



Article Full-Field Super-Resolution Terahertz Imaging Based on Rotating Coherent Scattering Microscopy

Duoxuan Ma¹, Jie Zhao^{1,2,*}, Dayong Wang^{1,2,*}, Hao Lin¹, Lu Rong^{1,2}, Yunxin Wang^{1,2} and Shufeng Lin¹

- ¹ Department of Physics and Optoelectronics, Faculty of Science, Beijing University of Technology, Beijing 100124, China
- ² Beijing Engineering Research Center of Precision Measurement Technology and Instruments, Beijing University of Technology, Beijing 100124, China
- * Correspondence: zhaojie@bjut.edu.cn (J.Z.); wdyong@bjut.edu.cn (D.W.); Tel.: +86-010-6739-2489 (J.Z. & D.W.)

Abstract: For decades, terahertz (THz) microscopic imaging has been limited by the resolution of the system due to the larger wavelength, the power of the source, and the equivalent noise power of the detector, so a lot of research has focused on single-point scanning imaging. With the development of hardware, full-field THz imaging based on high-power continuous-wave THz sources have been developed such as the direct intensity imaging method and lensless coherent imaging. In particular, the THz direct intensity imaging method requires no complicated computational reconstruction, while the high resolution, as a key issue, still needs to be improved. In this paper, the rotating coherent scattering microscopy was applied to THz imaging for the first time. Here, we designed and fabricated a hemisphere lens with high-resistance silicon. The tilted hemisphere lens transformed the incident divergent beam into a plane wave, and the total internal reflection occurred in the planar surface within the hemispherical lens, and generated evanescent waves in the rare medium. At the same time, the sample was placed very close to the plane of the hemispherical lens, so that the sample was illuminated by the evanescent waves. The scattered waves carried high frequency information to the far field, and thus through an objective, the super-resolution imaging was achieved along a single direction. Then, the hemispherical lens was rotated to obtain coherent scattering microscopic images under different evanescent wave illumination angles. Finally, the full-field super-resolution imaging results were obtained through incoherent superposition.

Keywords: terahertz imaging; full-field; super-resolution; evanescent wave; rotating coherent scattering microscopy

1. Introduction

Terahertz (THz) waves are electromagnetic waves with the wavelengths between 30 µm and 3 mm. They have special properties including a fingerprint spectrum characteristic, superior penetrability to non-metallic and non-polar materials, and low single photon energy being safe to the sample and the operator. Therefore, THz imaging has important potential in characterizing a wide range of materials and the imaging of biological tissues. Both pulsed-wave (PW) THz imaging and continuous-wave (CW) THz imaging have been developed in the last decade [1] to enrich the field of THz research. At the same time, THz medical imaging applications such as biological tissue water content analysis [2], lesion tissue identification [3–5], and burn identification [6,7] have been proposed. However, unlike visible light imaging systems, the long wavelength of THz waves and the relative scarcity of available optical components make high-resolution and super-resolution imaging difficult. In particular, the optical field carrying the subwavelength structural information of the sample cannot propagate to the far field, which is one of the limitations of THz imaging in biomedical imaging.

In order to break the diffraction limited resolution, solid immersion lenses [8–11], super-oscillatory lenses [12], meta lenses [13], and the dielectric sphere [14] are usually



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Copyright: © 2023 by the authors. Licensee MDPI, Basel, Switzerland. This article is an open access article distributed under the terms and conditions of the Creative Commons Attribution (CC BY) license (https:// creativecommons.org/licenses/by/ 4.0/). used to form a focused spot with a subwavelength size. For PW THz, scattering media are used in wavefront shading to spatio-temporal focusing for THz optical correction systems [15] and ghost imaging [16]. Then, super-resolution imaging can be achieved by scanning the sample point by point by using the focused spot as the illumination beam. Because of the high transmittance and high refractive index of silicon and high resistivity float zone silicon (HRZF-Si) in the THz band, the solid immersion lens is used for pointscanning imaging [17–19]. When a dielectric particle of wavelength magnitude is placed in the terahertz wave focus position, a terajet beyond the diffraction limit can be generated, significantly improving the spatial resolution of the terahertz imaging system [20]. In particular, it is easy to generate photonic hooks due to the asymmetry of mesoscale dielectric particle structures such as cylinder, half-cylinder, and cubic particle [21]. In addition to the factor of the imaging resolution, the main reason preventing the wide application of THz imaging is the slow acquisition time of the conventional point-scanning method, and the high-power requirement of the source for the THz full-field imaging. With the development of high-power CW and PW THz sources such as gas lasers, cavity-based photoconductive sources [22], and high-sensitivity area array detectors such as pyroelectric detectors and microbolometers, full-field imaging has become possible. However, the problem of low imaging resolution caused by the long wavelength still exists.

