

Article

Fault-Tolerant Optimal Consensus Control for Heterogeneous Multi-Agent Systems

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Abstract: This study explores fault-tolerant consensus in leader–following heterogeneous multi-agent systems, focusing on actuator failures in uncrewed aerial vehicles (UAVs) and uncrewed ground vehicles (UGVs). An optimization-based fault-tolerant consensus algorithm is proposed. The algorithm utilizes the Euler–Lagrange formula to ensure system consistency under actuator failures, with the Lyapunov stability theory proving the asymptotic stability of the consistency error. The algorithm is applied to heterogeneous multi-agent systems of UAVs and UGVs to derive optimal fault-tolerant consensus control laws for each vehicle type. Simulation experiments give evidence for the feasibility of the proposed control strategy.

Keywords: uncrewed aerial vehicle; uncrewed ground vehicle; heterogeneous multi-agent system; actuator failures; consensus; Lyapunov stability theory; optimal method



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1. Introduction

Due to rapid advancements in science, technology, and evolving societal needs, researchers have consistently prioritized the collaborative control of multi-agent systems. Especially in recent years, rapid development has been seen. It has achieved a large number of application results in the field of engineering, such as UAV formation [1,2], intelligent city traffic [3], smart grid [4,5], etc. Consistency is the core issue of collaborative control, and corresponding control protocols are designed according to different controlled objects and working environments to achieve the convergence and stability of the controlled system states. Reference [6] proposed a control method based on the bat algorithm, using an improved bat algorithm to find the optimal control gains. It aims to enhance the robot's trajectory tracking accuracy and compares the trajectory tracking accuracy and control energy consumption of two robots. Reference [7] addresses the control problem of a single-link mechanical arm and introduces a practical control method. It proposes a finite-time disturbance observer to estimate external disturbances and ensures that tracking errors converge to a specified bounded set within a finite time. It demonstrates that the closed-loop system is globally finite-time stable. Reference [8] investigates the finite-time consensus problem for a class of general linear leader–follower multi-agent systems using event-triggered mechanisms. A distributed event-triggering strategy based on observers is proposed. Under given conditions, it ensures that the tracking error converges to zero within a finite time.

Multi-agent systems are primarily categorized into homogeneous and heterogeneous types. The consistency inquiry of homogeneous multi-agent systems has achieved fruitful results [9–12]. During actual operation or use, most systems exhibit heterogeneous characteristics. Heterogeneous multi-agent systems are structurally constrained and mainly

unable to achieve complete state consistency. Based on this, Scholars both domestically and internationally are increasingly concentrating on the study of consensus in heterogeneous multi-agent systems [13–19]. In conjunction with the increasing working time of intelligent agents and the complex and changeable actual environment, individual intelligent agents will inevitably encounter failures, and multi-agent systems cannot solve this problem through their attributes. Therefore, ensuring multi-agent systems achieve consistency during failures has become a subject of great concern. Reference [20] proposed an approach utilizing inner and outer loops to accomplish the control objective of multiple uncrewed aerial vehicles following a leader aircraft in the presence of actuator failures. The outer loop is responsible for designing position state control laws to uphold the formation flight, while the inner loop addresses actuator effects through adaptive control laws for UAV attitudes. Reference [21] implemented a distributed sliding mode observer (SMO) for each trailing UAV, estimating necessary reference values through information exchange among neighboring UAVs. Adaptive neural fault-tolerant control (FTC) units were subsequently devised for the UAV to converge toward the benchmark value produced by the distributed SMO in case of actuator failures. Reference [22] examined the coordination of drones in formation under conditions involving leader and actuator failures. The study applied boundary layer theory and devised a control protocol featuring adaptive mechanisms for compensating actuator deficiencies. Reference [23] devised a formation control law with adaptive mechanisms for multi-octocopter drone models, taking into account uncertainties and actuator failures. Reference [24] proposed a new adaptive backstepping method related to command filters to address model uncertainties and input saturation problems for multiple UAVs under input saturation, actuator failures, and external disturbances, designing a robust controller. The aforementioned studies focus exclusively on homogeneous multi-agent systems, with limited research outcomes on achieving fault-tolerant consistency in heterogeneous multi-agent systems. Reference [25] investigated a collaborative fault-tolerant output regulation control approach for linear heterogeneous multi-agent systems operating under directed network topologies. The objective was to ensure system stability despite actuator failures. Reference [26] examines fault-tolerant consistency in heterogeneous multi-agent systems. The study introduces a sliding mode observer aimed at achieving consistent system control in the presence of uncertainties and actuator faults. While both references explored fault-tolerant control in heterogeneous multi-agent systems, they primarily discussed generic models rather than specific physical implementations.

Building on the preceding analysis, this paper aims to investigate the consistency issues in leader-following heterogeneous UAV-UGV systems featuring faulty followers. Specifically, this paper designs a fault-tolerant consistency controller for leader-following heterogeneous multi-agent systems encountering partial actuator failures. The contributions of this study are outlined below:

Firstly, this paper introduces dynamic models for intelligent agent systems and formulates them using Kronecker products in state space. It then constructs the Laplacian matrix of the communication topology.

The paper proposes a fault-tolerant consistency controller for leader-following multi-agent systems in the presence of actuator failures, validated using Lyapunov stability theory. The algorithm shows robust fault tolerance to constant and time-varying actuator faults without needing to solve the Hamilton–Jacobi–Bellman equation.

Performance index functions are designed for each UAV and UGV, aiming to minimize the performance index of each UAV and UGV pair to achieve overall minimization for the entire heterogeneous multi-agent system. The fault-tolerant consistency controller obtained through this optimization process is considered the optimal controller, ensuring leader-following consistency under conditions of actuator failures in both UAVs and UGVs.

The remaining sections of this study are organized as follows. Necessary background and system models related to the problem of fault-tolerant consensus in heterogeneous multi-agent leader-following systems are provided in Section 2. Theorem designs that address the problem of designing control protocols for UAVs and UGVs are introduced in

Section 3. Section 4 presents numerical simulations of multiple UAVs and UGVs, comparing them with existing algorithms. Section 5 summarizes the whole work.

2. Preliminaries

This section primarily covers fundamental concepts related to UAVs and UGVs, discussing the application of graph theory to delineate system interrelationships and presenting the state-space equations for UAV and UGV systems.

2.1. Graph Theory

Based on the relevant theories of graph theory, we describe the communication topology of multi-agent systems. The unoriented weighted graph $G = (V, E, A)$ comprises $k + 1$ vertices, $V = (v_0, v_1, v_2, \dots, v_k)$ representing the complete set of vertices. Each vertex corresponds to an agent, which v_0 denotes the leader. Let $E = \{e_{ij} = (v_i, v_j)\}$ denote the edges between vertices, with $e_{ij} = (v_i, v_j)$ representing the edge from vertex v_i to vertex v_j . The connection between two vertices through an edge indicates the existence of information exchange between them. If bidirectional communication is allowed, the graph is undirected, or directed. $A = [a_{ij}]_{n \times n}$ stands for the adjacency matrix describing relationships between followers, where the a_{ij} is the edge $e_{ij} = (v_i, v_j)$'s weight. If there is an edge $e_{ij} \in E$ between vertices i and j , then $a_{ij} > 0$; otherwise, $a_{ij} = 0$. $\mathcal{N}_i$ denotes the neighbor set of the i -th agent, represented as $\mathcal{N}_i = \{V_j \in \mathcal{V}, |e_{ji} \in E\}, i = 1, 2, \dots, k$.

In an unoriented graph, the degree of a node denotes its number of neighbors, specifically the count of connecting edges per node. Let $D = \text{diag}\{d_1, d_2, \dots, d_k\}$ denote the degree matrix of the unoriented graph, defined as $d_i = \sum_{j=1}^n a_{ij}$. The Laplacian matrix of the graph is defined as $L = D - A$, where A is the adjacency matrix. $\zeta = \text{diag}(a_{01}, a_{02}, \dots, a_{0k})$, and it represents the Laplacian matrix, which describes the communication relationships between leaders and followers.

