



Article Energy Concepts and Critical Plane for Fatigue Assessment of Ti-6Al-4V Notched Specimens

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Abstract: In the present paper, the fatigue life assessment of notched structural components is performed by applying a critical plane-based multiaxial fatigue criterion. Such a criterion is formulated by using the control volume concept related to the strain energy density criterion. The verification point is assumed to be at a given distance from the notch tip. Such a distance is taken as a function of the control volume radii around the notch tip under both Mode I and Mode III loading. The accuracy of the present criterion is evaluated through experimental data available in the literature, concerning titanium alloy notched specimens under uniaxial and multiaxial fatigue loading.

Keywords: control volume concept; critical plane approach; fatigue life assessment; severely notched specimens; strain energy density

1. Introduction

From the pioneering work by Jasper at the beginning of the 1920s [1], energy-based criteria have been widely used for estimating multiaxial fatigue lifetime of engineering components subjected to time-varying loading [2–10]. The fundamental idea on which such criteria are based is the assumption that energy (calculated in different ways) is always proportional to fatigue damage.

Among the different energy-based criteria available in the literature [2], those proposed by Garud [3] and Ellyin et al. [4–6] are very interesting. The multiaxial fatigue assessment has to be performed through the cyclic plastic deformation according to Garud, whereas Ellyin et al. argued that both cyclic plastic energy and elastic energy have to be properly taken into account in the fatigue lifetime estimation.

It is worth noting that the fatigue life of notched structural components subjected to cyclic loading can be evaluated by means of energy-based concepts. In particular, the concept of strain energy density (SED) has originally been implemented in different criteria available in the literature to predict the fatigue behavior of notched components under uniaxial tensile loading [7,8]. Subsequently, SED-based criteria have been formulated for multiaxial loading [9,10].

The main drawback of the above criteria is that the fatigue behavior is assumed to depend only on the stresses at the notch tip. Therefore, any SED-based criterion cannot be applied at the tip of sharp notches since both the stress state and SED tend toward infinite.

In order to overcome the above problem, Lazzarin and Zambardi suggested considering a small but finite volume of material close to the notch tip (that is, the point of stress singularity), over which the SED has a finite value [11]. More precisely, the fatigue damage parameter for blunt and sharp notched structural components under tensile loading (Mode I) is the mean value of the SED, related to a control volume around the notch tip [11,12]. The radius of the above volume depends on the unnotched specimen fatigue limit, the notch stress intensity factor (NSIF) range and the elastic Poisson's

ratio. The Lazzarin and Zambardi criterion has also been extended to notched structural components subjected to multiaxial loading [13–18] as well as to welded joints [19–21].

Recently, an attempt to perform the fatigue lifetime assessment of notched specimens through energy concepts has been made by Carpinteri and co-workers [22–24], relatively to Ti–6Al–4V titanium alloy specimens under uniaxial and multiaxial loading (biaxiality ratio 0.6 and 2.0), where the control volume concept has been implemented in the original formulation of the critical plane-based multiaxial fatigue criterion [25,26].

In the present paper, the above criterion is proposed to be applied together with the control volume concept, and fatigue assessment is performed in a verification point at a distance related to energy concepts.

It is validated by means of experimental data related to V-notched specimens made of titanium grade 5 alloy, subjected to mixed mode loading [27]. Such material and other titanium alloys have attracted significant interest being extensively used in leading industries, due to their low density and high specific strength at elevated temperature (aeronautics, nuclear energy) and their compatibility with human tissues (applications in the biomedical field) [28–32]. In the latter field, such materials can be used, for example, in the form of β -type titanium porous structures [30,31], and functionally graded Ti-6Al-4V alloy interconnected mesh structures [32].

In Section 2, the theoretical framework of the strain-based criterion by Carpinteri et al. is outlined, also implementing the concept of control volume [22–24]. Then, the validation of such a criterion by means of experimental data for combined tension and torsion cyclic loading on V-notched specimens is shown in Section 3, and finally, the conclusions are drawn in Section 4.

2. Theoretical Framework of Strain-Based Multiaxial Fatigue Criterion

The strain-based multiaxial fatigue criterion by Carpinteri et al. [25,26] is related to the critical plane approach and consists of three steps detailed in the following sub-sections: Step I, where the verification point position (point *P*) is analytically defined by means of the control volume concept, Step II, where the critical plane orientation is theoretically determined, Step III, where the fatigue life assessment is performed in such a plane at point *P*. The criterion is suitable to be applied to ductile materials under low cycle fatigue loading.

