



Article Impedance Modeling Based Method for Sub/Supsynchronous Oscillation Analysis of D-PMSG Wind Farm

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Abstract: Subsynchronous oscillation (SSO) is a critical issue for the direct-drive permanent magnet synchronous generator (D-PMSG) based wind farm integrated to a weak onshore AC grid. To analyze the mechanism of the SSO phenomenon of D-PMSG based wind farm, widely used impedance-based stability analysis method is utilized in this paper. First, the impedance model based on the harmonic linearization theory of grid-connected D-PMSG is proposed, and the mechanism of sub/supsynchronous currents coupling is analyzed quantitatively for the first time. Then, based on the impedance model and relative stability criterion, the influence of wind farm operating parameters and grid impedance on stability is discussed. Simulations are carried out to verify the correctness of theoretical analysis.

Keywords: direct-drive permanent magnet synchronous generator (D-PMSG); frequency coupling; harmonic linearization; impedance modeling; sub/supsynchronous oscillation

1. Introduction

Recently, renewable energy generation has been developing rapidly all around the world due to the depletion of traditional energy and serious environmental pollution. Wind and solar energy with the benefits of cleanness, short construction cycle, and low running cost, have become the promising energy source. For practical power grids, the doubly fed induction generator (DFIG) and the direct-drive wind generator (direct drive permanent magnet synchronous generator (D-PMSG)) are the most applied generators for wind turbines due to the advantages of variable speed-based operation and independent control of active and reactive power [1]. Compared to DFIG, D-PMSG uses full power converters and has lower maintenance cost. The back-to-back pulse width modulation (PWM) converter isolates the generator from the grid, which improves the low voltage ride through ability. Because of this, D-PMSG based wind farms get a wide range of applications.

Due to the reverse distribution of the energy and power load in China, the renewable energy, mainly based on the large-scale of wind and solar power, long-distance high voltage direct current (HVDC) transmission system and series compensation transmission lines are widely utilized in nowadays power grid. However, previous researches pointed out that subsynchronous oscillation (SSO) is a potential problem in this series-compensated and HVDC transmission system [2,3]. On the other hand, with the increase of the wind energy, the short circuit ratio (SCR) at the point of common coupling (PCC) will decrease since the wind farm cannot provide enough support to the power grid, which will worsen the stability of power grid.

The SSO of grid-connected wind farm has been detected worldwide, for instance, in the wind farms of USA (Texas, 2009), China (GU yuan, Hebei Province, 2011) [4,5]. The above events are all due

to the series compensation or HVDC transmission, which has already been analyzed and classified as subsynchronous resonance (SSR), subsynchronous control interaction (SSCI) [6–8]. Theoretical research and simulation studies have been conducted to investigate the mechanism and characteristics of these phenomena. Various countermeasures have also been proposed to solve the SSR problem [9–11].

A new type of sub/supsynchronous oscillation which had no relation with series compensation was detected the D-PMSG based full-converter wind farm in Xinjiang, China, in July 2015 [12,13]. The continuous oscillation of power grid initiated shafting torsional vibration of synchronous generators outside 200 km, which finally resulted in the decrease of HVDC power. The analysis of the accident shows that the operating adjustments of HVDC have no relation with this type of SSO. Besides, since the natural torsional frequency of shafting vibration in direct drive permanent magnet synchronous generator is very low (1–10 Hz), and the generator and power system are isolated by back-to-back PWM converter, subsynchronous torsional interactions (SSTI) will not occur in D-PMSG based wind farm.

1.1. Related Works

Plenty of researches have been carried out to study on the mechanism of the SSO of the grid-connected D-PMSG farm. But yet the cause of this new type of SSO is not clear.

Time-domain simulation, eigenvalue analysis, and impedance-based stability analysis are the mostly used methods in the analysis of SSO. It is intuitive to observe the SSO phenomenon by using time-domain simulation. However, it has difficulties in figuring out the interactions between the wind farm and power system. Eigenvalue analysis has the advantages in the mechanism analysis of SSO but this method needs plenty of information of power system and it is not realistic to apply in the large-scale system. Impedance-based stability analysis is a newly developed method in the analysis of SSO. In this method, D-PMSGs are considered to provide a capacitive impedance for the system which will lead to SSO. This method is not limited by the system scale and can be used in the black-box systems, which have flexible application scenario.

