

# Article

# Design Optimization Approach of a Large-Scale Moving Framework for a Large 5-Axis Machining Center

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Received: 21 July 2018; Accepted: 5 September 2018; Published: 10 September 2018



# Featured Application: The proposed 3-step design optimization method based on multi-objective optimization and finite element analysis can be considered as a guide for optimizing large-scale moving frameworks to balance the moving mass, material costs, and structural stiffness.

Abstract: The traditional machine tool design method with metal materials makes large-scale moving structures very heavy, which seriously impacts dynamic performance and results in significant energy consumption. Using sandwich structures of composite materials to replace metal materials is an important strategy for lightweight large-scale moving structures. However, this kind of substitution is generally believed to be difficult because foam-filled sandwich structures usually show nonlinear characteristics and must balance the moving mass, material costs, and structural stiffness. In the present study, we proposed a design optimization approach for a large-scale moving framework in a large 5-axis machining center (L5AMC) considering large dimensions in the *x*, *y*, and *z* work space and high machining speed with the aim of minimizing the displacements of the milling head. An improved approach, named the 3-step design optimization, was executed to obtain the optimum framework structures to solve the contradiction between the moving mass, material costs, and structural stiffness. This approach was based on multi-objective optimization and finite element analysis. The structural stiffness of the framework after optimization increased by 89% compared with before optimization although the mass increased by 6% and the material costs increased by 9%. A finite element simulation under four given operational loads showed that the displacements of the milling head were all less than the design requirement of 0.25 mm. The results indicated that the proposed 3-step design optimization approach for the optimal design of a large-scale moving framework was feasible and successful. A 40 m  $\times$  6 m  $\times$  4 m L5AMC prototype was manufactured, and the actual verification results indicated that the large-scale moving framework fully met the design requirements of the L5AMC and reduced energy consumption.

**Keywords:** large-scale moving structure; 3-step design optimization; sandwich structure; multi-objective optimization; finite element analysis



#### 1. Introduction

The demands for processing complex parts with a free-form surface have resulted in increased use of 5-axis machine tools in automotive, aerospace, die making, and many other industries [1,2]. The role of the machine tool is to ensure the precise movement relationship between the tool and the workpiece. Meanwhile, the moving parts of machine tools consume large amounts of energy [3]. Therefore, precision and energy consumption are guidelines for machine tool design, and are influenced by many factors including the stiffness error caused by structural deformation, assembly error results in tool position error, system dynamic responses under excitation of operational loads, and so on [4–7]. In order to reduce energy consumption, lightweight design and optimization techniques are applied to decrease the moving masses and improve the mass-to-payload ratio [8,9]. Over the last few decades, to improve the accuracy, stiffness, and dynamic performance of machine tools, various lightweight and optimization design methods and strategies have been investigated by many researchers at the early design stage; consequently, structural optimization and lightweight methods have been successfully applied in optimizing dynamical systems and lightweight machines [10–18].

Lightweight design countermeasures are usually taken through appropriate material selection and implementing a structural optimization method. Kim et al. [12] presented a method using composite-foam-resin concrete sandwich structures instead of metal materials for the lightweight design of micro-EDM machines. Li et al. [13] reported a stiffness design of machine tool structures based on a biologically inspired topology optimization method, while Kroll et al. [14] discussed the general influence of lightweight design approaches on energy efficiency in machine tools, as well as restrictions on the maximum mass reduction for structural components. Li and Lu [15] reported a design scheme of a lightweight wind turbine tower based on the integration of nanostructured materials produced by a surface mechanical attrition treatment process; the study results revealed that there is sufficient margin for further weight reduction in the traditional wind turbine tower design. In optimization design, Strano et al. [16] proposed an optimization model suitable for press frame designs with respect to energy efficiency. Wu et al. [17] presented an optimization approach for the concept design of machine tools; the results showed that the principal dimensions of all structural parts could be determined while minimizing the weight of the machine and maintaining sufficient stiffness. In order to analyze the dynamic behavior and tool deviations, a dynamic model of a 3-axis gantry milling machine considering axis coupling effects was proposed by Wang et al. [18]. Sandwich structures are commonly used materials for lightweight designs, and their mechanical behaviors are based on their structural features: They are built from two layers, i.e., a stiff and strong skin layer, and a compliant and lightweight core layer [19]. There have been a number of applications in civil and military aircrafts, launch vehicles, wind turbine blades, and marine structures in which composite and sandwich material systems were used as primary structures [20]. Sandwich structures can often sustain large deformations under constant load, enabling them to absorb significant amounts of energy, and to have higher mechanical properties [21–27].

