

Article

Stability and Maximum Power Point Operation of Induction-Generator Wind Turbines with Stator-Side Frequency Control

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Abstract

Maintaining stable operation and maximum power extraction in wind turbines under significant wind speed variations remains a key challenge in wind energy systems. This study aims to analyze the stability and maximum power point operation of a wind turbine equipped with a squirrel-cage induction generator using stator-side frequency control. This study examines the operational performance of medium-power wind turbines in the kilowatt range under significant wind speed variability. The analysis focuses on a turbine equipped with a squirrel-cage induction generator and a control architecture that incorporates a power converter integrated into the stator circuit. The findings show that adjusting the stator frequency through the converter allows the generator to track the optimal rotational speed, ensuring operation at the maximum power point across a wide range of wind conditions. Based on these results, the study defines the stable operating region of the turbine under time-varying wind speeds, making it suitable for distributed energy projects in coastal regions where wind can be highly variable. It also shows that, for a given electrical load, the generator must be calibrated to an appropriate maximum stator frequency to maintain stable and efficient energy conversion.

Keywords: wind system; wind turbine; system stability; *PID* controller; significant wind speed variations; induction generators; power converter

1. Introduction

Electricity generation from renewable energy sources has become a significant component of the energy mix in Romania and Europe. In 2024, 46.9% of electricity in the European Union (EU) was produced from renewable sources [1]. The share of renewables in Romania's electricity production in 2024 exceeded the EU average, reaching 50%. Among the categories of renewable energy sources at the EU level, wind energy holds the largest share at 39.1%, followed by hydroelectric power (29.9%) and solar power (22.4%) [1].

There are various solutions for utilizing wind energy: either through independent wind farms or by integrating them with other renewable energy sources. For instance, ref. [2] proposes the use of a wind turbine (WT) alongside a pumped-storage hydroelectric power plant. Simulations have shown that such a power plant effectively maintains the proper functioning of the energy system, even with fluctuations in wind speed and changes in load values [3]. In other scenarios, particularly in isolated and developing rural areas, the implementation of a wind energy system with hydroelectric energy storage via pumping



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from an open well is suggested [4]. Additionally, ref. [5] proposes a hybrid power facility that integrates thermal energy, wind power, photovoltaic (PV), and hydroelectric energy production, all facilitating stable operation of the energy system. In the case of wind systems, the choice of a specific type of wind turbine is made based on the characteristics of the area [6,7].

The efficient utilization of wind turbines (WTs) depends strongly on their deployment in locations with appropriate wind resources. Each wind farm exhibits distinct operational characteristics influenced by factors such as air density, local weather conditions, and blade deformation effects [8]. Accurately characterizing the aerodynamic behavior of wind turbines, which is often nonlinear and highly sensitive to environmental variations, is essential, as demonstrated in previous studies [9,10], which highlight the complexity of aerodynamic power conversion under variable operating conditions. Achieving maximum energy capture under varying operating conditions requires establishing a periodic relationship between the optimal mechanical angular speed and the corresponding wind velocity. This relationship is typically derived from mathematical models calibrated using experimental field data.

Wind speed is commonly monitored using small auxiliary wind turbines or sensors mounted on the nacelle [11,12]. However, nacelle-mounted sensors may not accurately reflect the wind speed acting directly on the rotor blades. In such cases, wind speed can be inferred by estimating torque and rotor speed and applying the inverse aerodynamic model of the turbine [13]. To ensure maximum electrical energy production, the turbine must operate at the maximum power point (MPP) across a wide range of wind speeds, independent of system configuration, as demonstrated in [14–16]. These works focus on maximum power point tracking (MPPT) strategies aimed at improving energy extraction under variable wind conditions. This requirement underscores the importance of analyzing turbine power curves under different wind conditions and determining the corresponding optimal power curve, as investigated in [17,18].

In addition, wind turbine operation has been extensively studied using various control strategies and monitoring techniques [19,20], which address system performance, dynamic behavior, and efficiency under fluctuating operating conditions. For instance, extended optimal torque control has demonstrated improvements of 2–7% in wind speed estimation accuracy and a 0.35% increase in energy efficiency [21]. PID-based controllers enable effective regulation of output power under fluctuating wind and load conditions, contributing to voltage stability [22]. For permanent-magnet synchronous generators, dual-loop control—combining torque and pitch regulation—has been recommended to enhance output power and overall energy yield [23]. Recent investigations have also examined the influence of power oscillation controllers on turbine structural dynamics, showing that their impact is comparable to wind-induced loads and significantly lower than that of transient three-phase short-circuit faults [24]. To mitigate mechanical vibrations, active load control strategies employing pitch regulation have been proposed while maintaining conventional aerodynamic power control [25].

As the penetration of variable renewable generators increases, the need for complementary resources capable of providing frequency regulation becomes more pronounced [26,27]. In isolated networks powered exclusively by renewable energy sources, system stability and frequency control pose significant challenges. Hybrid renewable energy systems—such as combinations of hydropower, pumped storage, and wind generation—have been proposed to address these concerns [28].

Recent studies have investigated advanced MPPT strategies based on adaptive and intelligent control methods, including machine learning and data-driven approaches [29,30]. In addition, recent works (2023–2025) have focused on improving the performance of

induction generator-based wind systems through enhanced control strategies and optimization techniques [31–33]. Conventional *MPPT* strategies are typically based on torque control or predefined power curves, while more recent approaches incorporate adaptive, model-based, or intelligent control techniques to improve performance under variable wind conditions. More recently, intelligent control approaches, such as fuzzy logic, neural networks, and hybrid models, have been proposed to enhance the efficiency and robustness of wind energy conversion systems.

This study investigates the performance of a wind turbine equipped with a squirrel-cage induction generator, focusing on its dynamic behavior under varying wind speeds. Particular attention is given to maintaining system stability in the presence of large wind speed fluctuations.

The main objective of this paper is to analyze the stability and maximum power point operation of a wind energy system equipped with a squirrel-cage induction generator using stator-side frequency control under significant wind speed variations.

The methodology is based on analytical modeling of turbine and generator power characteristics, stability analysis using both graphical and mathematical approaches, and the implementation of a *PI*-based control strategy to regulate stator frequency and ensure optimal operation.

While stability-oriented *MPPT* approaches have been investigated in the literature, this paper provides additional insight into the stability of wind energy systems equipped with squirrel-cage induction generators operated under stator-side frequency control. Unlike conventional *MPPT* approaches based on torque control or rotor-side converters, the proposed method investigates the stability of the operating point under varying wind conditions and identifies the conditions under which stable maximum power point operation can be ensured. In addition, the study provides a combined analytical framework that links turbine aerodynamics, generator electrical characteristics, and frequency-based control, enabling a structured evaluation of stable and unstable operating regions.

Compared to previous studies by the authors, which focused primarily on the determination of optimal operating regions and power characteristics, the present work explicitly investigates the stability of the operating point under stator-side frequency control. In particular, it demonstrates that multiple steady-state solutions may exist for a given wind speed, while only one ensures stable operation under perturbations.

The proposed approach is developed within a simplified analytical framework, which allows a clear physical interpretation of the relationship between turbine aerodynamics, generator characteristics, and stator frequency control. The purpose of this simplification is to enable a structured analysis of system stability rather than to reproduce all practical nonlinear effects.

Compared to conventional *MPPT* approaches and commercial implementations, which focus primarily on energy maximization, the present study explicitly investigates the stability of the operating point and highlights the existence of multiple feasible operating frequencies with different stability properties. The paper is structured as follows. Section 2 presents the determination of turbine and generator characteristics, Section 3 describes system operation in the optimal region, Section 4 analyzes stability, and Section 5 presents control and simulation results, followed by conclusions.

Following the research carried out, the use of a *PI* type regulator, interconnected between the electrical network and the stator of the induction generator with the rotor in short circuit, allows the wind system to operate stably at the maximum power point at a wind speed variation in the range: 3–10 m/s.

2. Determining the Power Characteristics of the Turbine and Generator

The analyzed system is based on a 55 kW wind turbine, which is representative of medium-power and distributed wind energy applications, including small-scale installations and isolated or rural energy systems. While modern wind farms operate at higher power levels, such systems remain relevant for decentralized energy production.

The technical data used in this study are derived from a real wind turbine and are employed as a reference case for analytical modeling and stability analysis. The data refers to a 55 kW wind turbine described in the literature [33], used as a reference case for analysis, without being limited to a specific manufacturer model. These data form the basis for the turbine power characteristics presented in Figure 1.

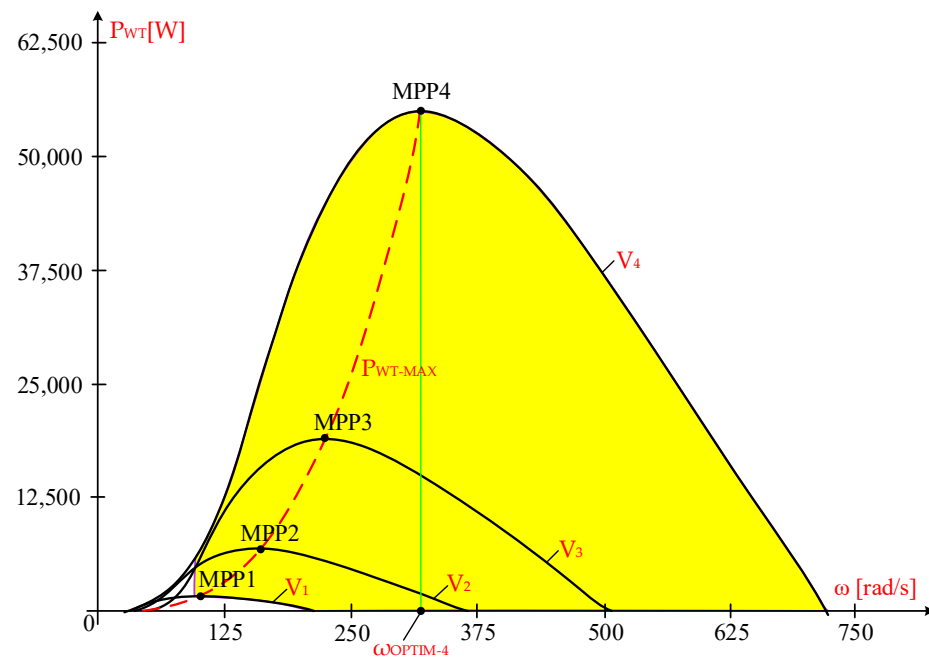


Figure 1. Wind turbine power characteristics as a function of mechanical angular speed (ω) for four wind speeds ($V_1 = 3$ m/s, $V_2 = 5$ m/s, $V_3 = 7$ m/s, and $V_4 = 10$ m/s). The curves represent the variation in turbine power P_{WT} with respect to ω at different wind speeds.

