



# Supporting Information

## Synergistic Tribo-Activity of Nanohybrids of Zirconia/ Cerium-Doped Zirconia Nanoparticles with Nano Lamellar Reduced Graphene Oxide and Molybdenum Disulfide

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### S1. Experimental Details

For each experiment arithmetic mean of the diameter of each ball ( $d_1$ ,  $d_2$  and  $d_3$ ) was taken as given by equation (1). The three stationary balls were not disturbed while taking the readings and the wear scar diameter was taken by Image acquisition system.

### Tribological Parameters

#### Mean Wear Scar Diameter (MWD)

$$d = \frac{d_1 + d_2 + d_3}{3} \quad (1)$$

#### Mean Wear Volume (MWV)

$$\text{Wear volume, } V = \frac{\pi d_0^4}{64 r} \left\{ \left( \frac{d}{d_0} \right)^4 - \left( \frac{d_0}{d_0} \right) \right\} \quad (2)$$

$$\text{Hertzian diameter, } d_0 = 2 \left( \frac{3Pr}{4E} \right)^{\frac{1}{3}} \quad (3)$$

$$\text{Where, } \frac{1}{r} = \frac{1}{r_1} + \frac{1}{r_2}$$

$$\frac{1}{E^*} = \frac{1 - \nu_1^2}{E_1} + \frac{1 - \nu_2^2}{E_2}$$

Where,  $E^*$  = Resultant modulus of elasticity

$\nu$  = Poisson's ratio

$r$  = Radius of steel ball

$E_1 = E_2 = 206 \text{ GPa}$

$\nu_1 = \nu_2 = 0.3$

$P$  = Actual load in Newton on each of the three horizontal balls that is 0.408 times of applied load.

### **Wear Rate**

Overall, running-in and steady-state wear rates have been calculated on the basis of observed mean wear volume data at different time intervals. Mean wear volumes at different times (0.25, 0.50, 0.75, 1, 1.25 and 1.5 h) for each experiment were plotted with time and a linear regression model was fitted on the points including origin to find out overall wear rate.