The structure design methods in existing literatures cannot be directly adapted to the design optimization framework for a large 5-axis machining center (L5AMC) due to the large dimensions in the *x*, *y*, and *z* work space and high machining speed. The traditional machine tool design method makes the amount of metal used to build the large-scale moving framework account for most of the total weight, and thus, it seriously impacts the dynamic performance and results in significant energy consumption. Hence, using sandwich structures of composite materials to replace metal materials to improve dynamic performance and reduce energy consumption has been a key technology for large-scale moving framework structure design. However, this kind of substitution is generally believed to be difficult because foam-filled sandwich structures usually show nonlinear characteristics and must balance the moving mass, material costs, and structural stiffness. Although studies on lightweight and optimized machine tool structures have long been presented, the design optimization of a large-scale moving framework to improve structural performance and reduce energy consumption still exhibits many challenges, such as how to avert the sandwich panel to generate the well-known

"curtain effect" [28] due to the large dimensions of the framework structure, how to guarantee high machining speed, lightweight moving mass, and the higher structural rigidity. Therefore, the primary objective of this study was to propose a design optimization framework approach for L5AMC to meet the large dimensions in the work space, and to minimize the displacements of the milling head while maintaining lightweight design for good dynamic drive performance, higher structural stiffness, and low material costs. To achieve these goals, the present study presented an improved approach, named the 3-step design optimization, to obtain the optimum framework structures and solve the contradiction between the moving mass, material costs, and structural stiffness. This approach was based on multi-objective optimization and finite element analysis method.

# 2. Overall Layout Analyses

# 2.1. Structural Configuration Analysis

Most common 5-axis machine tools have three structural configurations: TTTRR, RRTTT, and RTTTR [29], where the three Ts represent translational axes (the *x*-, *y*-, and *z*-axis) and the two Rs represent rotational axes (the A- and C-axis, or B- and C-axis). Table 1 depicts the structural characteristics of the three configurations.

No	Configuration	Diagram	A Typical Topology Diagram	Structure Characteristics
1	TTTRR	Z <sup>z</sup> VArB	Reference body x-axis Workpiece Tool A- or B-axis C-axis	The cutting tool is supported by a double pan head. Three translational axes describe a fixed Cartesian frame, which can be set on the tool or workpiece side as required.
2	RRTTT	x Tool Workpiece	A- or B-axis C-axis Workpiece Tool	The workpiece is supported by a double turntable. Three translational axes can be set on the tool or workpiece side as required.
3	RTTTR	Tool z Workpiece	Reference body C-axis y-axis y-axis y-axis y-axis y-axis A- or B-axis	The workpiece is supported by a turntable, and the cutting tool is supported by a single pan head. Three translational axes can be set on the tool or workpiece side as required.

**Table 1.** Characteristics of three structural configurations of 5-axis machine tools.

From Table 1, it is observed that the TTTRR structure machine tool can be used for fabricating large parts because the three T and two R axes can all be set on the cutting tool side, and the workpiece can be fixed. Therefore, the TTTRR 5-axis machine tool has a large bearing capacity. In the same way, the RRTTT structure machine tool can be used for fabricating small parts due to the two R axes being set on the workpiece side. Compared to the TTTRR and RRTTT, the RTTTR structure machine tool can be used for fabricating medium-sized parts.

#### 2.2. Overall Layout of the L5AMC

Based on the above structural configuration analysis, the L5AMC proposed in this paper used the TTTRR structure because it was designed for fabricating large composite material free-form surface parts. The structure of the L5AMC had 40 m × 6 m × 4 m large translational axes, a  $\pm 110^{\circ}$  swing angle of the B-axis, and a  $\pm 360^{\circ}$  turning angle of the C-axis. The design requirements for maximum deformation of the milling head was 0.25 mm in the *x*, *y*, and *z* coordinate directions. Figure 1 presents the overall layout of the L5AMC proposed in this paper.



