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Designing Protograph LDPC Codes for Differential Chaotic Bit-Interleaved Coded Modulation System for Underwater Acoustic Communications

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Abstract: Underwater acoustic (UWA) communications face many challenges, such as large multipath delay, severe fading and the time-varying distortions. Chaotic modulations have shown advantages in UWA communications, but the reliability of current chaotic modulations is still not guaranteed. In this paper, a short-length protograph low-density parity-check (P-LDPC) code design framework for the differential chaotic bit-interleaved coded modulation (DC-BICM) system for UWA communication is proposed. This design framework, considering the requirements of short codes in UWA communications, integrates the DC-BICM system, UWA channel and the differential evolutionary code searching algorithm. Through this design framework, the optimized short P-LDPC code can be obtained. Simulation results show that the DC-BICM system with the proposed P-LDPC code can obtain more than 0.48 dB coding gain and reduce 32.6%~69.5% of the average number of iterations compared with the counterparts. Moreover, the reconstructed underwater image with the proposed P-LDPC code is clearest with the highest peak-signal-noise ratio value when compared with counterparts.

Keywords: differential chaos shift keying; bit-interleaved coded modulation; protograph low-density parity-check codes; underwater acoustic communications; short codes



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1. Introduction

Underwater acoustic sensor networks (UASN), as important components of the underwater Internet of Things (UIoT), can strongly support the research for ocean science [1]. In the UASN, underwater acoustic (UWA) communication technology plays an important role in ocean information transmission. However, the current UWA communication technologies suffer from problems such as low throughput, low reliability, and high power consumption [2]. These problems are mainly caused by complicated UWA communication channels, including large multi-path delay, fading and different kinds of time-varying distortions.

Chaotic modulations adopt chaotic waveforms to bear information symbols [3]. Benefiting from anti-fading and anti-interference abilities, chaotic modulations have been considered as a good alternative technology for complex communication applications, including IoT scenarios, wireless body area networks (WBAN) and so on. Chaotic modulation can be clarified into two kinds: coherent and non-coherent. In coherent chaotic communication, chaotic shift keying (CSK) performs well in the price of complexity [4], which is an important factor to be considered in UWA communications. Non-coherent chaotic communications adopt the received signal and its delay version to perform correlation operations

in the non-coherent demodulation process, and the complexity can be reduced effectively in this way [5]. In [6], a robust differential chaos shift keying (DCSK) was proposed, and it was further optimized as a frequency-modulated DCSK (FM-DCSK) [7], which was applied to the image transmission [8] considering only modulation without any other improved image processing method [9]. DCSK has advantages of low cost and low complexity due to the structure of the transmitted reference mode, and this structure does not need channel estimation. Moreover, DCSK is robust to the multi-path fading and time-varied fading environment, which is suitable for the UWA communication environment [10].

Chaotic modulations have shown great potential and progress for UWA communications over the last two decades. A chaotic direct-sequence spread-spectrum (CDSSS) system was designed for UWA communications [11] and were further tested at the bay [12]. Moreover, the CDSSS system was also applied for secure UWA communications [13]. In [14], a multi-carrier chaotic modulation scheme was proposed for UWA communications. To further improve the system performance and security, a DCSK system based on orthogonal frequency-division multiplexing (OFDM) technology, named the OFDM-DCSK system, was introduced in [15]. Considering the higher requirements of low complexity and low power in UIoT scenarios, a joint energy and correlation detection-assisted non-coherent OFDM-DCSK system was proposed in [16]. However, dedicated research studies regarding coding schemes for DCSK-based UWA systems are quite limited, and these coding schemes are essential for reliable transmission in UWA communications.

We next survey the coding schemes used in UWA communications, we provide an overview on the coding schemes adopted in the DCSK-based systems, and then, we describe the contributions of this work.

1.1. Existing Coding Schemes for UWA Communications

Currently, the coding schemes designed for the UWA communications are considerably limited. In [17], convolutional codes and Reed Solomon codes were tested for UWA communications. Moreover, the multiple-input-multiple-output systems and space-time coding techniques were combined for high-rate communication for high-rate UWA transmission in [18]. In addition, the nonbinary LDPC codes were designed for multicarrier UWA communications [19]. In [20], an adaptive modulation and coding system was constructed for underwater OFDM transmission. Targeting UWA channels, the protograph low-density parity-check (LDPC) codes [21] were firstly investigated in [22], and the finite-length extrinsic information transfer (EXIT) analyses were proposed in [23]. Most recently, the deep joint source-channel coding and modulation scheme was proposed for UWA communications in [24].

1.2. The Coding Schemes for the DCSK-Based Systems

During the past several decades, many coding schemes have been developed to ensure reliability of the DCSK-based systems. The trellis-coded differential chaotic modulation (TC-DCM) scheme was proposed for band-limited systems [25]. To improve the performance of the TC-DCM system, the turbo TC-DCM system [26] was proposed, where two trellis codes are parallel concatenated with the M -ary DCSK scheme. The TC-DCM system with serial concatenated trellis codes [27] was proposed to achieve a lower error floor, compared with the turbo TC-DCM system. Further, the differential chaotic bit-interleaved coded modulation (DC-BICM) was proposed for the DCSK system over multipath Rayleigh channels [28], and the protograph LDPC (P-LDPC) codes were adopted in this system. The nonbinary P-LDPC codes were applied in the coded DCSK modulation over Rayleigh fading channels in [29], and this coded DCSK system has a simpler structure, compared with the DC-BICM system. An iterative receiver based on P-LDPC codes was proposed for the DCSK system to obtain better performance in [30], and then, the P-LDPC codes were redesigned for the iterative receiver [31]. This iterative receiver is a single-receiver model, not a multi-receiver model [32]. For power line communications (PLC), the performance and capacity of the DC-BICM system were analyzed in [33], and the P-LDPC codes were

redesigned for the PLC channel. The combination of DC-BICM and the iterative receiver was studied in [34]. In [35], the P-LDPC code was redesigned for the DC-BICM system with the shuffled scheduling decoding algorithm. Moreover, the joint source and channel coding systems based on the double P-LDPC codes were used in the DCSK systems in [36,37].

