sub>N4</sub>);  $E_G$  is the total energy of pristine graphene substrate structure;  $x$  is the number of carbon atoms that were removed from the pristine graphene;  $\mu_C$  is the chemical potential of carbon, defined as the total energy of each carbon atom in the pristine graphene;  $y$  is the number of embedded N atoms;  $\mu_N$  is the chemical potential of nitrogen (defined as half of the total energy of the N<sub>2</sub> molecule). As the formation energy of SVGN<sub>3</sub> is 3.50 eV [55] and that of DVG<sub>N4</sub> is 3.88 eV, we will choose SVGN<sub>3</sub> as the study object.

## Tables

**Table S1.** Testing the binding energy ( $E_b$ ) under several functional (PBE, RPBE, PBE+D3) for 3d elements.

	$E_b/\text{eV(PBE)}$	$E_b/\text{eV(RPBE)}$	$E_b/\text{eV(PBE+D3)}$
TiG	-1.98	-1.28	-1.98
TiGN <sub>3</sub>	-6.29	-5.94	-6.45
Ti <sub>2</sub> GN <sub>3</sub>	-9.92	-8.90	-9.92
VG	-1.20	-0.84	-1.20
VGN <sub>3</sub>	-5.80	-5.32	-5.80
V <sub>2</sub> GN <sub>3</sub>	-7.79	-6.84	-7.79
CrG	-0.31	-0.09	-0.31
CrGN <sub>3</sub>	-3.73	-3.25	-3.73
Cr <sub>2</sub> GN <sub>3</sub>	-5.70	-4.71	-5.70
MnG	-0.23	0.04	-0.27
MnGN <sub>3</sub>	-3.98	-3.51	-3.98
Mn <sub>2</sub> GN <sub>3</sub>	-5.75	-3.99	-5.75
FeG	-1.17	-0.49	1.13
FeGN <sub>3</sub>	-4.57	-3.67	-4.82
Fe <sub>2</sub> GN <sub>3</sub>	-7.21	-4.95	-7.15
CoG	-1.24	-0.99	-1.17
CoGN <sub>3</sub>	-4.96	-4.65	-4.89
Co <sub>2</sub> GN <sub>3</sub>	-7.07	-6.81	-6.93
NiG	-1.52	-1.01	-1.52
NiGN <sub>3</sub>	-4.48	-3.90	-4.26
Ni <sub>2</sub> GN <sub>3</sub>	-6.58	-5.76	-6.56
CuG	-0.29	0.00	-0.29
CuGN <sub>3</sub>	-3.12	-2.59	-3.12
Cu <sub>2</sub> GN <sub>3</sub>	-4.54	-3.83	-4.50

**Table S2.** The formation energy of SVGN<sub>3</sub> and DVGN<sub>4</sub>

	SVGN <sub>3</sub>	DVGN <sub>4</sub>
formation energy(eV)	3.50[55]	3.88

**Table S3.** The zero-point energy (ZPE), and entropic correction (TS, T = 298.15K) of H<sub>2</sub>.

Species	ZPE/eV	TS/eV
H <sub>2</sub>	0.269	0.404

**Table S4.** The adsorption energy ( $\Delta E_{H^*}$ ), zero-point energy difference ( $\Delta E_{ZPE}$ ), and entropic correction difference ( $T\Delta S_{H^*}$ ,  $T = 298.15K$ ), Gibbs free energy ( $\Delta G_{H^*}$ ) of H–SACs at a potential  $U = 0$ . The ZPE and entropy of the substrate are negligible.