2.2. UGV Dynamics Model

According to Reference [27], a single UGV model be simplified as Equation (1):

$$\begin{cases} \dot{p}_{gi} = v_{gi} \\ \dot{v}_{gi} = u_{gi} \end{cases} \quad (1)$$

where $p_{gi} = [p_{gi}^x, p_{gi}^y]^T$ denotes the position in XY space, $v_{gi} = [v_{gi}^x, v_{gi}^y]^T$ denotes velocity, which corresponds to the speed of the UGV moving along the direction of p_{gi} , and $u_{gi} = [u_{gi}^x, u_{gi}^y]^T$ signifies the input of the agent i . For m UGVs, the formula is transformed into the following states:

$$\dot{x}_{Gi} = A_G x_{Gi} + B_G u_{Gi} \quad (2)$$

where $x_{Gi} = (p_i, v_i)^T$, $p_i = (p_i^x, p_i^y)$, $v_i = (v_i^x, v_i^y)$, $u_{Gi} = (u_i^x, u_i^y)$, $i = 1, 2, \dots, m$.

$$A_G = \begin{bmatrix} 0 & 1 \\ 0 & 0 \end{bmatrix} \otimes I_2, B_G = \begin{bmatrix} 0 \\ 1 \end{bmatrix} \otimes I_2.$$

A_G, B_G , respectively, represent the state-space matrix and input-state matrix of the UGVs. $\otimes$ denotes the Kronecker product, indicating that the multi-UGV system is a linear system. Considering the failure of actuators in UGV, $u_{Gi}^f = (u_{ix}^f, u_{iy}^f)$ represents the input after the actuator failure. The specific expression u_{Gi}^f is as follows:

$$u_{Gi}^f = (I_2 - \mathcal{P}_{Gi})u_{Gi}, \quad (3)$$

where the equation $\mathcal{P}_{Gi} = \text{diag}(\rho_{ix}, \rho_{iy}) \in R^2$ is central to our analysis. This paper primarily examines partial actuator failures within a multi-following uncrewed ground vehicle system, in which ρ_{ix}, ρ_{iy} does not uniformly equal one across all instances. The dynamic model of each of the m UGVs in the system can be represented as follows:

$$\dot{x}_{Gi} = A_G x_i + B_G u_{Gi}^f, \quad i = 1, 2, \dots, m \quad (4)$$

For the m UGVs actuator failure model described by Equation (4), when the multi-UGV system achieves consensus, it means that all the UGV's states satisfy the following equation:

$$\lim_{t \rightarrow \infty} \|p_i(t) - p_0(t)\| = 0, \quad \lim_{t \rightarrow \infty} \|v_i(t) - v_0(t)\| = 0 \quad (5)$$

2.3. UAV Dynamics Model

According to reference [27], a single UAV model be defined as Equation (6):

$$\begin{aligned} \ddot{p}^x &= g\theta \\ \ddot{p}^y &= -g\phi \\ \ddot{p}^z &= f_z/m - g \\ g\ddot{\phi} &= M_\phi/I_x \\ g\ddot{\theta} &= M_\theta/I_y \\ \ddot{\psi} &= M_\psi/I_z \end{aligned} \quad (6)$$

where p^x, p^y, p^z represents the UAV's positions in the X, Y, Z axes; ϕ, θ , and ψ corresponds to the rotation angle of the UAV along X, Y, and Z axes, respectively. f_z denotes the lift force in the Z axes; $M_\phi/I_x, M_\theta/I_y, M_\psi/I_z$ represents the control input for rotating the UAV around the three coordinate axes.

If there is one leader UAV and $n - m$ follower UAVs, then Equation (6) above can be transformed into a state equation:

$$\begin{aligned} \dot{x}_{A0} &= A_A x_{A0} \\ \dot{x}_{Ai} &= A_A x_{Ai} + B_A u_{Ai} \end{aligned} \quad (7)$$

where $x_{Ai} = (p_i, v_i, \Omega_i, \dot{\Omega}_i)^T$, $p_i = (p_i^x, p_i^y, p_i^z)^T$, $v_i = (v_i^x, v_i^y, v_i^z)^T$, $u_{Ai} = (u_i^x, u_i^y, u_i^z)^T$.

$$\Omega_i = (g\theta_i, -g\phi_i, \psi)^T, \dot{\Omega}_i = (g\dot{\theta}_i, -g\dot{\phi}_i, \dot{\psi})^T, \quad i = m, m+1, \dots, n$$

$x_{A0} = (p_0, v_0, \Omega_0, \dot{\Omega}_0)^T$, $p_0 = (p_0^x, p_0^y, p_0^z)^T$, $v_0 = (v_0^x, v_0^y, v_0^z)^T$ represents the leader UAV's state.

$$A_A = \begin{bmatrix} 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \\ 0 & 0 & 0 & 0 \end{bmatrix} \otimes I_3, \quad B_A = \begin{bmatrix} 0 \\ 0 \\ 0 \\ 1 \end{bmatrix} \otimes I_3.$$

A_A, B_A , respectively, represent the state-space matrix and input-state matrix of the UAVs. $\otimes$ denotes the Kronecker product, indicating that the multi-UAV system is a linear system. Considering the failure of actuators in UAV, $u_{Ai}^f = (u_{ix}^f, u_{iy}^f, u_{iz}^f)$ represents the input after the actuator failure. The specific expression u_{Ai}^f is as follows:

$$u_{Ai}^f = (I_3 - \mathcal{P}_{Ai})u_{Ai}, \quad (8)$$

where the equation $\mathcal{P}_{Ai} = \text{diag}(\rho_{ix}, \rho_{iy}, \rho_{iz}) \in R^3$ is central to our analysis. This paper primarily examines partial actuator failures within a multi-following uncrewed aerial vehicle system, in which $\rho_{ix}, \rho_{iy}, \rho_{iz}$ does not uniformly equal one across all instances. The dynamic model of each of the $n - m$ UAVs in the system can be represented as follows:

$$\dot{x}_{Ai} = A_A x_{Ai} + B_A u_{Ai}^f \quad (9)$$

For the $n - m$ UAVs actuator failure model described by Equation (9), when the multi-UAV system achieves consensus, this implies that all states of the UAVs satisfy the following equation:

$$\lim_{t \rightarrow \infty} \|X_{Ai}(t) - X_{A0}(t)\| = 0 \quad (10)$$

2.4. Heterogeneous Multi-Agent System

By establishing fault models for UAVs and UGVs using Equations (4) and (9), the expression of the state variable for a heterogeneous multi-agent system can be constructed by merging state variables. The state variable model for heterogeneous systems is defined as follows:

$$\begin{bmatrix} \dot{X}_G \\ \dot{X}_A \end{bmatrix} = \begin{bmatrix} A_G & 0 \\ 0 & A_A \end{bmatrix} \begin{bmatrix} X_G \\ X_A \end{bmatrix} + \begin{bmatrix} B_G & 0 \\ 0 & B_A \end{bmatrix} \begin{bmatrix} U_G \\ U_A \end{bmatrix} \quad (11)$$

$$\dot{X} = AX + BU$$

where $X = (X_G^T, X_A^T)^T$, $A = \begin{pmatrix} A_G & 0 \\ 0 & A_A \end{pmatrix}$, $B = \begin{pmatrix} B_G & 0 \\ 0 & B_A \end{pmatrix}$, $X_G = (x_{G1}, x_{G2} \dots x_{Gm})^T$.

$$X_A = (x_{A(m+1)}, x_{A(m+2)} \dots x_{An})^T, \text{ and } U = (U_G^T, U_A^T)^T,$$

$$U_G = (u_{G1}^f, u_{G2}^f \dots u_{Gm}^f)^T, U_A = (u_{A(m+1)}^f, u_{A(m+2)}^f \dots u_{An}^f)^T.$$

