



Article

# 3-D Printed Fabry–Pérot Resonator Antenna with Paraboloid-Shape Superstrate for Wide Gain Bandwidth

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**Abstract:** A three-dimensional (3-D) printed Fabry–Pérot resonator antenna (FPRA), which designed with a paraboloid-shape superstrate for wide gain bandwidth is proposed. In comparison with the commonly-adopted planar superstrate, the paraboloid-shape superstrate is able to provide multiple resonant heights and thus satisfy the resonant condition of the FPRA in a wide frequency band. A FPRA working at 6 GHz is designed, fabricated, and tested. Considering the fabrication difficulty caused by its complex structure, the prototype antenna was fabricated by using the 3-D printing technology, i.e., all components of the prototype antenna were printed with photopolymer resin and then treated by the surface metallization process. Measurement results agree well with the simulation results, and show the 3-D printed FPRA has a  $|S_{11}| < -10$  dB impedance bandwidth of 12.4%, and a gain of 16.8 dBi at its working frequency of 6 GHz. Moreover, in comparison with the planar superstrate adopted in traditional FPRAs, the paraboloid-shape superstrate of the proposed FPRA significantly improves the 3-dB gain bandwidth from 6% to 22.2%.

Keywords: wideband; gain bandwidth; Fabry-Pérot resonator antenna; 3-D printing

# 1. Introduction

High gain antennas are desirable in many applications, such as radar, wireless communication and microwave power transmission. As a kind of widely used high gain antennas, the Fabry–Pérot resonant antenna (FPRA) is formed by placing a superstrate with partial reflection property in front of an excitation antenna with a ground plane [1–5]. Various antennas have been selected as the excitation antenna for the FPRA, such as the open waveguide antenna, the microstrip antenna, and the microstrip array antenna [1,4,6]. The superstrate could be a homogeneous dielectric substrate [3,7], or metamaterial inspired one, that is usually a printed circuit board (PCB) etched periodic microstrip unit cells [2,4,8,9]. In comparison with other high gain antennas such as parabolic antennas and microstrip array antennas, the FPRA possesses advantages of high gain, low profile, and high radiation efficiency.

The FPRA achieves a high gain owing to the multiple reflections between its superstrate and ground plane. By properly determining the distance between the superstrate and ground plane, the multiple reflections are able to create an in-phase electromagnetic (EM) field on its aperture, i.e., over its superstrate. However, the multiple reflections may cause a strong resonant property and thus lead to the FPRAs' performances—such as the gain—being sensitive to the resonant height, i.e., the distance between the superstrate and the ground plane. So far, most FPRAs adopt a planar superstrate that means a fixed resonant height, and thus lead to a narrow gain bandwidth. For example, the 3-dB gain bandwidths of the FPRAs in [3,5,10] are 2, 1, and 0.8% respectively. As was pointed out in [11], the 3-dB gain bandwidth for a FPRA is usually less than 3%. The narrow gain bandwidth seriously limits the practical applications of the FPRAs.

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Many technologies have been proposed to enhance the FPRAs' gain bandwidth [6–8,12–18] and most of them can be divided into three categories. The first is adopting non-uniform superstrate or non-uniform ground plane, such as superstrate with tapered-sized FSS (frequency selective surface) or ground plane with tapered-sized HIS (high impedance surface) [7,12,13]. The second is designing superstrates with positive phase gradient, i.e., the superstrates' reflection phase increasing with frequency [8,14–17]. The third is employing an antenna array instead of a single antenna as the excitation antenna to feed a FPRA [6,18].

Quite differently from the aforementioned technologies, this work explores enhancing the FPRAs' gain bandwidth by designing a paraboloid-shape superstrate. Unlike planar superstrates used in most FPRAs, the cambered superstrate adopted by the proposed FPRA is able to create various resonant heights which satisfy the resonant conditions of the FPRA at a wide range of frequencies. To the best of our knowledge, this technology has never been investigated in previous studies.

To validate the proposed technology, a sample FPRA working at 6 GHz will be presented. Considering its complex structure, especially the paraboloid-shape superstrate, the prototype antenna will be fabricated by using the three-dimensional (3-D) printing technology. The 3-D printing technology also identified as additive manufacturing or rapid prototyping has been gradually used for fabricating microwave and millimeter components—such as antennas, filters, waveguides, 3-D metamaterials, etc. [19–22]—as it has the advantage of fabricating complex structures at a low cost. The 3-D printing technology enables designers have more freedom in their designs. The research work in [23] demonstrates the 3-D printed and surface metallized microwave components have nearly identical performances with solid metal structures if their skin depths of metal operate identically. Nowadays, by adopting some technologies such as using a beam of laser to solidify liquid photopolymer resin layer, a 3-D printing operation can achieve a very high printing precision of  $\pm 50~\mu m$ , while also guaranteeing good surface quality [24].