2.1. Step I: Verification Point Position

The fatigue lifetime is computed at point P which is on the notch bisector at a certain distance, r, from the notch surface [25,26] (Figure 1). The expression of the above distance is obtained by means of a best fitting procedure (details are provided in Reference [24]) and is given by [22]:

$$r = -(0.221)^{\lambda - 1.484} \cdot R_m + 11.3R_m \tag{1}$$

where λ is the ratio between the amplitude of the remote shear stress and the amplitude of the remote normal stress (named biaxiality ratio) and R_m is computed as the mean value of R_1 (control volume radius under Mode I loading) and R_3 (control volume radius under Mode III loading). The last ones are calculated by the SED criterion, and are functions of notch stress intensity factor (NSIF) ranges (ΔK_{1A} , ΔK_{3A}), high-cycle fatigue strengths of smooth specimens ($\Delta \sigma_{1A}$, $\Delta \tau_{3A}$) and the notch geometry [33]. More precisely, the above radii are computed according to the following equations [33]:

$$R_1 = \left(\sqrt{2\mathbf{e}_1} \cdot \frac{\Delta K_{1A}}{\Delta \sigma_{1A}}\right)^{\frac{1}{1-\lambda_1}} \tag{2a}$$

$$R_3 = \left(\sqrt{\frac{\mathbf{e}_3}{1+\nu_e}} \cdot \frac{\Delta K_{3A}}{\Delta \tau_{3A}}\right)^{\frac{1}{1-\lambda_3}} \tag{2b}$$

where e_1 and e_3 are two parameters depending on the V-notch geometry, v_e is the elastic Poisson ratio, and λ_1 and λ_3 are the eigenvalues for Mode I and Mode III, respectively, calculated by means of finite element analysis, as is discussed in Reference [33].



Figure 1. Verification point position according to the control volume concept for V-notch.

A finite element model is employed in order to numerically compute the strain state at verification point *P* [24]. In particular, linear transient dynamic analyses are performed on notched specimens through the Commercial Package Straus7[®] [34], by adopting both 6- and 8-node tridimensional finite elements. Only one half of each specimen is modeled, taking advantage of the geometric symmetry. Moreover, the adopted discretization is shown in Figure 2, where the finite element mesh is that adopted after a convergence analysis, being the minimum finite element size equal to about 0.25 times the value of the notch root radius.



Figure 2. Discretization adopted for the finite element model.

2.2. Step II: Critical Plane Orientation

Let us consider the strain state at point *P* and a generic time instant *t* of the fatigue loading history, the principal strain ε_1 , ε_2 and ε_3 (with $\varepsilon_1 \ge \varepsilon_2 \ge \varepsilon_3$) and the corresponding directions 1, 2 and 3 (identified by means of the principal Euler angles ϕ , θ and ψ) can be determined. Since the principal

directions are usually time-varying under fatigue loading, Carpinteri et al. proposed to compute the averaged directions $\hat{1}$, $\hat{2}$ and $\hat{3}$ on the basis of the instantaneous ones, through the averaged values of the principal Euler angles [35].

Then, the critical plane orientation is regarded to depend on such averaged directions. In more detail, the normal vector w to the critical plane is assumed to be linked to the 1-direction through an off-angle δ , given by the following empirical expression [25,26]:

$$\delta = \frac{3}{2} \left[1 - \left(\frac{1}{2\left(1 + \nu_{eff}\right)} \frac{\gamma_a}{\varepsilon_a} \right)^2 \right] 45^\circ$$
(3)

being v_{eff} the effective Poisson ratio (that is, function of both elastic, v_e , and plastic, v_p , Poisson's ratio), and ε_a and γ_a the strain amplitudes in the well-known tensile and torsional Manson–Coffin equations, respectively. Note that the above rotation (Equation (2)) has to be performed from $\hat{1}$ to $\hat{3}$ in the principal plane $\hat{1}\hat{3}$.