**Figure 1.** Preliminary design of the L5AMC: (**A**) overall layout; (**B**) large-scale moving framework; (**C**) portal.

#### 3. Materials and Methods

#### 3.1. Design Optimization Methods

The large-scale moving framework with the 8040 mm  $\times$  3270 mm  $\times$  1680 mm portal (Figure 1) was one of the most important components of the L5AMC. According to the traditional machine tool design method, the amount of metal used to build the framework accounts for most of the total weight, which seriously impacts the dynamic performance and results in significant energy consumption. Therefore, the traditional machine tool design method is not suitable for the large-scale moving framework, which requires lightweight design for good dynamic drive performance, higher specific stiffness, and high positioning accuracy and machining precision. To achieve these goals, we presented an improved method, named the 3-step design optimization. It included the following three steps: (1) Using sandwich structures of composite materials to replace metal materials to achieve lightweight design of the large-scale moving framework; (2) multi-objective optimization of sandwich structures to solve the contradiction between the moving mass, material costs, and structural stiffness; and (3) design optimization framework structures to minimize the displacements of the milling head based on finite element analysis (FEA) method.

#### 3.2. General Model of the Sandwich Structure

In this study, we first replaced metal materials with sandwich structures of composite materials to reduce the mass of the framework, and by doing so, guaranteeing the structural stiffness as high as possible based on multi-objective optimization and FEA. Figure 2 presents the general model of the sandwich structure of composite materials.



Figure 2. General model of sandwich structure: (A) in three dimensions; (B) in the z-direction.

From Figure 2, it is observed that following relationships exist:

$$\begin{cases}
 a = t_s n \\
 d = 2a + c
\end{cases}$$
(1)

where *a* and *c* represent the thickness of the skin layer and core layer, respectively; *d*, *b*, and *l* represent the total thickness, width, and length of the sandwich structure, respectively;  $t_s$  represents the thickness of each skin layer; and *n* represents the layer number of the skin layer.

#### 3.3. General Method for Optimization of Sandwich Structural Parameters

To balance the moving mass, material costs, and structural stiffness while considering nonlinear characteristics of the foam-filled sandwich structures, the optimal sandwich structural parameters were obtained by employing the multi-objective optimization method. The general formula for multi-objective optimization is as follows:

$$\min_{x} \quad F(x) = (f_1(x), f_2(x), f_3(x), \dots, f_i(x))^T \\ x_i^l \le x_i \le x_i^u \quad i = 1, \dots N$$
(2)

where  $f_1, f_2, f_3, ..., f_i$  are the objective functions;  $x_i^l$  and  $x_i^u$  are the lower and upper bounds of the design variables; and *N* is the number of variables.

In general, conflict occurs when several objectives are considered within the optimization, meaning that an increased performance in one objective may lead to decreased performance in others [30]. Therefore, there is a trade-off between objectives. In this study, multi-objective optimization acted to solve the contradiction between the mass, material costs, and structural stiffness.

For the general model of the sandwich structure (Figure 2), the equivalent bending stiffness (*EI*) of the sandwich panel can be expressed as follows [12]:

$$\begin{cases}
EI = E_s I_s + E_c I_c \\
E_s I_s = E_s \left[\frac{bd^3}{12} - \frac{bc^3}{12}\right] \\
= E_s \left[\frac{ab(a+c)^2}{2} + \frac{ba^3}{6}\right] \\
E_c I_c = E_c \frac{bc^3}{12}
\end{cases}$$
(3)

Furthermore, the equivalent mass of the sandwich panel can be expressed as:

$$\begin{cases} m = m_s + m_c = V\rho \\ m_s = V_s \rho_s = 2abl\rho_s \\ m_c = V_c \rho_c = cbl\rho_c \end{cases}$$
(4)

Similarly, the material cost (*C*) can be expressed as follows:

$$\begin{cases}
C = C_s + C_c = m \times C_{kg} \\
C_s = m_s C_{kgs} \\
C_c = m_c C_{kgc}
\end{cases}$$
(5)

where subscripts *s* and *c* represent the skin material and core material, respectively; *E* represents young's modulus; *I* represents moment of inertia; *m* represents the mass;  $\rho$  represents the equivalent mass density; *V* represents the total volume; and  $C_{kg}$  represents the material cost per kg.