Progress has been made in the study of impedance-based stability analysis. Existing approaches to analyzing such instability problems focus on small-signal impedance modeling [14]. As mentioned above, since the DC link capacitor between two converters isolates the machine side converter (MSC) and the grid side converter (GSC), the interactions between the GSC and the power grid are mainly concerned. Impedance-based stability analysis separates the inverter-grid system into two independent parts and calculates their impedance respectively. The inverter-grid system will remain stable if the ratio between the grid impedance and the inverter output impedance satisfies the Nyquist stability criterion.

There are two methods to construct this impedance model: (1) transform the converter model into the dq reference frame, and use small-signal linearization; (2) use harmonic linearization method and directly model the three-phase positive- and negative-sequence impedance in the phase domain [15,16]. The first method could easily obtain the impedance model for the *dq*-domain control system. However, several limitations were discussed: not suitable for unbalanced grid; the dq impedance is coupled and it is hard to measure in practical systems. The harmonic linearization method overcomes these disadvantages by modeling three-phase voltage source inverter (VSC) impedance directly in the phase domain. Despite the complex derivation, this method is widely used to investigate the impedance characteristic of grid-connected full converter wind farm. The work in References [17,18] analyzed the interaction between D-PMSGs and grid by experimentally measuring the impedance, but the mathematical expression was not proposed. Reference [19] built the impedance model of grid-connected VSC and it was further developed in Reference [20] to describe impedance characteristics of LCL-type converter, but the stability analysis was not mentioned in both articles. References [21,22] modeled the D-PMSG impedance and analyzed the system stability with or without outer-loop control, but the frequency coupling was not considered. The coupling phenomenon introduced by phase locked loop (PLL) was discussed in References [23–25] and derived the coupled impedance model of grid-connected converter. However, this model was too complicated and the relationship of sub/supsynchronous currents was not analyzed either.

1.2. Main Contribution

Most existing literature assumed that the PCC voltage perturbation at f_p will only bring the same frequency error components in Park's transformation. Moreover, the output current harmonic component at coupled frequency $2f_1 - f_p$ was neglected. However, these assumptions are obviously incorrect according to time-domain simulation results.

Based on the existing researches, this paper constructs the impedance model of grid-connected D-PMSG by using harmonic linearization small-signal modeling method. By reasonable simplification, the outer-loop control of converter is not considered [26], and the converter model is treated as voltage-controlled voltage source. It is worth mentioning that the frequency coupling of PLL and the relationship between sub/supsynchronous coupling currents are analyzed quantitatively. The simplified PWM converter and related theoretical analysis were all verified by simulation then. Furthermore, based on the correct impedance model and relative stability criterion, the impedance sensitivity of wind farm operation parameters and the influence on system stability are discussed. Finally, a time-domain simulation of SSO appearance when SCR decreases is carried out, which is theoretically explained.

2. Impedance Characteristics Analysis of D-PMSG

This section constructs the impedance model of grid-connected D-PMSG based wind farm. The structure diagram of the wind farm integrated in weak AC grid is presented first. Secondly, two assumptions are adopted to simplify the D-PMSG to a grid-connected converter. Then, the small-signal model of PLL considering frequency coupling is proposed, which is a key step to apply the harmonic linearization in different reference frame. Based on the PLL model, harmonic components in current control loop could be further obtained. Another simplification is about the PWM converter model. Finally, the impedance of D-PMSG is calculated and the relationship between coupled currents is analyzed.

2.1. Simplified Model of D-PMSG

The structure diagram of D-PMSGs integrated in a weak AC grid is shown in Figure 1. The wind farm in Xinjiang consists of hundreds of 1.5 MW D-PMSGs. Every unit is radially connected to 35 kV bus through a 0.69/35 kV transformer. Then, the electric power is collected at the 35-kV substation and next transmitted along higher voltage level transmission lines, to the 750-kV power grid 200 km away. The thermal synchronous power units are also connected to the common bus. Extra power is transmitted along HVDC to Eastern China. Since the transmission line has a long-distance and multi-stage transformers boost the voltage, the grid side equivalent impedance is as large as 0.4 pu [21]. The SCR is 2.5 (<3) and the grid wind farm integrate into belongs to weak AC grid [27].



Figure 1. Structure diagram of D-PMSGs integrated in a weak AC grid.

As shown in Figure 2, grid-connected D-PMSG unit consists of wind turbine, permanent magnet synchronous generator, machine side converter (MSC), and grid side converter (GSC). The MSC controls the rotor speed to track the maximum wind power. The GSC is controlled to maintain the DC-link voltage and the output power factor.



Figure 2. Schematic diagram of D-PMSG.