Methodology

The methodology adopted in this study is based on analytical modeling of the wind turbine and induction generator characteristics, using technical data from a 55 kW system. The turbine power curves are determined as functions of wind speed and mechanical angular speed.

The analysis is based on several simplifying assumptions, including constant air density, steady-state aerodynamic conditions, and negligible losses in the power conversion process. These assumptions are adopted to isolate the fundamental mechanisms governing system behavior and to enable a clear analytical interpretation of the stability of the operating point. While more detailed models could include additional nonlinear effects and losses, the present formulation focuses on capturing the essential relationships required for stability analysis.

These assumptions allow a tractable analytical description of the system behavior while preserving the main physical relationships.

System stability is evaluated using both graphical analysis of power characteristics and dynamic analysis based on motion equations. In addition, a *PI*-based control strategy is implemented to regulate the stator frequency, enabling the system to track the optimal operating point under variable wind conditions.

Although the analysis is performed for a specific power rating, the methodology can be extended to higher power systems.

To determine the power characteristics of the turbine and generator, the technical data of a wind system with a capacity of 55 kW were analyzed [34]. Within the wind speed range of 3 m/s to 10 m/s, the wind turbine operates at maximum power points (*MPP*), as shown in Figure 1.

In this range, the wind speed varies in proportion:

$$\frac{V_{MINIM}}{V_{MAX}} = \frac{3}{10} \quad (1)$$

Consequently, the generator speed must be adjusted within a ratio of 1 to 3.3.

To achieve the highest energy performance in this range of rotational speeds, adjustments are made to the voltage and frequency at the generator using power converters in the following configurations [35,36]:

- Connection to the stator, in the case of induction generators with a short-circuited rotor.
- Connection to the rotor, in the case of induction generators with a wound rotor.

Induction generators with a wound rotor can use two converters: one for the stator winding and another for the rotor winding [37]. Connection to the stator, in the case of induction generators with a short-circuited rotor. This configuration allows direct control of the stator frequency and voltage, enabling effective regulation of the generator speed and simplified control architecture. However, it requires a power converter rated for the full generator power.

From a practical and control perspective, the choice between stator-side and rotor-side converter configurations involves distinct trade-offs. Rotor-side converter solutions (e.g., in wound-rotor induction generators) enable reduced converter ratings and improved efficiency, but require more complex machine construction, including slip rings and associated maintenance. In contrast, stator-side converter configurations, as considered in this study, provide direct control of stator voltage and frequency, resulting in a simpler control structure and a clearer relationship between electrical control variables and the operating point of the system, at the expense of requiring a full-rated converter.

In the analyzed case, due to the significant variation in wind speed (3–10 m/s), the generator rotational speed must be adjusted over a wide range, which necessitates the use of a power electronic converter, either on the stator or rotor side, in order to maintain operation near the maximum power point. The stator-side configuration is adopted in this work because it enables a more direct and physically interpretable analysis of the relationship between stator frequency, operating point selection, and system stability, which is the main focus of the study.

In ref. [34], the analysis provided a detailed examination of induction generators with a wound rotor, using a power converter in the rotor circuit to achieve turbine operation at the maximum power point. Under this condition, the voltage at the slip rings exceeds twice the nominal stator voltage when the wind speed reaches 10 m/s. Consequently, the rotor, which has a special design, is more expensive than the conventional variant.

The power of the turbine at wind speed V depends on the mechanical angular speed ω and the blade pitch angle β of the turbine blades. At wind speeds above 10 m/s, the blade pitch angle is adjusted to maintain the structural integrity of the wind system. The shaft power generated by a three-blade wind turbine is calculated using the following relationship:

$$P_{WT}(\omega, V, \beta) = \rho \cdot \pi \cdot R_p^2 \cdot C_p(\lambda, \beta) \cdot V^3 \quad (2)$$

where ρ represents the air density at the operational site of the wind turbine (WT), R_p denotes the radius of the turbine rotor, and $C_p(\lambda, \beta)$ is the power conversion coefficient (where $\lambda = \omega \cdot R_p / V$). The power conversion coefficient $C_p(\lambda, \beta)$ for a wind turbine with three blades and a blade pitch angle β is determined using the following relationship:

$$C_p(\lambda, \beta) = c_1 \left(\frac{c_2}{\lambda} - c_3 \right) e^{-\frac{c_4}{\lambda}} \quad (3)$$

where c_1, c_2, c_3 , and c_4 are constructive constants provided in the turbine catalogue and d is a factor that accounts for the rotational effects of the turbine blades:

$$\frac{1}{\lambda} = \frac{1}{\lambda} \exp(-d \cdot \beta) - 0.035 = \frac{V}{R_p \cdot \omega} \exp(-d \cdot \beta) - 0.035 \quad (4)$$

By substituting λ , the power conversion coefficient is obtained as follows:

$$C_p(\lambda) = c_1 \left[c_2 \left(\frac{V}{R_p \cdot \omega} \exp(-d \cdot \beta) - 0.035 \right) - c_3 \right] \exp^{-c_4 \left(\frac{V}{R_p \cdot \omega} - 0.035 \right)} = a \left(\frac{V}{R_p \cdot \omega} \exp(-d \cdot \beta) - b \right) \exp^{-c \left(\frac{V}{\omega} \right)} \quad (5)$$

By substituting the expression of the power coefficient $C_p(\lambda, \beta)$ given in Equation (5) into the aerodynamic power Equation (2), the wind turbine power is obtained in the form:

$$P_{WT}(\omega, V, \beta) = a \left(\frac{V}{\omega} \exp(-d \cdot \beta) \cdot \cos\left(\frac{\pi}{180} \cdot \beta\right) - c \right) \exp\left[d \left(\frac{V}{\omega} \right)\right] V^3 \quad (6)$$

The values of the parameters a, b, c , and d are derived from experimental data reported in the literature for a 55 kW wind turbine [34,38]. These parameters were identified by fitting analytical expressions to the experimentally obtained turbine power curves, ensuring an accurate representation of the power–speed characteristics used in this study. For the analyzed case, the parameter values are $a = 19,182$, $b = 1.3877 \cdot 10^{-2}$, $c = 57.65$ and $d = 0$.

Equation (7) is obtained from Equation (6) by rearranging the terms and expressing the turbine power as a function of the wind speed V and the mechanical angular speed ω :

$$P_{WT}(\omega, V) = 19,182 \left(\frac{V}{\omega} - 1.3877 \cdot 10^{-2} \right) \cdot \exp^{-57.65 \left(\frac{V}{\omega} \right)} \cdot V^3 \quad (7)$$

This relationship highlights that turbine power is governed by the interplay between wind speed and rotational speed, reflecting the underlying aerodynamic conversion process and explaining why a specific angular speed optimizes energy extraction for each wind condition. In the following, ω denotes the mechanical angular speed of the generator shaft (high-speed shaft), unless explicitly stated otherwise.

The technical data from a 55 kW wind turbine [38], equipped with an induction generator featuring a short-circuited rotor, have been processed. The power characteristics of the turbine at four wind speeds, $V_1 = 3$ m/s, $V_2 = 5$ m/s, $V_3 = 7$ m/s, and $V_4 = 10$ m/s, are as follows:

$$P_{WT-1}(\omega, 3) = 19,182 \left(\frac{3}{\omega} - 1.3877 \cdot 10^{-2} \right) \cdot \exp^{-57.65 \left(\frac{3}{\omega} \right)} \cdot 3^3 \quad (8)$$

$$P_{WT-2}(\omega, 5) = 19,182 \left(\frac{5}{\omega} - 1.3877 \cdot 10^{-2} \right) \cdot \exp^{-57.65 \left(\frac{5}{\omega} \right)} \cdot 5^3 \quad (9)$$

$$P_{WT-3}(\omega, 7) = 19,182 \left(\frac{7}{\omega} - 1.3877 \cdot 10^{-2} \right) \cdot \exp^{-57.65 \left(\frac{7}{\omega} \right)} \cdot 7^3 \quad (10)$$

$$P_{WT-4}(\omega, 10) = 19,182 \left(\frac{10}{\omega} - 1.3877 \cdot 10^{-2} \right) \cdot \exp^{-57.65 \left(\frac{10}{\omega} \right)} \cdot 10^3 \quad (11)$$

The key characteristic of the maximum power generated by the P_{WT-MAX} turbine, obtained through analytical fitting of experimental data, is expressed as:

$$P_{WT-MAX}(\omega) = 1.6744 \cdot 10^{-3} \cdot \omega^3 \quad (12)$$

is presented in Figure 1. The EG power depends on the stator voltage, U (for the nominal voltage $U_N = 230$ V and frequency $f = 50$ Hz), as well as the mechanical angular speed ω , exhibiting a power characteristic of the form [34]:

$$P_{EG}(\omega) = - \frac{3 \cdot 230^2 \left(\frac{3.8179 \cdot 10^{-2}}{1 - 3.1847 \cdot 10^{-3} \cdot \omega} \right)}{\left(3.8179 \cdot 10^{-2} + \frac{3.8179 \cdot 10^{-2}}{1 - 3.1847 \cdot 10^{-3} \cdot \omega} \right)^2 + 1.31^2} \quad (13)$$

This formulation shows that the generator power is directly influenced by the stator electrical quantities, particularly the frequency, which acts as a control variable and determines the electromechanical energy conversion process, thereby defining the system operating point.

Since the wind system operates over a wide range of rotational speeds, it requires variable voltages and frequencies, without saturating the magnetic core, that is, at nominal stator flux. By maintaining a constant stator flux, based on the converter interposed between the grid and generator, the following result is obtained:

$$\frac{U}{f_1} = \frac{230}{50} = 4.6 \text{ [V/Hz]} \quad (14)$$

The generator's power characteristic, P_{EG} , is thus obtained,

$$P_{EG}(\omega, f) = - \frac{3 \cdot 4.6^2 \left(\frac{3.8179 \cdot 10^{-2}}{1 - \frac{0.15915}{f} \cdot \omega} \right)}{\left(3.8179 \cdot 10^{-2} + \frac{3.8179 \cdot 10^{-2}}{1 - \frac{0.15915}{f} \cdot \omega} \right)^2 + \left(\frac{1.31}{50} \right)^2} \quad (15)$$

depending on the mechanical angular speed ω and the stator frequency f . This expression shows that the generator power depends on both the mechanical angular speed and the stator frequency, indicating that the operating point of the system can be controlled through electrical parameters.