To better describe the communication relationship between heterogeneous systems, a simple linear transformation needs to be applied to the Laplacian matrix of the system. The system consists of m UGVs and $n - m$ UAVs, with a total of n agents. L is the corresponding Laplacian matrix, is shown as follows:

$$L = \begin{bmatrix} L_{AA} & L_{AG} \\ L_{GA} & L_{GG} \end{bmatrix}.$$

where L_{AG}, L_{GA} represents information between heterogeneous agent systems. Regarding the actuator fault model of n heterogeneous agent systems described by Equation (11), when the heterogeneous multi-agent system reaches consensus, it implies that all agent states satisfy the following equation:

$$\begin{aligned} \lim_{t \rightarrow \infty} \|p_i(t) - p_0(t)\| &= 0, \lim_{t \rightarrow \infty} \|v_i(t) - v_0(t)\| = 0 \\ \lim_{t \rightarrow \infty} \|\Omega_i(t) - \Omega_0(t)\| &= 0, i = m+1, m+2, \dots, n \\ \lim_{t \rightarrow \infty} \|\dot{\Omega}_i - \dot{\Omega}_0\| &= 0, i = m+1, m+2, \dots, n \end{aligned} \quad (12)$$

Assumption 1. The communication graph between agent systems is firmly connected, and at least one follower is linked to a leader.

Assumption 2. During the operation of the leader–follower multi-agent system, the leader agent will not experience failures.

3. Design and Analysis of Fault-Tolerant Consensus Controllers

This section addresses the problem described in Equation (12) by designing and analyzing fault-tolerant consensus controllers of heterogeneous multi-agent fault models. The theoretical effectiveness of the proposed algorithm is subsequently demonstrated.

The following describes the performance index parameters for each follower agent:

$$J_i = \int_0^C \left[\left(u_i^f(t) \right)^T H u_i^f(t) + \sum_{j \in \mathcal{N}_i} (a_{ij}(x_i - x_j) + a_{0i}(x_i - x_0))^T Q \sum_{j \in \mathcal{N}_i} a_{ij}(x_i - x_j) + a_{0i}(x_i - x_0) \right] dt \quad (13)$$

where $i = 1, 2, \dots, n$, C represents a constant greater than zero, indicating the integral's upper bound. $\left(u_i^f(t) \right)^T$ represents the transpose operation of a vector. H and Q are both positive definite symmetric matrices.

Theorem 1. Consider a leader–follower multi-agent system:

$$\begin{aligned} \dot{x}_0 &= Ax_0 \\ \dot{x}_i &= Ax_i + Bu_i^f \end{aligned} \quad i = 1, 2, \dots, n \quad (14)$$

Assume that the leader–follower multi-agent system (14) satisfies Assumptions 1 and 2. For the leader–follower multi-agent system with actuator faults described by Equation (14), the optimal controller $u_i^*(t)$, which minimizes the performance index parameters (13), can be represented:

$$u_i^*(t) = -\frac{|\mathcal{N}_i|}{2} (I - \mathcal{P}_i)^{-1} H^{-1} B^T \eta_i^*(t) \quad (15)$$

where $|\mathcal{N}_i|$ denotes the number of neighbor agents in the i -th agent's neighbor set. H^{-1} represents the positive definite symmetric matrix's inverse matrix in the performance index parameters. Under this optimal controller $u_i^*(t)$, the consensus error of the systems (14) can asymptotically converge to zero.

Proof of Theorem 1. Define the consensus tracking error of the i -th agent, shown as follows:

$$e_i(t) = \sum_{j \in \mathcal{N}_i} a_{ij}(x_i - x_j) + a_{0i}(x_i - x_0), \quad i = 1, 2, \dots, n. \quad (16)$$

By utilizing the dynamic equation of the system (14), the time derivative of Equation (16) will be obtained:

$$\dot{e}_i(t) = Ae_i(t) + \sum_{j \in \mathcal{N}_i} a_{ij}B(u_i^f(t) - u_j^f(t)) + a_{0i}Bu_i^f(t) \quad (17)$$

Furthermore, we assume that the controllers of all agents in $\mathcal{N}_i$ of the i -th agents are mutually independent.

Define the performance index function for the consensus error system described by Equation (16) as follows:

$$J_i = \int_0^T \left[\left(u_i^f(t) \right)^T H u_i^f(t) + e_i^T(t) Q e_i(t) \right] dt. \quad (18)$$

Define the Hamiltonian parameters:

$$\begin{aligned} H_i(t, e_i, u_i^f, \eta_i) &= e_i^T(t) Q e_i(t) + \left(u_i^f(t) \right)^T H(t) u_i^f(t) \\ &\quad + \eta_i^T(t) \left(Ae_i(t) + \sum_{j=1}^n a_{ij}B(u_i^f(t) - u_j^f(t)) + a_{0i}Bu_i^f(t) \right). \end{aligned} \quad (19)$$

where $\lambda_i \in R^n$ is an auxiliary variable. Performing some mathematical transformations on the Hamiltonian function represented by Equation (19), we can obtain the following expression:

$$\begin{aligned}
 H_i(t, e_i(t), u_i^f(t), \eta_i(t)) &= e_i^T(t) Q e_i(t) + \left(u_i^f(t)\right)^T H u_i^f(t) \\
 &\quad + \eta_i^T(t) \left(A e_i(t) + \sum_{j \in \mathcal{N}_i} (B u_i^f(t) - B u_j^f(t))\right) \\
 &= \sum_{j \in \mathcal{N}_i} x_i^T(t) Q x_i(t) - 2 \sum_{j \in \mathcal{N}_i} x_i^T(t) Q x_j(t) + \left(u_i^f(t)\right)^T H u_i^f(t) \\
 &\quad + \sum_{j \in \mathcal{N}_i} x_j^T(t) Q x_j(t) \\
 &\quad + \eta_i^T(t) \left(A e_i(t) + \sum_{i=1}^N a_{ij} B (u_i^f(t) - u_j^f(t)) + a_{0i} B u_i^f(t)\right).
 \end{aligned} \tag{20}$$

By computing the partial derivatives of $H_i(t, e_i(t), u_i^f(t), \eta_i(t))$ concerning $u_i^f(t)$ and $\eta_i(t)$, respectively, we obtain:

$$\begin{aligned}
 \frac{\partial H_i(t, e_i(t), u_i^f(t), \eta_i(t))}{\partial u_i^f(t)} &= 2H(I_k - \mathcal{P}_i)u_i(t) + (a_{0i} + |\mathcal{N}_i|)B^T \eta_i(t) \\
 \frac{\partial H_i(t, e_i(t), u_i^f(t), \eta_i(t))}{\partial e_i(t)} &= \sum_{j \in \mathcal{N}_i} 2Q(x_i(t) - x_j(t) + a_{0i}(x_i(t) - x_0(t))) + A^T \eta_i(t).
 \end{aligned} \tag{21}$$

Therefore, the optimal fault-tolerant controller is obtained:

$$\begin{cases} u_i^*(t) = -\frac{|\mathcal{N}_i| + a_{0i}}{2} (I - \mathcal{P}_i)^{-1} H^{-1} B^T \eta_i^*(t) \\ \eta_i^*(t) = -\sum_{j \in \mathcal{N}_i} 2Q(x_i(t) - x_j(t) + a_{0i}(x_i(t) - x_0(t))) - A^T \eta_i(t) \end{cases}, i = 1, 2, \dots, n. \tag{22}$$

Next, the primary analysis focuses on whether the controller represented by Equation (22) can achieve consensus for Equation (14) under actuator faults. With the principles of optimal control theory, the controller Equation (22) satisfies the following:

$$H_i(t, e_i^*(t), u_i^*(t), \eta_i^*(t)) = 0 \tag{23}$$

where $e_i^*(t), \eta_i^*(t)$ stand for the optimal consensus error and optimal coefficient of the i the agent under the optimal fault-tolerant control $u_i^*(t)$. For this purpose, the Lyapunov function for the defined Equation (14) is as follows:

$$V_i(e_i^*(t)) = \frac{1}{2} \int_t^\infty [(u_i^*(t))^T H u_i^*(t) + (e_i^*(t))^T Q e_i^*(t)] dt, i = 1, 2, \dots, n \tag{24}$$

where $H \in R^{m \times m}, Q \in R^{n \times n}$ are both symmetric positive definite matrices. According to the properties of positive definite matrices, Equation (24) illustrates a positive definite function.