It is well understood that the small signal disturbance from the GSC cannot transmit to the MSC since the DC capacitor decouples the interactions between two converters. Therefore, the generator and the MSC is usually simplified as controlled current source when applying the small signal stability analysis. On the other hand, the outer loops of VSC control, DC voltage control, and reactive power control are proved not to take part in the dynamics under frequency band of SSO, 10~100 Hz approximately [26]. Consequently, the impedance model constructed in this paper mainly concerns the influence of GSC control parameters, operating condition. The structure diagram of simplified grid-connected D-PMSG system is shown in Figure 3. For the reasons above, V_{dc} is assumed constant in this study and the active and reactive current references (I_{dref} and I_{qref}) are assumed constant.



Figure 3. Circuit and control of grid-connected D-PMSG.

Phase voltages are denoted as v_a , v_b , and v_c , while phase currents as i_a , i_b , and i_c . In *d-q* axis, recall the current as i_d , i_q . The *ABC/dq* transformation reference angle θ_{pll} is the output of PLL, whose function is obtaining the phase angle of AC voltage. The block diagram of PLL is depicted in Figure 4, where $H_{PLL}(s)$ is the PLL regulator which uses a PI controller and an integrator. Current errors are adjusted by the current controller and added with feedforward compensation. The results v_{dref} , v_{qref} are the dq-domain voltage references, which are transformed to v_{aref} , v_{bref} , and v_{cref} for PWM.



Figure 4. Block diagram of PLL.

2.2. Small-Signal Modeling of the PLL

As described in Figure 4, phase voltages are transformed to dq-domain voltage v_d and v_q by Park's transformation. When there is a harmonic frequency f_p component in PCC voltage, the output angle θ_{pll} will be $\theta_1 + \Delta \theta$. The Park's transformation could be broken into two parts as follows:

$$T(\theta_{pll}) = \frac{2}{3} \begin{bmatrix} \cos \theta_{pll} & \cos(\theta_{pll} - 2\pi/3) & \cos(\theta_{pll} + 2\pi/3) \\ -\sin \theta_{pll} & -\sin(\theta_{pll} - 2\pi/3) & -\sin(\theta_{pll} + 2\pi/3) \end{bmatrix}$$

$$= \begin{bmatrix} \cos \Delta \theta & \sin \Delta \theta \\ -\sin \Delta \theta & \cos \Delta \theta \end{bmatrix} T(\theta_1(t))$$
(1)

where $T(\theta_1)$ is the Park's transformation when $\theta_{pll} = \theta_1 = \omega_1 t$.

In the time domain, the phase voltage with a small-signal perturbation can be written as:

$$v_a(t) = V_1 \cos \omega_1 t + V_p \cos(\omega_p t + \varphi_{up})$$
⁽²⁾

where V_1 corresponds to the magnitude of the fundamental voltage at frequency f_1 , V_{p_i} with ϕ_{up} correspond to the magnitude and phase of the positive-sequence perturbation at frequency f_p .

Similar to phasor analysis, in the frequency domain, the voltage (1) could be written as:

$$\mathbf{V}_{a}[f] = \begin{cases} \mathbf{V}_{1}, f = f_{1} \\ \mathbf{V}_{p}, f = f_{p} \end{cases}$$
(3)

where $\mathbf{V}_1 = V_1$, $\mathbf{V}_p = V_{p^*} e^{j\phi_{up}}$ correspond to the fundamental and disturbance voltage in frequency domain.

For linearization, apply $T(\theta_1)$ to (3), and define $V_{dv}[f]$, $V_{qv}[f]$ as frequency domain d and q outputs:

$$\mathbf{V}_{dv}[f] = \begin{cases} V_1, \ \mathrm{dc} \\ \mathbf{V}_p, f = f_p - f_1 \end{cases}$$
(4)

$$\mathbf{V}_{qv}[f] = -j\mathbf{V}_p, f = f_p - f_1 \tag{5}$$

According to (1), considering $\Delta \theta$, v_q is easily found to be:

$$v_q(t) \approx -\Delta\theta(t)v_{dv}(t) + v_{qv}(t) \tag{6}$$

For voltage perturbation at f_p , remove terms in $\Delta \theta(t)$ proportional to second and higher orders by the harmonic linearization principle, then $\Delta \theta(t)$ is given by

$$\Delta \boldsymbol{\theta}[f] = G_p(s) \mathbf{V}_p, f = f_p - f_1 \tag{7}$$

Applying convolution to (4), (5), and (7), and neglecting terms in v_q proportional to the second order, the result of (6) in frequency domain is as follows:

$$\mathbf{V}_q[f] = -G_p(s)V_1\mathbf{V}_p - j\mathbf{V}_p, f = f_p - f_1$$
(8)