In recent years, the full-field CW-THz imaging technology includes the phase-contrast imaging methods [1,23] and the direct intensity imaging methods. The former is represented by digital holography [24,25], ptychography [26–28], and transport-of-intensity equation (TIE) imaging [29]. In these methods, two-dimensional (2D) photosensitive elements are used to record the interference or diffraction pattern of the samples under the THz illumination, and various reconstruction algorithms have been proposed to retrieve the distribution of the complex electromagnetic field in the sample plane. The latter makes use of the parabolic reflectors/spherical lenses or the lens sets. The sample and the 2D photosensitive element are in the object–image conjugate plane of the lens or lens group to satisfy the imaging condition [30].

In the aspect of far-field and full-field direct intensity imaging, assuming the wavelength of the THz wave fixed, when the 2D photosensitive elements are used to record the intensity image, the size of each pixel is often smaller than the wavelength, and therefore the imaging resolution depends on the numerical aperture (NA) of the microscopic objective according to the well-known Abbe's theoretical resolution formula, which is also related to the recording distance and the effective aperture of the microscopic objective. Microscopic imaging systems with higher NA have a higher resolution. There are usually two methods to improve the spatial resolution: the first is to expand the NA to include more high frequency information in the passband and the second assumes that the NA is fixed and illuminates the sample by the tilted plane wave or the evanescent wave along the surface so that the part of the spatial spectrum of the sample with higher spatial frequencies is shifted into the passband of the imaging system.

In the aspect of improving the NA, since it is equal to be $n\sin\alpha$, where α is the aperture angle of the objective accepting light and n is the object–space refractive index, it can be effectively enhanced by immersion methods. The related advanced work on visible light could inspire research and be helpful for design in the THz band. In 2009, J. Lee et al. reported near-field high resolution by self-assembled nanoscale spherical lenses [31]. In 2011, Z. Wang et al. used microspheres for the first time to improve the resolution of a far-field white light microscopy imaging system [32]. Furthermore, these studies used solid-state microspheres rather than high-refractive index matching liquid media to enhance the resolution of the imaging system. However, the properties of the materials, objects, media, etc. need to be considered, so these methods cannot be directly applied to the THz band. Although it is not practical to find high RI matching liquids in the THz band, recently, we introduced the solid immersion method into the full-field THz direct intensity imaging method and analyzed the imaging properties of a hemispherical solid immersion lens (h-SIL) by ray tracing simulation. The secondary reflection produced an additional inverted

image with a small field curvature. By blocking the direct refracted image, high-fidelity imaging was achieved [33].

In another aspect of the super-resolution imaging realized by the tilted illumination shifting frequency, significant progress has been made in visible light. In 2013, X. Hao et al. achieved total internal reflection (TIR) through a triangular prism to generate evanescent waves. Super-resolution imaging was achieved by illuminating a three-directional striped sample deposited directly on the TIR interface with the evanescent waves [34]. On the other hand, fluorescence microscopy imaging methods have gained a lot of research and applications. To suppress the background noise, the fluorescence excitation region is confined to the propagation direction of the evanescent waves by TIR, thus enhancing the contrast of imaging [35]. This has also led to the study of the scattered direct intensity imaging method of non-fluorescent objects illuminated by evanescent waves using TIR fluorescence microscopy (TIRFM) [36,37]. In 2013, P. Olshausen et al. used an inverse TIR fluorescence system to achieve super-resolution images of label-free microspheres [38]. Compared with the prismatic illumination scheme, the objective illumination scheme is able to obtain different angular illumination directions without moving the sample, just simply by loading different grating on the spatial light modulator (SLM). The reconstruction method was acquired by incoherent superposition of the images illuminated by the evanescence wave from 72 different directions to achieve an imaging resolution beyond the diffraction limit. In 2016, the direct intensity imaging method under different transverse wave vectors were recorded in a single image acquisition time by rotating the incident beam direction at a high speed, which has the advantage of real-time recording without the reconstruction process [39], which is named as the rotating coherent scattering (ROCS) microscopy.