However, the aforementioned coding schemes were not designed for the DCSK-based UWA communications, and this paper fulfills this gap by designing short P-LDPC codes for UWA communications with the DC-BICM system.

This paper includes the following contributions:

- (1) The DC-BICM system with P-LDPC codes is investigated over the UWA channels, showing the potential benefits of this system.
- (2) A design framework of short P-LDPC codes is proposed for the DC-BICM system over the UWA channels. This framework is based on the differential evolution algorithm, and the DC-BICM system is embedded in the design process. Simulation results show that the designed P-LDPC codes achieve good performance for the DC-BICM-based UWA communications.

The remainder of the paper is organized as follows. Section 2 describes the DC-BICM system and the UWA channel model. The design framework of short P-LDPC codes is presented in Section 3. Simulation results are provided in Section 4, and this paper is finally concluded in Section 5.

2. The DC-BICM System over Underwater Acoustic Channels

In this section, the DC-BICM system is described in detail, and the UWA channel adopted in this paper is also elaborated.

The system model is shown in Figure 1. At the transmitter, a binary independent and identically distributed (i.i.d.) source generates the information sequence $\mathbf{b} = \{b_1, b_2, \dots, b_k\}$. Then, it is encoded by the P-LDPC channel encoder to the codeword sequence $\mathbf{c} = \{c_1, c_2, \dots, c_n\}$. Using the generalized variable degree matched mapping (GVDDMM) rule [38], the codeword sequence $\mathbf{c}$ is mapped to the transmitted symbol sequence $\mathbf{s} = \{s_1, s_2, \dots, s_l\}$, $s \in S$, $S = \{0, 1, \dots, M-1\}$, $M = 2^t$ and $t \in \mathbb{N}^+$, $l = \lceil n/M \rceil$, where S is the set of signal labels. Here, the square constellation is adopted. Further, the symbol sequence $\mathbf{s}$ is modulated by the M -ary DCSK modulator to obtain the transmitted signal $\mathbf{x}$. In this process, a chaotic reference signal $\mathbf{c}_x = \{c_{x,1}, c_{x,2}, \dots, c_{x,\beta}\}$ is generated by the chaotic generator with logistic mapping, i.e., $x_{k+1} = 1 - 2x_k^2$. The length of this chaotic reference signal is β , defined as the spreading factor. Another length- β signal $\mathbf{c}_y = \{c_{y,1}, c_{y,2}, \dots, c_{y,\beta}\}$ is the quadrature version of $\mathbf{c}_x$, and it is obtained from $\mathbf{c}_x$ by the Hilbert transform. These two independent orthogonal chaotic signals $\mathbf{c}_x$ and $\mathbf{c}_y$ are used to constitute the information-bearing signal $\mathbf{m}_s$, given by $\mathbf{m}_s = a_s \mathbf{c}_x + b_s \mathbf{c}_y$, where a_s and b_s represent the real part and imaginary part of the a complex symbol s_i , $1 \leq i \leq l$, respectively. Finally, the transmitted signal $\mathbf{x}$ is made up of $\mathbf{c}_x$ and $\mathbf{m}_s$, as described in the following.

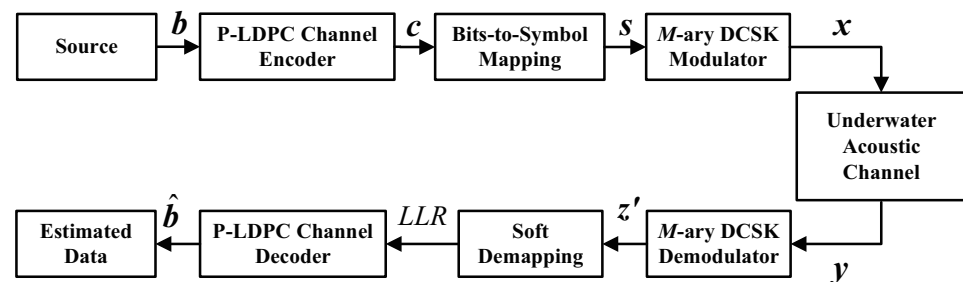


Figure 1. System model of the UWA communications with DC-BICM.

Figure 2a depicts the structure of the M -ary DCSK modulator. The transmitted signal for the i -th symbol duration is

$$x(t) = x_r(t) \cos(2\pi f_1 t + \phi_1) + x_i(t) \cos(2\pi f_2 t + \phi_2), \quad (1)$$

where $x_r(t)$ and $x_i(t)$ represent the reference signal and the information-bearing signal, respectively. Moreover, ϕ_1 and ϕ_2 represent the phase angles of the orthogonal modulated carriers, respectively, and f_1 and f_2 denote the frequencies of these two carriers, respectively. The expressions of $x_r(t)$ and $x_i(t)$ are given by

$$\begin{aligned} x_r(t) &= \sqrt{\frac{E_s}{2}} \sum_{k=1}^{\beta} c_{x,k} p(t - kT_c), \\ x_i(t) &= \sqrt{\frac{E_s}{2}} \sum_{k=1}^{\beta} m_{x,k} p(t - kT_c), \end{aligned} \quad (2)$$