Note that $\Delta \theta = H_{\text{pll}}(s) \mathbf{V}_{q}$, then $G_{p}(s)$ can be solved from (8):

$$G_p(s) = [-jH_{pll}(s)] / [1 + V_1H_{pll}(s)], f = f_p - f_1$$
(9)

To get the frequency errors of Park's transformation, the final step is to obtain the response of $\cos(\theta_{\text{pll}}(t))$. Since $\cos(\theta_{\text{pll}}(t)) = \cos(\theta_1(t) + \Delta\theta(t)) = \cos\omega_1 t - \sin(\omega_1 t) \Delta\theta(t)$, apply convolution again:

$$\cos \theta_{pll}[f_p] = \frac{1}{2} \frac{H_{pll}(s-j2\pi f_1)}{1+V_1H_{pll}(s-j2\pi f_1)} \mathbf{V}_p = T_p(s) \mathbf{V}_p$$

$$\cos \theta_{pll}[2f_1 - f_p] = -T_p(s) \widetilde{\mathbf{V}}_p$$
(10)

From above we can find that a voltage perturbation at f_p will result in both f_p and $2f_1 - f_p$ errors in Park's transformation, which gives a primary explanation of why sub/supsynchronous components usually exist together.

A simulation experiment was conducted to verify the correctness of (10). Appendix A gives the setup parameters of the experiment. The voltages at PCC are $V_1 = 566$ V, $\mathbf{V}_p = V_p e^{j\phi}_{up} = 20 \cdot e^{j\pi/4}$. The response of $\cos(\theta_{pll}(t))$ is depicted in Figure 5, compared with theoretical calculated results.



Figure 5. Frequency response of cosine of PLL angle to perturbation in phase a voltage. (**a**) Magnitude comparison; (**b**) Phase comparison. Solid lines: model prediction; Marking points: simulation results.

2.3. Impedance Modeling of D-PMSG

2.3.1. Harmonic Components in Control Loop

It is easily to get from Figure 3 that the modulating signals, current, and PCC voltage satisfy:

$$L\frac{d}{dt}\begin{bmatrix} i_a\\i_b\\i_c\end{bmatrix} = \begin{bmatrix} v_{ga}\\v_{gb}\\v_{gc}\end{bmatrix} - \begin{bmatrix} v_a\\v_b\\v_c\end{bmatrix}$$
(11)

In order to solve (11) for impedance in the frequency domain, the sequence components in the modulating signals should be found as functions of the voltage and current perturbations. In the previous section, we have initially reached a conclusion that sub/supsynchronous always appear together. Therefore, for the voltage of (2), the current can be assumed as:

$$i_a(t) = I_1 \cos(\omega_1 t + \varphi_{i1}) + I_p \cos(\omega_p t + \varphi_{ip}) + I_{p2} \cos((2\omega_1 - \omega_p)t + \varphi_{ip2})$$
(12)

where the annotations similar to (2). Other phase currents can be inferred.

Recall that currents *id* and *iq* are outputs of a *dq*-domain transformation, which in the frequency domain involves a convolution of the frequency components in the phase currents, with the frequency components in Park's transformation. Currents in frequency domain can be defined as (3), and frequency

components of Park's transformation are described in (10). Table 1 shows the possible combinations to consider in the convolution, it is worth noting that second and higher orders small signals are neglected. The *dc* components are not listed here, because *id* and *iq* would be exactly equal to I_{dref} and I_{qref} at the stable operating point.

$I_a[f], I_b[f], I_c[f]$	$T(\theta_1)$	$I_d[f], I_q[f]$
f_1	f_p $2f_1 - f_n$	$\begin{array}{c} f_1 - f_p \\ f_n - f_1 \end{array}$
f_p $2f_1 - f_p$	f_1 f_1	$ \begin{array}{c} f_p & f_1 \\ f_1 & -f_p \end{array} $

Table 1. Frequency components in *dq*-domain current.