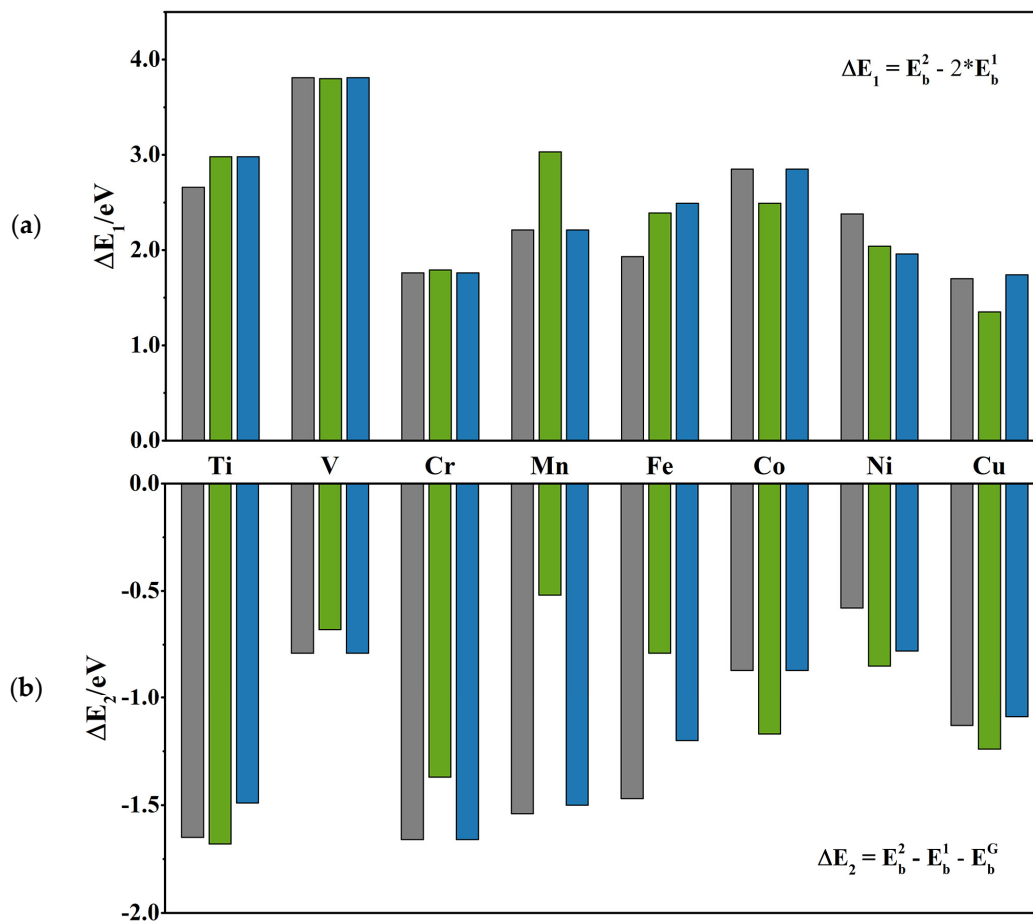
	$\Delta E_{H^*}/\text{eV}$	$\Delta E_{ZPE}/\text{eV}$	$T\Delta S_{H^*}/\text{eV}$	$\Delta G_{H^*}/\text{eV}$
Ti	-0.995	0.0885	-0.189	-0.72
V	-0.665	0.0245	-0.182	-0.46
Cr	-0.595	0.0125	-0.172	-0.41
Mn	-0.485	0.0035	-0.196	-0.29
Fe	-0.675	0.0175	-0.172	-0.49
Co	-0.175	0.0415	-0.180	0.05
Ni	-0.185	0.0495	-0.191	0.06
Cu	0.095	0.0425	-0.032	0.17
Zr	-0.965	0.0025	-0.171	-0.79
Nb	-1.055	0.0205	-0.181	-0.85
Mo	-0.975	0.0385	-0.187	-0.75
Tc	-0.765	0.0425	-0.187	-0.54
Ru	-0.495	0.0545	-0.191	-0.25
Rh	-0.675	0.0765	-0.132	-0.47
Pd	-0.355	0.0755	-0.194	-0.09
Ag	0.365	0.0235	-0.175	0.56
Hf	-1.425	0.0095	-0.174	-1.24
Ta	-1.375	0.0265	-0.181	-1.17
W	-1.425	0.0435	-0.186	-1.20
Re	-1.335	0.0505	-0.187	-1.10
Os	-0.975	0.0405	-0.181	-0.75
Ir	-1.425	0.0805	-0.194	-1.15
Pt	-1.335	0.0775	-0.192	-1.07
Au	-0.935	0.0645	-0.186	-0.68