Table 2 depicts the objective functions defined within the size optimization.

Objective	Function	Description
Minimize	Mass	Defined by Equation (4)
Minimize	Material costs	Defined by Equation (5)
Maximize	Stiffness	Defined by Equation (3)

Table 2. Objective functions defined within the size optimization.

#### 3.4. Materials for Sandwich Structure

Skin layer materials were preliminary selected as carbon fiber (CF), glass fiber (GF), and Al, respectively; core layer materials were preliminary selected as polyvinyl chloride (PVC) foam, and polyurethane (PUR) foam, respectively. The design variables were n,  $t_s$  and c. Table 3 lists the above materials' properties used within the optimization studies.

	]	Material Propertie	s	$C_{kg}$ (USD/kg)	
Material Type	E (GPa)	G (GPa)	ho (kg/m <sup>3</sup> )		
CF	200	4.4	1650	60	
GF	16.7	2.237	1704	15	
Al	70	26.1	2700	6	
PVC foam	0.13	0.035	100	55	
PUR foam	0.055	0.021	150	22	
PVC foam PUR foam	0.13 0.055	0.035 0.021	100 150	55 22	

Table 3. Materials properties and the costs used within the optimization studies.

Note: Data were taken from the literature [30,31], and costs were converted from SEK to USD.

#### 4. Modeling and Stiffness Analysis

#### 4.1. Sandwich Structural Parameters Optimization

The multi-objective optimization has a rather different perspective compared with single-objective optimization. There is only one global optimum in single-objective optimization, but in multi-objective optimization there is a set of solutions, named the Pareto-optimal set, which are considered to be equally important; all of them constitute global optimum solutions [32–34]. Non-dominated Sorting Genetic Algorithm II (NSGA-II) is regarded as an effective and efficient multi-objective optimization technique in various applications [33,34]. To optimize the sandwich structures, multi-objective optimization of sandwich structural parameters based on an improved NSGA-II algorithm were conducted using MATLAB R2013a software according to Equations (3)–(5), where the lower and upper bounds of the design variables were:  $0.1 \le t_s \le 1.0$ ,  $1 \le n \le 10$  and  $20 \le c \le 30$  respectively. The detailed optimization process of the sandwich structural parameters will be reported in another investigation. Table 4 listed two of the optimal results from the Pareto-optimal set of the sandwich structural parameters in combination with commercial specifications of skin layer and core layer materials for further framework structural optimization.

Table 4. Two of the optimal results of the sandwich structure of the portal.

Name	Material Type —	Parameters			Properties	
Iname		n	<i>t<sub>s</sub></i> (mm)	<i>c</i> (mm)	EI (Nm <sup>2</sup> )	<i>m</i> (kg/m <sup>2</sup> )
Composite plate Reinforced composite plate	CF + PVC CF + PVC	4 8	0.57 0.57	24 20	0.27 0.47	8.104 14.770

Figure 3 presented the schematic diagrams of the two types of sandwich panels, where,  $[0^{\circ} -45^{\circ} 45^{\circ} 0^{\circ}]$  and  $[0^{\circ} 0^{\circ} -45^{\circ} 0^{\circ} 0^{\circ} 45^{\circ} 0^{\circ} 0^{\circ}]$  represent orientation angle of CF in per layer. Zero degree orientation angle is for axial load (*z*-direction load in the present study), and  $\pm 45^{\circ}$  orientation angles are for shear load (*x*-direction or *y*-direction load in the present study).



Figure 3. Two types of sandwich panels: (A) composite plate; (B) reinforced composite plate.

#### 4.2. Modeling for Large-Scale Moving Framework

In order to analyze the maximum displacements of the milling head, models of the large-scale moving framework were established (Figure 4). They were composed of aluminum alloy beams (used internal support structure), composite plates, and small aluminum alloy panels placed on the left and right sides. Different aluminum alloy beams were used for mounting purposes and to enhance system stiffness to avert the sandwich panel generating the well-known "curtain effect" (see Figure A1) due to the large dimensions of the portal. Table A1 lists the major material parameters used for the design of the large-scale moving framework.