# 2. Resonant Condition for FPRA

As illustrated in Figure 1, a typical FPRA includes an excitation antenna, a superstrate and a ground. The EM energy emerges from the excitation antenna and undergoes multiple reflections between the superstrate and the ground. By using of the ray tracing model [1,16], assuming the EM ray is with an incident angle of  $\theta$ , and denoting the ith transmitted ray to be Rayi ( $i = 0, 1, 2 \dots$ ), the phase difference  $\varphi$  between two adjacent rays can be expressed as

$$\varphi = \varphi_s - \frac{k \cdot 2H}{\cos(\theta)} + \varphi_G - (-k \cdot 2H \cdot \tan(\theta)\sin(\theta))$$
 (1)

where  $k = 2\pi f/c$  is the wave number, f is the working frequency, c is the light velocity,  $\phi_S$  and  $\phi_G$  are the phases of reflection coefficients for the superstrate and the ground respectively, and H is the resonant height.

In order to obtain high gain at  $\theta$  direction, all transmitted rays should be in phase, and hence the phase difference  $\varphi$  between two adjacent rays should be  $2n\pi$  (n=0,1,2...). For most practical applications, the FPRAs are required to have maximum gain at the broadside direction ( $\theta=0$ ), and hence the resonant height H should satisfy the resonant condition as

$$H = \frac{c}{4\pi f}(\varphi_s + \varphi_G + 2n\pi), \ n = 0, 1, 2 \dots,$$
 (2)

where n is usually chosen as 0 to realize a low profile for the FPRA.

For a perfect electric conducting (PEC) ground plane, its reflection phase  $\varphi_G$  is a constant of  $\pi$ . The reflection phase of a superstrate  $5\varphi_S$  normally varies with the frequency. Hence for a FPRA with a fixed resonant height H, the resonant condition illustrated by Equation (2) is satisfied only within a narrow frequency band. This is why most FPRAs have a narrow gain bandwidth. Moreover, it can be

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expected that the FPRA is able to achieve a wide gain bandwidth if the FPRA's configuration provides multiple resonant heights.

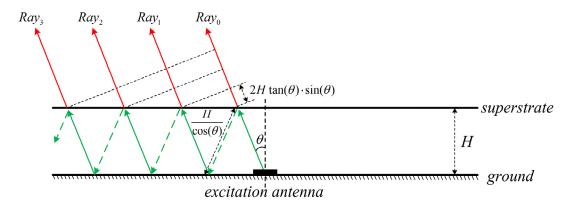


Figure 1. Schematic view of the ray tracing model for Fabry–Pérot resonator antenna.

### 3. Design of the Proposed FPRA with Wide Gain Bandwidth

### 3.1. Configuration of the Proposed FPRA

As shown in Figure 2, the proposed FPRA is mainly composed of a metallic grating superstrate with a paraboloidal shape, a ground plane, and an open-ended feeding circular waveguide acting as its excitation antenna. The FPRA is fed from a WR-159 standard rectangular waveguide, and a transition is connected between the circular and the rectangular waveguides. The circular superstrate diameter and thickness are L=200 mm and thickness t=2 mm. The width of the metallic strip and the spacing distance between two adjacent metallic strips are W=5 mm and P=20 mm, respectively. The heights of the cavity and the paraboloid-shape superstrate are  $H_c$  and  $H_p$ , respectively. The radius and insertion length of the feeding circular waveguide are  $R_f=14.5$  mm and  $H_f=5$  mm, respectively. The working frequency of the proposed FPRA is 6 GHz, and thus its diameter L of 200 mm corresponds to an electrical dimension of  $4\lambda$ , where  $\lambda$  is the wavelength at 6 GHz in the free space.

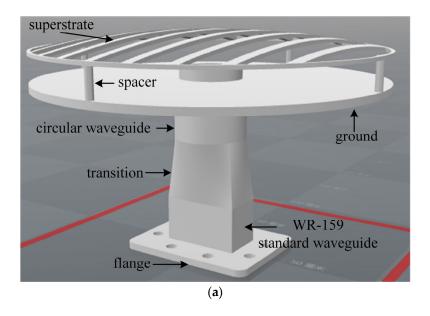
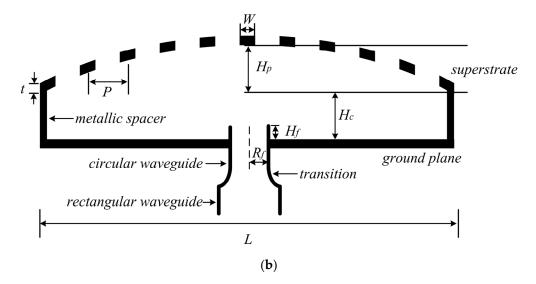


Figure 2. Cont.