For H–Co1–SVGN<sub>3</sub> ( $T=298.15K$ ), (1) Geometry optimization is performed first, followed by vibration frequency calculation (releasing H atom; fixing Co, C, and N atoms), and finally, VASPKIT post-processing software calculates the zero-point energy ( $ZEP = 0.176\text{eV}$ ) and entropy ( $TS = 0.022\text{eV}$ ) of the adsorbed hydrogen. (2) Similarly, the zero-point energy ( $ZEP = 0.1345\text{ eV}$ ) and entropy ( $TS = 0.202\text{ eV}$ ) of hydrogen in the gas phase H<sub>2</sub> molecule were calculated. (3) We take the difference between the zero-point energy and the entropy of the adsorbed hydrogen and gas phase hydrogen to get  $\Delta E_{ZPE} = 0.0415\text{eV}$  and  $T\Delta S_{H^*} = -0.180\text{eV}$ . (4) According to the formula  $\Delta G_{H^*} = \Delta E_{H^*} + \Delta E_{ZPE} - T\Delta S_{H^*}$ , the Gibbs free energy of H adsorption in the H–Co1–SVGN<sub>3</sub> system is  $0.05\text{eV}$ , which is consistent with previous work.[38]

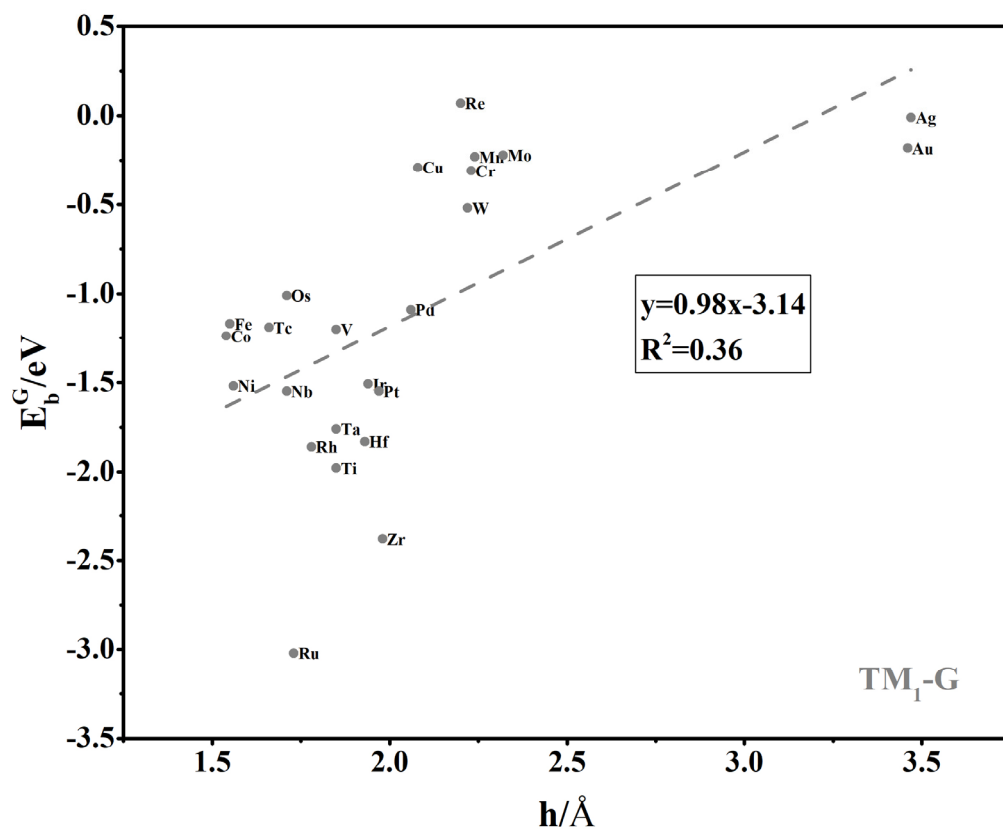
**Table S5.** The adsorption energy ( $\Delta E_{H^*}$ ), zero-point energy difference ( $\Delta E_{ZPE}$ ), and entropic correction difference ( $T\Delta S_{H^*}$ ,  $T = 298.15\text{K}$ ), Gibbs free energy ( $\Delta G_{H^*}$ ) of H–DACs at a potential  $U = 0$ . The ZPE and entropy of the substrate are negligible.