Based on reference [28], the optimal Hamiltonian function $H_i(t, e_i^*(t), u_i^*(t), \eta_i^*(t))$ represented by Equation (19) can be rewritten in the following form:

$$\begin{aligned}
 H_i(t, e_i^*(t), u_i^*(t), \eta_i^*(t)) &= (e_i^*(t))^T Q e_i^*(t) + (u_i^*(t))^T H u_i^*(t) \\
 &\quad + \frac{\partial V_i^T(e_i^*(t))}{\partial e_i^*(t)} \left(A e_i(t) + \sum_{i=1}^n a_{ij} B (u_i^*(t) - u_j^*(t)) + a_{0i} B u_i^*(t)\right)
 \end{aligned} \tag{25}$$

Therefore, Equations (23) and (25) will be transformed into the following:

$$\begin{aligned} & \frac{\partial V_i^T(e_i^*(t))}{\partial e_i^*(t)} \left(Ae_i(t) + \sum_{i=1}^n a_{ij}B(u_i^*(t) - u_j^*(t)) + a_{0i}Bu_i^*(t) \right) \\ & = -((e_i^*(t))^T Q e_i^*(t) + (u_i^*(t))^T H u_i^*(t)). \end{aligned} \quad (26)$$

Furthermore, by differentiating the Lyapunov function defined by Equation (24), we obtain the following:

$$\dot{V}_i(e_i^*(t)) = \frac{\partial V_i^T(e_i^*(t))}{\partial e_i^*(t)} \left(Ae_i(t) + \sum_{i=1}^n a_{ij}B(u_i^*(t) - u_j^*(t)) + a_{0i}Bu_i^*(t) \right) \quad (27)$$

According to Equation (26),

$$\dot{V}_i(e_i^*(t)) = -((e_i^*(t))^T Q e_i^*(t) + (u_i^*(t))^T H u_i^*(t)). \quad (28)$$

Since both matrix Q and matrix H are positive definite symmetric matrices, $\dot{V}_i(e_i^*(t))$ is a negative definite function. According to the Lyapunov stability theory, $e_i^*(t)$ will asymptotically converge to zero. $\square$

From the performance index functions, it can be seen that if J_i reaches a minimum value, then the state error between the agents in the i -th agent's neighbor set $\mathcal{N}_i$ and the i -th agent also reaches a minimum value. Furthermore, according to Assumption 1, it can be obtained that if all J_i reach minimum values, the entire multi-agent system's state can achieve consensus. Therefore, from Theorem 1, it can be concluded that the controller u_i^* can achieve consensus on the state of the system (14).

According to Theorem 1, performance index functions are defined for each UAV and UGV as follows:

$$\begin{aligned} J_i &= \int_0^\infty [(u_{Gi}^f(t))^T H_G u_{Gi}^f(t) + e_{Gi}^T Q_G e_{Gi}] dt, \\ W_i &= \int_0^\infty [(u_{Ai}^f(t))^T H_A u_{Ai}^f(t) + e_{Ai}^T Q_A e_{Ai}] dt, \end{aligned} \quad (29)$$

where when $i = 1, 2, \dots, m$ is used, it represents UGV, and when $i = m + 1, m + 2, m + 3, \dots, n$ is used, it represents UAV. H_G, Q_G, H_A, Q_A are both positive definite symmetric matrices.

Due to the different dimensions of the state vectors of UAVs and UGVs, weight coefficient matrices are designed as follows:

$$\begin{aligned} Q_G &= 60 * I_4, H_G = 5 * I_2 \\ Q_A &= 60 * I_{12}, H_A = 5 * I_3 \end{aligned}$$

According to Assumption 1, it can be inferred that if all J_i and W_i reach minimum values, the entire leader-following multi-agent system's state can achieve consensus. Therefore, from Theorem 1, it can be concluded that the controller u_i^* can achieve consensus on the multi-agent system's state. Obtain the optimal fault-tolerant consensus controllers for each UAV and UGV, respectively:

For UGV:

$$\begin{cases} u_{Gi}^*(t) = -\frac{|\mathcal{N}_i| + a_{0i}}{2} (I_2 - \mathcal{P}_{Gi})^{-1} H_G^{-1} B_G^T \eta_i^*(t), & i = 1, 2, \dots, m. \\ \eta_i^*(t) = -Q_G e_G - A_G^T \eta_i(t) \end{cases} \quad (30)$$

UGV control law:

$$u_{Gi}^*(t) = -\frac{|\mathcal{N}_i| + a_{0i}}{2}(I_2 - \mathcal{P}_{Gi})^{-1}H_G^{-1}B_G^T(x_{Gi}(t) - x_{A0}(t)) \quad (31)$$

For UAV:

$$\begin{cases} u_{Ai}^*(t) = -\frac{|\mathcal{N}_i| + a_{0i}}{2}(I_3 - \mathcal{P}_{Ai})^{-1}H_A^{-1}B_A^T\eta_i^*(t) \\ \eta_i^*(t) = -Q_A e_A - A_A^T \eta_i(t) \end{cases} \quad i = m+1, \dots, n \quad (32)$$

UAV control law:

$$u_{Ai}^*(t) = -\frac{|\mathcal{N}_i| + a_{0i}}{2}(I_3 - \mathcal{P}_{Ai})^{-1}H_A^{-1}B_A^T(x_{Ai}(t) - x_{A0}(t)) \quad (33)$$

For any two agents i and j in the leader-following multi-agent system, there are two cases for an agent j , (1) $j \in \mathcal{N}_i$, in which case, according to the above analysis, $e_i^*(t)$ asymptotically converges to zero, thus indicating that agents i 's states and agents j 's states tend to be consistent; (2) $j \notin \mathcal{N}_i$, according to Assumption 1, it is known that there is a path between any two agents, and by the transitivity of states, the states of agents i and j tend to be consistent. It can be inferred that the consistency error of the system (11) under actuator failure can asymptotically converge to zero at this time.

4. Simulations

In this section, simulations are performed to validate the effectiveness of the proposed algorithm (31) and (33). The experiment involves a leader UAV, three follower UAVs, and three UGVs forming the system. MATLAB 2017a is used as the experimental platform.

The Laplacian matrix corresponding to the undirected communication topology is shown below:

$$L = \begin{bmatrix} 3 & -1 & -1 & 0 & 0 & -1 \\ -1 & 3 & -1 & 0 & -1 & 0 \\ -1 & -1 & 3 & -1 & 0 & 0 \\ \underbrace{0 & 0 & -1}_{L_{AA}} & \underbrace{3 & -1 & -1}_{L_{AG}} \\ 0 & -1 & 0 & -1 & 3 & -1 \\ \underbrace{-1 & 0 & 0}_{L_{GA}} & \underbrace{-1 & -1 & 3}_{L_{GG}} \end{bmatrix} \quad \zeta = \begin{bmatrix} 1 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 \end{bmatrix}$$

Each UAV has a 12-dimensional state, while the state vector of the UGV is 4-dimensional. The correlation coefficient matrix of the system (11) is as previously designed.