$$\frac{V}{l} = K \frac{P}{H}$$

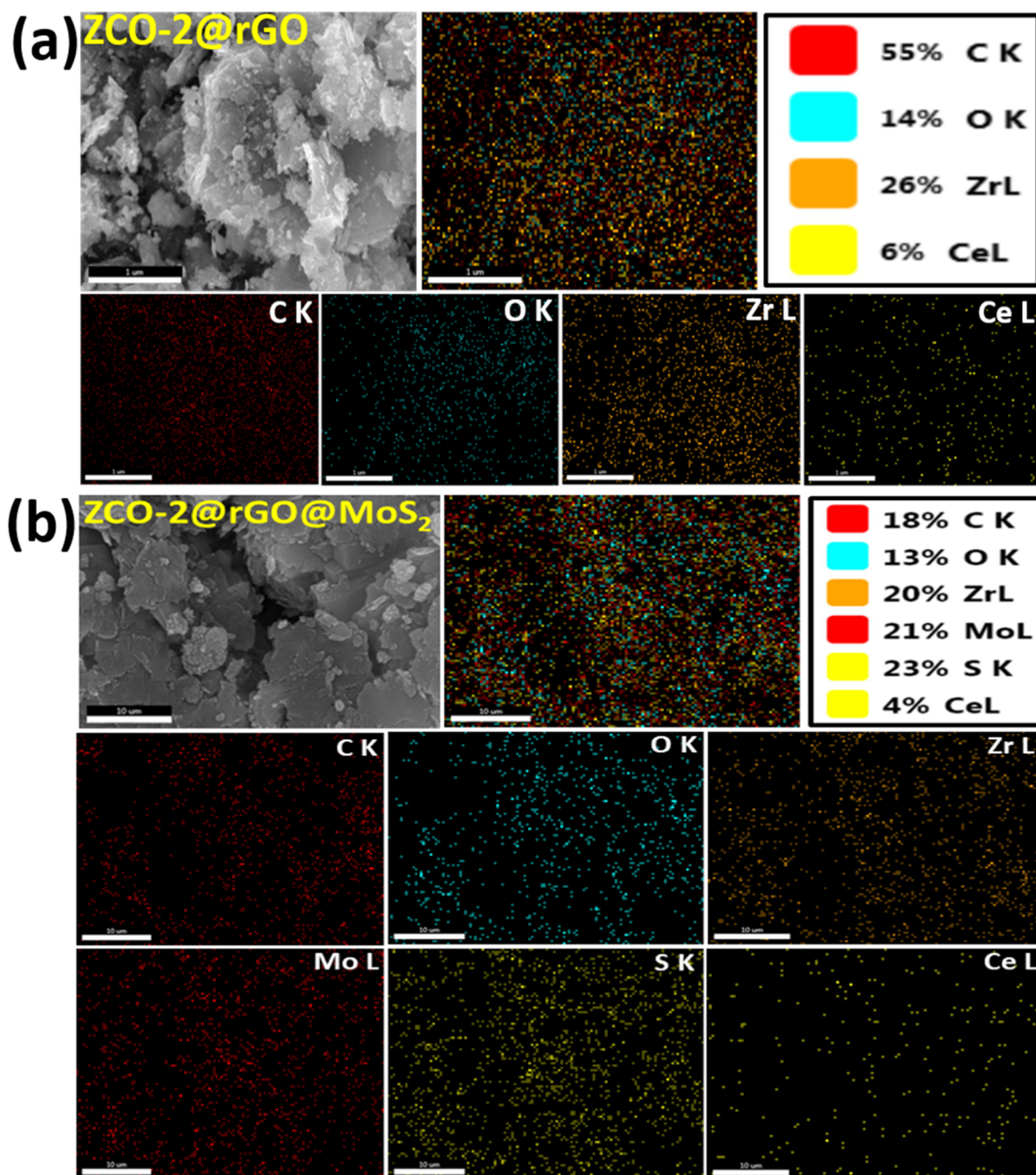
$V$  = mean wear volume

$l$  = sliding distance ( $2\pi r.N$ )

$K$  = wear coefficient

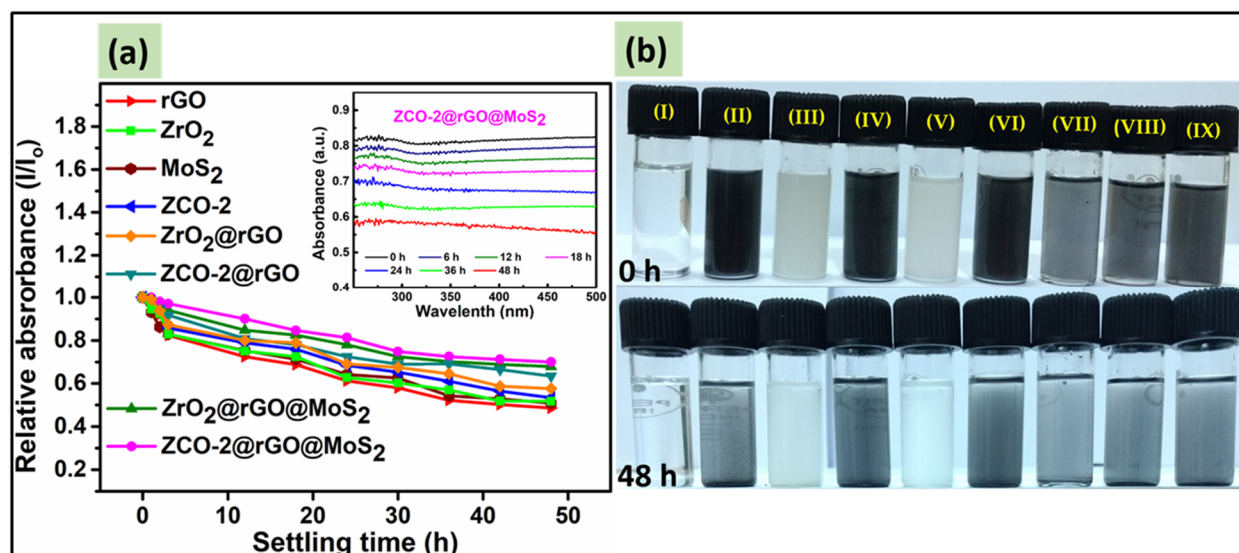
$H$  = hardness of steel ball (59-61 HRC)