Combine the frequency components in Table 1 noting that $I_d [f_p - f_1]$ is the conjugate of $I_d [f_1 - f_p]$:

$$\mathbf{I}_{d}[f_{p} - f_{1}] = -2jT_{p}(j2\pi f_{p})\mathbf{V}_{p}I_{1}\sin\varphi_{i1} + \mathbf{I}_{p} + \mathbf{I}_{p2}$$

$$\mathbf{I}_{q}[f_{p} - f_{1}] = +2jT_{p}(j2\pi f_{p})\mathbf{V}_{p}I_{1}\cos\varphi_{i1} - j\mathbf{I}_{p} + j\mathbf{\widetilde{I}}_{p2}$$
(13)

Figure 3 depicts a *dq*-domain current controller, according to its diagram, the *dq* reference voltages are given by:

$$\begin{cases} \mathbf{V}_{dref} = H_i(s)(I_{dref} - \mathbf{I}_d) - \omega_1 L \mathbf{I}_q \\ \mathbf{V}_{qref} = H_i(s)(I_{qref} - \mathbf{I}_q) + \omega_1 L \mathbf{I}_d \end{cases}, H_i(s) = K_{pi} + K_{ii}/s$$
(14)

It is easy to find that the dq reference voltages have dc and $(fp - f_1)$ components. Moreover, (14) can be further described as:

$$V_{dref}[dc] = V_1 - \omega_1 L I_1 \sin \varphi_{i1}$$

$$V_{qref}[dc] = \omega_1 L I_1 \cos \varphi_{i1}$$
(15)

$$\mathbf{V}_{dref}[f_p - f_1] = -H_i(s)\mathbf{I}_d[f_p - f_1] - \omega_1 L \mathbf{I}_q[f_p - f_1]
\mathbf{V}_{qref}[f_p - f_1] = -H_i(s)\mathbf{I}_q[f_p - f_1] + \omega_1 L \mathbf{I}_d[f_p - f_1]$$
(16)

These signals are convoluted with inverse Park's transformation to generate their phase-domain counterparts. Counting equations (10) and (13~16) together, the harmonics of phase-domain voltage references are as followings:

$$\mathbf{V}_{aref}[f_p] = H_i(s - j\omega_1)I_1T_p(s)e^{j\varphi_{i1}}\mathbf{V}_p + V_1T_p(s)\mathbf{V}_p + [j\omega_1L - H_i(s - j\omega_1)]\mathbf{I}_p$$
(17)

$$\mathbf{V}_{aref}[2f_1 - f_p] = -H_i(s - j\omega_1)I_1T_p(s)e^{j\varphi_{i1}}\widetilde{\mathbf{V}}_p - V_1T_p(s)\widetilde{\mathbf{V}}_p + [j\omega_1L - H_i(s - j\omega_1)]\mathbf{I}_{p2}$$
(18)

2.3.2. Simplified Model of the Converter

The converter depicted in Figure 3 uses pulse width modulation techniques. The amplitude of output phase voltage could reach as large as $V_{dc}/2$, correspond modulation factor is 1. Therefore, to get good control performance, it is necessary to take account in this characteristic when designing both system setup parameters and control strategies.

On one hand, in the design of the grid-connected converter parameters under the unit power factor control, it is worth mentioning that the output voltage, current, PCC voltage, and power grid voltage meet the relationship shown in Figure 6.



Figure 6. Phasor analysis of VSC ac side voltage.

From the following figure, we can conclude that usually $U_{pwm} < U_s$ since the soothing inductance usually smaller than line inductance L_{line} . As a result, it will be praised if the *dc* side voltage V_{dc} is set to be twice as large as V_{sa} , at least.

On the other hand, modulation factor in PWM should not be larger than 1 the carrier usually uses (-1, 1) triangular wave. Therefore, in control strategy design, the three-phase voltage reference should be divided by $V_{dc}/2$, amplitude limiter should be added respectively.

If the grid-connected GSC of D-PMSG system satisfied the two conditions above, the VSC could be supposed as a voltage-controlled voltage source, and v_{ga} , v_{gb} , and v_{gc} would follow v_{aref} , v_{bref} , and v_{cref} . To verify the correctness of the assumption, a simulation experiment was conducted. The structure diagram of experimental circuit is shown in Figure 3. The converter side parameters are listed in Appendix A. The grid side parameters used in this simulation are as follows: $V_{sa} = 650$ V, no resistance, and L_{line} increases from 0.3 mH to 0.46 mH at 3 s. The converter output voltage compared with reference voltage is depicted in Figure 7.



Figure 7. Voltage tracking verification of D-PMSG's grid side converter (GSC).