where E_s is the symbol energy, T_c is the chip time, and $p(t)$ is the square-root-raised-cosine filter. The transmitted signal x is then sent over the UWA channel [39,40], modeled as

$$h(t) = \sum_{\ell=0}^{L-1} h^\ell(t) \delta(t - \ell T_c), \quad (3)$$

where the channel memory length L is set to 24, the Rayleigh fading taps are assumed with an exponentially decaying power delay profile losing 1.66 dB per tap, and $\delta(\cdot)$ is the Dirac delta function. The information symbol duration is defined as $T_s = 2\beta T_c$. The taps $\{h^\ell(n)\}$ have the following correlation structure:

$$\mathbb{E}\{h^{\ell'}(t') h^\ell(t)^*\} = J_0(2\pi(t' - t) f_D T_c) \delta(\ell' - \ell), \quad (4)$$

where $J_0(\cdot)$ is the first-kind Bessel function with zero orders, $h^\ell(t)^*$ is the conjugate of the $h^\ell(t)$, and f_D is the maximum Doppler frequency.

The structure of the M -ary DCSK demodulator is shown in Figure 2b. The received signal is given by

$$y(t) = h(t) \otimes x(t) + n(t), \quad (5)$$

where $n(t)$ represents the additive white Gaussian noise (AWGN), and $\otimes$ means convolution operation. When $y(t)$ is received by the M -ary DCSK demodulator, two corresponding modulated carrier frequencies are used to separate $y(t)$. Next, two corresponding matched filters are adopted for these separated signals, and then, the filtered signals are sampled. In this way, the chaotic reference signal and information signal are demodulated, denoted by $\tilde{c}_x$ and $\tilde{m}_s$, respectively. Using the Hilbert filter, the signal $\tilde{c}_y$ is obtained from $\tilde{c}_x$. In this way, the decision variable $z = (z_a, z_b)$ can be obtained by [28]

$$\begin{aligned} z_a &\approx \sum_{l=1}^L h_l^2 a_s E_s / 2 + \sum_{k=1}^{\beta} \sum_{l=1}^L h_l \sqrt{E_s / 2} c_{x,k-\tau_l} \eta_{k+\beta} \\ &\quad + \sum_{k=1}^{\beta} \sum_{l=1}^L h_l \sqrt{E_s / 2} (a_s c_{x,k-\tau_l} + b_s c_{y,k-\tau_l}) \eta_k \\ &\quad + \sum_{k=1}^{\beta} \eta_k \eta_{\beta+k}, \end{aligned} \quad (6)$$

$$\begin{aligned}
 z_b \approx & \sum_{l=1}^L h_l^2 b_s E_S / 2 + \sum_{k=1}^{\beta} \sum_{l=1}^L h_l \sqrt{E_S / 2} c_{x,k-\tau_l} \eta_{k+\beta} \\
 & + \sum_{k=1}^{\beta} \sum_{l=1}^L h_l \sqrt{E_S / 2} (a_s c_{x,k-\tau_l} + b_s c_{y,k-\tau_l}) \tilde{\eta}_k \\
 & + \sum_{k=1}^{\beta} \tilde{\eta}_k \eta_{\beta+k}.
 \end{aligned} \quad (7)$$

Normalized signal $\mathbf{z}'$ can be computed by $\mathbf{z}' = \mathbf{z} / \left(h \cdot \frac{E_s}{2}\right)$, where $h = \sum_{l=1}^L \alpha_l^2$ denotes the partial channel state information. The conditional probability density function (PDF) of $\mathbf{z}' = (z'_a, z'_b)$ for the m -th modulated symbol is given by

$$p(\mathbf{z}' | s_m) = \frac{1}{2\pi\sigma^2} \exp\left(\frac{(z'_a - \bar{\mu}_a)^2 + (z'_b - \bar{\mu}_b)^2}{-2\sigma^2}\right), \quad (8)$$

where the means of z'_a and z'_b are denoted by $\bar{\mu}_a$ and $\bar{\mu}_b$, respectively. Additionally, σ^2 represents the variance of z'_a and z'_b , as they have the same variance. Then, $\mathbf{z}'$ is used to calculate the log-likelihood ratios (LLRs) L_z by the soft demapper using the Gaussian approximation (GA) method, i.e.,

$$L_z(i) = \log \frac{\sum_{m:d_i(m)=0} p(\mathbf{z}' | s_m) p(s_m)}{\sum_{m:d_i(m)=1} p(\mathbf{z}' | s_m) p(s_m)}, \quad (9)$$

where $p(s_m)$ represents a priori probability of the m -th symbol s_m . Finally, the LLRs are adopted as the initial information by the P-LDPC decoder with the belief propagation (BP) decoding algorithm, and the outputs of the decoder are the estimated source sequence $\hat{\mathbf{b}}$.

