



# Analysis of the Piezoelectric Properties of Aligned Multi-Walled Carbon Nanotubes

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As we noted before, the occurrence of an elastic strain  $\Delta L$  in the carbon nanotube will lead to the formation of an internal field strength  $E_{def}$  associated with the manifestation of

piezoelectric effect. According to the theory of the piezoelectric effect, the internal field value  $E_{def}$  can be estimated as:

$$E_{def} = \frac{e}{\epsilon_0 \epsilon_{||}} \frac{\Delta L}{L} \quad (1)$$

where  $\epsilon_{||}$  is the longitudinal dielectric constant of a CNT;  $e = \sigma/E$  is the piezoelectric coefficient, and  $\sigma$  is the mechanical stress of the CNT. Under the condition of the formation of tensile deformation, the positive piezoelectric charges are focused on the nanotube top and an internal field strength  $E_{def}$  is directed from the top to the bottom of the nanotube.

When a sawtooth voltage pulse is applied to a strained CNT, a redistribution of deformation  $\Delta L$  and the corresponding internal electric field  $E_{def}$  is observed under the action of the inverse piezoelectric effect. In the region of the current–voltage characteristic (CVC) from  $-3$  to  $3$  V, an additional compressive strain arises ( $\Delta L(t) = \Delta L - \Delta L'(t)$ ) and the value of the corresponding initial internal field  $E_{def}(t)$  decreases. As a result, the resistance of the nanotube decreases and corresponds to the low-resistance state  $R_{LR}$ .

At the time  $t = t_0$  ( $U = 3$  V), there is a jump of  $dU/dt$  and the relaxation of excessive stress. As a result, there is a hysteresis, the area of which is determined by the value of the oppositely directed current density [29]:

$$i(t_0) = (E(t_0) + E_{def}(t_0)) \frac{L \epsilon_0 \epsilon_{||}}{U(t_0)} \frac{dE(t)}{dt} - \frac{\Delta L(t)}{U_{piezo}} \frac{d\sigma(t)}{dt} \quad (2)$$

where  $U_{piezo}$  is the potential corresponding to the strain  $\Delta L$ . As a result, the nanotube switches into a high-resistance state, with resistance  $R(t)$  being proportional to the strain  $\Delta L(t) = \Delta L + \Delta L'(t_0)$ .

In region from  $3$  to  $-3$  V of the CVC, the internal field  $E_{def}(t)$  increases due to additional strain  $\Delta L(t) = \Delta L + \Delta L'(t)$  and partially compensates for the external field  $E(t)$ . At  $U(t) \rightarrow 0$ , the strain  $\Delta L'(t)$  tends to zero and the resistance is determined by the initial strain  $\Delta L$  of the nanotube.

Thus, the redistribution of strain and piezoelectric charge leads to hysteresis in the current–voltage characteristics and the appearance of memristive switching of the strained carbon nanotube.

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