So, in this paper, the switching dynamics process of converter will not be detailed described. The simplified converter model is proposed and verified in this section, which satisfies:

$$\begin{aligned}
v_{ga}(t) &= v_{aref}(t) \\
v_{gb}(t) &= v_{bref}(t) \\
v_{gc}(t) &= v_{cref}(t)
\end{aligned} (19)$$

2.3.3. Impedance Analysis of D-PMSG

Transforming (11) to frequency domain, at the voltage perturbation frequency f_p :

$$sL\mathbf{I}_a(f_p) = \mathbf{V}_{ga}[f_p] - \mathbf{V}_a[f_p]$$
⁽²⁰⁾

Positive-sequence impedance is defined as:

$$Z_p(s) = -\mathbf{V}_p(s) / \mathbf{I}_p(s) \tag{21}$$

Introducing (17), frequency-domain version of (19) and (20) in (21), the positive-sequence impedance of the grid-connected D-PMSG can be easily obtained:

$$Z_p(s) = \frac{j\omega_1 L - sL - H_i(s - j\omega_1)}{H_i(s - j\omega_1)I_1T_p(s)e^{j\varphi_{i1}} + V_1T_p(s) - 1}$$
(22)

Of course, the impedance characteristics have also been verified by simulation. Directly apply voltage $v_a(t) = 565.3\cos(2\pi f_1 t) + 20\cos(2\pi f_p t + \pi/4)$, $f_p = (0, 100 \text{ Hz})$ at PCC, and the other set up parameters remained the same as Appendix A. Voltage and current signals collected and analyzed by FFT tools, the calculated simulation results compared with impedance prediction are shown in Figure 8. From the phase characteristics we can find that the D-PMSG's equivalent inductance X_{PMSG} is positive at subsynchronous frequency while negative (capacitive) at supsynchronous frequency.



Figure 8. Frequency response of grid-connected D-PMSG's impedance. (**a**) Magnitude comparison; (**b**) Phase comparison. Solid lines: model prediction; Marking points: simulation results.

2.3.4. Frequency Coupling of the Sub/Supsynchronous Currents

Furthermore, the relationship between sub/supsynchronous currents could be analyzed. Since there is no $(2f_1 - f_p)$ harmonic voltage at PCC, phase-domain voltage reference at $(2f_1 - f_p)$ satisfies:

$$\mathbf{V}_{aref}[2f_1 - f_p] = \mathbf{V}_{ga}[2f_1 - f_p] = j(2\omega_1 - \omega_p)L\mathbf{I}_a[2f_1 - f_p]$$
(23)

Introducing (18) into (23), and eliminating V_p by (22), the current response is given by:

$$\mathbf{I}_{p2}[2f_1 - f_p] = \frac{H_i(j\omega_1 - j\omega_p)I_1T_p(s)e^{j\varphi_{i1}} + V_1T_p(s)}{1 - [H_i(j\omega_1 - j\omega_p)I_1T_p(s)e^{j\varphi_{i1}} + V_1T_p(s)]}\widetilde{\mathbf{I}}_p$$
(24)

For the system parameters setup in 2.2 section, it can be calculated that $I_{p2} = 0.7754 \cdot e^{j_3} \cdot (-I_p)$. In the simulation experiment conducted in 2.2, the comparison of sub/supsynchronous FFT results is shown in the following Figure 9. It is worth mentioning that for clearly observing, phases of the insignificant frequency components except for 20, 50, and 80 Hz are neglected. The simulation results in Figure 9 verified the correctness of (24) at 20 Hz. By changing the frequency of voltage perturbation, the correctness at (0, 100 Hz) could be validated, too.



Figure 9. Frequency components in output currents. (a) Magnitude; (b) Phase.

3. Impedance-Based Stability Analysis of SSO

The impedance-based stability analysis was widely used and developed in recent years. It was firstly proposed to analyze the stability of inverter-grid system in Reference [19]. Under the assumption that the inverter is controlled as a current source parallel with an output impedance, it will remain stable with a nonideal grid if the ratio of the grid impedance to the inverter output impedance satisfies the Nyquist criterion. It was developed by proposing a simplified method based on aggregated RLC circuit model to intuitively explain and quantitatively evaluate this type of SSO [5]. This method has a clear physical meaning and is easy to carry out as follows: at the resonant frequency f_r decided by negative X_{PMSG} and positive X_{Grid} , if the total resistance $R_{PMSG} + R_{Grid}$ is negative, the grid-connected D-PMSG system will be unstable. This paper chose this method to analyze grid-connected D-PMSG stability, and simulation is conducted to verify the correctness.