The system primarily considers the partial failure of actuators. Therefore, all followers' actuator failure coefficients must be set between 0 and 1 in the simulation. This experiment finds the following failure coefficient scenarios.

$$\mathcal{P}_{A1} = \begin{bmatrix} 0.5 & 0 & 0 \\ 0 & 0.3 & 0 \\ 0 & 0 & 0.6 \end{bmatrix}, \mathcal{P}_{A3} = \begin{bmatrix} 0.5 \cos t & 0 & 0 \\ 0 & 0.8 & 0 \\ 0 & 0 & 0.2 \end{bmatrix}, \mathcal{P}_{G1} = \begin{bmatrix} 0.1 & 0 \\ 0 & 0.8 \sin t \end{bmatrix}$$

According to the above coefficient matrix and failure coefficient design, MATLAB simulation is employed to verify the control algorithm (31) and algorithm (33) proposed for the heterogeneous multi-agent system.

To highlight the superior convergence speed of the proposed algorithm, this study compares it with the consensus algorithm for heterogeneous multi-agent systems described in reference [29], under typical initial conditions. Initial states are randomly set between 0 and 10.

Initial states are as follows: UAV0's position is (8.14, 9.05, 1.26) m, with a velocity of (9.13, 6.32, 0.97) m/s and attitude angles of (0,0,0) $^{\circ}$ with angular velocities of (0,0,0) $^{\circ}$ /s; UAV1's position is (2.78, 5.46, 9.57) m, with a velocity of (9.64, 1.57, 9.7) m/s and attitude angles of (0,0,0) $^{\circ}$ with angular velocities of (0,0,0) $^{\circ}$ /s; UAV2's position is (9.57, 4.85, 8) m, with a velocity of (1.41, 4.21, 9.15) m/s and attitude angles of (0,0,0) $^{\circ}$ with angular velocities of (0,0,0) $^{\circ}$ /s; UAV3's position is (7.92, 9.59, 6.55) m, with a velocity of (0.35, 8.49, 9.33) m/s and attitude angles of (0,0,0) $^{\circ}$ with angular velocities of (0,0,0) $^{\circ}$ /s; UGV1's position is (6.78, 7.57) m, with a velocity of (7.43, 3.92) m/s; UGV2's position is (6.55, 1.71) m, with a velocity of (7.06, 1.31) m/s; UGV3's position is (2.76, 0.46) m, with a velocity of (0.97, 8.23) m/s.

The initial states of the agents in reference [28] are as follows: UAV1's position is (6.94, 3.17, 50) m, with a velocity of (0.34, 4.38, 1.31) m/s and attitude angles of (0,0,0) $^{\circ}$ with angular velocities of (0,0,0) $^{\circ}$ /s; UAV2's position is (7.65, 7.95, 50) m, with a velocity of (4.89, 4.45, -2) m/s and attitude angles of (0,0,0) $^{\circ}$ with angular velocities of (0,0,0) $^{\circ}$ /s; UAV3's position is (7.09, 7.54, 50) m, with a velocity of (6.79, 6.55, -1) m/s and attitude angles of (0,0,0) $^{\circ}$ with angular velocities of (0,0,0) $^{\circ}$ /s; UGV1's position is (1.19, 4.98) m with a velocity of (9.59, 2.55) m/s; UGV2's position is (5.85, 2.23) m with a velocity of (7.53, 2.55) m/s.

The parameters are $\alpha = 0.1$, $\beta = 0.8$, $\gamma_1 = 4.0$, $\gamma_2 = 1.5$; $g_1 = 0.1$, $g_2 = 0.8$.

Utilizing the algorithms presented in Equations (31) and (33) and comparing them with those from Reference [29], simulations of the UAV and UGV systems are depicted in Figures 1–12. The comparison demonstrates that both protocols facilitate consensus among UAVs and UGVs.

Figures 1 and 2 illustrate that the methods proposed in (31) and (33) for addressing leader–following consistency outperform the approach presented in reference [29], demonstrating superior performance. Figure 1 illustrates the stabilization of the position consistency error in the X-direction between the UAV and UGV systems when using the optimal fault-tolerant consistency protocol $t = 10$ s. Figure 2 shows the position stabilization between the UAV and UGV systems in the X-direction. $35 \leq t \leq 45$ when employing the consistency protocol from reference [29].

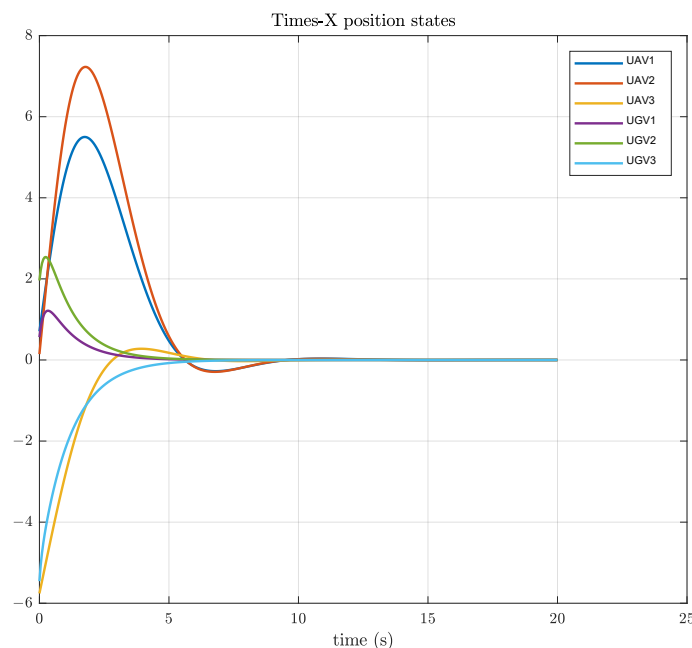


Figure 1. Consistency error in the X-direction position between the following UAV, UGV, and the leader.

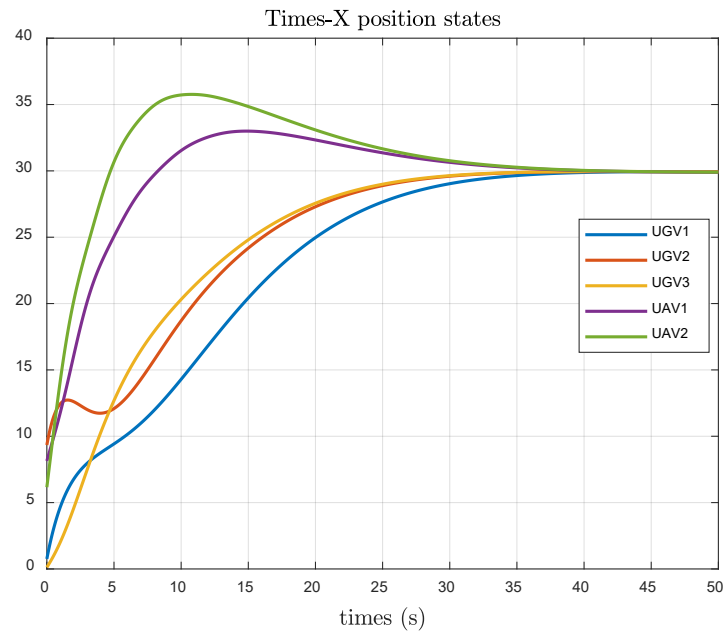


Figure 2. The position variables of UAV and UGV in the X-direction are in Reference [29].

Figure 3 shows that under the optimal fault-tolerant consistency protocol, the UAV and UGV systems stabilize regarding position consistency error in the Y-direction between $10 \leq t \leq 15$. Figure 4 demonstrates that using the consistency protocol proposed in Reference [29], the UAV and UGV systems stabilize regarding the position in the Y-direction $40 \leq t \leq 45$.