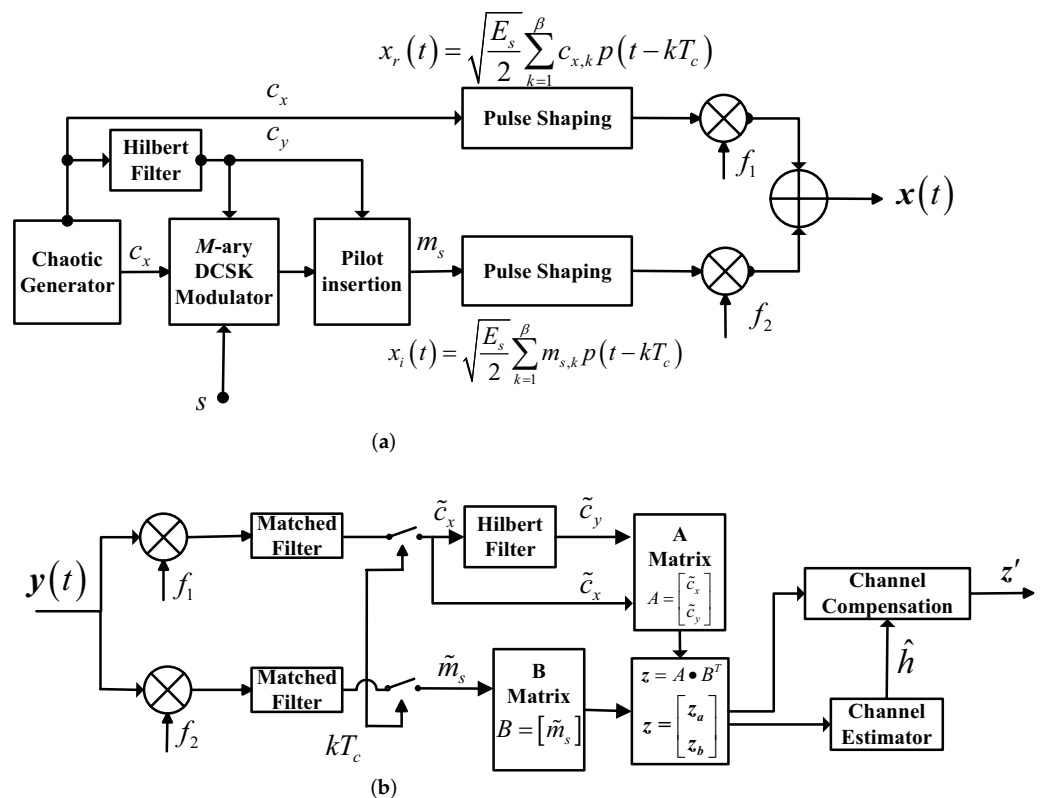


Figure 2. Structures of M-ary DCSK modulator (a) and demodulator (b).

The belief propagation (BP) decoding algorithm is described briefly [35]. The BP decoding algorithm includes four steps:

- Step 1. Initialization.* The LLRs $L_z(i)$ obtained from the soft demapping module in the DC-BICM system (Equation (9)) feeds into the P-LDPC channel decoder to initialize the LLR messages in the decoder.
- Step 2. LLRs updating.* This step consists of two kinds of message-updating processes. The first is the check-to-variable (CTV) message updating from the check node (CN) to the variable node (VN) in the P-LDPC codes, and the second is the variable-to-check (VTC) message updating from the VN to the CN in the P-LDPC codes. The two procedures run in turn.
- Step 3. Termination decision.* When the maximum iteration number is reached or the decoded sequence satisfies the parity-check equation, the iteration of Step 2 will terminate. Otherwise, the iteration between the CTV message updating and VTC message updating in Step 2 will continue.
- Step 4. Output.* When the iteration stops, the decoded sequence will output as the estimated source sequence.

Note that the LLRs $L_z(i)$ calculated by the demapping module from the demodulator of the DC-BICM system have important effects on the P-LDPC decoder. They are closely related.

3. Proposed Design of Protograph LDPC Codes for the DC-BICM-System-Based UWA Communications

In UWA communications, the packet length is usually short [20]. In this case, the existing theoretical analysis tool, such as the EXIT algorithm [41] or protograph EXIT (PEXIT) algorithm [42], would not be accurate. Inspired by the work [43,44], we propose a design framework of short P-LDPC codes for the DC-BICM system over UWA channels, and the proposed design framework is detailed in Algorithm 1.

This algorithm mainly consists of two parts, namely *Initialization* and the *Code design process*.

Initialization. This part determines the structure of the initial base matrix $\mathbf{B}_{init}$ and the parameters of the code searching algorithm. Generally, in the design process of the P-LDPC codes, decoding threshold, linear minimum distance growth (LMDG) and code searching complexity have to be considered. A good base matrix usually contains one or more degree-1 variable nodes (VNs), some degree-2 VNs and a punctured high-degree VN. Meanwhile, the maximum number of degree-2 VNs N_{d2}^{max} is directly related to the LMDG property directly, and the relation is specified by

$$N_{d2} \leq N_{d2}^{max} = m - N_{d1} - 1, \quad (10)$$

where N_{d1} and N_{d2} are the numbers of degree-1 and degree-2 VNs, respectively. Moreover, the size of the base matrix is of great importance on the searching complexity and optimization space, i.e., the tradeoff between the base matrix dimension and the design complexity needs to be considered. Taking all these factors into consideration, the initialization parameters are given in Table 1. A rate-1/2 protograph base matrix with size 6×10 is considered, where the number of the degree-1 VN and degree-2 VN is 2. In the code design process, 50 candidates and 2000 generations are adopted.

Algorithm 1 The Proposed Design Framework of P-LDPC Codes for the DC-BICM System over UWA Channels**Initialization:**

- (a) Determine the parameters of base matrix $\mathbf{B}_{init}$, including code rate, size, puncture position and so on.
- (b) Calculate the key parameters of the base matrix, including the number of degree-1 and degree-2 VNs (N_{d1} and N_{d2}).
- (c) Choose the appropriate parameters of the code searching algorithm, including the number P of candidates, crossover probability p_c , mutation probability p_m and so on.
- (d) Choose the design signal-to-noise ratio according to the scenario requirement.