**Figure 4.** Models of the framework: (**A**) Three-dimensional model; (**B**) finite element model of portal before optimization; (**C**) finite element model after optimization; (**D**) support model.

In these models,  $F_x$ ,  $F_y$ , and  $F_z$  represent loads acting on the milling head in the x, y, and z directions, respectively. The milling head was mounted at the end of the lifting beam.

#### 4.3. System Stiffness Analysis

It is well known that the system stiffness of the framework *K* can be expressed as follows:

$$\begin{cases}
K_x = \frac{F_x}{\Delta x} \\
K_y = \frac{F_y}{\Delta y} \\
K_z = \frac{F_z}{\Delta z}
\end{cases} (6)$$

where  $K_x$ ,  $K_y$ , and  $K_z$  represent the system stiffness of the framework in the three coordinate directions;  $F_x$ ,  $F_y$ , and  $F_z$  represent loads acting on the milling head in the three coordinate directions; and  $\Delta x$ ,  $\Delta y$ , and  $\Delta z$  represent the displacement of the milling head in the three coordinate directions.

Consequently, minimizing the displacements of the milling head is a key step to ensuring system stiffness, positioning accuracy, and machining precision when the loads are given. Table 5 lists the four given values of operational loads for further design optimization of the framework.

No	Name	Operational Loads	Description	Given Value
1	Load 1	G	G = mg ( <i>m</i> represents mass of the framework, <i>g</i> represents gravity acceleration)	-
2	Load 2	$G + F_x$	$G = mg$ and $F_x = ma_x$ ( $a_x$ represents acceleration in the <i>x</i> -direction. The maximum $a_x$ is for starting and stopping)	$a_{xmax} = 1.5 \text{ m/s}^2$
3	Load 3	$G + F_y$	$G = mg$ and $F_y = ma_y$ ( $a_y$ represents acceleration in the <i>y</i> -direction. The maximum $a_y$ is for starting and stopping)	$a_{ymax} = 1.5 \text{ m/s}^2$
4	Load 4	$G + F_z$	$G = mg$ and $F_z = ma_z$ ( $a_z$ represents acceleration in the <i>z</i> -direction. The maximum $a_z$ is for starting and stopping)	$a_{zmax} = 1.5 \text{ m/s}^2$

Table 5. Operational loads for the milling head in the manufacturing process.

#### 5. Optimization Design for the Framework

#### 5.1. Optimization Designs for the Portal

In order to determine the optimum structure of the large-scale moving framework, the portal structure was first optimized based on the FEA method after the sandwich structural parameters optimization. The FEA was carried out to analyze the maximum deformation of the portal under the given operational loads. Boundary conditions are use to describe the interaction of the structure with its environment as shown in Figure 5, where vertical support of the portal is applied as fixed vertical displacement at marked positions, as shown in Figure 5A. Horizontal support of the portal is applied as fixed displacement in *x*-direction and fixed displacement in *y*-direction at marked positions, as shown in Figure 5B. The weight of the traverse and lifting beam is applied as forces in their center of gravity (COG), as shown in Figure 5C. The acceleration for these two components is also applied at their center of gravity. The COG is rigidly linked to the connection points of the portal. Similarly, the weight of the milling head was considered by a point mass at its mass origin. The point mass was connected to all gravity and acceleration loads, as shown in Figure 5D. The top view of all boundary conditions is shown in Figure 5E.



**Figure 5.** Boundary conditions for composite framework: (**A**) marked positions of vertical support of the portal; (**B**) marked positions of horizontal support of the portal; (**C**) forces direction in the center of gravity (COG) of the traverse and lifting beam; (**D**) forces direction in milling head; (**E**) the top view of all boundary conditions.

A finite element model of the original design of the portal (D0) was first created as shown in Figure 4B. For finite element analysis, aluminum alloy beams were included in the finite element model as beam elements glued to the panel elements. The finite element analysis used small deformations linear-elastic model, in which shell elements adopted four node linear elements Kirchhoff plate theory (in-plane), composite material was with nine node integration trough thickness, beam elements adopted two node linear elements with linear elastic material, and loads (Table 5) and boundary conditions (Figure 5) were used for the simulation analysis. However, the FEA results showed that the displacement of the milling head did not meet the requirements. So, we carried out the structural optimization of the portal. Figure 6 and Table 6 presented a comparison of the portal's performance before and after design optimization.



