



Article Performance of the Compliant Foil Gas Seal with Surface Micro-Textured Top Foil

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Featured Application: Compliant foil gas seals, as a non-contact sealing mechanism with high self-adaptability, are used in the main bearing cavity of aero engines.

Abstract: In various fields, micro-textures have been successfully applied to the surface of friction pairs to effectively improve flow field and friction performance. This paper aims to investigate how different textures affect the sealing performance of compliant foil gas film seals. In theoretical simulations, a facile method for characterizing the shape of micro-textures is proposed, and the equilibrium relationship between the gas film pressure, gas film thickness, and foil deformation is established. The transient Reynolds equation considering the eccentric convergence problem and abrupt Rayleigh step changes is solved to analyze the static and dynamic characteristics. The results show that (i) compared with the directionality of the texture, the gas volume accommodated by the texture has a greater impact on the sealing performance, and a convergent texture can effectively control the leakage rate; (ii) when the texture depth exceeds 9 μ m, the sealing system may be unstable; (iii) the compliant foil seal is well suited to higher-speed service conditions, and the inverted triangular texture shows the best comprehensive sealing performance.

Keywords: compliant foil gas seal; micro-texture; image recognition; sealing performance

1. Introduction

As an aircraft is susceptible to random uncertainty excitation during operation [1], which may induce seal instability or failure, designing a seal structure with good high-speed stability and strong autonomous adjustment capability is of great importance for the development of aerospace engines. The compliant foil seal (CFS) is a new type of non-contact seal [2]. Compared with the traditional gas film sealing structure, which has a rigid floating ring, the compliant foil can undergo adaptive deformation under load; moreover, there is Coulomb friction between the contact elements [3,4]. Owing to these advantages, the sealing structure can rapidly adapt to the operating position, spontaneously adjust the balanced relationship between the friction pair, load, and gas film, ensure gas film stability, and prevent friction and collision. Therefore, a sealing structure with a compliant sealing surface or flexible support has considerable potential for application in the sealing components of rocket turbine pumps and aero-engine systems [5,6].

In the 1990s, Salehi and Heshmat proposed a CFS structure based on the study of foil bearings, and they tested it at 55,000 rpm and 560 °C [7–9]. Regarding the theoretical study, they established the governing equation of the film pressure by considering the turbulence effect and analyzed the sealing performance of CFS under high-speed operation conditions using the method of successive over-relaxation [10]. Kim [11] combined the perturbation method for a floating ring seal with the finite element method for a flexible foil to analyze its characteristics and found that the eccentricity decreases while the direct stiffness and damping coefficient increases as the bump foil thickness increases. Lee et al. [12] designed



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Copyright: © 2022 by the authors. Licensee MDPI, Basel, Switzerland. This article is an open access article distributed under the terms and conditions of the Creative Commons Attribution (CC BY) license (https:// creativecommons.org/licenses/by/ 4.0/). a floating ring seal structure using a bump foil to support the ring, which demonstrated its stability at high speed through eddy current stability experiments. Ding [13] used the PH linear method to study the steady-state flow field characteristics of a cylindrical spiral-groove gas film seal and found that the sealing pressure difference has a significant effect on the steady-state characteristics. Wang [5] analyzed the sealing characteristics and dynamic properties of CFS and tested the effect of different surface roughness values on the start-stop cycle performance of high-speed elastic foil sealing [14]. The results showed that improving the interface surface properties can effectively attenuate the hysteresis effect of the seal.

Interface modeling of the friction pair has a significant impact on the flow field, dynamic pressure effect, and friction performance [15,16]. Stull's [17] introduction of a series of cavities in the diverging curved walls of a two-dimensional ribbed diffuser or Mariotti's [18] application of transverse grooves on both sides of the stern side can produce locally stable flow re-circulation. The textured surface of the diamond-like carbon film is machined on the dry gas seal ring, and its trapping effect contributes significantly to the improvement of friction performance [19,20]. Moreover, the parameters of pits are the keys to affecting friction performance [19,21]. The shape design of the texture successfully utilizes the knowledge of biomimicry; for instance, streamlined grooves in dolphin skin were used by Lang [22] and a semi salix leaf textured face was processed by Bai [23]. With the widespread application of texture, optimization or hybrid processing techniques such as mask deposition and laser cladding are gradually developed [24]. Thus far, research on the surface modeling of friction pairs of the cylinder gas seal has mainly focused on the design of dynamic pressure grooves [25–27]. Most of these studies have used CFD software, where procedures such as geometric modeling and mesh division are relatively cumbersome.