The maximum power characteristic of the turbine, $P_{WT-MAX}(\omega)$, intersects the maximum power points (MPP) in Figure 1: MPP_1 at wind speed $V_1 = 3$ m/s, MPP_2 at wind speed $V_2 = 5$ m/s, MPP_3 at wind speed $V_3 = 7$ m/s, and MPP_4 at wind speed $V_4 = 10$ m/s.

Variations in wind speed lead to dynamic operation of the wind turbine, with variable speeds at the maximum power point [15]. Considering the dynamic nature of the process, the equation of motion is expressed as follows. The model is developed under simplifying assumptions in order to capture the main dynamic behavior of the system [39,40]:

$$J \cdot \frac{d\omega}{dt} = M_{WT} - M_{EG} \quad (16)$$

where ω represents the mechanical angular speed at the generator shaft (high-speed shaft), after the gearbox, MAS, at the EG shaft; J denotes the equivalent moment of inertia; and $d\omega/dt$ signifies the time derivative of MAS. M_{WT} refers to the moment provided by the WT, as it relates to the shaft of the EG, and M_{EG} indicates the electromagnetic moment at the EG shaft. By multiplying by ω , the power equation is derived [41]:

$$J \cdot \frac{d\omega}{dt} \cdot \omega = P_{WT} - P_{EG} \quad (17)$$

where P_{WT} denotes the useful power supplied by WT, measured at the EG shaft, while P_{EG} denotes the electromagnetic power at the EG shaft. The wind system operates at the intersection of the electric generator, $P_{EG}(\omega)$, and wind turbine, $P_{WT}(\omega)$, power characteristics. This equation represents the dynamic balance between the mechanical power provided by the turbine and the electromagnetic power of the generator, determining the variation in the rotational speed over time.

From a local stability perspective, the operating point can be evaluated using a derivative-based condition derived from the motion Equation (17). Stability requires that small deviations in mechanical angular speed produce restoring behavior, which can be expressed as:

$$\frac{d(P_{WT} - P_{EG})}{d\omega} < 0 \quad (18)$$

evaluated at the equilibrium point.

This condition ensures that an increase in ω leads to a decrease in the net accelerating power, driving the system back to equilibrium. Conversely, if the derivative is positive, the operating point becomes unstable.

From a physical perspective, this condition indicates that system stability depends on the balance between the mechanical power provided by the turbine and the electrical power absorbed by the generator. A stable operating point is achieved when deviations in rotational speed generate a restoring effect, driving the system back toward equilibrium. When the wind turbine (WT) captures maximum wind energy, it operates at maximum power points (MPP) [42]. To achieve this, the electric generator power characteristic (P_{EG}) must align with the maximum power characteristic produced by the turbine, as shown in Figure 1. The power extracted from the stator, through the power converter located between the generator and the grid, influences the power characteristic of the electric generator (P_{EG}).

The validity of the proposed analytical framework is supported by the consistency between the different analysis methods employed, including analytical modeling, graphical interpretation of power characteristics, and dynamic simulation results. This combined approach allows cross-verification of the system behavior and provides a coherent description of the stability of the operating point.

3. Functionality of the System in the Optimal Zone

Due to the continuous variation in wind speed, enabling the turbine to operate at maximum power points (MPP), as shown in Figure 1, requires adjusting the generator's rotational speed of the generator by changing the frequency and stator voltage.

The adjustment of stator voltage and frequency is accomplished using a converter placed between the grid and the generator, as shown in Figure 2 [34].

The power of the induction generator is derived from the steady-state model of the induction machine, where the electromagnetic power is expressed as a function of slip and stator voltage. In the present analysis, a simplified analytical formulation is used, in which

the machine parameters (such as inductances and resistances) are incorporated into the coefficients of the expressions:

$$P_{EG}(s, U_S) = 3 \frac{U_S^2 \cdot \left(\frac{R_R}{s} \right)}{\left(R_S + \frac{R_R}{s} \right)^2 + 1.31^2} \quad (19)$$

depends on the slip s and the square of the voltage U_S^2 .

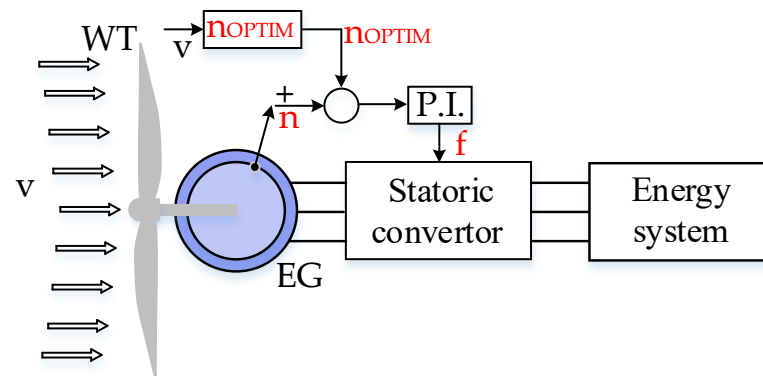


Figure 2. Wind system using an induction generator and stator converter.

Since the voltage-to-frequency ratio remains constant, voltage can be replaced with frequency f . By substituting slip s with mechanical angular speed ω and frequency f :

$$s = 1 - \frac{0.15915}{f} \cdot \omega \quad (20)$$

the power of the induction generator, $P_{EG}(\omega, f)$, is obtained as a function of two variables: ω and f , as illustrated in Figure 3.

$$P_{EG}(\omega, f) = -3 \cdot \frac{4.6^2 \cdot \left(\frac{3.8179 \cdot 10^{-2}}{\left(1 - \frac{0.15915}{f} \cdot \omega \right)} \right)}{\left(\frac{3.8179 \cdot 10^{-2} + \frac{3.8179 \cdot 10^{-2}}{\left(1 - \frac{0.15915}{f} \cdot \omega \right)}}{f^2} \right)^2 + \left(\frac{1.31}{50} \right)^2} \quad (21)$$

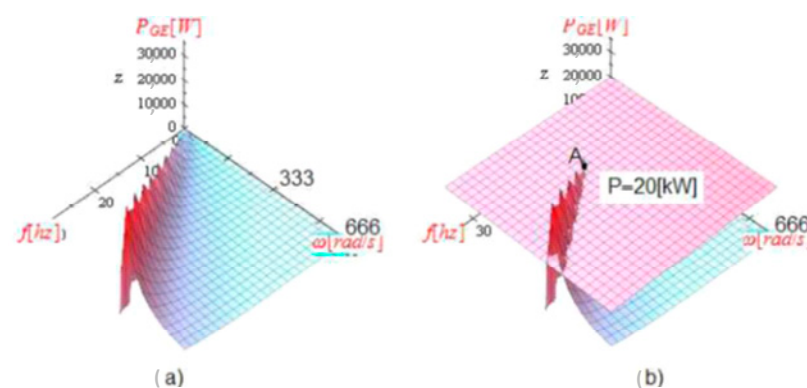


Figure 3. Characteristics of power and operating points: (a) Power variation as a function of frequency and mechanical angular velocity; (b) Power reserve variation.

This formulation makes it possible to analyze how variations in stator frequency influence the generator power and consequently the system operating point.

In Figure 3, the power characteristics are shown for frequency intervals of 0–50 Hz and mechanical angular speed ranging from 0 to 333 rad/s. These power characteristics are particularly useful for visually estimating the power reserve at a specified induction generator power value.

For an induction generator power rating of $P = 20$ kW, as shown in Figure 3b, it is observed that the power reserve increases with increasing frequency and decreases with decreasing frequency, ultimately becoming negative at low frequencies. This value is selected as a representative operating point within the operating range of the 55 kW reference wind turbine, allowing a clearer analysis of power characteristics and stability behavior under varying operating conditions.

Among the power characteristics, $P_{EG}(\omega, f)$ reveals the power reserves. Thus, considering an induction generator power value of $P_{EG}^*(\omega, f) = 20$ kW, or:

$$20,000 = -3 \cdot \frac{4.6^2 \left(\frac{3.8179 \cdot 10^{-2}}{1 - \frac{0.15915}{f} \cdot \omega} \right)}{\left(\frac{3.8179 \cdot 10^{-2} + \frac{3.8179 \cdot 10^{-2}}{1 - \frac{0.15915}{f} \cdot \omega}}{f^2} \right)^2 + \left(\frac{1.31}{50} \right)^2} \quad (22)$$

The critical operating point A (Figure 3b) is defined by the coordinates $f^* = 15$ Hz and $\omega^* = 103.1$ rad/s, as determined from the power equation:

$$\left\{ \begin{array}{l} 20,000 = -3 \cdot \frac{4.6^2 \left(\frac{3.8179 \cdot 10^{-2}}{1 - \frac{0.15915}{f} \cdot \omega} \right)}{\left(\frac{3.8179 \cdot 10^{-2} + \frac{3.8179 \cdot 10^{-2}}{1 - \frac{0.15915}{f} \cdot \omega}}{f^2} \right)^2 + \left(\frac{1.31}{50} \right)^2} \\ f = 15 \end{array} \right. \quad (23)$$

The system's operational area, at a generator power of 20 kW, is feasible only when the frequency exceeds 15 Hz, and the power reserve increases as the frequency rises:

$$\Delta P_{EG-RESERVE} = \Delta P_{EG-MAXIM} - 20,000 \quad (24)$$

By adjusting the frequency, f , and the stator voltage, the optimal mechanical angular speed, ω_{OPTIM} , is achieved according to the wind speed, as shown in Figure 1. At constant stator flux (10), the generator power in steady state equals that of the turbine (2):

$$19,182 \left(\frac{V}{\omega} - 1.3877 \cdot 10^{-2} \right) \cdot e^{-57.65 \left(\frac{V}{\omega} \right)} \cdot V^3 = - \frac{3 \cdot 4.6^2 \left(\frac{3.8179 \cdot 10^{-2}}{1 - \frac{0.15915}{f} \cdot \omega} \right)}{\left(\frac{3.8179 \cdot 10^{-2} + \frac{3.8179 \cdot 10^{-2}}{1 - \frac{0.15915}{f} \cdot \omega}}{f^2} \right)^2 + \left(\frac{1.31}{50} \right)^2} \quad (25)$$

Given the negligible inertia of the converter between the generator and the grid, compared to the turbine's mechanical inertia, the stator frequency, f , is reached without delay. Under maximum power point (MPP) conditions, the mechanical angular speed follows the relation $\omega_{opt} = k \cdot V$. Therefore, the stator frequency, f , is adjusted to enable the wind turbine (WT) to operate at the maximum power point, continuously maintaining the optimal mechanical angular speed:

$$\omega_{OPTIM} = 32.026 \cdot V \quad (26)$$

depending on the wind speed, V . In steady-state operation, the powers are equivalent, meaning $P_{WT}(\omega, V) = P_{EG}(\omega, f)$.