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**Figure 2.** Configuration of the proposed FPRA. (a) 3-D view; (b) cross-section view with main structural parameters.

## 3.2. FPRA with a Traditionial Planar Superstrate

To provide a performance comparison, and moreover some necessary design data for the proposed FPRA, a FPRA with a traditional planar superstrate is designed first. This FPRA is also with a metallic grating superstrate. Except for the planar configuration of its superstrate, this antenna has the same structure (see Figure 3) and nearly the same parameters as that of the proposed FPRA with a paraboloid-shape superstrate.

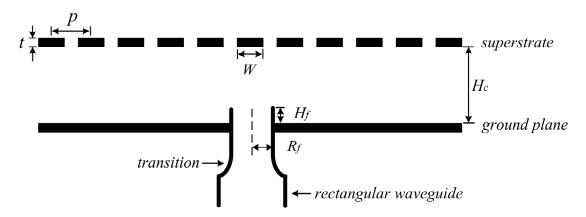


Figure 3. Cross-section of the FPRA with a planar superstrate.

The unit cell of the planar metallic grating superstrate is illustrated in Figure 4a, by applying four periodic boundaries to surround the unit cell and two ports located above and below the unit cell, the reflection phase of the superstrate is calculated. Figure 4b shows the simulated reflection coefficient of the superstrate. As can be seen from Figure 4b, the reflection coefficient phase varies with frequency and its value is  $145^{\circ}$  at the working frequency 6 GHz. Then according to Equation (2), the resonant height  $H_c$  for the FPRA with a traditional planar superstrate is initially chosen to be 22.5 mm. To finely determine  $H_c$ , a popular commercial software CST (computer simulation technology) microwave studio (MWS) based on the finite integration technique (FIT) is employed, and the gain against  $H_c$  is simulated, as shown in Figure 5. Obviously, the optimal value of  $H_c$  is 23 mm, which corresponds to

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a peak gain of 17 dBi at the working frequency of 6 GHz. The 3-dB gain bandwidth for this PPRA is narrow as can be seen in Figure 5, only about 6% (from 5.81 GHz to 6.17 GHz).

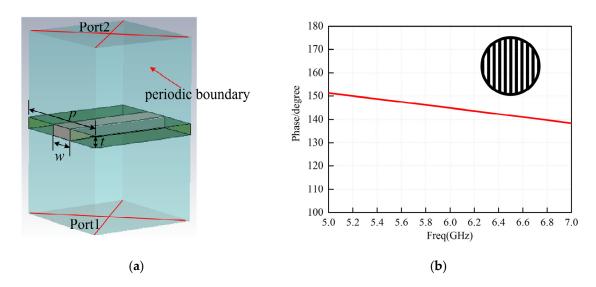
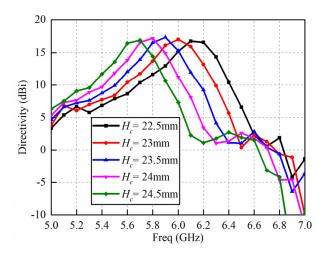


Figure 4. (a) Simulation model of the unit cell; (b) reflection phase of the planar superstrate.



**Figure 5.** Gain-frequency response against  $H_c$  for the FRPA with a traditional planar superstrate.

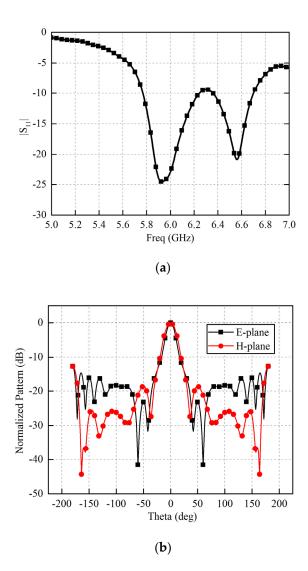
Figure 6 illustrates the simulated  $|S_{11}|$  and radiation pattern at 6 GHz. It can be seen from Figure 6a,b, the  $|S_{11}| < -10$  dB impedance bandwidth is 7.8% (from 5.77 GHz to 6.24 GHz) and a good radiation pattern is obtained at its working frequency of 6 GHz.