Code Design Process:

- 1: Generate P base matrices $\mathbf{B}^{(1)}[p]$ randomly with initialized parameters in Table 1, $p = \{1, 2, \dots, P\}$.
- 2: **for** $g = 1; g \leq G; g++$ **do**
- 3: **for** $p = 1; p \leq P; p++$ **do**
- 4: Use PEG algorithm to generate the corresponding PCMs $\mathbf{H}^{(g)}[p]$.
- 5: Apply $\mathbf{H}^{(g)}[p]$ to the DC-BICM system over UWA channels, evaluate the BER at a certain SNR value, and save the BER result to $V_{BER}^{(g)}[p]$.
- 6: **end for**
- 7: Perform the crossover and mutation operations to update the base matrices and obtain $\mathbf{B}^{(g+1)}[p]$:
- 8: **for** $p = 1; p < P; p++$ **do**
- 9: Mutation operation:

$$\mathbf{M}^{(g)}[p] = \text{round}(\mathbf{B}^{(g)}[r_1] + p_m(\mathbf{B}^{(g)}[r_2] - \mathbf{B}^{(g)}[r_3])), \quad (11)$$

where r_1, r_2, r_3 are chosen from $\{1, 2, \dots, P\}$ randomly.

- 10: Crossover operation:

$$\mathbf{D}^{(g)}[p] = \begin{cases} \mathbf{M}^{(g)}[p] & \text{with probability } p_c, \\ \mathbf{B}^{(g)}[p] & \text{with probability } 1 - p_c. \end{cases} \quad (12)$$

- 11: **if** $V_{BER}^{(g)}[p] < V_{BER}^{(g-1)}[p]$ **then**
- 12: $\mathbf{B}^{(g+1)}[p] = \mathbf{B}^{(g)}[p]$,
- 13: **else**
- 14: $\mathbf{B}^{(g+1)}[p] = \mathbf{D}^{(g)}$.
- 15: **end if**
- 16: **end for**
- 17: **end for**
- 18: $\rho = \arg \min_p V_{BER}^{(G)}[p], p = \{1, 2, \dots, P\}$
- 19: **return** $\mathbf{B}^{(G)}[\rho]$

Table 1. Initialization parameters used in Algorithm 1 of the base matrix and code searching algorithm.

	Rate	Size	N_{d2}	N_{d1}	P	G	p_c	p_m
$\mathbf{B}_{init}^{(1)}$	1/2	6×10	2	2	50	2000	0.7	0.2

The base matrix is initialized as

$$\mathbf{B}_{init} = \begin{pmatrix} 0 & 1 & b_{1,3} & b_{1,4} & b_{1,5} & b_{1,6} & b_{1,7} & b_{1,8} & b_{1,9} & b_{1,10} \\ 1 & 0 & b_{2,3} & b_{2,4} & b_{2,5} & b_{2,6} & b_{2,7} & b_{2,8} & b_{2,9} & b_{2,10} \\ 0 & 0 & b_{3,3} & b_{3,4} & b_{3,5} & b_{3,6} & b_{3,7} & b_{3,8} & b_{3,9} & b_{3,10} \\ 0 & 0 & b_{4,3} & b_{4,4} & b_{4,5} & b_{4,6} & b_{4,7} & b_{4,8} & b_{4,9} & b_{4,10} \\ 0 & 0 & b_{5,3} & b_{5,4} & b_{5,5} & b_{5,6} & b_{5,7} & b_{5,8} & b_{5,9} & b_{5,10} \\ 0 & 0 & b_{6,3} & b_{6,4} & b_{6,5} & b_{6,6} & b_{6,7} & b_{6,8} & b_{6,9} & b_{6,10} \end{pmatrix}, \quad (13)$$

where $b_{i,j} = \{0, 1\}$, $i = \{1, 2, \dots, 6\}$, and $j = \{3, 4, \dots, 10\}$.

Code design process. This part realizes the code-searching process based on the differential evolution (DE) algorithm [45]. First, generate P base matrices $\mathbf{B}^{(1)}[p]$ randomly from $\mathbf{B}_{init}$ with the parameters in Table 1 (Line 1). At the g -th generation, p parity-check matrices (PCMs) $\mathbf{H}^{(g)}[p]$ are constructed from $\mathbf{B}^{(g)}[p]$ by the progressive edge growth (PEG) algorithm [46]. Note that the length-4 cycles are avoided as much as possible in the PEG process. Then, these PCMs are applied in the DC-BICM system over UWA channels to evaluate the bit error rate (BER) at a certain signal-to-noise ratio, and the results are saved to $V_{BER}^{(g)}[p]$. Note that $V_{BER}^{(0)}[p]$, $p = \{1, 2, \dots, P\}$ are all set to 1. When all BERs are obtained, the crossover and mutation operations are used to generate new base matrices according to Equation (12) and Equation (11). Afterward, the base matrices are updated according to the BER values (Lines 11–15). After G generations, the base matrix with the lowest BER is chosen as the optimized result.

Using the proposed design framework, the optimized base matrix is given by

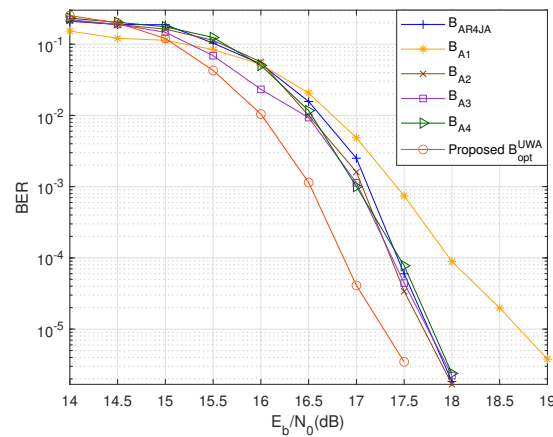
$$\mathbf{B}_{opt}^{UWA} = \begin{pmatrix} 0 & 1 & 0 & 0 & 1 & 1 & 0 & 0 & 0 & 1 \\ 1 & 0 & 0 & 0 & 1 & 1 & 1 & 0 & 0 & 0 \\ 0 & 0 & 1 & 1 & 1 & 1 & 1 & 1 & 0 & 0 \\ 0 & 0 & 0 & 0 & 1 & 1 & 1 & 1 & 1 & 1 \\ 0 & 0 & 0 & 1 & 1 & 0 & 0 & 1 & 1 & 1 \\ 0 & 0 & 1 & 0 & 0 & 1 & 0 & 0 & 1 & 1 \end{pmatrix}. \quad (14)$$