4. Stability Issues in System Control Through the Enforcement of Optimal RPM

This section investigates the stability of the wind energy system when operating at or near the maximum power point under varying wind conditions. The analysis focuses on how the selection of stator frequency influences the stability of the operating point.

A combined analytical and graphical approach is employed. It is based on:

- The comparison between turbine and generator power characteristics;
- The dynamic behavior derived from the motion equation.

This approach allows identifying stable and unstable operating regions and provides a clear physical interpretation of system behavior under small disturbances in wind speed.

The stator frequency and voltage must be closely coordinated with the wind speed, as they directly influence the position and stability of the operating point. A fluctuation in wind speed is considered as follows:

$$V(t) = \left(6 + 2 \cdot \sin \frac{2 \cdot \pi}{666} \cdot t \right) = 6 + 2 \cdot \sin 9.43 \cdot 10^{-3} \cdot t \quad (27)$$

This variation is used to evaluate the system response to small disturbances, which is essential for determining the stability of the operating point. The optimal mechanical angular speed is as follows:

$$\omega_{OPTIM}(t) = 32.026 \cdot \left(6 + 2 \cdot \sin \frac{2 \cdot \pi}{666} \cdot t \right) = 6 + 2 \cdot \sin 9.43 \cdot 10^{-3} \cdot t \quad (28)$$

The stability analysis presented in this section is based on a combined analytical and graphical approach, supported by the dynamic equations of motion of the system. This approach allows a physically intuitive interpretation of stability by analyzing the interaction between turbine and generator power characteristics under varying wind conditions.

The process is visualized by solving the motion Equation (12), where the system's total moment of inertia, comprising the turbine and generator, is $J = 0.7 \text{ kg} \cdot \text{m}^2$, leading to the motion equation:

$$0.7 \cdot \frac{d\omega}{dt} \cdot \omega = P_{WT} - P_{EG} \quad (29)$$

Consequently, a system of differential equations arises: the equation of motion and the frequency regulator equation.

$$\begin{cases} 0.7 \cdot \frac{d\omega}{dt} \cdot \omega = P_{WT} - P_{EG} \\ f - f_{OPTIM} = K_1 \cdot [\omega - 32.026 \cdot (6 + 2 \cdot \sin 9.43 \cdot 10^{-3} \cdot t)] + K_2 \int \omega - 32.026 \cdot (6 + 2 \cdot \sin 9.43 \cdot 10^{-3} \cdot t) \cdot dt \end{cases} \quad (30)$$

At the initial conditions, when $t = 0$:

$$P_{EG}(\omega, f) = - \frac{3 \cdot 4.6^2 \left(\frac{3.8179 \cdot 10^{-2}}{1 - \frac{0.15915}{f} \cdot \omega} \right)^2}{\left(\frac{3.8179 \cdot 10^{-2} + \frac{3.8179 \cdot 10^{-2}}{1 - \frac{0.15915}{f} \cdot \omega}}{f^2} \right)^2} + \left(\frac{1.31}{50} \right)^2 \quad (31)$$

The wind speed value of 6 m/s is selected as a representative operating point within the normal operating range of the wind turbine, corresponding to a region where maximum power point operation is relevant.

The stability analysis is performed by considering small variations in wind speed (e.g., from 6 m/s to 6.5 m/s) to evaluate the local stability of the system around the maximum power point.

The same analytical approach can be applied to other wind speed values.

At time $t = 0$, the generator's power equals that of the turbine (13), and at a wind speed of $V(0) = 6 \text{ m/s}$, it follows that:

$$19,182 \left(\frac{6}{\omega} - 1.3877 \cdot 10^{-2} \right) \cdot \exp^{-57.65 \left(\frac{6}{\omega} \right)} \cdot 6^3 = - \frac{3 \cdot 4.6^2 \left(\frac{3.8179 \cdot 10^{-2}}{1 - \frac{0.15915}{f} \cdot \omega} \right)^2}{\left(\frac{3.8179 \cdot 10^{-2} + \frac{3.8179 \cdot 10^{-2}}{1 - \frac{0.15915}{f} \cdot \omega}}{f^2} \right)^2} + \left(\frac{1.31}{50} \right)^2 \quad (32)$$

It is assumed that the mechanical angular speed ω is equal to the optimal value, ω_{OPTIM} , which is:

$$\omega_{OPTIM}(0) = 32.026 \cdot 6 = 192.16 \text{ [rad/s]} \quad (33)$$

According to the equality of powers (20), two values for the optimal frequency are obtained: $f_1 = 23.695 \text{ Hz}$ and $f_2 = 30.344 \text{ Hz}$.

The characteristics of the generator's power at the two frequency values, $f_1 = 23.695$ Hz and $f_2 = 30.344$ Hz, are as follows:

$$P_{EG-1}(\omega, 23.695) = - \frac{3 \cdot 4.6^2 \left(\frac{3.8179 \cdot 10^{-2}}{1 - \frac{0.15915}{23.695} \cdot \omega} \right)}{\left(\frac{3.8179 \cdot 10^{-2} + \frac{3.8179 \cdot 10^{-2}}{1 - \frac{0.15915}{23.695} \cdot \omega}}{23.695^2} \right)^2 + \left(\frac{1.31}{50} \right)^2} \quad (34)$$

$$P_{EG-2}(\omega, 30.344) = - \frac{3 \cdot 4.6^2 \left(\frac{3.8179 \cdot 10^{-2}}{1 - \frac{0.15915}{30.344} \cdot \omega} \right)}{\left(\frac{3.8179 \cdot 10^{-2} + \frac{3.8179 \cdot 10^{-2}}{1 - \frac{0.15915}{30.344} \cdot \omega}}{30.344^2} \right)^2 + \left(\frac{1.31}{50} \right)^2} \quad (35)$$

The operating point is located at the intersection of the generator power characteristic, P_{EG} , and the turbine power characteristic, P_{WT} . The question arises as to whether the system is stable at both frequency values, f_1 and f_2 .

Stability of the System in Response to Frequency Changes

The turbine's power characteristic, when $V = 6$ m/s, is:

$$P_{WT-6}(\omega) = 19,182 \left(\frac{6}{\omega} - 1.3877 \cdot 10^{-2} \right) \cdot e^{-57.65 \left(\frac{6}{\omega} \right)} \cdot 6^3 \quad (36)$$

intersections occur with those of the generator, $P_{EG-1}(\omega, 23.695)$ and $P_{EG-2}(\omega, 30.344)$, at points *A*, *MPP*, *B*, *C*, and *D*, as shown in Figure 3. The points *A*, *B*, *C*, *D*, and *MPP* represent the operating points defined by the intersection of the turbine power characteristic and the generator power characteristics at different stator frequencies. Each point corresponds to a specific operating condition of the system, characterized by a particular mechanical angular speed and power level.

The stability of each operating point is determined by analyzing the relative variation in turbine and generator power with respect to changes in rotational speed. A stable operating point is characterized by the tendency of the system to return to equilibrium after a small disturbance, whereas an unstable point leads to divergence from the initial operating condition.

It is considered that the wind speed increases from 6 m/s to 6.5 m/s, and the initial operating point, *MPP*, will move in the direction indicated in Figure 4.

The turbine's characteristic when $V = 6.5$ m/s is as follows:

$$P_{WT-6.5}(\omega) = 19,182 \left(\frac{6.5}{\omega} - 1.3877 \cdot 10^{-2} \right) \cdot \exp^{-57.65 \left(\frac{6.5}{\omega} \right)} \cdot 6.5^3 \quad (37)$$

Based on this characteristic, the points *A*, *MPP*, *B*, *C*, and *D* on the turbine power characteristic at $V = 6$ m/s will correspond to A^* , P_1 , P_2 , B^* , C^* , and D^* . When the wind speed changes, the operating point shifts along the corresponding power characteristic, leading to new equilibrium points (e.g., $A \rightarrow A^*$, $MPP \rightarrow P_2$). These transitions illustrate how the system responds dynamically to external disturbances.

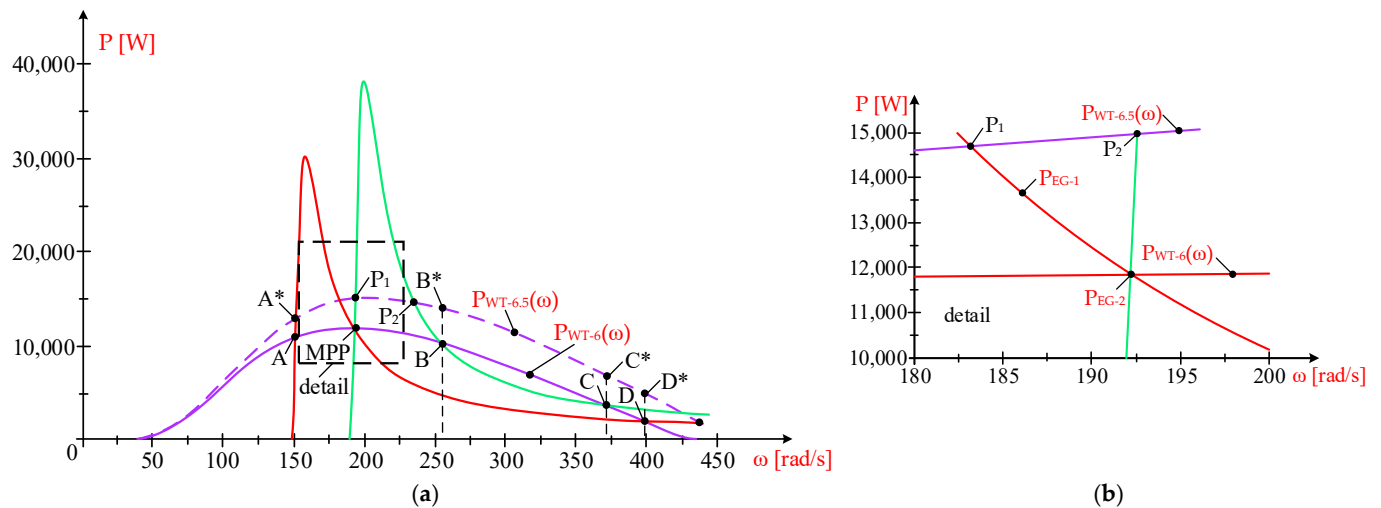


Figure 4. Characteristics of power and operating points: (a) Power variation curve; (b) Details on operating points.