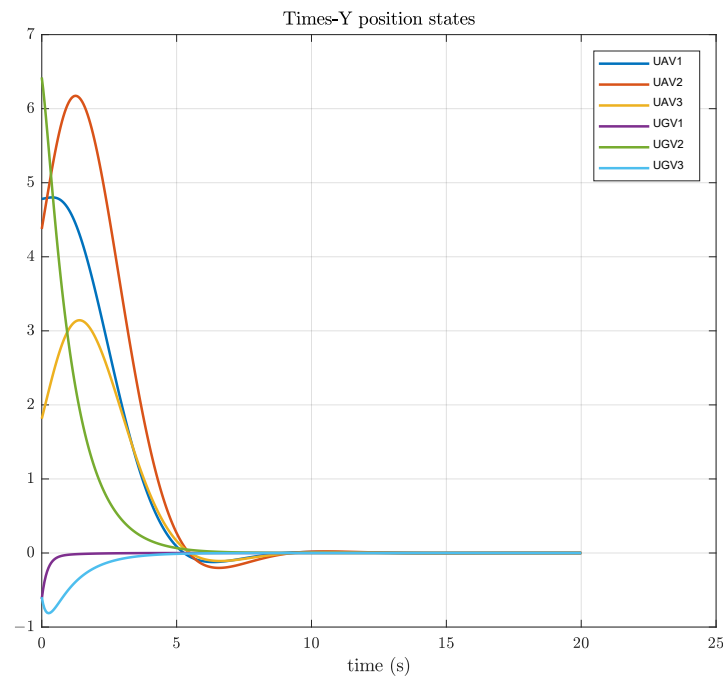


Figure 3. Consistency error in the Y-direction position between the following UAV, UGV, and the leader.

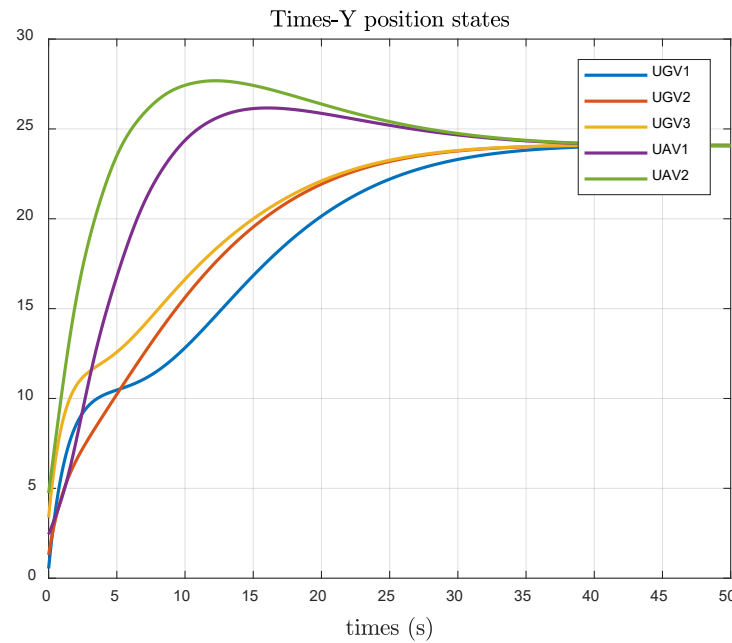


Figure 4. The position variables of UAVs and UGVs in the Y-direction are in Reference [29].

Figure 5 illustrates the stabilization of position consistency error in the Z-direction for the UAV system at $t = 10$ s under the optimal fault-tolerant consistency algorithm. The consistency algorithm presented in reference [29] is designed only for the UAV and UGV systems in the XY plane, thus not considering the position state in the Z-direction.

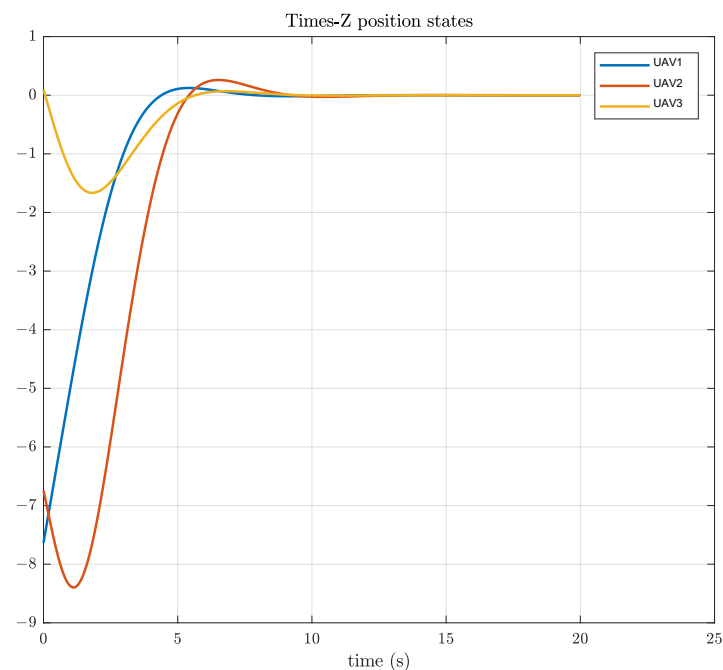


Figure 5. Consistency error in the Z-direction position between the following UAV and the leader.

Figure 6 illustrates that the UAV and UGV systems achieve stable velocity consistency errors in the X-direction $t = 10$ s under the optimal fault-tolerant consistency algorithm. Figure 7 demonstrates that using the consistency control algorithm from reference [29], the UAV and UGV systems achieve stable velocity states in the X-direction between $40 \leq t \leq 45$.

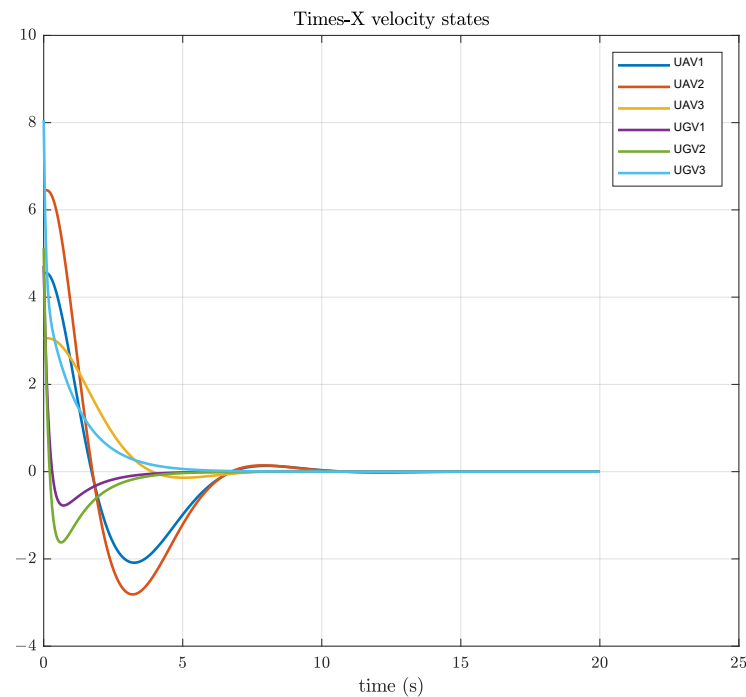


Figure 6. Consistency error in velocity along the X-direction between the following UAV, UGV, and the leader.