# 3.3. Proposed FPRA with a Paraboloid-Shpae Superstrate

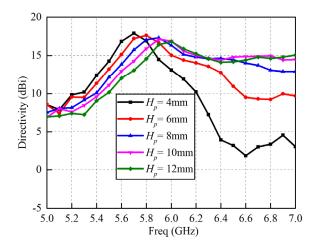
To broaden the gain bandwidth of the FPRA, a paraboloid-shape superstrate is designed to replace the traditional planar superstrate. Compared to a planar one, a cambered superstrate provides multiple resonant heights, and thereby satisfies the resonant condition in a wide frequency band.

Figure 7 gives the simulated gain–frequency response against  $H_p$  for the proposed FPRA. One can observe that the higher  $H_p$  (from 4 mm to 12 mm), the wider gain bandwidth can be achieved, but the peak gain will drop slightly. When  $H_p$  is up to 10 mm, the increase of  $H_p$  will not bring the improvement of bandwidth any more. For the purpose of wideband and high-gain performance,  $H_p$  is set as 10 mm.

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**Figure 6.** Simulated performances of the FPRA with a traditional planar superstrate. (a)  $|S_{11}|$ ; (b) radiation pattern at 6 GHz.



**Figure 7.** Gain-frequency response against  $H_p$  for proposed FPRA.

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#### 4. Fabrication, Measurements, and Discussion

To validate the proposed FPRA, a prototype antenna will be fabricated and tested. The complex structure, especially the paraboloid-shape superstrate, may make the fabrication very difficult. Hence 3-D printing technology is employed to fabricate the proposed antenna (see Figure 8). In this work, all components of the proposed antenna are printed using a laser to solidify liquid photopolymer resin which is then treated by the surface metallization including the following step: (1) the printing material of resin is treated by a sequence of chemicals to activate the material's surface; (2) 0.5  $\mu$ m of Ni is electrolessly plated on the surface, the Ni serves as a seed layer for the later process; (3) 1–2  $\mu$ m copper is electrolessly plated above the surface of Ni; (4) 6  $\mu$ m of copper is electroplated to increase the thickness of the copper and guarantee the layer is much larger than the skin depth (the value is 0.84  $\mu$ m for copper at 6 GHz); (5) finally, 0.15  $\mu$ m of silver is plated on the surface of the copper to prevent oxidation.



**Figure 8.** Photograph of the proposed 3-D printed antenna. A waveguide to coaxial connector is used to feed the antenna.

For the 3-D printed antenna, its input reflection coefficient was measured with an Agilent network analyzer N5230A. The simulated and measured  $|S_{11}|$  are plotted and compared in Figure 9. The measured results are in good agreement with simulated ones, and indicate a  $|S_{11}| < -10$  dB impedance bandwidth of about 12.4% (from 5.8 GHz to 6.53 GHz).

The radiation pattern of the 3-D printed antenna is measured in an anechoic chamber. Figure 10 plots the co-polarization and cross-polarization in E-plane and H-plane at 5.8, 6, 6.2, and 6.5 GHz respectively. It can be observed that the proposed FPRA performs good directive radiation patterns at all of those frequency points. The measured cross polarizations are also presented, which are less than -25 dB at the broadside. The polarization of the FPRA is consistent with that of the feeding antenna, which can be easily changed by employing a feeding antenna with a different polarization. With the increase of frequency, the side-lobe levels are also increased, this phenomenon has been observed with many wideband Fabry–Pérot resonator antennas [25].

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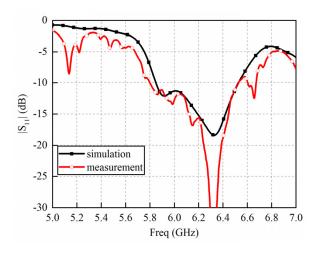


Figure 9. Simulated and measured reflection coefficients for the proposed FPRA.