Recently, this super-resolution imaging method has received some attention in the field of THz imaging. In 2021, J. Zhao et al. numerically simulated one-dimensional THz spoof surface plasmons (SSP) illuminating a one-dimensional sample [40], and presented the scattered field distribution located at one wavelength distance behind the sample, and obtained high-resolution images by the iterative reconstruction algorithm based on a series of scattered field distributions with nine different frequency shifts. Since the SSP provides only a single direction surface wave, multiple wavelengths are required to fill the Fourier spectrum to reconstruct the complex electromagnetic field distribution. However, a THz far-field and full-field direct intensity imaging method based on the evanescent wave (or the surface waves) illumination has not been proposed yet.

In this paper, we designed and built a THz-ROCS microscopic imaging system. The incident THz divergent beam is transformed by the spherical refractive surface of a hemispherical lens and produces the plane wave inside the lens. Then, the plane wave incidents on the planar interface of the hemispherical lens satisfies the condition of TIR, which generates the evanescent wave. The evanescent wave illuminates the sample immediately adjacent to the interface, producing the scattered waves that carry high-frequency information to propagate to the far-field. An objective collects the scattered waves to form the high-resolution image at its output plane. By rotating the hemispherical lens, multiple images under different high transverse wave vector illuminations can be obtained. Finally, through the incoherent superposition of these images, the full-field image of a 2D grating with a period of 150 μ m was achieved experimentally beyond the diffraction-limited resolution.

2. Principle of THz ROCS

The key point of ROCS microscopy is to generate rotatable, highly transverse wave vector illumination. However, unlike visible light, the THz direct intensity imaging method is limited by the sensitivity or scarcity of the optical elements and the detector, making it difficult to modulate the illumination direction by ring illumination or the SLM. Furthermore, in the THz band, there lacks a high RI matching solution and commercial instruments similar to those used in TIRF microscopy. Thus, new illumination schemes need to be developed.

TIR is the most common method to generate evanescence waves. Assuming that the wave vector in air is equal to the free-space wave vector k_0 ($k_0 = 2\pi/\lambda$), a spherical wave

(1)

with a small divergence angle is generated outside the hemispherical lens made by HRZF-Si, as shown in Figure 1. Under the paraxial approximation, it could be transformed by the spherical surface into a plane beam in the dense medium, whose propagation direction makes an angle of θ with the normal to the planar surface of the hemispherical lens. This plane wave is reflected at the planar surface, being the interface between HRZF-Si and the air. The RI of the medium of the hemispherical lens and the air are *n* and 1.0, respectively. Then, the transverse wave vector at the reflecting surface is $k_x = n \sin\theta k_0$, according to Maxwell's boundary conditions, and this transverse wave vector should be the same in both the hemispherical lens medium and in the air medium. The wave vector k_0 and the component of the wave vector k_z , k_x satisfy the Pythagorean theorem $k_x^2 + k_z^2 = k_0^2$. In the case when $k_x > k_0$, which also means θ is greater than the critical angle θ_c of the total internal reflection ($\theta_c = \arcsin(1/n)$). Then, $k_z^2 < 0$, which means that it is in the imaginary field. There exists an evanescent wave in the air medium close to the planar surface and cannot be propagated to the far-field. The transverse wave vector of the evanescent wave becomes bigger when continuously increasing the incident angle θ . At the same time, when illuminating the sample by the evanescent wave, the interaction with the sample generates a scattered light field that will shift the spatial spectrum of the sample and propagate the part with higher frequencies to the far field. The scattered waves are then collected by an imaging objective, located above, whose optical axis is parallel to the normal of the planar surface of the hemispherical lens. Here, we analyzed the position relationship between the hemispherical lens and the point source of the divergence beam. The radius of the hemispherical lens with refractive index n is r. Then, the distance along the optical axis from the point source to the planar surface of the hemispherical lens is D, expressed as:



Figure 1. Top view and side view of the TIR schematic based on a hemispherical lens.