$P$  = applied load (0.408x392N)

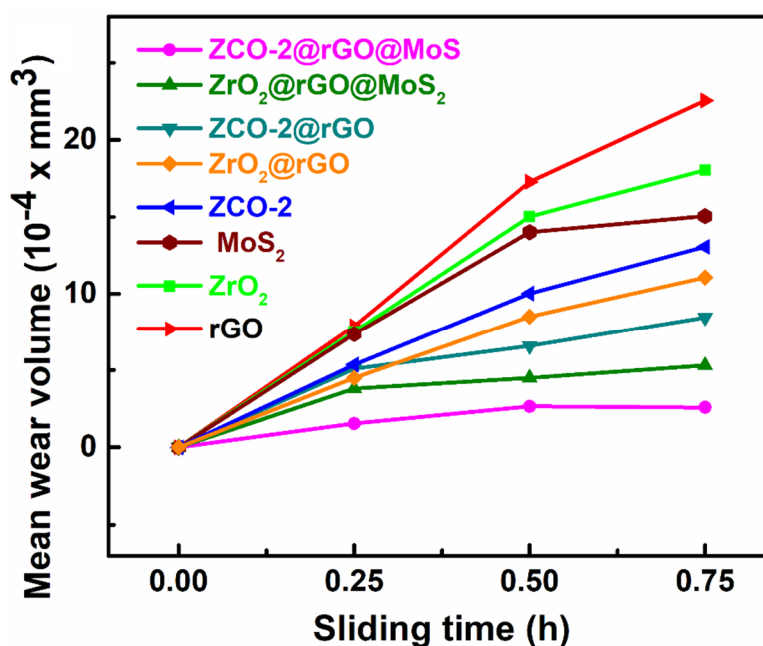


**Figure S1.** EDX elemental mapping of (a) ZCO-2@rGO, and (b) ZCO-2@rGO@MoS<sub>2</sub> nanomaterials.

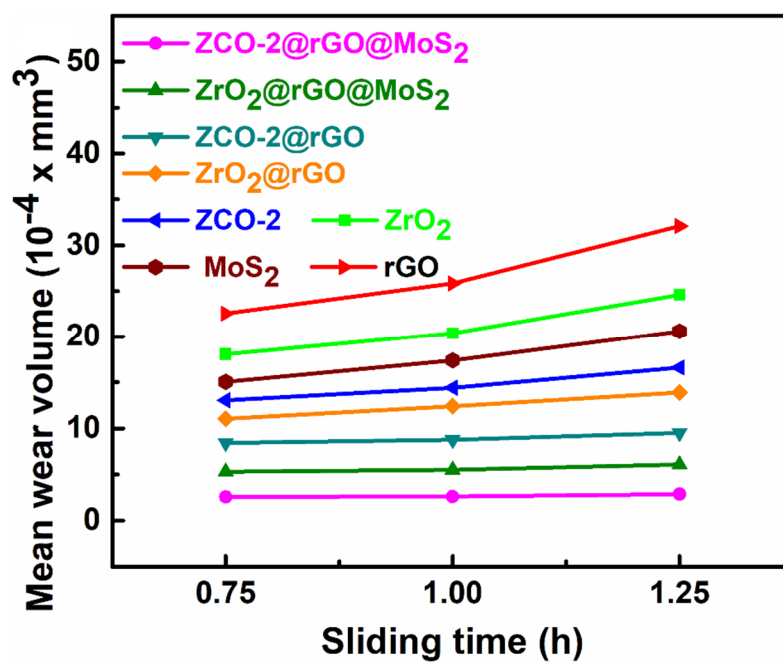
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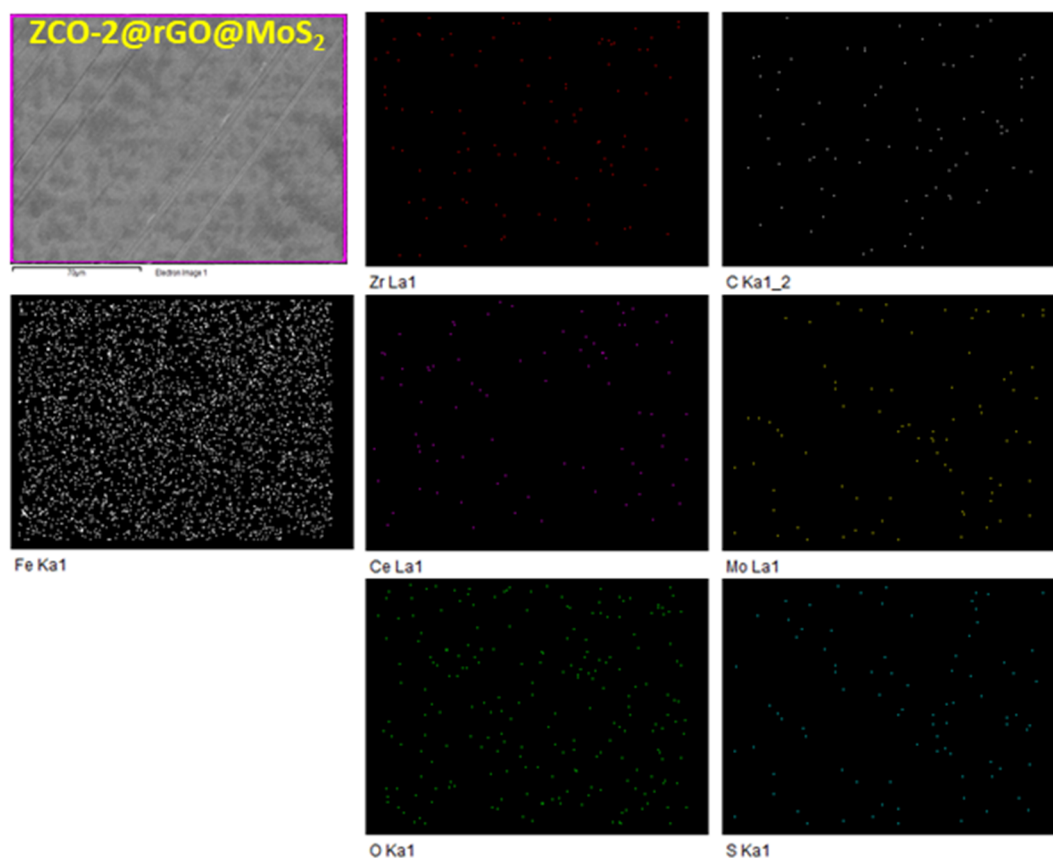
**Figure S2.** (a) Dispersion stabilities of base oil containing rGO, ZrO<sub>2</sub>, MoS<sub>2</sub>, ZCO-2, ZrO<sub>2</sub>@rGO, ZCO-2@rGO, ZrO<sub>2</sub>@rGO@MoS<sub>2</sub> and ZCO-2@rGO@MoS<sub>2</sub> studied by UV-vis spectrophotometry (inset showing a decrease in absorbance of 320 nm band against time). (b) Optical photographs of (I) plain PO, and PO with dispersed nanoadditives (II) rGO, (III) ZrO<sub>2</sub>, (IV) MoS<sub>2</sub>, (V) ZCO-2, (VI) ZrO<sub>2</sub>@rGO, (VII) ZCO-2@rGO, (VIII) ZrO<sub>2</sub>@rGO@MoS<sub>2</sub>, and (IX) ZCO-2@rGO@MoS<sub>2</sub> at zero time and after 48 hours.



**Figure S3.** Determination of running-in wear rate by varying mean wear volume with time (h) for paraffin oil containing (0.125% w/v) nanoadditives at 392 N applied load.



**Figure S4.** Determination of steady-state wear rate by varying mean wear volume with time (h) for paraffin oil containing (0.125% w/v) nanoadditives at 392 N applied load.



**Figure S5.** Elemental mapping of worn surface lubricated with blend of ZCO-2@rGO@MoS<sub>2</sub> nanohybrid in paraffin oil at 392 N applied load.