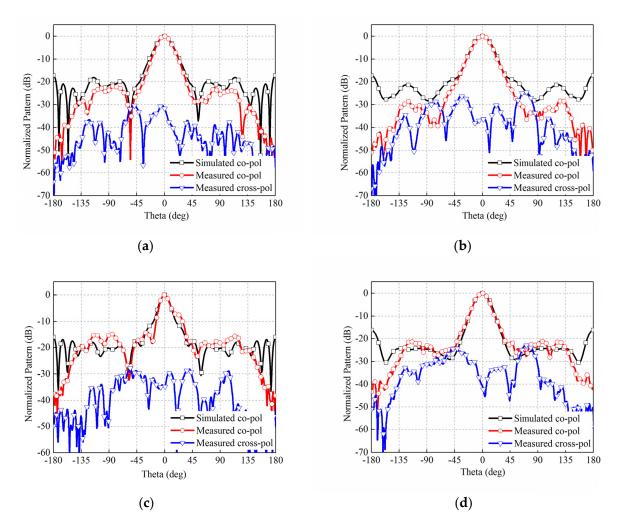
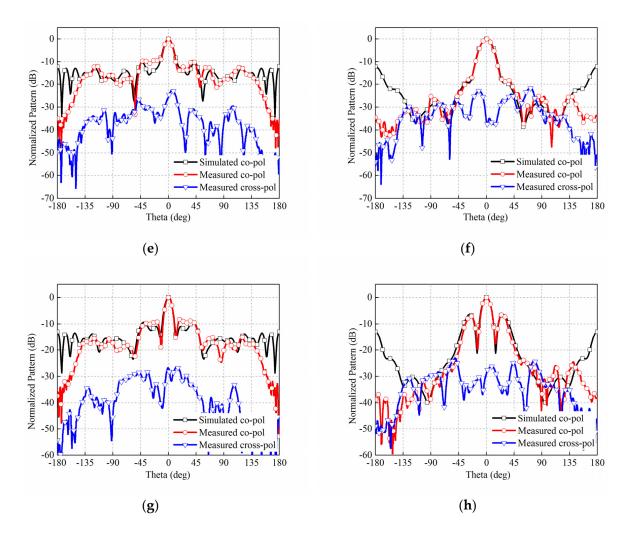


Figure 10. Cont.

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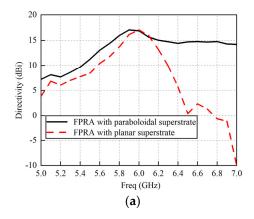


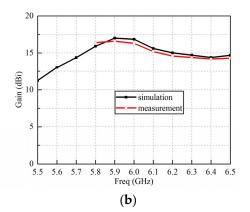
**Figure 10.** Normalized radiation patterns of the proposed FPRA: (a) E-plane at 5.8 GHz; (b) H-plane at 5.8 GHz; (c) E-plane at 6 GHz; (d) H-plane at 6 GHz; (e) E-plane at 6.2 GHz; (f) H-plane at 6.2 GHz; (g) E-plane at 6.5 GHz; and (h) H-plane at 6.5 GHz.

The simulated gains against the frequency for the proposed FPRA with a paraboloid-shape superstrate and the FPRA with a traditional planar superstrates are presented and compared in Figure 11a. The 3-dB gain bandwidths for those two FPRAs are 22.2% (from 5.67 to 7 GHz) and 6% (from 5.81 to 6.17 GHz), respectively. It is obvious that the paraboloidal superstrate significantly improves the gain bandwidth in comparison with a traditional planar one. Figure 11b compares the simulated and measured gain–frequency response for the proposed FPRA, one can observe they are in good agreement.

Table 1 lists 3-dB gain bandwidths of a few FPRAs designed in previous literatures, and are compared to that in this work. One can observe that the FPRA proposed in this work achieves a larger 3-dB gain bandwidth than those FPRAs in previous studies.

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**Figure 11.** (a) Gain bandwidth comparison between FPRA with planar superstrate and paraboloidal superstrate; (b) simulated and measured gain–frequency response for the proposed FPRA.

**Table 1.** Comparison of the 3-dB gain bandwidth between a few FPRAs in literatures and the FPRA proposed in this work.

Reference	Electrical Area ( $\lambda_0^2$ )	3-dB Bandwidth (%)
[8]	17.9	12.6%
[12]	10.7	8.5%
[16]	16	10.6%
[17]	16	15.1%
This work	12.56	22.2%

### 5. Conclusions

For the FPRA, the wide bandwidth is an attractive property in many applications. A novel technology of designing a paraboloid-shape superstrate to enhance the gain bandwidth of the FPRA is proposed. Compared to a traditional planar superstrate, this cambered superstrate is able to produce multiple resonant heights, and thereby satisfy the resonant condition in a much wider frequency range. In this work, a sample FPRA working at 6 GHz is designed and tested, and the 3-D printing technology is employed for fabricating the prototype antenna. For this 3-D printed antenna, its measured results agree well with the simulated ones, which demonstrate the high fabrication precision of the 3-D printing technology. Moreover, in comparison with the traditional planar superstrate, the proposed paraboloid-shape superstrate significantly improves the FPRA's 3-dB gain bandwidth from 6% to 22.2%.

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**Author Contributions:** Q.C. proposed the idea and designed the antenna in the study and K.X. performed the experiment measurements and data processing. Q.C. and X.C. wrote and revised the paper. All authors read and approved the manuscript for publication.

Conflicts of Interest: The authors declare no conflict of interest.

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