In summary, research on the characteristics of compliant foil gas seals has mainly focused on structural design. Although some researchers have conducted theoretical analyses and experimental tests, results on the accurate design of the micro-textures on the surfaces of compliant foil gas seals are relatively scarce. In the present study, numerical modeling was used to calculate the flow field distribution of the compliant foil gas seal, and to evaluate the influence of micro-texture shapes, depth, and rotational speed on the sealing performance. With these works done, the optimal matching method can be determined.

2. Materials and Methods

2.1. Geometric Model

The structure of the compliant foil gas seal is shown in Figure 1. It mainly consists of a sealing cavity, flexible sealing surface, and rotating shaft. The flexible sealing surface includes a bump foil and a top foil with flexible support. The top foil is bent on the highpressure side to form an extension, which serves to fix the foil and block the leakage channel.



Figure 1. (a) Schematic of the compliant foil gas seal. (b) Mechanisms for the lubricating gas film formation.

In Figure 1, θ_1 is the angle between the free end of the bump foil and the fixed end, p is the gas film pressure, h is the thickness of the gas film, t_b and t_p are the thicknesses of the

bump foil and the flat foil, respectively, h_c is the texture depth, e is the eccentricity distance, R is the outer diameter of the rotation axis, and O_1 and O_2 are the centers of the sealing cavity and the rotation axis, respectively.

The rotor is installed eccentrically in the sealing cavity. When the compliant foil gas seal is in the normal working condition, the bump foil and top foil are slightly deformed under the viscous shear of the sealing medium, as shown in Figure 2a. A micro-scale wedge-shaped gap of $10–30 \,\mu\text{m}$ is formed between the friction pairs, which separates the friction and sealing pairs and produces a good hydrodynamic pressure effect, thereby forming a rigid pressurized air film to achieve lubrication and sealing. The structural parameters of the bump foil are shown in Figure 2b.



Figure 2. (a) Deformation of the foil. (b) Structural parameters of the bump foil.

In Figure 2b, u, r_b , s, l, and α are the deformation, radius, pitch, half chord length, and wrapping angle of the foil, respectively, and L is the seal width.

2.2. Micro-Texture Model

The upper surface of the flat foil is in contact with the sealing medium, and microtextures are formed on the surface via laser marking, as shown in Figure 3, where *L* is the seal width, *a* and *b* are the structural parameters of the texture, N_t is the number of cycles. When acquiring surface data, the texture first needs to be drawn on a 1:1 scale. Then, the image is converted into a series of matrices by the recognition method; the size of the matrix is consistent with the size of the flow field matrix.



Figure 3. Distribution of the micro-textures.

3. Theoretical Model

3.1. Reynolds Equation and Gas Film Thickness Control Equation

The compliant foil gas seal problem can be categorized as a micro-scale flow field problem. Therefore, the flow field can be considered as a laminar flow in this study. Moreover, the following assumptions are made: there is no slip at the fluid-solid interface, the sealing medium is an ideal gas, and the physical parameters remain unchanged. The pressure solution model can be obtained as follows:

$$\frac{\partial}{\partial \theta} \left(PH^3, \frac{\partial P}{\partial \theta} \right) + \left(\frac{R}{L} \right)^2 \frac{\partial}{\partial Z} \left(PH^3, \frac{\partial P}{\partial Z} \right) = \Lambda \frac{\partial (PH)}{\partial \theta} + 2\gamma \Lambda \frac{\partial (PH)}{\partial T}$$
(1)