The spatial frequency that can pass through the passband of the system to participate in imaging is shown in Figure 2. In the case of the normal incidence illumination, the NA of the imaging system is determined by the aperture angle α (NA = sin α), and is less than 1. The system can only transfer the spatial frequency information inside the gray circular region, and the highest wave vector is NA k_0 , as shown in Figure 2 denoted by the blue dashed line. When $\alpha = 90^\circ$, the cutoff spatial frequency is denoted by the black dashed line, corresponding to the free space wave vector k_0 . In the case of illumination with the inclined plane wave or the evanescent wave, the transverse wave vector of the illumination beam is no longer equal to zero. The passband will follow the illumination wave vector to shift with the distance $k_x = n \sin\theta k_0$, denoted by the red dashed line. At this time, the spatial frequency information in the red region can be received by the system. It is worth noting that when evanescent wave illumination is used, the frequency shift of the passband can exceed k_0 , then super-resolution imaging can be achieved.



Figure 2. The relationship between the incidence angle, the aperture angle, and the passband in the wave vector space under the tilted plane wave illumination and the TIR mode, respectively.

When the direction of the incident evanescent wave rotates relative to the sample, the frequency shift direction will be changed accordingly, and the corresponding passband will rotate around the center. Specifically, the direct intensity imaging results under different directions of illumination with the number N are recorded by rotating the hemispherical lens. Here, the ROCS principle is considered for reconstruction, and the super-resolution image is obtained by the direct superimposition of frequency-shifted images, which is recorded as I_{final} [38]:

$$I_{final} = \frac{1}{N} \sum_{m=1}^{N} [f(\mathbf{r}) \cdot E_m(\mathbf{r}, \phi_m) \otimes h_c(\mathbf{r})]^2, \qquad (2)$$

where *r* denotes the lateral position in the *x*–*y* plane; *f* is the field distribution of the sample; E_m is the electric field function of the evanescent wave incident from the direction of illumination ϕ_m ; h_c is the coherent point spread function (PSF) of the imaging system; and \otimes denotes the convolution operation. Consider the sample as the sum of point scatterers at different positions, then

$$f(\mathbf{r}) = \sum_{j} f_{j}(\mathbf{r}) = \sum_{j} \delta(\mathbf{r} - \mathbf{r}_{j}),$$
(3)

and set the field image of the *j*th scatterer to be

$$F_{m,j}(\boldsymbol{r},\boldsymbol{\phi}_m) = f_j(\boldsymbol{r}) \cdot E_m(\boldsymbol{r},\boldsymbol{\phi}_m) \otimes h_c(\boldsymbol{r}). \tag{4}$$

This leads to the intensity under the illumination of the one-directional evanescent wave being:

$$I_m = \left[\sum_j F_{m,j}(\boldsymbol{r}, \boldsymbol{\phi}_m)\right]^2.$$
(5)

At this time, the total intensity of the final image is:

$$I_{final} = \frac{1}{N} \sum_{m=1}^{N} \left[\sum_{j} \left| F_{m,j}(\mathbf{r}, \phi_m) \right|^2 + \sum_{j \neq k} 2 \left| F_{m,j} \right|^2 \cdot \left| F_{m,k} \right|^2 \cdot \sum_{m=1}^{N} \cos(\varphi_{m,j} - \varphi_{m,k}) \right].$$
(6)

where $\varphi(\mathbf{r}; \phi_m)$ is the phase of the field image that depends on the position \mathbf{r} of the scatterer and the direction of illumination ϕ_m . The former term of the above equation represents the incoherent images of different scatterers, and the latter term represents the cosine sum of the phase differences of the point scatterers in all illumination directions.