4. Simulation Results and Discussions

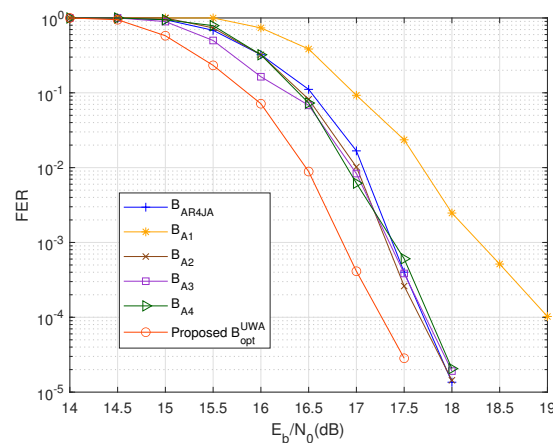
This section presents the simulation results, which consist of two parts: performance comparison between the optimized P-LDPC code and the existing codes and underwater image transmission comparison. The simulation environment is in C++ language using Visual Studio 2019 with an Intel(R) Core(TM) i7-10700F CPU (2.90 GHz). The code length is fixed at 500 bits for all simulations. The maximum frame number is 1×10^6 , and the simulation is terminated when there are 100 frame errors at each SNR value. We denote the optimized codes from ([35], Equation (12)), ([31], Equation (12)), ([34], Equation (20)), ([35], Equation (8)) and ([33], Equation (29)) by $\mathbf{B}_{AR4JA}$, $\mathbf{B}_{A1}$, $\mathbf{B}_{A2}$, $\mathbf{B}_{A3}$, and $\mathbf{B}_{A4}$, respectively. The maximum number of iterations in the decoding process is 50. The normalized Doppler frequency $f_D T_s$ is set to 10^{-5} [40]. The other parameters of the utilized UWA channel are described in Section 2.

4.1. Performance Comparison

Figure 3 compares the BER and frame error rate (FER) performance, respectively, between the proposed $\mathbf{B}_{opt}^{UWA}$ and other P-LDPC codes for the DC-BICM system over the UWA channels. In Figure 3a, $\mathbf{B}_{opt}^{UWA}$ achieves coding gains of 0.6, 0.9, 0.54, 0.49 and 0.48 dB at $BER = 1 \times 10^{-3}$, compared with $\mathbf{B}_{AR4JA}$, $\mathbf{B}_{A1}$, $\mathbf{B}_{A2}$, $\mathbf{B}_{A3}$, and $\mathbf{B}_{A4}$, respectively. Moreover, $\mathbf{B}_{opt}^{UWA}$ outperforms $\mathbf{B}_{A1}$ by 1.53 dB at $BER = 4 \times 10^{-6}$. In addition, the proposed $\mathbf{B}_{opt}^{UWA}$ performs best among these codes for the DC-BICM system over the UWA channels. In other words, the existing P-LDPC codes are all not suitable for the DC-BICM system over the UWA channel, and the proposed design framework is essential and meaningful. It can be seen from Figure 3b that FER performance has the same trend as the BER curves.



(a)



(b)

Figure 3. Performance comparison between $\mathbf{B}_{opt}^{UWA}$ and the existing counterparts, for $\beta = 256$ and $f_D T_s = 10^{-5}$. (a) BER; (b) FER.

Figure 4 compares the average number of iterations. As shown in this figure, $\mathbf{B}_{AR4JA}$, $\mathbf{B}_{A2}$, $\mathbf{B}_{A3}$, and $\mathbf{B}_{A4}$ all converge faster than $\mathbf{B}_{A1}$, and $\mathbf{B}_{opt}^{UWA}$ converges fastest among them. It is noted that at $E_b/N_0 = 16.5$ dB, the number of iterations for $\mathbf{B}_{opt}^{UWA}$ is reduced by around 40.9%, 69.5%, 33%, 32.6%, and 35.8%, respectively, compared to $\mathbf{B}_{AR4JA}$, $\mathbf{B}_{A1}$, $\mathbf{B}_{A2}$, $\mathbf{B}_{A3}$, and $\mathbf{B}_{A4}$.

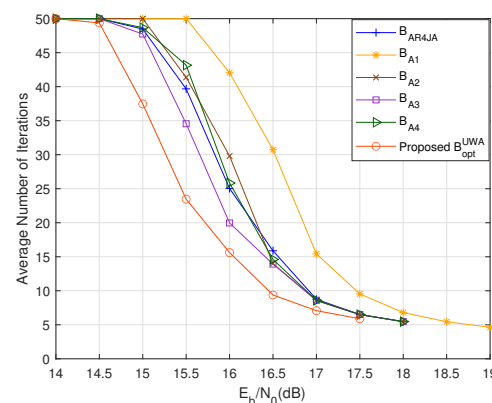


Figure 4. Comparison of the average number of iterations between the proposed $\mathbf{B}_{opt}^{UWA}$ and the existing codes for $\beta = 256$ and $f_D T_s = 10^{-5}$.