Considering the Coulomb friction between the bump foil and the sealing cavity and ignoring the concavity or convexity of the flat foil in the radial direction, Iordanoff's [28] stiffness model with one end fixed and one end free is used to characterize the deformation of the bump foil. Thus, the static film thickness formula can be obtained as follows:

$$H = \begin{cases} 1 + \varepsilon \cos \theta + H_{c} + \frac{(P-1)}{K_{b}} & (\theta, Z) \in \text{Textured region} \\ 1 + \varepsilon \cos \theta + \frac{(P-1)}{K_{b}} & (\theta, Z) \in \text{Non-textured region} \end{cases}$$
(2)

The dimensionless parameters are defined as follows:

$$Z = \frac{z}{L}, \ H = \frac{h}{h_0}, \ P = \frac{p}{p_a}, \ T = \tau t, \ \Lambda = \frac{6\omega\mu r^2}{p_a h_0^2}, \ \gamma = \frac{\tau}{\omega}, \ H_c = \frac{h_c}{h_0}, \ K_b = \frac{k_b h_0}{p_a}$$
(3)

where z is the axial coordinate, t is the motion time, k_b is the bump foil stiffness, h_0 is the average gas film thickness, p_a is the ambient pressure, τ is the angular velocity of the vortex, μ is the viscosity of the lubricant gas, γ is the perturbation ratio, Λ is the compressibility coefficient, ε is the eccentricity, and *P*, *Z*, *H*, *T*, *H*_c, and *K*_b are the corresponding dimensionless parameters.

After the displacement perturbation and velocity perturbation at the equilibrium position, the dimensionless perturbation is obtained as follows:

$$\Delta X = \frac{\Delta x}{h_0} = |\Delta X|e^{iT}, \ \Delta Y = \frac{\Delta y}{h_0} = |\Delta Y|e^{iT}$$
(4)

The Taylor series expansions for the gas film pressure, gas film thickness, and foil deformation with the perturbation parameters are expressed as follows:

$$\begin{cases}
P_t = P + P_x \Delta X + P_x' \Delta X + P_y \Delta Y + P_y' \Delta Y \\
H_t = H + H_x \Delta X + H_x' \Delta \dot{X} + H_y \Delta Y + H_y' \Delta \dot{Y} \\
U_t = U + U_x \Delta X + U_x' \Delta \dot{X} + U_y \Delta Y + U_y' \Delta \dot{Y}
\end{cases}$$
(5)

After considering the time term, the gas film thickness deviates from the static gas film thickness *H*, and the gas film thickness under perturbation is obtained as follows:

$$H_t = H + (\Delta X \sin \theta - \Delta Y \cos \theta) + \Delta U_t \tag{6}$$

Combining Equations (5) and (6), the following can be deduced:

$$\begin{cases} H_x = U_x + \sin \theta, H_x' = U_x' \\ H_y = U_y - \cos \theta, H_y' = U_y' \end{cases}$$
(7)

According to the relationship between the gas film pressure and the deformation of the bump foil, the following can be obtained:

$$P = K_{\rm b}U + C_{\rm b}\gamma \frac{\partial U}{\partial T} + 1 \tag{8}$$

Substituting Equations (5) and (7) into Equation (8) gives the following equation, where C_b is the dimensionless damping of the foil:

$$\begin{cases} P_x = K_b H_x - C_b H_x' - K_b \sin \theta \\ P_x' = K_b H_x' + C_b h_x - C_b \sin \theta \end{cases} \begin{pmatrix} P_y = K_b H_y - C_b H_y' + K_b \cos \theta \\ P_y' = K_b H_y' + C_b H_y + C_b \cos \theta \end{cases}$$
(9)

3.2. Boundary Conditions

The mandatory boundaries at the inlet and outlet locations are expressed as follows, where p_i is the inlet pressure:

$$\begin{cases} Z = 0, P = \frac{p_i}{p_a}, P_x = P_x' = P_y = P_y' \\ Z = L, P = 1, P_x = P_x' = P_y = P_y' \end{cases}$$
(10)

The circular boundary in the middle section is expressed as follows:

$$\begin{cases}
P(\theta, Z) = P(\theta + 2\pi, Z) \\
P_x(\theta, Z) = P_x(\theta + 2\pi, Z), P_x'(\theta, Z) = P_x'(\theta + 2\pi, Z) \\
P_y(\theta, Z) = P_y(\theta + 2\pi, Z), P_y'(\theta, Z) = P_y'(\theta + 2\pi, Z)
\end{cases}$$
(11)