	$\Delta E_{H^*}/\text{eV}$	$\Delta E_{ZPE}/\text{eV}$	$T\Delta S_{H^*}/\text{eV}$	$\Delta G_{H^*}/\text{eV}$
Ti	-0.595	0.1595	-0.202	-0.23
V	-1.335	0.0415	-0.185	-1.11
Cr	-0.605	0.0165	-0.178	-0.41
Mn	-0.345	0.0325	-0.157	-0.16
Fe	-0.545	0.0505	-0.191	-0.30
Co	-0.695	0.0435	-0.184	-0.47
Ni	-0.935	0.0425	-0.182	-0.71
Cu	-1.105	0.0655	-0.188	-0.85
Zr	-0.965	0.0035	-0.169	-0.79
Nb	-1.505	0.0365	-0.189	-1.28
Mo	-0.655	0.0165	-0.179	-0.46
Tc	-1.245	0.0545	-0.192	-1.00
Ru	-0.865	0.0345	-0.167	-0.66
Rh	-0.605	0.0365	-0.191	-0.38
Pd	-0.685	0.0405	-0.189	-0.46
Ag	-0.665	0.0455	-0.186	-0.44
Hf	-1.215	0.0065	-0.169	-1.04
Ta	-1.395	0.0385	-0.189	-1.17
W	-1.255	0.0275	-0.185	-1.04
Re	-0.335	0.0575	-0.189	-0.09
Os	-0.595	0.0605	-0.177	-0.36
Ir	-0.805	0.0615	-0.167	-0.58
Pt	-0.695	0.0545	-0.170	-0.47
Au	-0.665	0.0695	-0.188	-0.40

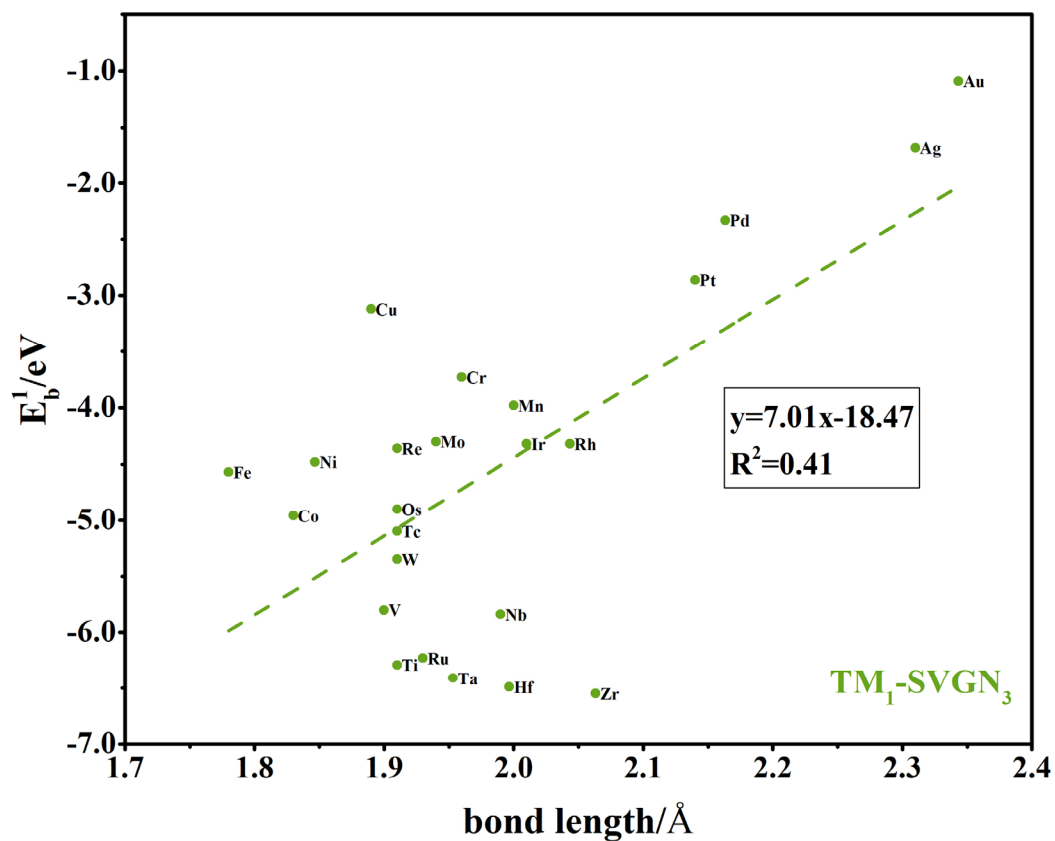
## Figures



**Figure S1.** (a)  $\Delta E_1$  is the difference between  $E_b^2$  and  $2 * E_b^1$ . (b)  $\Delta E_2$  is the difference between  $E_b^2$  and  $(E_b^1 + E_b^G)$ . (Gray, green, and blue histograms represent for PBE, RPBE, and PBE+D3, respectively.)