3.1. Impedance Sensitivity Analysis

Based on the correct and effective impedance model, influence of control and circuit parameters can be further discussed. The impedance dynamics effects on SSO stability would be explained, too. It can be inferred from (22) that the impedance characteristics are mainly influenced by initial operating conditions which are decided by power flow, also affected by control parameters of PLL and dq-current controller.

3.1.1. Impedance Sensitivity of Voltage Drops

When the fundamental voltage drops from 1.0 pu (636.4 V) to 0.6 pu while the other parameters in (22) keep the same as Appendix A, the impedance characteristics dynamics is shown in Figure 10. The reactance X_{PMSG} and resistance R_{PMSG} are listed below separately. It can be concluded that the X_{PMSG} changes from inductive to capacitive, crossing zero at 50 Hz. R_{PMSG} are negative around 50 Hz. To be noticed that X_{PMSG} gets larger along with voltage drops lower, while the resistance curve moves to the positive direction. Larger X_{PMSG} means lower resonant frequency but larger R_{PMSG} brings bigger total resistance, which means the influence on stability depends on which one is dominant.



Figure 10. Impedance sensitivity of voltage (Drops). (a) Reactance *X*_{PMSG}; (b) Resistance *R*_{PMSG}.

3.1.2. Impedance Sensitivity of Current Drops

Voltage remaining no changed at 1.0 pu, the impedance characteristics dynamics when the current reference I_{dref} drops from 1.0 pu (1847 A) to 0.6 pu is shown in Figure 11. It is worth noting that the output fundamental current equals to I_{dref} under the control strategy. X_{PMSG} gets lager and R_{PMSG} decreases while the output current drops. It can be inferred that this system will be more unstable.



Figure 11. Impedance sensitivity of current (Drops). (a) Reactance *X*_{PMSG}; (b) Resistance *R*_{PMSG}.

3.1.3. Impedance Sensitivity of PLL Parameters

Both voltage and current reference set at 1.0 pu increase the K_p and K_i and capture the impedance curve dynamics. The results are shown in Figure 12. From (a) we can know that when K_p increases alone, X_{PMSG} curve changes lightly while the equivalent R_{PMSG} curve becomes "wider", which means the frequency range of negative resistance is larger. Thus, larger K_p is not conducive to system stability. Whereas, the variation of K_i does not have obvious impact on stability.



Figure 12. Impedance sensitivity of PLL parameters (Increase). (a) Sensitivity of PLL proportional constant K_p ; (b) Sensitivity of PLL integral constant K_i .

3.1.4. Impedance Sensitivity of Current Controller Parameters

Similarly, the impedance curve dynamics while increasing the current controller parameters K_{pi} and K_{ii} are shown in Figure 13. It can be concluded that adjustments of K_{pi} and K_{ii} hardly affect the stability because the zero crossing frequency of resistance is nearly not changed.



Figure 13. Impedance sensitivity of current controller parameters (Increase). (a) Sensitivity of proportional constant K_{pi} in $H_i(s)$; (b) Sensitivity of integral constant K_{ii} in $H_i(s)$.

3.2. SSO Simulation and Theoretical Explanation

The structure diagram of the studied system is shown in Figure 14. The converter side parameters are set as Appendix A, the grid side parameters set in simulation are as Table 2. The SCR decreases from 5.37 to 2.13 at 3 s, and decreases to 1.73 at 4 s.



Figure 14. Diagram of subsynchronous oscillation (SSO) studied simulation system.

Table 2.	Grid	side	imped	lance	parameters.
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Symbol	Item	Value
V_s	System Voltage	0.82 kV (L-L, RMS)
	L_{g1} : Before 3 s	0.2 mH
L_g	$L_{g2}: 3 \sim 4 \text{ s}$	0.495 mH
	L_{g3} : After 4 s	0.62 mH
R_{f}	Filter resistance	0.02 Ω
$\dot{C_f}$	Filter capacitance	500 µF

Furthermore, the power waveform and current spectrum analysis are shown in Figure 15. From (a) we can find that the output power of D-PMSG oscillates twice at the SCR changing moments. The first oscillation quickly stabilized, but the second oscillation at 24 Hz gradually diverges until the system crashes. The magnitude of harmonic components at 5.5 s in output current is shown in Figure 15b, the 26/74 Hz sub/supsynchronous currents exist simultaneously.



Figure 15. Power waveform and current spectrum analysis of SSO. (**a**) Output power oscillation frequency; (**b**) Harmonic current components at 5.5 s.