2.3. Step III: Fatigue Life Assessment

The fatigue life assessment is performed through the following expression, where the left-hand term corresponds to an equivalent strain whose amplitude is a function of the amplitudes $\eta_{N, a}$ and $\eta_{C, a}$ of both the normal and the tangential displacement vectors [25,26]:

$$\varepsilon_{eq,a} = \sqrt{(\eta_{N,a})^2 + \left(2\left(1 + \nu_{eff}\right) \cdot \frac{\varepsilon_a}{\gamma_a}\right)^2 (\eta_{C,a})^2}$$
(4)

Note that all terms in Equation (3) depend on the number of loading cycles to failure. Moreover, the values of $\eta_{N, a}$ and $\eta_{C, a}$ are obtained from an analytical procedure by taking into account both the strain tensor at point *P* and the critical plane orientation. Details can be found in Reference [24].

The fatigue life (i.e. the theoretical number of loading cycles to failure, N_f) is iteratively computed by equaling Equation (4) [24] with the Manson–Coffin normal strain amplitude ε_a .

3. Criterion Validation

In order to check the accuracy of the criterion presented in Section 2, some experimental data are selected from the technical literature [27,33]. Such data are related to uniaxial and multiaxial fatigue tests (with nominal loading ratio equal to -1) carried out on circumferentially V-notched cylindrical specimens characterized by (Figure 3):

- V-notch with a depth of 6 mm;
- Opening angle of 90°;
- Notch root radius of 0.1 mm.



Figure 3. Geometrical sizes of the titanium alloy V-notched specimens subjected to tension and/or torsion fatigue loading.

The above specimens were made of grade 5 titanium alloy (Ti-6Al-4V), commonly used in aerospace and naval applications. The above titanium alloy is characterized by very good static and fatigue properties (Table 1) with a high strength-to-mass ratio.

E	ν _e	σ _u	σ _y	Δ <i>K</i> _{1A}	ΔK _{3A}	$\Delta \sigma_{1A}$	Δτ _{3A}
[GPa]	[-]	[MPa]	[MPa]	[MPa·mm ^{0.445}]	[MPa·mm ^{0.333}]	[MPa]	[MPa]
110.0	0.3	978.0	894.0	452.0	1216.0	950.0	776.0

Table 1. Static and fatigue properties of material examined [27,33].

The Manson–Coffin parameters of both tensile and torsional equations are reported in Reference [22].

By taking full advantage of v_e , ΔK_{1A} , ΔK_{3A} , $\Delta \sigma_{1A}$ and $\Delta \tau_{3A}$, the control volume radii R_1 and R_3 are equal to 0.051 mm and 0.837 mm, respectively.

Before being fatigue tested, the specimens have been polished in order to remove surface scratches and marks due to machine tools. Fatigue tests have been performed by means of an MTS 809 servo-hydraulic axial-torsional testing system with a 100 kN axial cell and a 1100 Nm torsion cell. Moreover, all tests have been carried out under load control, with a frequency between 10 and 15 Hz. Details of the loading conditions related to the experimental fatigue tests being examined are reported in Reference [27,33]. In particular, we consider four different loading conditions characterized by experimental fatigue life, $N_{f,exp}$, between 10^3 and $6 \cdot 10^5$ loading cycles, and more precisely:

- 1. Pure tension fatigue loading;
- 2. Pure torsion fatigue loading;
- 3. Combined in-phase ($\Phi = 0^{\circ}$) tension and torsion fatigue loading;
- 4. Combined out-of-phase ($\Phi = 90^{\circ}$) tension and torsion fatigue loading.

The biaxiality ratio λ related to multiaxial loading conditions is equal to 2.

According to the above loading conditions, the value of the distance r (Equation (1)) turns out to be:

- (a) $r = 1.9 \cdot R_m$ for pure tension fatigue loading ($\lambda = 0$);
- (b) $r = 11.3 \cdot R_m$ for pure torsion fatigue loading ($\lambda = \infty$);
- (c) $r = 10.8 \cdot R_m$ for combined tension and torsion fatigue loading ($\lambda = 2.0$).

Figure 4 shows experimental fatigue life, $N_{f,exp}$, plotted against the theoretical one, N_f . In particular, 79% of results is conservative and 63% is included into 3× band. Moreover, we can remark that better estimations are obtained by considering only the in-phase multiaxial fatigue data (Figure 4b) since all the results fall within 3× band, whereas almost all the results related to out-of-phase data are outside the above band (Figure 4c).

In any case, when estimations do not fall within the reference bands, the errors made by the present criterion are, in general, on the conservative side. This strongly supports the idea that the Carpinteri et al. criterion, applied together with the control volume concept, can be used successfully to assess notched components in situations of practical interest, always allowing an adequate margin of safety to be reached.