From Figures 3 and 4, it can be seen that the DC-BICM system with proposed $\mathbf{B}_{opt}^{UWA}$ can perform best in both error-rate performance and converge speed.

4.2. Underwater Image Transmission Comparisons

To test and verify the performance of the DC-BICM system with the proposed $\mathbf{B}_{opt}^{UWA}$ over the UWA channel, the underwater image transmission comparisons are presented in this part.

The underwater image transmission system is shown in Figure 5. The process of image pre-processing includes the discrete cosine transform (DCT) and quantization. Through the pre-processing operation, the underwater image can be represented by binary bit streams, and these bit streams are divided into frames with equal length. Then, these equal-length frames are fed into the P-LDPC channel encoder of the DC BICM system over the UWA channel (shown in Figure 1), and the P-LDPC channel decoder outputs the estimated sequence. This estimated sequence goes to the image post-processing operation to recover the underwater image and to calculate the image quality. The post-processing operation includes the calculation of the gray values of the received image and the inverse DCT (IDCT) operation. After the IDCT operation, the original underwater image is recovered. The processes of image pre-processing and post-processing are the same the process of [47]. The image transmission system in [47] is a combination of the joint source-channel coding and separated source-channel coding (SSCC) technologies, and the underwater image transmission system in this paper is a kind of SSCC system. Moreover, we compare the performance between the proposed P-LDPC code and its counterparts in this system. They are all single-receiver [28] and not multi-receiver architectures [48], and that which we focus on in this paper is code design.

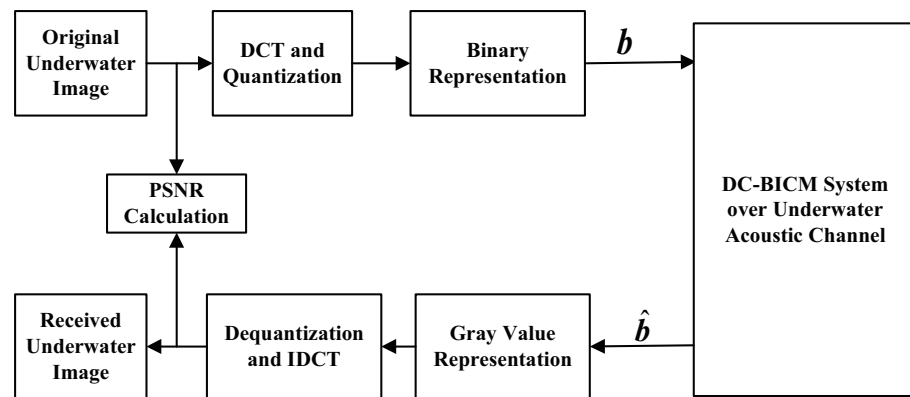


Figure 5. Underwater image transmission system.

The peak signal-to-noise ratio (PSNR) is adopted to describe the quality of recovered images objectively, and the recovered images are also shown to describe the quality directly. The PSNR is computed by

$$PSNR = 10 \times \lg \frac{A^2 \times W \times L}{\sum_{m=1}^W \sum_{n=1}^L (I_T(m, n) - I_R(m, n))^2}, \quad (15)$$

where $W \times L$ is the size of the underwater image size, and the original image and recovered image are represented by $I_T(m, n)$ and $I_R(m, n)$, respectively. The peak value of signals for the gray underwater images is represented by A , whose value is 255.

Figure 6 shows the reconstructed underwater images with different codes when $E_b/N_0 = 17$ dB. It can be seen that the reconstructed image with $\mathbf{B}_{AR4JA}$ is clearer than the images with $\mathbf{B}_{A1}$, $\mathbf{B}_{A2}$, $\mathbf{B}_{A3}$ and $\mathbf{B}_{Ar}$, and the quality of the reconstructed images with $\mathbf{B}_{A1}$ (Figure 6c) is the worst among these images. The reconstructed images with $\mathbf{B}_{opt}^{UWA}$ are clearest (Figure 6g).