Theoretical analysis is conducted to explain this simulation result. Since the current reference does not change, from Figure 6 we can know that the voltage at the PCC will drop along while the grid inductance L_g is increasing. So, the output power is also decreasing. Quantitative stability analysis should be done to figure out why the second oscillation is unstable. In these two SCR condition, calculate the power flow, then the total impedance of D-PMSG and grid $Z_{PMSG} + Z_{GRID}$ could be obtained as follows:

$$Z_{total}(s) = Z_{PMSG} + Z_{GRID} = R_{PMSG} + R_{GRID} + j(X_{PMSG} + X_{GRID}) = \frac{j\omega_1 L - sL - H_i(s - j\omega_1)}{H_i(s - j\omega_1)I_1 T_p(s)e^{j\varphi_{i1}} + V_1 T_p(s) - 1} + (R_f + \frac{1}{sC_f}) / / (sL_g)$$
(25)

Then, according to the developed RLC circuit-based stability criterion mentioned in the beginning of this section, the system will be unstable if:

$$R_{total}(f_r) < 0, \text{ when } X_{total}(f_r) = 0$$
(26)

This criterion is easier to implement by plotting them in the same figure and the direction of R_{total} at the resonant frequency is obviously to see. The analysis shown in Figure 16 gives the impedance comparison of D-PMSG and grid when SCR = 2.13 and 1.73.



Figure 16. Impedance comparison of *Z*_{*PMSG*} and *Z*_{*Grid.*}

The green vertical line indicates that the total resistance at the resonant frequency is positive when SCR = 2.13, which means this system is stable. This is consistent with the power waveform after 3 s in Figure 15a.

When SCR decreases to 1.73, the total resistance at the resonant frequency 72.77 Hz is -0.04, and this system is judged unstable under this operating condition. The f_p supsynchronous oscillation current will be captured by the GSC controller and introduces a $(2f_1 - f_p)$ subsynchronous current in return, as discussed before, about 27 Hz and 73 Hz, respectively. Moreover, the power will oscillate at a frequency of 23 Hz ($|f_p - f_1|$), which is very close to the simulation results after 4 s, considering the calculating and modeling errors. It can be concluded that the mechanism of SSO when SCR decreases is theoretically revealed.

4. Discussion

This paper focus on the modeling and analysis of sub/supsynchronous oscillation in D-PMSG based wind farm integrated to a weak AC grid. The small-signal harmonic linearization method is utilized to develop the positive sequence of the GSC. In this main step, the dynamics of PLL under harmonic voltage perturbation is analyzed. Moreover, the mechanism of sub/supsynchronous currents frequency coupling is revealed quantitatively. Based on the impedance model, the influence of converter parameters is further discussed. Finally, the influence of the SCR of AC system on SSO is well explained by impedance-based stability analysis. Simulation experiments are carried out to verify these theoretical discussions. Following conclusions can be made:

- 1. The D-PMSG's equivalent inductance *X*_{PMSG} is positive at subsynchronous frequency while negative (capacitive) at supsynchronous frequency, which means the resonance between D-PMSG and weak grid occurs at the supsynchronous frequency. The relationship of coupled sub/supsynchronous currents could be quantitatively calculated.
- 2. The D-PMSG's impedance is sensitive to the PCC voltage and output current, which are decided by power flow. Further proof that when the output current is relatively small as a result of low wind speed, it is very likely to observe oscillations in this system. The influence of control parameters is also discussed. No obvious impact of current controller is found.
- 3. A simulation experiment was conducted to study the mechanism of SSO when SCR decreases. Both simulation results and theoretical analysis proved that when the grid side impedance increases, the grid-connected D-PMSG system will be more unstable.

Future work based on the work in this paper will discuss the following several issues: The first issue is about how to obtain the reduced-order equivalent model of wind farm which contains hundreds of wind turbine generators. The second issue focus on oscillation suppression, proposing advice related to parameters adjustment or additional damping control strategy. The last issue will discuss the interaction with synchronous generator, further analyzing the accident in Xinjiang, China.

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Appendix A

The PSCAD-EMTDC simulation experimental parameters setup in this paper are as following: Fundamental frequency: $f_1 = 50$ Hz; dc bus voltage: $V_{dc} = 1300$ V; dq current controller parameters: $H_i(s) = (K_{pi} + K_{ii}/s)$ where $K_{pi} = 0.25$ and $K_{ii} = 355$; PLL parameters: $H_{pll}(s) = (K_p + K_i/s)/s$ where $K_p = 0.085$ and $K_i = 32$; current reference: $I_{dref} = 1847$, $I_{qref} = 0$; converter circuit parameters: L = 0.15 mH.

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