**Figure 6.** Comparison of the portal's structure and FEA deformation cloud map (taking load 1 as an example) before and after design optimization: (**A**) structure of D0; (**B**) total deformation of D0; (**C**) *x*-direction deformation of D0; (**D**) *y*-direction deformation of D0; (**E**) *z*-direction deformation of D0; (**F**) structure of D1; (**G**) total deformation of D1; (**H**) *x*-direction deformation of D1; (**I**) *y*-direction deformation of D1; (**J**) *z*-direction deformation of D1.

Description		Before (D0)	After (D1)
Maximum deformation (mm) (Taking Figure 6 as an example)	Total <i>x</i> -direction <i>y</i> -direction z-direction	$\Delta_{\text{total}} = 0.166$ $\Delta_x = 0.163$ $\Delta_y = 0.015$ $\Delta_z = 0.108$	$\Delta_{\text{total}} = 0.080$ $\Delta_x = 0.076$ $\Delta_y = 0.014$ $\Delta_z = 0.054$
Mass Stiffness material costs		100% 100% 100%	106% 189% 109%

Table 6. Comparison of portal's performance before and after design optimization.

From Table 6, it is observed that compared with the structure of D0 before optimization, although the mass of structure D1 after optimization increased by 6% and the material costs increased by 9%, its stiffness increased by 89%, and the maximum deformation of D1 was much smaller than that of D0. Therefore, the portal structure was optimized as D1.

#### 5.2. Design Optimization for the Framework

In the former analysis and determination of the portal structure, a finite element model including the traverse and lifting beam was created to analyze the structural behavior of the composite structure, as shown in Figure 4C. Isotropic aluminum and orthotropic composite materials were used in the analysis of the plates. We used the material specifications for AMPREG21 laminating sandwich panels provided by Gurit (Wattwil, Switzerland). The final design was examined in a detailed finite element analysis, which included all components of the large-scale moving framework. Table 7 lists the analysis results of the maximum displacements of the milling head in 3 coordinate directions after design optimization of the framework.

Position	Load Cases						
rosition	Load 1	Load 2	Load 3	Load 4			
One of the cloud maps	<b>L</b> max	<b>L</b> inax	Contraction of the second seco	Amax			
$\Delta x_{\rm max} \ ({\rm mm})$	0.03	0.20	0.02	0.04			
$\Delta y_{\rm max}  ({\rm mm})$	0.04	0.03	0.19	0.04			
$\Delta z_{max} (mm)$	0.19	0.18	0.18	0.20			

Table 7. Maximum displacements of the milling head after design optimization of the framework.

From Table 7, it is observed that the displacements of the milling head were less than the design requirement of 0.25 mm in all load cases. Meanwhile, the stress inside the laminate was much lower than the allowable material limits. This indicated that the 3-step design optimization approach proposed in this study for the optimal design of a large-scale moving framework structure was feasible and successful.

## 6. Prototype Verification

To evaluate the performances of the large-scale moving framework, a 40 m  $\times$  6 m  $\times$  4 m L5AMC prototype was manufactured. Then, design precision inspections, error compensation, and machining precision tests were carried out to verify the structural integrity of the framework. The actual tests scenes are shown in Figure 7.



**Figure 7.** Actual test scenes: (**A**) inspection of a translational axis using a laser interferometer; (**B**) inspection of a rotational axis using a laser tracker; (**C**) milling head inspection; (**D**) dynamic drive performance inspection; (**E**) processing test; (**F**) a processed sample.

Detailed position geometric error modeling, identification, and compensation for the L5AMC prototype have been reported [1]. Table 8 presents some inspection results of the L5AMC prototype related to the framework.

According to the inspection results in Table 8, the large-scale moving framework exhibits a great comprehensive accuracy. Using sandwich structures of composite materials to replace metal materials makes the mass of the framework lightweight. The total mass of the framework with composite materials was 64.57% compared with metal materials. Zulaika et al. [35] reported 13% less energy due

to mass reduction above 20% in mobile structural components. Therefore, the actual verification results indicated that the large-scale moving framework based on the proposed 3-step design optimization approach fully met the design requirements of the L5AMC and reduced energy consumption.