A graphical analysis of the power characteristics allows the identification of the nature of the operating points.

The operating points A , B , C , D , and MPP correspond to the intersections between turbine and generator power characteristics at different stator frequencies.

Their stability depends on the response of the system to small perturbations in rotational speed. Points A , C , and D represent stable equilibrium conditions, where deviations lead to restoring behavior, whereas point B corresponds to an unstable equilibrium, where perturbations cause divergence from the operating point.

This analysis confirms that multiple operating points may exist under the same wind conditions, but their stability properties differ significantly. An important observation is that, for a given wind speed, multiple stator frequency values may satisfy the steady-state power balance condition. However, only one of these frequencies ensures the stable operation of the system.

This result can be further interpreted from a control-theoretic perspective. For a given wind speed, the steady-state condition may admit multiple equilibrium solutions corresponding to different stator frequency values (e.g., f_1 and f_2). However, the stability analysis—performed both mathematically, using the motion equation, and graphically, using the power characteristics—shows that only one of these solutions ensures stable operation under small wind perturbations.

This demonstrates that satisfying the steady-state power balance alone is not sufficient to guarantee stability, and that the selection of the operating frequency must explicitly account for stability constraints. This aspect highlights a non-trivial characteristic of the control problem and represents a key contribution of the present study.

Consequently, the operating point must be selected not only based on power matching but also considering stability constraints, which represent a critical limitation of conventional *MPPT* approaches that assume a unique optimal operating condition.

The stability of the system can be analyzed at the two frequency values, f_1 and f_2 , by utilizing the power equation:

$$J \cdot \frac{d\omega}{dt} \cdot \omega = P_{WT} - P_{EG} \quad (38)$$

or the motion equation at $f_1 = 23.695$ Hz:

$$0.7 \cdot \frac{d\omega}{dt} \cdot \omega = 19,182 \left(\frac{6.5}{\omega} - 1.3877 \cdot 10^{-2} \right) \cdot \exp^{-57.65 \left(\frac{6.5}{\omega} \right)} \cdot 6.5^3 + \frac{3 \cdot 4.6^2 \left(\frac{3.8179 \cdot 10^{-2}}{1 - \frac{0.15915}{23.695} \cdot \omega} \right)}{\left(\frac{3.8179 \cdot 10^{-2} + \frac{3.8179 \cdot 10^{-2}}{1 - \frac{0.15915}{23.695} \cdot \omega}}{23.695^2} \right)^2 + \left(\frac{1.31}{50} \right)^2} \quad (39)$$

for the mechanical angular speed ω at f_1 , $\omega(0) = 192.16$, and the equation of motion at $f_2 = 30.344$ Hz

$$0.7 \cdot \frac{d\Omega}{dt} \cdot \Omega = 19,182 \left(\frac{6.5}{\Omega} - 1.3877 \cdot 10^{-2} \right) \cdot \exp^{-57.65 \left(\frac{6.5}{\Omega} \right)} \cdot 6.5^3 + \frac{3 \cdot 4.6^2 \left(\frac{3.8179 \cdot 10^{-2}}{1 - \frac{0.15915}{30.344} \cdot \Omega} \right)}{\left(\frac{3.8179 \cdot 10^{-2} + \frac{3.8179 \cdot 10^{-2}}{1 - \frac{0.15915}{30.344} \cdot \Omega}}{30.344^2} \right)^2 + \left(\frac{1.31}{50} \right)^2} \quad (40)$$

For the mechanical angular speed Ω at f_2 , $\Omega(0) = 192.16$.

Thus, the following system of differential equations was obtained:

$$\left\{ \begin{array}{l} 0.7 \cdot \frac{d\omega}{dt} \cdot \omega = 19,182 \left(\frac{6.5}{\omega} - 1.3877 \cdot 10^{-2} \right) \cdot \exp^{-57.65 \left(\frac{6.5}{\omega} \right)} \cdot 6.5^3 + \frac{3 \cdot 4.6^2 \left(\frac{3.8179 \cdot 10^{-2}}{1 - \frac{0.15915}{23.695} \cdot \omega} \right)}{\left(\frac{3.8179 \cdot 10^{-2} + \frac{3.8179 \cdot 10^{-2}}{1 - \frac{0.15915}{23.695} \cdot \omega}}{23.695^2} \right)^2 + \left(\frac{1.31}{50} \right)^2} \\ 0.7 \cdot \frac{d\Omega}{dt} \cdot \Omega = 19,182 \left(\frac{6.5}{\Omega} - 1.3877 \cdot 10^{-2} \right) \cdot \exp^{-57.65 \left(\frac{6.5}{\Omega} \right)} \cdot 6.5^3 + \frac{3 \cdot 4.6^2 \left(\frac{3.8179 \cdot 10^{-2}}{1 - \frac{0.15915}{30.344} \cdot \Omega} \right)}{\left(\frac{3.8179 \cdot 10^{-2} + \frac{3.8179 \cdot 10^{-2}}{1 - \frac{0.15915}{30.344} \cdot \Omega}}{30.344^2} \right)^2 + \left(\frac{1.31}{50} \right)^2} \\ \omega(0) = 192.16 \\ \Omega(0) = 192.16 \end{array} \right. \quad (41)$$

By solving this system, one can determine the changes in mechanical angular speed over time and draw conclusions regarding the stability of the system, as discussed below. By increasing the wind speed from 6 m/s to 6.5 m/s, the initial operating point, with $\omega(0) = 192.16$ rad/s, shifts along the generator's power characteristic:

$$P_{EG-1}(\omega, 23.695) = - \frac{3 \cdot 4.6^2 \left(\frac{3.8179 \cdot 10^{-2}}{1 - \frac{0.15915}{23.695} \cdot \omega} \right)}{\left(\frac{3.8179 \cdot 10^{-2} + \frac{3.8179 \cdot 10^{-2}}{1 - \frac{0.15915}{23.695} \cdot \omega}}{23.695^2} \right)^2 + \left(\frac{1.31}{50} \right)^2} \quad (42)$$

At $f_1 = 23.695$ Hz, after 44 s, the mechanical angular speed is:

$$\omega(44) = 443.19 \text{ rad/s} \gg \omega(0) = 192.16 \text{ rad/s} \quad (43)$$

Given that the initial and final values of the mechanical angular speed differ significantly, it follows that at $f_1 = 23.695$ Hz the system is unstable, as illustrated in Figure 4.

Similarly, by increasing the wind speed from 6 m/s to 6.5 m/s, the initial operating point shifts along the generator's power characteristic:

$$P_{EG-2}(\omega, 30.344) = - \frac{3 \cdot 4.6^2 \left(\frac{3.8179 \cdot 10^{-2}}{1 - \frac{0.15915}{30.344} \cdot \omega} \right)}{\left(\frac{3.8179 \cdot 10^{-2} + \frac{3.8179 \cdot 10^{-2}}{1 - \frac{0.15915}{30.344} \cdot \omega}}{30.344^2} + \left(\frac{1.31}{50} \right)^2 \right)} \quad (44)$$

At frequency $f_2 = 30.344$ Hz, after 66 s, the mechanical angular speed is measured at $\Omega(66) = 192.57$ rad/s, which is close to the initial value of $\Omega(0) = 192.16$ rad/s.

The initial and final values of the mechanical angular speed are very similar, indicating that at $f_2 = 30.344$ Hz the system is stable, as shown in Figure 5.

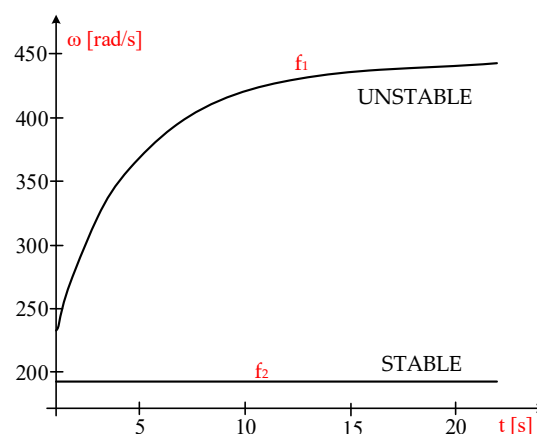


Figure 5. Variations in MAS at frequencies f_1 and f_2 .

From Figure 5, it is clear that at frequency f_1 , the MAS increases from the initial value of $\omega(0) = 192.16$ rad/s to $\omega(48) = 443.2$ rad/s after approximately 48 s. This indicates that the operation is unstable at the *MPP* point, which is also observable in the detailed view of Figure 4, where the operating point has shifted to *D*, significantly distant from the initial operating point.

From the initial *MPP* operating point at $f_2 = 30.344$ Hz, by increasing the wind speed to 6.5 m/s, the system stabilizes at the operating point P_2 (Figure 3—detail), at $\Omega(11) = 192.57$. This is also validated by the equation of motion, of the form:

$$\left\{ \begin{array}{l} 0.7 \cdot \frac{d\Omega}{dt} \cdot \Omega = 19,182 \left(\frac{6.5}{\Omega} - 1.3877 \cdot 10^{-2} \right) \cdot \exp^{-57.65 \left(\frac{6.5}{\Omega} \right)} \cdot 6.5^3 + \frac{3 \cdot 4.6^2 \left(\frac{3.8179 \cdot 10^{-2}}{1 - \frac{0.15915}{30.344} \cdot \Omega} \right)}{\left(\frac{3.8179 \cdot 10^{-2} + \frac{3.8179 \cdot 10^{-2}}{1 - \frac{0.15915}{30.344} \cdot \Omega}}{30.344^2} + \left(\frac{1.31}{50} \right)^2 \right)} \\ \Omega(0) = 192.16 \end{array} \right. \quad (45)$$

In conclusion, the combined graphical and dynamic analysis demonstrates that system stability is strongly dependent on stator frequency selection. Although multiple operating points may satisfy the steady-state power balance, only specific frequency values ensure stable operation under wind disturbances.

This analysis provides a physically meaningful interpretation of stability and emphasizes that the existence of stable and unstable operating regions is strongly dependent on the selected stator frequency, which must be carefully considered when designing control strategies for maximum power point operation.