3. Simulation and Experimental Results

Numerical simulations were first performed based on Equation (4). A simple sample containing two point scatterers and a complicated sample with several microspheres were selected. For simplification, the magnification of the imaging system was assumed to be a unit. Figure 3 shows the results for the two point scatterers with the distance of 150 μ m. The wavelength of the incident THz wave was 119 μ m, and the NA of the imaging system was 0.6, which yielded a theoretical resolution of 162.6 μ m ($d = 0.82\lambda/NA$). Therefore, the scatterer sample could not be distinguished when normally incident by the plane wave, as shown in Figure 3a. When the sample was illuminated by an evanescent wave with a 1.17 k_0 transverse wave vector through the TIR, the cross-section of the corresponding image, as shown in Figure 3b, and the two scatterers could be distinguished. It is worth noting that the peaks of the scatterers under high transverse wave vector illumination were 250 µm apart from each other, which indicates that in this case, the imaging resolution was enhanced, and at the same time, the measured distance between two distinct intensity peaks in the image plane was larger than the actual distance between two point scatterers and was an interference effect depending on the phase delay, which is like a kind of aberration under a single illumination angle. Therefore, the ROCS method needs incoherent superposition with different images under as many illuminating directions as possible to obtain an aberration-free result.



Figure 3. Simulated images of two point scatterers with a spacing of 150 μ m under (**a**) illumination with the normal incident plane wave and (**b**) illumination with an evanescent wave of 1.17 k_0 transverse wave-vector through TIR.

Figure 4 shows the simulated imaging results of the multiple microsphere samples. The radius of each microsphere was 25 μ m, which were assumed to be transparent to the THz wave such as the HRFZ-Si material with an absorption coefficient of 0.04 cm⁻¹ [41], and the other parameters were the same as the previous one. Figure 4a–e depicts five of the direct intensity imaging results under a different illumination direction (represented by the white arrow) every 20° of rotation. According to the principle of ROCS, the intensity of 18 images was superposed to obtain the final result shown in Figure 4f. Compared with the direct intensity imaging result shown in Figure 4g with the normal incident mode, the imaging resolution was greatly improved. From the profile curve in Figure 4f, the two microspheres could be resolved based on the two distinct peaks, even with the low

contrast. It is worth noting that more acquisition at different angles will benefit the final superimposed image. However, it will increase the complexity of the setup and acquisition time. Usually, there can be a compromise between the acquisition time and the quality of the final intensity image.



Figure 4. (**a**–**e**) Five simulated imaging results with the high transverse wave vector illumination at 20° , 40° , 60° , 80° , and 340° among the total 18 images, (**f**) the superimposed final image with 18 different intensity images, and (**g**) imaging result with the normal-incident illumination.

Then, an experimental verification was performed. The experimental setup is shown in Figure 5. The THz source was an infrared-pumped methanol laser (295-FIRL-HP) with an output frequency of 2.52 THz. The THz wave is a monochromatic coherent light with a small divergence angle about 0.63°, which is a longitudinally polarized Gaussian beam. The power can reach up to 400 mW by adjusting the pump power and the THz laser cavity length. In order to guarantee the optical elements are centered, we adjusted the center of all of the optical elements to the same height with the help of the liquid crystal sheets. The beam passed through a pair of off-axis parabolic mirrors with focal lengths of 50.8 mm and 152.4 mm to expand the radius of the beam from 9 mm to 27 mm. Next, a TPX lens with the diameter of 50.8 mm and focal length of 50 mm converged the parallel beam at the position of 50 mm + 35.9 mm (calculated according to Equation (1)) in front of the hemispherical lens, designed and fabricated with HRZF-Si, whose refractive index n was 3.418 under illumination with a 2.52 THz wave, and the radius r was 25.4 mm. Then, the spherical beam refracted into the helispherical lens and became the plane beam. The total internal reflect occurred on the planar surface of the Si-air plane. Here, the hemispherical lens was fixed by a rotator mount and the sample was fixed to the center of the flat surface of the hemispherical lens with alcohol under van der Waals interaction. When rotating the rotator to an angle of 70° between the plane and the optical axis, the normal angle of the incident beam was about 20°. At this time, the frequency shift was 1.17 k_0 . A magnified imaging system with an aperture of about 70 mm and a numerical aperture of about 0.6 was placed at a distance of more than 40 mm from the sample to the THz camera with a microbolometer area-array detector. The pixel size of the detector was 35 μ m \times 35 μ m, and arranged into a rectangle with 384×288 pixels.