	Test Content	Design Request	Measured Value		
	<i>x</i> axis (m)	40	40.02		
Stroke	<i>y</i> axis (m)	6	6.01		
	z axis (m)	4	4.01		
	Translational axes	Testing equipmen	t: laser interferometer		
	Taking the <i>y</i> axis as an example, maximum	0.25 /0.04	Forward: 0.041/0.021		
Positioning accuracy and	positioning error and repeatability (mm)/full stroke	0.25/0.04	Reverse: 0.148/0.028		
repeatability	Rotational axes	Testing equipment: laser tracker			
	Taking the <i>B</i> axis as an example, maximum	1/0/	$0-110^{\circ}: 0.079/0.034$		
	positioning error and repeatability (°)/full stroke	1/0.4	-110°-0°: 0.056/0.023		
Comple machining	Roughness $R_a$ (µm)	3.2	No abnormality, <3.2		
Sample machining	Contour accuracy (mm)	$\pm 0.05$	No abnormality, $<\pm 0.05$		
Total mass of the framework (kg): 2199.81 (proposed in this study)					
	3406.92 (Est	imation by metal materi	al)		

Table 8.	Inspection	results of t	he L5AMC	prototype r	elated to the	e framework
Indic 0.	inspection	icourto or t		prototypen	ciated to the	, munice work

## 7. Conclusions

The present study proposed a design optimization large-scale moving framework approach for an L5AMC to solve the contradiction between the moving mass, material costs, and structural stiffness. Based on the conducted analyses, the following conclusions can be drawn.

- 1. To design an optimized large-scale moving framework for the L5AMC, an improved approach, named the 3-step design optimization, was introduced to obtain the optimum framework structures based on multi-objective optimization and finite element analysis.
- 2. The structural stiffness of the framework after optimization increased by 89% compared with before optimization, although the mass increased by 6% and the material costs increased by 9%. The finite element simulation results showed that the displacements of the milling head were below 0.21 mm in all load cases, which were less than the design requirement of 0.25 mm.
- 3. The actual verification results indicated that the large-scale moving framework based on the proposed 3-step design optimization approach fully met the design requirements of the L5AMC and reduced energy consumption.
- 4. The proposed 3-step design optimization approach based on multi-objective optimization and finite element analysis can be considered as a guide for optimizing large-scale moving structures to balance the moving mass, material costs, and structural stiffness.

**Author Contributions:** G.Z. analyzed the data and drafted the present report. P.L. contributed the analysis ideas. X.M. checked the test data. Y.W. carried out the finite element analysis. F.X. conducted the prototype test. And S.Y. proposed the analytical method.

Funding: This research received no external funding.

Acknowledgments: This work was supported by the State Key Laboratory for Manufacturing Systems Engineering at Xi'an Jiaotong University of China (grant number: sklms2017008), the National Torch Plan of China (grant number: 2012GH040610), and the Jiangsu Kunshan Cultivation Project of Scientific and Technological Achievements of China (grant number: KH1003).

**Conflicts of Interest:** The authors declare no conflict of interest. The founding sponsors had no role in the design of the study; in the collection, analyses or interpretation of data; in the writing of the manuscript; nor in the decision to publish the results.

#### Appendix A

Table A1. Major material parameters used for the framework.

	Sandwich Panel		Aluminum Alloy	Aluminum Alloy	
Parameters –	CF	CF Foam		Beams	
Layer mass per unit area, $\rho_1$ (kg/m <sup>2</sup> )	0.833	1.44			
Density, $\rho_2$ (kg/m <sup>3</sup> )			2700	3386	
Young's modulus, $E_0^{\circ}$ (GPa)	134.50				
Young's modulus, $E_{90}^{\circ}$ (GPa)	49.90				
Young's modulus, E(GPa)		0.130	75	92.75	
Shear modulus, G_0_90 (GPa)	30.90				
Shear modulus, G_90_90 (GPa)	19.20				
Poisson's ratio, v	0.28		0.30	0.30	

#### Appendix B



Figure A1. Schematic diagram of "curtain effect" (modified and redrawn from Reference [36]).

Explanation: when the object AB (e.g., curtain or cable) is large, its center point drops from O to O' due to the action of the self-weight G and generates a deflection. This is called the "curtain effect".

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