Figure 4. Accuracy of the present criterion in estimating the fatigue lifetime of Ti-6Al-4V notched specimens: (a) Uniaxial loading, (b) multiaxial proportional loading, (c) multiaxial non-proportional loading.

Figure 5 shows $N_{f,exp}$ as a function of the equivalent strain amplitude, $\varepsilon_{eq, a}$ (see Equation (4)). Note that the solid line is the experimental tensile Manson–Coffin equation. Since all the theoretical data lie very close to the experimental curve, it can be concluded that the accuracy level of the employed criterion is satisfactory.



Figure 5. Experimental fatigue life $N_{f,exp}$ against equivalent strain amplitude $\varepsilon_{eq,a}$.

The above considerations can also be made by examining the values of the error index, *I*, computed as follows [24]:

$$I = \frac{\varepsilon_{eq,a} - \varepsilon_a}{\varepsilon_a} \cdot 100\%$$
(5)

In particular, Figure 6 shows the relative frequency of the *I* absolute value. It can be observed that the frequency distribution is close to zero, with 74% of the results in the range $0\% \le |I| \le 15\%$.



Figure 6. Absolute value of the error index *I* according to the present criterion.

In conclusion, we can remark that the implementation of energy concepts, based on the control volume, in the above strain-based multiaxial fatigue criterion appears an interesting tool for evaluating the fatigue behavior of severely notched components.

4. Conclusions

In the present paper, the fatigue life assessment of notched structural components has been performed by applying a critical plane-based multiaxial fatigue criterion. Such a criterion has been formulated by using the control volume concept related to the strain energy density criterion.

The material point located at a given distance from the notch tip is assumed to be the verification point. Such a distance has been taken to be a function of the control volume radii around the notch tip under both Mode I and Mode III loading. Once the position of the verification point and the orientation of the critical plane have been analytically determined, the fatigue lifetime has theoretically been evaluated through an equivalent normal strain amplitude, acting on the critical plane, together with the tensile Manson–Coffin curve.

The accuracy of the present criterion is evaluated through experimental data available in the literature, related to titanium alloy V-notched specimens under uniaxial and multiaxial fatigue loading. As far as the experimental data here examined are concerned, the joint application of the strain-based criterion and the control volume concept provides quite satisfactory fatigue life estimations.

On the basis of the encouraging results herein obtained, the present criterion seems to be able to correctly estimate the fatigue life of a structure with a stress concentrator (as a notch), by reaching an adequate margin of safety. However, different materials, notch geometries, and loading conditions need to be examined in order to develop a useful fatigue design tool.

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Nomenclature

1,2,3	principal strain directions
î, 2, 3	averaged principal strain directions
Ε	elastic modulus
Ι	error index
N_f	theoretical fatigue life
N _{f,exp}	experimental fatigue life
P	verification point
r	distance of the verification point <i>P</i> from the notch tip
R_m	mean control volume radius
R_1	control volume radius related to Mode I
R_3	control volume radius related to Mode III
t	time
w	perpendicular unit vector to the critical plane
γa	Manson–Coffin shear strain amplitude
δ	angle between the averaged direction $\hat{1}$ and the normal w to the critical plane
ΔK_{1A}	notch stress intensity factor range under Mode I
ΔK_{3A}	notch stress intensity factor range under Mode III
$\Delta \sigma_{1A}$	high-cycle fatigue strength of smooth specimens under Mode I
$\Delta \tau_{3A}$	high-cycle Fatigue strength of smooth specimens under Mode III
$\varepsilon_1, \varepsilon_2, \varepsilon_3$	principal strains, with $\varepsilon_1 \ge \varepsilon_2 \ge \varepsilon_3$

ε_a Manson–Cottin normal strain amplitu

- $\varepsilon_{eq,a}$ equivalent normal strain amplitude
- $\eta_{N,a}$ amplitude of the normal displacement vector component acting on the critical plane
- $\eta_{C,a}$ amplitude of the tangential displacement vector component acting on the critical plane
- λ biaxiality ratio
- v_e elastic Poisson ratio
- v_{eff} effective Poisson ratio
- v_p plastic Poisson ratio
- σ_u ultimate tensile strength
- σ_y yield strength
- Φ phase angle between tension and torsion loading

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