5. Simulation of System Control Through Frequency Modification

Control of the wind system involves achieving a current mechanical angular speed, ω , equal to the optimal value, ω_{OPTIM} , which is defined as follows:

$$\omega_{OPTIM} = 32.026 \cdot V = 32.026 \cdot (6 + 2 \cdot \sin 9.43 \cdot 10^{-3} \cdot t) \text{ [rad/s]} \quad (46)$$

for a sinusoidal wind speed fluctuation, in the form:

$$V(t) = \left(6 + 2 \cdot \sin \frac{2 \cdot \pi}{666} \cdot t \right) = 6 + 2 \cdot \sin 9.43 \cdot 10^{-3} \cdot t \quad (47)$$

The differential equations of motion and the frequency regulator are as follows:

$$\begin{cases} 0.7 \cdot \frac{d\omega}{dt} \cdot \omega = P_{WT} - P_{EG} \\ f - f_{OPTIM} = K_1 \cdot (\omega - \omega_{OPTIM}) + K_2 \int (\omega - \omega_{OPTIM}) \cdot dt \end{cases} \quad (48)$$

it is obtained:

$$\left\{ \begin{array}{l} 0.7 \cdot \frac{d\omega}{dt} \cdot \omega = 19,182 \left[\frac{(6 + 2 \cdot \sin 9.43 \cdot 10^{-3} \cdot t)}{\omega} - 1.3877 \cdot 10^{-2} \right] \cdot \exp^{-57.65 \left(\frac{6 + 2 \cdot \sin 9.43 \cdot 10^{-3} \cdot t}{\omega} \right)} \\ (6 + 2 \cdot \sin 9.43 \cdot 10^{-3} \cdot t)^3 + \frac{3 \cdot 4.6^2 \left(\frac{3.8179 \cdot 10^{-2}}{1 - \frac{0.15915}{f} \cdot \omega} \right)}{\left(\frac{3.8179 \cdot 10^{-2} + \frac{3.8179 \cdot 10^{-2}}{1 - \frac{0.15915}{f} \cdot \Omega}}{f^2} \right)^2 + \left(\frac{1.31}{50} \right)^2} \\ \frac{df}{dt} = -0.17263 \cdot \left(\frac{d\omega}{dt} - 0.60401 \cdot \cos 0.00943 \cdot t \right) - 0.28 \cdot [\omega - 32.026 \cdot (6 + 2 \cdot \sin 9.43 \cdot 10^{-3} \cdot t)] \\ \omega(0) = 192.16 \\ f(0) = 30.344 \end{array} \right. \quad (49)$$

Tuning the frequency regulators involves determining the constants K_1 for proportionality and K_2 for integration.

The *PI* controller is designed based on an analytical and physically motivated approach, aiming to ensure that the mechanical angular speed follows the optimal value corresponding to the maximum power point.

Proportionality constant, K_1 . Only the proportional component of the regulator is considered:

$$f - f_{OPTIM} = K_1 \cdot (\omega - \omega_{OPTIM}) \quad (50)$$

and through derivation, it is obtained:

$$\frac{df}{dt} = K_1 \cdot \frac{d\omega}{dt} \quad (51)$$

resulting in:

$$K_1 = \frac{df}{d\omega} \approx \frac{\Delta f}{\Delta \omega} \quad (52)$$

The proportional gain K_1 determines the immediate response of the system to deviations between the actual and optimal mechanical angular speed. A higher value of K_1 increases the sensitivity of the control action, allowing faster correction of deviation.

Near the initial operating point, MPP , at a wind speed of $V(0) = 6$ m/s, from the power equality $P_{WT} = P_{EG}$, the optimal frequency $f_{OPTIM} = 30.344$ Hz was determined.

The proportionality constant K_1 is determined as follows:

A frequency value is selected, $f_2 = 31$ Hz, which is close to the initial frequency $f_1 = 30.344$ Hz, and the following is obtained:

$$\Delta f = f_2 - f_1 = 31 - 30.344 = 0.656 \text{ Hz} \quad (53)$$

The power characteristics of the generator at the two frequency values are:

$$P_{EG-1}(\omega) = - \frac{3 \cdot 4.6^2 \left(\frac{3.8179 \cdot 10^{-2}}{1 - \frac{0.15915}{30.344} \cdot \omega} \right)}{\left(\frac{3.8179 \cdot 10^{-2} + \frac{3.8179 \cdot 10^{-2}}{1 - \frac{0.15915}{30.344} \cdot \omega}}{30.344^2} \right)^2 + \left(\frac{1.31}{50} \right)^2} \quad (54)$$

$$P_{EG-2}(\omega) = - \frac{3 \cdot 4.6^2 \left(\frac{3.8179 \cdot 10^{-2}}{1 - \frac{0.15915}{31} \cdot \omega} \right)}{\left(\frac{3.8179 \cdot 10^{-2} + \frac{3.8179 \cdot 10^{-2}}{1 - \frac{0.15915}{31} \cdot \omega}}{31^2} \right)^2 + \left(\frac{1.31}{50} \right)^2} \quad (55)$$

For a wind speed of 6 m/s, the power characteristic of the turbine is obtained as follows:

$$P_{WT-6}(\omega) = 19,182 \cdot \left(\frac{6}{\omega} - 1.3877 \cdot 10^{-2} \right) \cdot \exp^{-57.65 \left(\frac{6}{\omega} \right)} \cdot 6^3 \quad (56)$$

The intersection points of the power characteristics of the generator, $P_{EG-1}(\omega)$ and $P_{EG-2}(\omega)$, with that of the turbine, $P_{WT-6}(\omega)$, are determined.

The power characteristics of both the turbine and the generator are shown in Figure 6, where the intersection points, A and B , of the power characteristics of the turbine and generator are also visible.

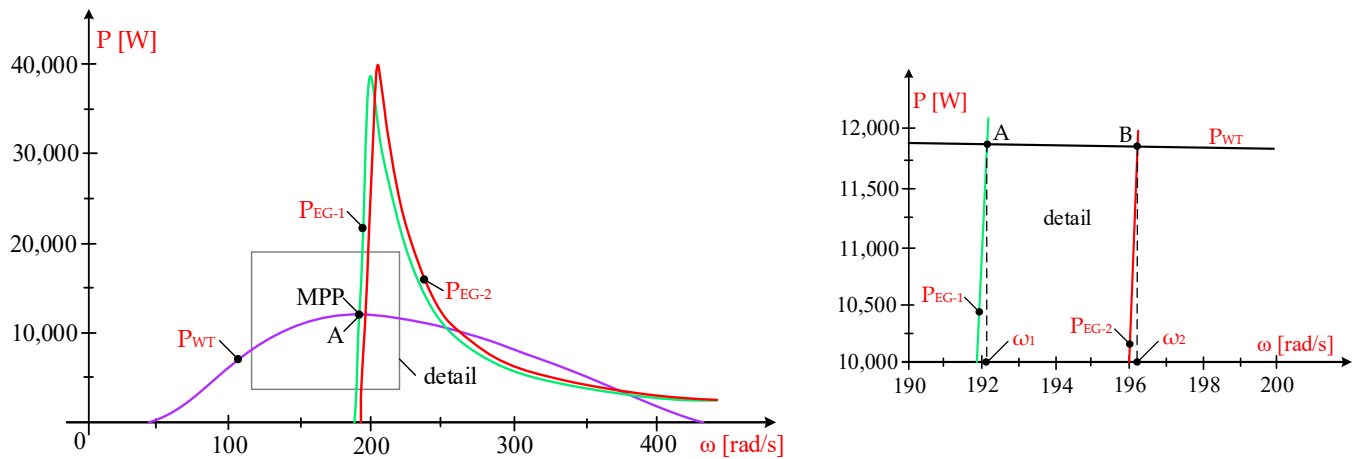


Figure 6. The power characteristics and the initial operating area.

At the equality of forces, the values of the mechanical angular velocities ω_1 for point A and ω_2 for point B are obtained:

Point A, $\omega_1 = 192.3$ rad/s:

$$19,182 \cdot \left(\frac{6}{\omega} - 1.3877 \cdot 10^{-2} \right) \cdot \exp^{-57.65 \left(\frac{6}{\omega} \right)} \cdot 6^3 = - \frac{3 \cdot 4.6^2 \left(\frac{3.8179 \cdot 10^{-2}}{1 - \frac{0.15915}{30.344} \cdot \omega} \right)}{\left(\frac{3.8179 \cdot 10^{-2} + \frac{3.8179 \cdot 10^{-2}}{1 - \frac{0.15915}{30.344} \cdot \omega}}{30.344^2} \right)^2 + \left(\frac{1.31}{50} \right)^2} \quad (57)$$

Point B, $\omega_2 = 196.1$ rad/s:

$$19,182 \cdot \left(\frac{6}{\omega} - 1.3877 \cdot 10^{-2} \right) \cdot \exp^{-57.65 \left(\frac{6}{\omega} \right)} \cdot 6^3 = - \frac{3 \cdot 4.6^2 \left(\frac{3.8179 \cdot 10^{-2}}{1 - \frac{0.15915}{31} \cdot \omega} \right)}{\left(\frac{3.8179 \cdot 10^{-2} + \frac{3.8179 \cdot 10^{-2}}{1 - \frac{0.15915}{31} \cdot \omega}}{31^2} \right)^2 + \left(\frac{1.31}{50} \right)^2} \quad (58)$$

The difference $\Delta\omega$ between the mechanical angular velocities ω_1 and ω_2 is:

$$\Delta\omega = \omega_2 - \omega_1 = 196.1 - 192.3 = 3.8 \text{ Hz} \quad (59)$$

and the proportionality constant K_1 is obtained:

$$K_1 = \frac{df}{d\omega} = \frac{0.656}{3.8} = 0.17263 \quad (60)$$

Integration constant, K_2 . To determine the integration constant K_2 , only the integration component of the regulator is considered:

$$f - f_{OPTIM} = K_2 \int (\omega - \omega_{OPTIM}) \cdot dt \quad (61)$$

and, through derivation, the following is obtained:

$$\frac{df}{dt} = K_2(\omega - \omega_{OPTIM}) \quad (62)$$

resulting in:

$$K_2 = \frac{\frac{df}{dt}}{(\omega - \omega_{OPTIM})} \approx \frac{\Delta f}{\Delta t(\omega - \omega_{OPTIM})} \quad (63)$$

The integral gain K_2 ensures the elimination of steady-state error by continuously adjusting the control signal based on the accumulated deviation in mechanical angular speed.