Figure 5. Schematic of the configuration of the THz-ROCS system.

Here, a HRZF-Si 2D grating with the period of 150 μ m (1.26 λ), made by deep silicon etching technology, was chosen as the sample. Based on the coherent light imaging, the theoretical resolution is 162.6 μ m, so the imaging system cannot resolve the detailed information of this grating when the THz beam illuminates the sample with normal incident mode. Through the evanescent wave illumination, according to the basic principle of the frequency shifting shown in Figure 2, this can be calculated so that it is possible to move the detail information between 55.1 μ m and 171.2 μ m into the passband of the system.

In the actual experiment, we chose to rotate the sample and not the incident wave for the convenience of operation to achieve illumination of the sample by the evanescent beam from different directions. By rotating the sample, we recorded the direct intensity imaging results under the evanescent wave illumination at 20° intervals. Figure 6a–c shows three of the direct intensity imaging method results for illumination at 60°, 210°, and 300°, which were the angles between the evanescent wave and the sample. The black arrow is the sample orientation and the red arrow is the evanescent wave illumination direction. The interference fringes can be clearly seen, which are related to the cosine item in Equation (6). Then, the images were rotated by taking the black arrow as the baseline, superimposed, and normalized to obtain the final intensity image in Figure 6d, where it can be seen that the sample details containing the concave–convex structure were resolved from the profile curve. The magnification of the imaging system was calculated to be 1.63 by dividing the grating period in the imaging plane by the actual period of the grating.



Figure 6. (**a–c**) Intensity images at the three rotation angles with a total of 18 angles under the evanescent wave illumination recorded by the microbolometer array detector and (**d**) the final intensity image through the superimposition of their rotated images.

It can be seen that the final image quality of Figure 6d was not so good. This is related to the type of sample used, and whether the material has a good transmission property to the THz wave. Therefore, it can be treated as a quasi-phase object, which has a concave-convex periodical structure with known spacing. Each cell of the mesh has the width and height with the sidewall angle due to being fabricated by the etching process. Therefore, the intensity image mainly includes the edges on the surface inherently with low contrast. Additionally, as the combination of the hemispherical lens and the sample is manually rotated through the mechanical rotator mount, the resulting angle rotation is not accurate enough. Therefore, when superimposing all of the intensity images, there will be some errors existing in the rotated images. Furthermore, the intensity distribution of the THz beam is not so uniform, which may impose a possible effect of degrading the quality of the final result.

4. Conclusions

Among the full-field THz imaging techniques based on high-power continuous-wave THz sources, direct intensity imaging exhibits advantages due to there being no need for complicated computational reconstruction, while the resolution as a key issue still needs to be improved because of the long wavelength of the THz waves. In this paper, ROCS microscopy was applied to THz imaging for the first time. A specific hemispherical lens was proposed to produce the evanescent wave illumination and to also support the sample. The multi-angle evanescent wave illumination was adopted, and the final result was obtained with the principle of the ROCS method to improve the lateral imaging resolution. a microscopic imaging setup based on a 2.52 THz high-power coherent THz source and an uncooled microbolometer array detector was built, and 2D grating with a period of 150 μ m (1.26 λ) was successfully resolved. The observed resolution breaks the theoretical diffraction-limited resolution given by Abbe's formula, which is determined by the wavelength and the numerical aperture of the coherent imaging system. Next, some resolution test targets were employed to calibrate the imaging system and experimentally achieve the diffraction-limited resolution of $\lambda/2$. The proposed method achieved THz super-resolution imaging under evanescent wave illumination, and provides a new way for THz full-field microscopic imaging.

Since the pixel size of the THz detector is close to the wavelength, compared with the visible and the infrared band, the current commercial THz image-plane systems are mainly telescopic. In this case, the working distance on the object side is short, usually less than 50 mm. This leads to the difficulty of inserting other optical elements such as hemispherical lens, etc. The hemispherical lens can also be reversely used as a solid immersion lens to further enhance the NA. If possible, the maximum frequency shifting distance generated by the evanescent wave illumination is nk_0 , and the maximum NA of the system can be improved to nk_0 . Therefore, the resolution by the evanescent wave illumination can ultimately be 1/2n times that of the diffraction limit.

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