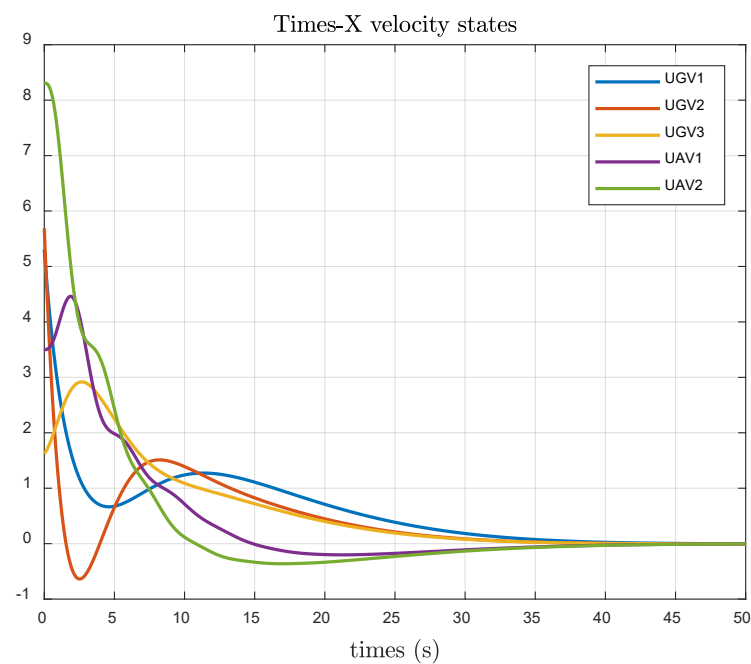


Figure 7. The velocity variables of UAV and UGV in the X-direction are in Reference [29].

Figure 8 illustrates that the UAV and UGV systems achieve stable velocity consistency errors in the Y-direction $t = 10$ s under the optimal fault-tolerant consistency algorithm. Figure 9 shows that using the consistency control algorithm from reference [29], the UAV and UGV systems achieve stable velocity states in the Y-direction $40 \leq t \leq 45$.

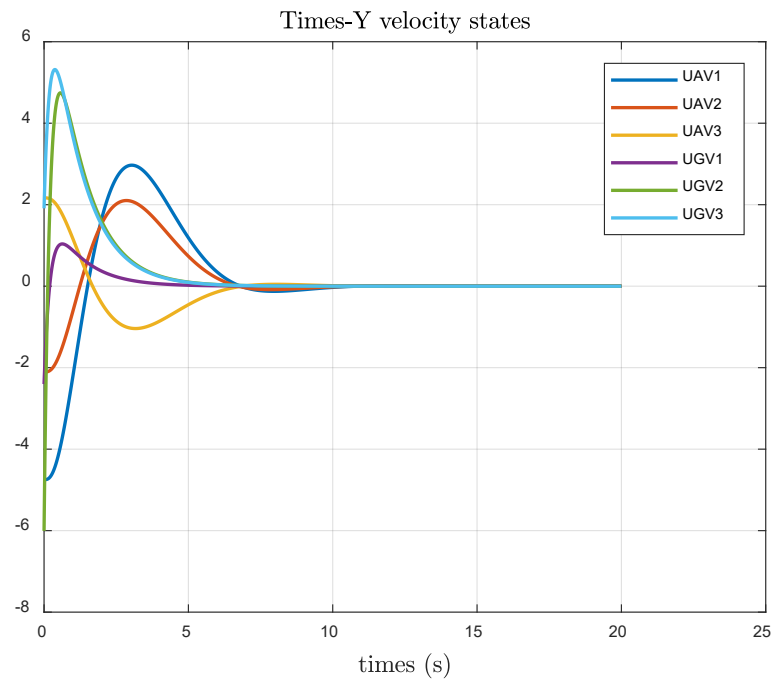


Figure 8. Consistency error in velocity along the Y-direction between the following UAV, UGV, and the leader.

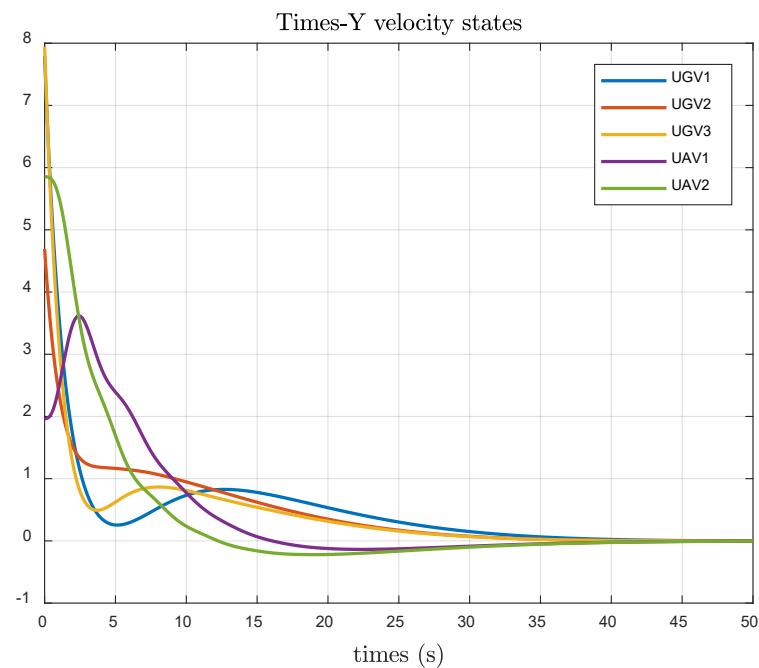


Figure 9. The velocity variables of UAV and UGV in the Y-direction are in Reference [29].

Figure 10 displays the stabilization of position consistency error in the Z-direction for the UAV system $t = 10$ s under the optimal fault-tolerant consistency algorithm. The consistency algorithm presented in Reference [29] is designed only for the UAV and UGV systems in the XY plane, thus not considering the velocity state in the Z-direction.

Figures 11 and 12 show that Figure 11 depicts the stabilization of the roll angle, yaw angle, pitch angle, and their corresponding angular velocities of the UAV system under the optimal fault-tolerant consistency protocol $5 \leq t \leq 10$. Figure 12 illustrates the stabilization of the roll angle, yaw angle, and their corresponding angular velocities of the UAV under the algorithm proposed in Reference [29] $t = 20$ s. It also demonstrates the optimal fault-

tolerant consistency algorithm's superiority, considering actuator faults. This algorithm enables heterogeneous multi-agent systems to achieve quicker consistency in the presence of faults, reducing the time required to complete tasks.

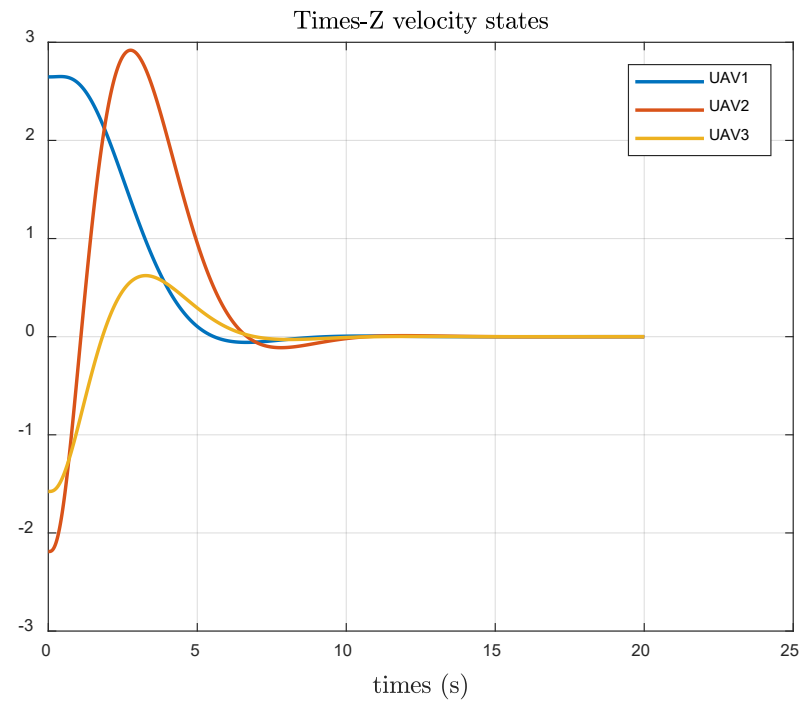


Figure 10. Consistency error in velocity along the Z-direction between the following UAV and the leader.