At frequencies $f_2 = 31$ Hz and $f_1 = 30.344$ Hz, the following results were obtained:

$$\Delta f = f_2 - f_1 = 31 - 30.344 = 0.656 \text{ Hz} \quad (64)$$

Near the initial operating point, *MPP*, at a wind speed of $V_0 = 6$ m/s, the optimal MAS is:

$$\omega_{OPTIM} = 32.026 \cdot 6 = 192.16 \text{ rad/s} \quad (65)$$

The time interval is derived from the motion equation:

$$J \cdot \frac{d\omega}{dt} \cdot \omega = P_{WT} - P_{EG} \quad (66)$$

or:

$$J \cdot \omega \cdot d\omega = (P_{WT} - P_{EG}) \cdot dt \quad (67)$$

and by integration we obtain:

$$0.7 \cdot \frac{\omega_2^2 - \omega_1^2}{2} = (P_{WT}(6) - P_{EG-MEDIU}) \cdot \Delta t \quad (68)$$

resulting in:

$$\Delta t = 0.7 \cdot \frac{\omega_2^2 - \omega_1^2}{2(P_{WT}(6) - P_{EG-MEDIU})} = 0.7 \cdot \frac{196.1^2 - 192.3^2}{2(P_{WT} - P_{EG-MEDIU})} = \frac{516.57}{(P_{WT} - P_{EG-MEDIU})} \quad (69)$$

The power of the turbine, $P_{WT}(6)$, at

$$\omega = \frac{\omega_2 + \omega_1}{2} = \frac{(196.1 + 192.3)}{2} = 194.2 \text{ Hz} \quad (70)$$

is:

$$\begin{cases} \omega = 194.2 \text{ Hz} \\ P_{WT} = 19,182 \left(\frac{6}{\omega} - 1.3877 \cdot 10^{-2} \right) \cdot \exp^{-57.65 \left(\frac{6}{\omega} \right)} \cdot 6^3 = 11,878 \text{ W} \end{cases} \quad (71)$$

Generator power at $\omega_1 = 192.3$ rad/s and $f_1 = 30.344$ Hz, is:

$$\left\{ \begin{array}{l} \omega = 192.3 \text{ Hz} \\ P_{EG-1} = - \frac{3 \cdot 4.6^2 \left(\frac{3.8179 \cdot 10^{-2}}{1 - \frac{0.15915}{30.344} \cdot \omega} \right)}{\left(\frac{3.8179 \cdot 10^{-2} + \frac{3.8179 \cdot 10^{-2}}{1 - \frac{0.15915}{30.344} \cdot \omega}}{30.344^2} \right)^2 + \left(\frac{1.31}{50} \right)^2} = 12,953 \text{ W} \end{array} \right. \quad (72)$$

and at $\omega_1 = 196.1$ rad/s and $f_2 = 31$ Hz it is:

$$\left\{ \begin{array}{l} \omega = 196.1 \text{ Hz} \\ P_{EG-2} = - \frac{3 \cdot 4.6^2 \left(\frac{3.8179 \cdot 10^{-2}}{1 - \frac{0.15915}{31} \cdot \omega} \right)}{\left(\frac{3.8179 \cdot 10^{-2} + \frac{3.8179 \cdot 10^{-2}}{1 - \frac{0.15915}{31} \cdot \omega}}{31^2} \right)^2 + \left(\frac{1.31}{50} \right)^2} = 12,953 \text{ W} \end{array} \right. \quad (73)$$

The generator's average power over the time interval t is the arithmetic mean of the two values, P_{EG-1} and P_{EG-2} , resulting in:

$$P_{EG-MEDIU} = \frac{P_{EG-1} + P_{EG-2}}{2} = \frac{12,953 + 10,712}{2} = 11,833 \text{ W} \quad (74)$$

thus, the value for the time interval t is:

$$\Delta t = \frac{516.57}{P_{WT} - P_{EG-MEDIU}} = \frac{516.57}{11,878 - 11,833} = 11.479 \text{ s} \quad (75)$$

Thus, the integration component of the value regulator is obtained:

$$K_2 = \frac{\frac{df}{dt}}{\omega - \omega_{OPTIM}} \approx \frac{\Delta f}{\Delta t(\omega - \omega_{OPTIM})} = \frac{0.656}{11.479(194.2 - 192.16)} = 0.028 \text{ s} \quad (76)$$

With these values, $K_1 = 0.17263$ and $K_2 = 0.028$, the differential equations of motion and the frequency regulator become:

$$\left\{ \begin{array}{l} 0.7 \cdot \frac{d\omega}{dt} \cdot \omega = 19,182 \left[\frac{(6 + 2 \cdot \sin 9.43 \cdot 10^{-3} \cdot t)}{\omega} - 1.3877 \cdot 10^{-2} \right] \cdot \exp^{-57.65 \frac{(6 + 2 \cdot \sin 9.43 \cdot 10^{-3} \cdot t)}{\omega}} \\ (6 + 2 \cdot \sin 9.43 \cdot 10^{-3} \cdot t)^3 + 3 \frac{4.6^2 \left[\frac{3.8179 \cdot 10^{-2}}{\left(1 - \frac{0.15915}{f} \cdot \omega \right)} \right]}{\left(\frac{3.8179 \cdot 10^{-2} + \frac{3.8179 \cdot 10^{-2}}{\left(1 - \frac{0.15915}{f} \cdot \omega \right)}}{f^2} \right)^2 + \left(\frac{1.31}{50} \right)^2} \\ \frac{df}{dt} = 0.17263 \left(\frac{d\omega}{dt} - 0.60401 \cdot \cos 0.00943 \cdot t \right) - 0.028 [\omega - 32.026 \cdot (6 + 2 \cdot \sin 9.43 \cdot 10^{-3} \cdot t)] \\ \omega(0) = 192.16 \\ f(0) = 30.344 \end{array} \right. \quad (77)$$

The tuning procedure is based on the dynamic behavior of the system derived from the motion equation, providing a physically consistent approach for selecting the controller parameters within the given operating range.

Knowing the dependence of frequency on wind speed as [9,13] $f_1 = 5 \cdot V$ gives the model frequency variation, f_1 :

$$f_1 = 5 \cdot V = 5 \cdot (6 + 2 \cdot \sin 9.43 \cdot 10^{-3} \cdot t) \text{ s} \quad (78)$$

By solving the system of differential equations, the variations in the actual frequencies, f (red), and modelled frequencies, f_1 (black), as well as the current angular velocities, ω (black), and the optimal angular velocities, ω_{OPTIM} (red), are obtained, as shown in Figure 7a,b.

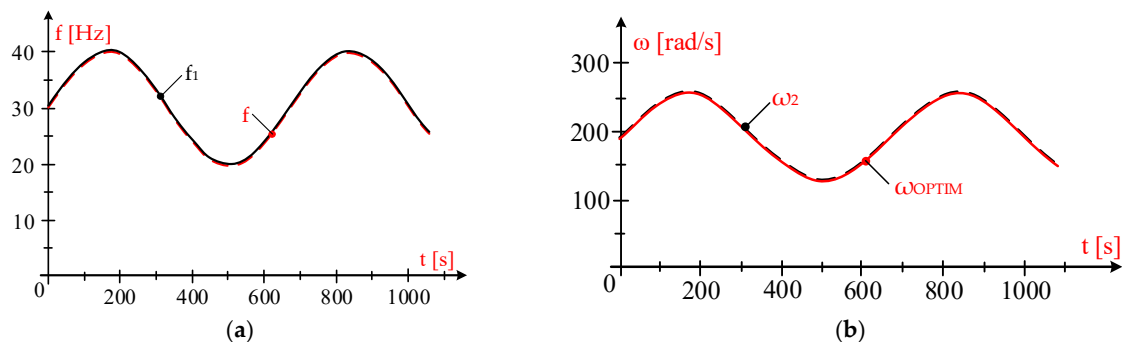


Figure 7. Temporal variations: (a) Frequency variation; (b) Variation in mechanical angular speed.

The same variations in frequency and angular mechanical velocities are also obtained at $K_1 = 0.1$ and $K_2 = 0.05$, using the equations:

$$\left\{ \begin{array}{l} 0.7 \cdot \frac{d\omega}{dt} \cdot \omega = 19,182 \left[\frac{(6 + 2 \cdot \sin 9.43 \cdot 10^{-3} \cdot t)}{\omega} - 1.3877 \cdot 10^{-2} \right] \cdot \exp^{-57.65 \left(\frac{(6 + 2 \cdot \sin 9.43 \cdot 10^{-3} \cdot t)}{\omega} \right)} \\ \quad + \frac{3 \cdot 4.6^2 \left(\frac{3.8179 \cdot 10^{-2}}{1 - \frac{0.15915}{f} \cdot \omega} \right)}{(6 + 2 \cdot \sin 9.43 \cdot 10^{-3} \cdot t)^3 + \frac{\left(\frac{3.8179 \cdot 10^{-2}}{1 - \frac{0.15915}{f} \cdot \omega} \right)^2}{\left(\frac{3.8179 \cdot 10^{-2} + \frac{3.8179 \cdot 10^{-2}}{1 - \frac{0.15915}{f} \cdot \omega}}{1 - \frac{0.15915}{f} \cdot \omega} \right)^2} + \left(\frac{1.31}{50} \right)^2} \\ \frac{df}{dt} = -0.1 \cdot \left(\frac{d\omega}{dt} - 0.60401 \cdot \cos 0.00943 \cdot t \right) - 0.05 \cdot [\omega - 32.026 \cdot (6 + 2 \cdot \sin 9.43 \cdot 10^{-3} \cdot t)] \\ \omega(0) = 192.16 \\ f(0) = 30.344 \end{array} \right. \quad (79)$$

Using the values of K_1 and K_2 , the generator's output power is related to the wind speed and the current mechanical angular speed, ω , as it approaches the optimal MAS, ω_{OPTIM} . The wind energy captured by the turbine reaches its peak, with the regulator adjusting the frequency and stator voltage in close correlation with the wind speed.

6. Results and Discussion

This study investigates the operational behavior of medium-power wind turbines equipped with squirrel-cage induction generators, controlled through stator-side frequency adjustment using a power electronic converter. The analysis covers wind speed variations from 3 m/s to 10 m/s and evaluates system stability under substantial fluctuations in wind conditions. By modifying the stator frequency, the generator's rotational speed can be regulated to ensure operation at the maximum power point (MPP).

6.1. Simulation Setup

The simulation model is based on a set of nonlinear differential equations describing the wind turbine and induction generator dynamics. The equations are solved numerically using standard integration methods.

Initial conditions are obtained from the steady-state solution of the system by setting the derivatives to zero. The model parameters correspond to the 55 kW reference wind turbine.