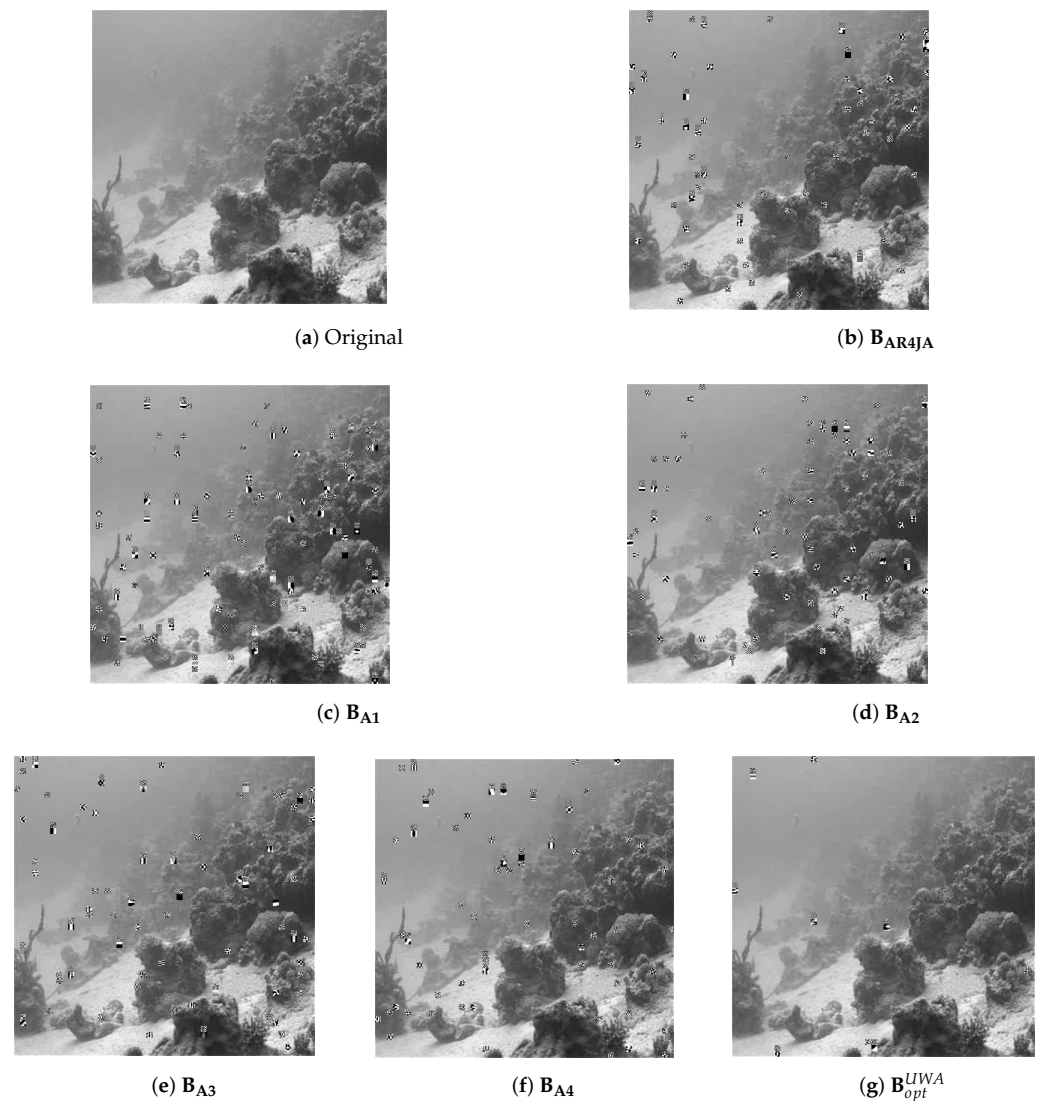


Figure 6. Reconstructed underwater images with different codes when $E_b/N_0 = 17$ dB.

Table 2 shows the PSNR value comparisons with different codes when $E_b/N_0 = 17$ dB. From this table, we can see that the reconstructed image with $\mathbf{B}_{AR4JA}$ has a higher PSNR value than $\mathbf{B}_{A1}$, $\mathbf{B}_{A2}$, $\mathbf{B}_{A3}$ and $\mathbf{B}_{A4}$. The PSNR value of the reconstructed image with $\mathbf{B}_{opt}^{UWA}$ is highest, and the reconstructed image with $\mathbf{B}_{A1}$ is the worst. This is consistent with the quality of the reconstructed images mentioned above.

Table 2. Comparison of PSNR values of different codes at $E_b/N_0 = 17$ dB.

E_b/N_0	$\mathbf{B}_{AR4JA}$	$\mathbf{B}_{A1}$	$\mathbf{B}_{A2}$	$\mathbf{B}_{A3}$	$\mathbf{B}_{A4}$	$\mathbf{B}_{opt}^{UWA}$
17dB	20.5466	18.5325	20.0685	20.3160	20.6202	26.8985

From Figure 6 and Table 2, we can see that the DC-BICM system with proposed $\mathbf{B}_{opt}^{UWA}$ can perform better than their counterparts in the underwater image transmission, which further shows the efficiency and advantage of the proposed design framework.

5. Conclusions

In this paper, we investigate the performance of a P-LDPC coded DC-BICM system over UWA channels, which greatly improves the transmission reliability. Moreover, we pro-

pose a short-length P-LDPC code design framework for the DC-BICM system, integrating the DC-BICM system, UWA channel and the DE code searching algorithm. With this design framework, an optimized short-length P-LDPC code is obtained. Simulation results show that the proposed P-LDPC code outperforms their counterparts in terms of error correction performance and convergence speed, and underwater image transmission comparisons show that images with the proposed P-LDPC code can achieve the highest PSNR value and have the best image quality. This means that the proposed design framework for the DC-BICM system for the UWA channel is meaningful and effective. This paper fills the vacancy in the research regarding designing short P-LDPC codes for UWA communications with the DC-BICM system, which contributes to improve the reliability of a coded chaotic modulation for UWA communication. In the future, the low complexity receiver will be further investigated for the DC-BICM system and UWA channel.

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Abbreviations

The following abbreviations are used in this manuscript:

UWA	Underwater Acoustic
DC-BICM	Differential Chaotic Bit-interleaved Coded Modulation
UASs	Underwater Acoustic Sensor networks
IoT	Internet of Things
UIoT	Underwater Internet of Things
CDSSS	Chaotic Direct-Sequence Spread Spectrum
DCSK	Differential Chaos Shift Keying
OFDM	Orthogonal Frequency-division Multiplexing
LDPC	Low-Density Parity Check
P-LDPC	Protograph Low-Density Parity Check
EXIT	Extrinsic Information Transfer
TC-DCM	Trellis-Coded Differential Chaotic Modulation
GVDMM	Generalized Variable Degree Matched Mapping
AWGN	Additive White Gaussian Noise
LLR	Log-Likelihood Ratios
GA	Gaussian Approximation
BP	Belief Propagation
LMDG	Linear Minimum Distance Growth
VN	Variable Nodes
PCM	Parity-Check Matrices

PEG Progressive Edge Growth
 BER Bit Error Rate
 FER Frame Error Rate

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