3.3. Static Sealing Performance Parameters

The key static characteristics parameters for evaluating the compliant foil gas seal are the gas film force *F*, mass leakage rate *Q*, attitude angle φ , and friction force *F*_f. In the following equations, the subscripts *h* and *v* represent the horizontal and vertical directions, respectively:

$$F_{\rm h,v} = \int_0^L \int_0^{2\pi} (p - p_{\rm a}) r \left\{ \begin{array}{c} \cos\theta\\ \sin\theta \end{array} \right\} d\theta dz, \ F = \sqrt{F_{\rm h}^2 + F_{\rm v}^2}$$
(12)

$$Q = \int_0^{2\pi} -\frac{\rho h^3}{12\mu} \frac{\partial p}{\partial z} r d\theta$$
(13)

$$\varphi = act \tan \frac{F_{\rm v}}{F_{\rm h}} \tag{14}$$

$$F_{fh,v} = \int_0^L \int_0^{2\pi} \left(-\frac{\partial p}{\partial \theta} \frac{h}{2} p + \mu \frac{\omega r}{h} \right) r \left\{ \begin{array}{c} \cos \theta \\ \sin \theta \end{array} \right\} d\theta dz, \ F_f = \sqrt{F_{fh}^2 + F_{fv}^2} \tag{15}$$

3.4. Dynamic Sealing Performance Parameters

The dynamic characteristic parameters for evaluating the stability of the compliant foil gas seal are the direct stiffness coefficients k_{xx} and k_{yy} , direct damping coefficients c_{xx} and c_{yy} , cross stiffness k_{xy} and k_{yx} , cross damping coefficients c_{xy} and c_{yx} , which are expressed as follows:

$$\begin{bmatrix} k_{xx} & k_{xy} \\ k_{yx} & k_{yy} \end{bmatrix} = -\frac{RLp_{a}}{h_{0}} \int_{0}^{1} \int_{0}^{2\pi} \begin{bmatrix} P_{x}\cos\theta & P_{y}\cos\theta \\ P_{x}\sin\theta & P_{y}\cos\theta \end{bmatrix} d\theta dZ$$
(16)

3.5. Calculation Flow

The flow chart for calculating the characteristic parameters of the compliant foil gas seal is shown in Figure 4.



Figure 4. Calculation flow chart.

3.6. Parameters Selection

The geometric structure and mechanical performance parameters of the compliant foil gas seal used in the calculation in this study are summarized in Table 1, and the operating parameters are listed in Table 2, where ρ is the viscosity of the lubricant gas and μ_f is the friction factor.

Table 1. Geometric structure and mechanical performance parameters.

Parameters	Values	Parameters	Values	Parameters	Values
<i>R</i> (mm)	25	<i>a</i> (mm)	2	r _b (mm)	3.365
<i>L</i> (mm)	26.67	<i>b</i> (mm)	3	α (°)	63.93
N_{t}	16	t _b (mm)	0.2016	v_{b}	0.3
<i>h</i> ₀ (μm)	10	<i>l</i> (mm)	1.778	<i>E</i> _b (Pa)	$2.14 imes10^{11}$
h _c (μm)	2	<i>s</i> (mm)	4.572		

Table 2. Operating parameters.

Parameters	Values	Parameters	Values	Parameters	Values
p _i (MPa)	0.16	μ_f	0.1	$ ho (kg \cdot m^{-3})$	$1.1425 \\ 1.8 imes 10^{-5}$
p _o (MPa)	0.101325	$n_r (r \cdot min^{-1})$	30,000	$\mu (Pa \cdot s)$	

3.7. Program Correctness Verification

The structural parameters of the non-slotted rigid floating ring used in the literature [29] are selected to verify the correctness of the flow field calculation program. The comparison results obtained when the eccentricity is 0.5 and the inlet pressure is 0.20 MPa are shown in Figure 5. The results of the two calculations are similar, which verifies the correctness of the calculation procedure in this study.



Figure 5. Computational program verification [29].