The control system is implemented using a *PI* regulator that adjusts the stator frequency to maintain operation at the maximum power point. Small variations in wind speed are introduced to evaluate system stability.

The system of nonlinear differential equations was solved numerically using a fixed-step fourth-order Runge–Kutta method implemented in a Scientific Workplace environment, based on the MAPLE computational core. The integration time step was selected to ensure numerical stability and accuracy of the results. Convergence of the numerical solution was verified by ensuring consistent system response for sufficiently small time-step variations.

The *PI* controller parameters were determined analytically based on the system dynamics derived from the motion equation, as described in Section 5. The controller was implemented in a standard *PI* form within the numerical simulation framework, using these parameters to regulate the mechanical angular speed towards its optimal value.

The values of the controller parameters are summarized in Table 1.

Table 1. *PI* controller parameters.

Parameter	Value
K_1 (Proportional gain)	0.17263
K_2 (Integral gain)	0.028

All simulations were performed within this numerical computing environment, enabling consistent evaluation of the system response under varying wind conditions.

6.2. Results

The main findings of the study can be summarized as follows:

1. Stator frequency and voltage adaptation:

The stator frequency and voltage were successfully adjusted in response to wind speed variations using the converter installed between the generator and the grid. This adjustment enabled the turbine to track the optimal mechanical speed corresponding to the *MPP*, as illustrated in Figure 7a.

2. Stability assessment across operating frequencies:

System stability was evaluated at multiple operating frequencies determined by the imposed wind speed. The analysis revealed distinct stable and unstable regions depending on the selected frequency, as demonstrated in Figures 4 and 5.

3. *PI* controller parameter identification:

The proportional and integral gains of the *PI* controller were determined based on the relationship between the actual mechanical angular speed ω and the optimal mechanical angular speed ω_{OPTIM} . Their effect is evident in the convergence behavior shown in Figure 7b, which demonstrates how the controller ensures operation near the optimal point.

To provide a clearer overview of the main findings, a summary of the results is presented in Table 2.

Table 2. Summary of main results.

Parameter/Condition	Value/Observation	Interpretation
Wind speed range	3–10 m/s	Operation at <i>MPP</i> feasible over a wide range
Frequency f_1	23.695 Hz	Unstable operation
Frequency f_2	30.344 Hz	Stable operation
Speed variation (f_1)	Large deviation	Indicates instability
Speed variation (f_2)	Small deviation	Indicates stable regime
Control method	<i>PI</i> controller	Ensures convergence to ω_{OPTIM}
Operating points	<i>A, B, C, D, MPP</i>	Define stable and unstable regions

6.3. Fundamental Aspects

The results highlight several fundamental aspects relevant to the operation of medium-power wind turbines:

- Wide wind speed variability requires flexible speed regulation:

Effective adjustment of the generator's rotational speed is essential for maximizing energy capture across a broad range of wind speeds. This is consistent with the behavior observed in Figure 7, where the mechanical angular speed follows the optimal value.

- Dual-frequency feasibility, but only one stable solution:

For a given wind speed, two frequency values may satisfy the power and speed requirements. Only one of the possible operating frequencies ensures stable operation, as shown in Figure 5. This distinction is critical for selecting appropriate control parameters.

- Proportional adjustment of electrical parameters:

Achieving optimal performance requires coordinated variation in stator frequency and voltage in proportion to wind speed, ensuring that the turbine consistently operates near the *MPP*.

6.4. Discussion

The findings demonstrate that incorporating a power converter in the stator circuit of the induction generator enables effective control of the turbine's operating point, allowing it to reach maximum power output under varying wind conditions. As shown in Figures 5 and 7, the system maintains stable operation when the stator frequency is properly adjusted.

The results indicate that the selection of the operating frequency must account not only for maximum power extraction but also for stability constraints. For a given wind speed, the steady-state condition may admit multiple operating solutions, while only one ensures stable behavior under wind perturbations.

In practical implementations, this implies that control strategies must be designed to avoid operating regions that, although satisfying steady-state conditions, may lead to unstable behavior under wind disturbances. This is particularly relevant for converter-based wind energy systems, where the control variables directly influence the operating point of the turbine-generator set. The analysis highlights the importance of correct frequency selection under stability constraints, as illustrated in Figure 5, where different operating regimes (stable and unstable) can be clearly identified.

The analysis was conducted using the technical specifications of a 55 kW wind turbine, providing realistic insights into the behavior of medium-scale systems. This choice supports the practical relevance of the obtained results. The study focuses on a wind energy system employing a squirrel-cage induction generator, which inherently offers fewer speed-control options compared to wound-rotor induction generators or permanent-magnet machines.

Despite these limitations, the proposed control strategy—based on stator frequency adjustment and *PI*-based speed tracking—proves effective in maintaining stable operation and ensuring that the turbine operates close to its optimal power point.

Compared to conventional *MPPT* strategies typically based on torque control or rotor-side power converters, the proposed approach emphasizes the role of stator-side frequency control and its impact on system stability. This allows not only tracking of the maximum power point but also explicit identification of stable and unstable operating regimes, which represents an important contribution to the analysis of induction generator-based wind systems. While many existing strategies prioritize energy maximization, the present study emphasizes the identification of stable and unstable operating regions, providing additional insight into system behavior.

The proposed approach is developed within an analytical framework that emphasizes the relationship between turbine aerodynamics, generator characteristics, and control through stator frequency adjustment. While the present study is primarily based on analytical modeling and simulation, it provides a structured foundation for understanding the stability behavior of wind energy systems operating at maximum power point.

While the present study is primarily based on analytical modeling and simulation, it provides a structured foundation for understanding the stability behavior of wind energy systems operating at maximum power point. In comparison with conventional *MPPT* strategies reported in the literature, such as classical *PI*-based control, torque control methods, and more advanced approaches including adaptive control and intelligent techniques (e.g., fuzzy logic and neural networks), the proposed approach focuses explicitly on the stability of the operating point.

While many existing methods primarily aim to maximize energy capture, often assuming a unique optimal operating condition, the present study demonstrates that multiple steady-state solutions may exist for a given wind speed, with different stability properties. This highlights the importance of incorporating stability considerations into control design, beyond mere power optimization.

Therefore, the main contribution of this work lies in the identification and analysis of stability constraints associated with stator-frequency-based control, providing a complementary perspective to existing *MPPT* strategies.

In addition, the obtained results are consistent with previously reported studies on induction generator-based wind energy systems operating under variable wind conditions. In particular, the identified behavior—namely the existence of multiple operating points for a given wind speed and their different stability properties—aligns with established theoretical and modeling results reported in the literature.

Furthermore, the observed relationship between stator frequency, rotational speed, and power characteristics is in agreement with classical models used in maximum power point tracking (*MPPT*) strategies. This consistency provides an indirect validation of the proposed analytical framework, supporting its physical relevance and correctness despite the absence of direct experimental data.

7. Conclusions

This paper analyzed the stability of medium-power wind turbines equipped with squirrel-cage induction generators, regulated through stator-side frequency control using a power electronic converter. The study focused on turbine behavior under significant wind speed variations and demonstrated that the proposed control strategy enables operation over a wide range of rotational speeds. Implementing this approach requires a power converter sized to match the generator's rated power, ensuring effective adjustment of electrical parameters.

To maintain operation at the maximum power point, a dedicated *PI* controller was designed and implemented. By modifying the stator frequency, the controller adjusts the available power reserve of the turbine. The results show that when the operating frequency is reduced, the turbine's aerodynamic power can exceed the generator's electrical capability, causing the rotational speed to rise beyond acceptable limits. This highlights the importance of selecting appropriate frequency values to ensure both optimal energy capture and stable system operation.

Overall, the findings confirm that stator frequency-based control, combined with a properly tuned *PI* regulator, provides an effective method for maximizing power extraction while preserving the stability of medium-power wind turbines equipped with squirrel-cage induction generators.

The analysis reveals that, for a given wind speed and maximum power operating condition, the power balance equation may admit multiple stator frequency solutions. However, only one of these solutions ensures local stability of the operating point; in the analyzed case, this corresponds to the higher stator frequency, while the lower frequency leads to instability under small wind variations. This result highlights the importance of considering stability constraints in addition to maximum power extraction when selecting the operating frequency.

The results provide additional insight into the stability-oriented analysis of stator-side frequency control, showing that, although multiple operating conditions may satisfy the power balance, only specific stator frequency values ensure stable operation. This demonstrates that the stability constraints play a critical role in selecting the operating frequency when designing control strategies for induction generator-based wind energy systems.

Future work will focus on extending the proposed approach by incorporating more advanced stability analysis methods, such as small-signal modeling, eigenvalue analysis, and Lyapunov-based techniques, to provide a more rigorous theoretical validation of system behavior. In addition, experimental or hardware-in-the-loop validation will be considered to further confirm the applicability and robustness of the proposed approach under real operating conditions. Further developments will also address the integration of advanced control design strategies, including optimization-based tuning, model-based approaches, and comparative evaluations with conventional methods, with the aim of enhancing system performance, robustness, and practical applicability.

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Abbreviations

The following abbreviations are used in this manuscript:

<i>EU</i>	European Union
<i>PID</i>	Proportional, Integrator, Derivative
<i>MAS</i>	Mechanical angular speed
<i>WT</i>	Wind turbine
<i>V</i>	Wind speed
<i>PV</i>	Photovoltaic
<i>MPP</i>	Maximum power point
<i>MPPT</i>	Maximum power point tracking
<i>PI</i>	Proportional, Integrator controller
ω	Mechanical angular speed
ω_{OPTIM}	Optimal mechanical angular speed
P_{WT}	Power given by WT relative to the shaft of the electric generator
<i>EG</i>	Electric generator
P_{EG}	Power of the electric generator
<i>U</i>	Stator voltage
U_N	Nominal voltage
<i>f</i>	Stator voltage frequency
<i>J</i>	Equivalent inertia moment
M_{WT}	Moment provided by WT, relative to the EG shaft
M_{EG}	Electromagnetic moment at the EG shaft
<i>t</i>	Time moment
K_1	Proportionality constant
K_2	Integration constant
$A, B, C, D, A^*, B^*, C^*, D^*, P_1, P_2, P_3$	Operating points
β	Angle of the turbine blades' inclination
ρ	Air density at the operational site of the wind turbine
R_p	Radius of the turbine rotor
$C_p(\lambda, \beta)$	Power conversion coefficient
c_1, c_2, c_3, c_4	Constructive constants of the wind turbine

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