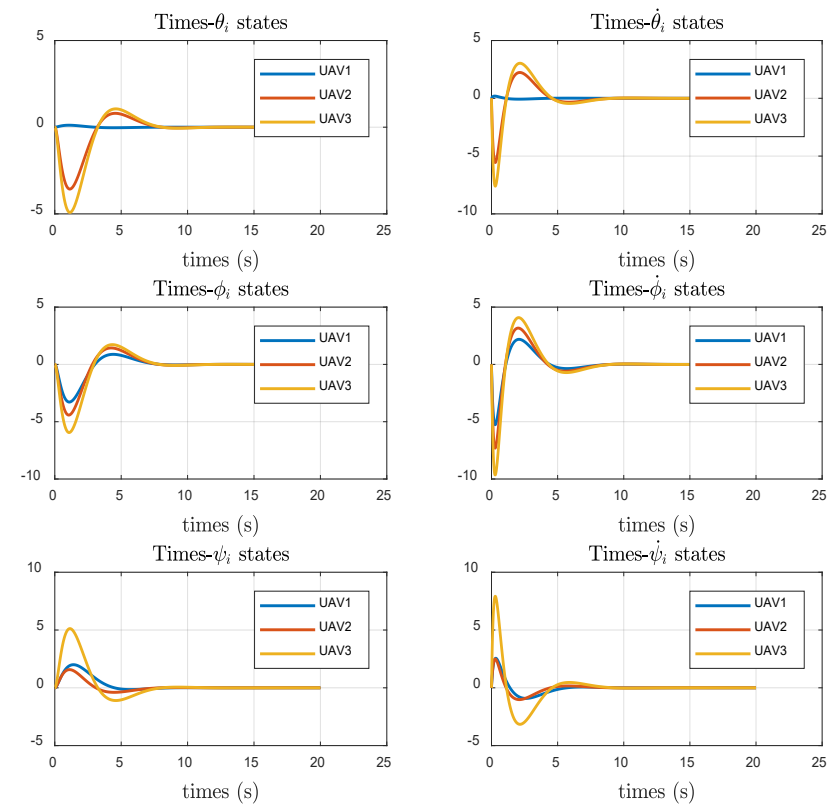


Figure 11. Consistency error in the attitude angles of the following UAV.

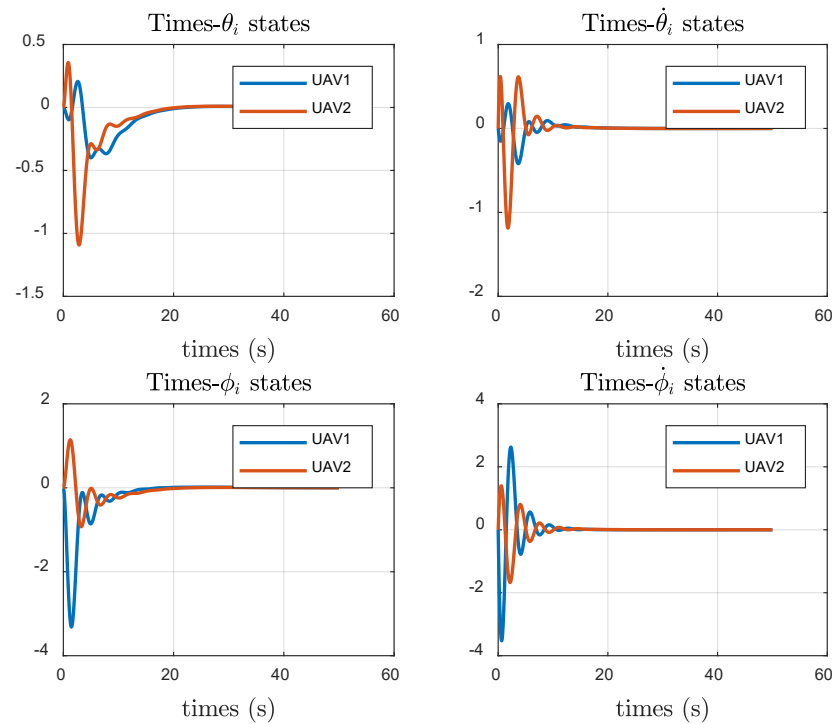


Figure 12. The state variables of the attitude angles of the UAV under the method proposed in Reference [29].

We plot the state trajectory of all UAVs and UGVs in this leader–following heterogeneous multi-agent system, as shown in Figure 13. The experimental outcomes show that the states of all following UAVs and UGVs converge to the leader’s position and velocity. This further demonstrates the efficiency and feasibility of the algorithm (31) and (33).

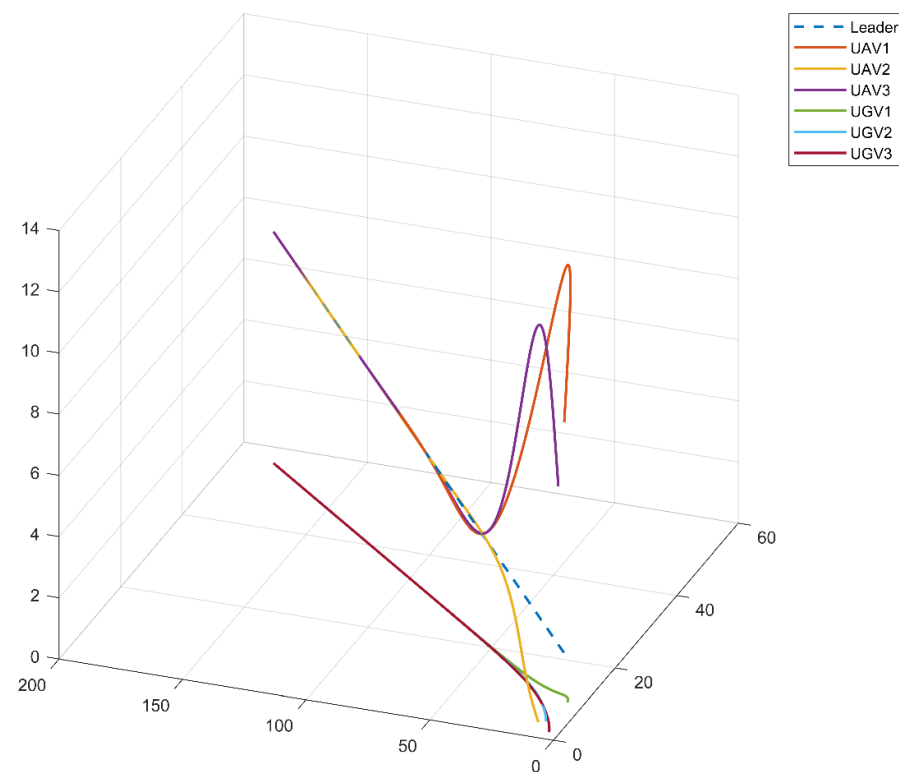


Figure 13. State trajectory plot of the leader–following heterogeneous multi-agent system.

5. Conclusions

This paper analyzes the dynamic models of uncrewed aerial vehicles and uncrewed ground vehicles to establish a heterogeneous system. Firstly, we build upon the communication topology of heterogeneous multi-agent systems. The fault-tolerant consensus control problem of the leader–follower multi-agent system under actuator partial failure is introduced. Based on the Euler-Lagrange equations, performance index functions are defined for each following UGV and UAV. Then, the optimal fault-tolerant consensus controller capable of handling actuator partial failure is obtained through optimization theory, and the proposed algorithm's stability is demonstrated using Lyapunov stability theory. Finally, MATLAB simulation experiments further corroborate the efficacy of the proposed algorithm. The algorithm ensures that UAVs and UGVs eventually converge to the leader's position and velocity. In the next step, the research will focus on the collaborative control of heterogeneous multi-agent systems, integrated with fault-tolerant mechanisms, and the theoretical results will be applied to engineering practice.

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