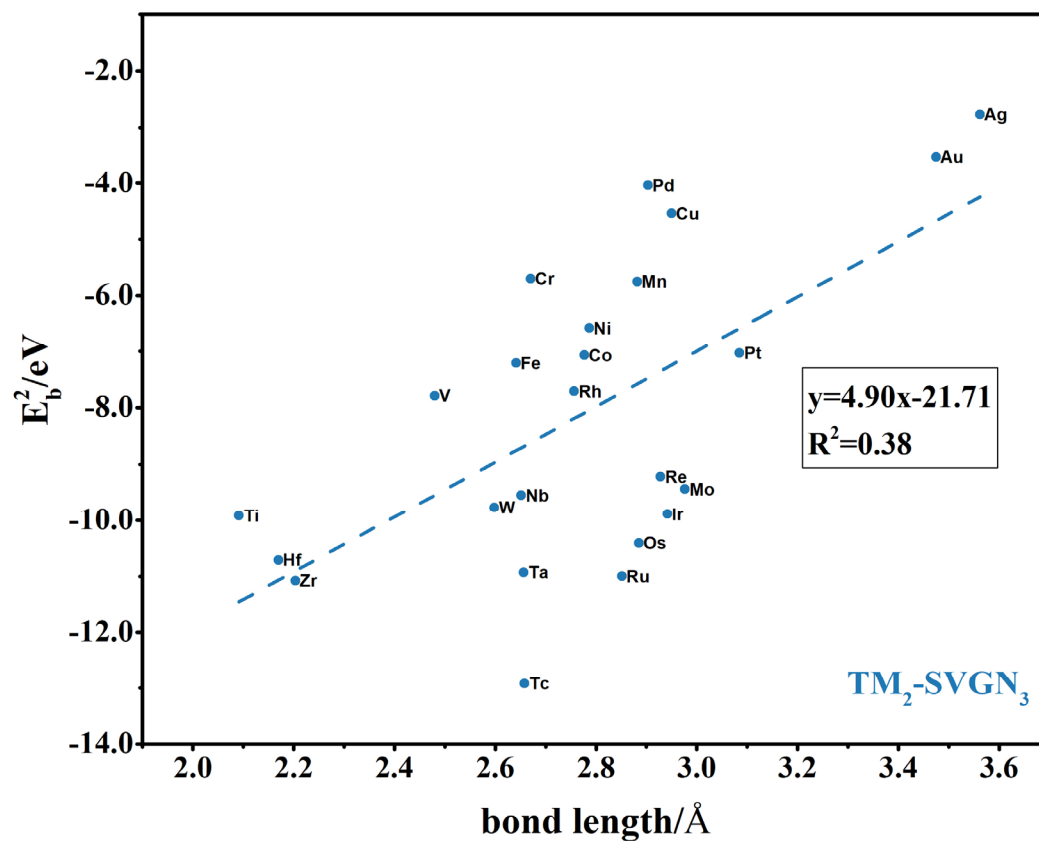


**Figure S2.** Correlation between the height ( $h$ ) from the M1 to the pure graphene and binding energy ( $E_b^G$ ) in TM<sub>1</sub>-G.



**Figure S3.** Correlation between the average distance ( $d_{\text{M1-Nx}}$ ) from the anchored M1 to the N atom and binding energy ( $E_b^1$ ) in  $\text{TM}_1\text{-SVGN}_3$ .





**Figure S4.** Correlation between the average distance ( $d_{\text{M1-Nx}}$  and  $d_{\text{M2-Nx}}$ ) from the dual-atoms (M1 and M2) to the N atom and binding energy ( $E_b^2$ ) in  $\text{TM}_2\text{-SVGN}_3$ .