4. Results

4.1. Distribution of the Gas Film Thickness and Gas Film Pressure

Using the parameters listed in Tables 1 and 2 for calculation, the thickness and pressure distribution of the gas film are obtained as shown in Figures 6 and 7, respectively. As can be seen, the minimum thickness of the gas film is attained at the pressure outlet position of $\theta = 180^{\circ}$. The pressure of the gas film is subject to a combination of the dynamic pressure effect and the wedge effect, and the pressure gradually decreases along the axial direction from the inlet until it reaches the ambient atmospheric pressure at the outlet of the sealing end face. Negative pressure appears near the higher region of the gas film pressure. Both the squeezing effect of the positive pressure and the adsorption effect of the negative pressure cause deformation of the bump foil.

Additionally, it can be seen from the pressure data in Figure 7 that the maximum pressure peak is 0.29 MPa for the circular texture, and the peaks of the maximum pressure for different textures are ordered from largest to smallest as: circle > square > diamond > ellipse > inverted triangle > triangle. The minimum pressure valley is 0.09 MPa for elliptical texture, and the valleys for different textures are ordered from smallest to largest as: ellipse < diamond < square < circle < inverted triangle < triangle. Figure 7c,f show that the triangular texture is a "narrow-to-wide" divergent texture while the inverted triangular texture is a "wide-to-narrow" convergent texture. After the gas flows into the inverted triangular micro-pit, it expands and slows down initially; then, owing to the sharp reduction of the flow channel, the direction of the velocity suddenly changes quite abruptly, and a large secondary dynamic pressure effect is formed when the gas flows out of the micro-pit. As can be seen, the directionality of the texture affects the pressure distribution even if the texture areas are equal. By contrast, the circular texture in Figure 6a and the square texture in Figure 6d, which correspond to a more regular shape, do not significantly change the velocity direction. For the elliptical texture in Figure 6b and the diamond-shaped texture in Figure 6e, the length in the axial direction is greater than that in the circumferential direction, which has a certain diversion effect.



Figure 6. The thickness of the gas film with (**a**) circular texture (**b**) elliptical texture (**c**) triangular texture (**d**) square texture (**e**) diamond-shaped texture and (**f**) inverted triangular texture.



Figure 7. The pressure of the gas film with (**a**) circular texture (**b**) elliptical texture (**c**) triangular texture (**d**) square texture (**e**) diamond-shaped texture and (**f**) inverted triangular texture.

4.2. Analysis of the Static Characteristics

As can be seen from Figure 8a,b, with the linear increase in rotational speed, the gas dynamic pressure effect is enhanced and the gas film force increases significantly. However, the accelerated Couette flow does not have a significant effect on the flow in the axial direction. Hence, the mass leakage rate does not change with the change of rotational speed: the mass leakage rate of the elliptical texture is the largest and its value is maintained close to $9.87 \times 10^{-4} \text{ kg} \cdot \text{s}^{-1}$. Figure 8c graphically shows the relationship between attitude angle and rotational speed. The attitude angles of the six texture types all show a decreasing trend as the rotational speed increases. A smaller attitude angle can make the operation of the sealing system more stable; thus, the higher the rotational speed, the better the stability of the compliant foil gas seal. Furthermore, it is found that when the rotational speed is 60,000 r ·min⁻¹, the minimum attitude angle of the triangular textures is 12.45°. In addition, as can be seen from the data in Figure 8d, when the rotational speed increases linearly, the viscous friction force also increases close to linearly because the speed gradient in the thickness direction of the gas film increases with the increase in rotational speed and the frequency of friction between the fluid layers.



Figure 8. (a) Description of force with rotational speed. (b) Description of leakage with rotational speed. (c) Description of attitude angle with rotational speed. (d) Description of friction with rotational speed.

As shown in Figure 9a,b, as texture depth increases, the gas film forces of the six textures all show a decreasing trend, and the mass leakages present a linear increasing trend. The gas film force and mass leakage rate of the elliptical texture change with the fastest speed, followed by the square texture. When $h_c < 5 \,\mu$ m, the gas film force and mass leakage of the circular texture exceed those of the diamond-shaped texture, whereas when $h_c \ge 5 \,\mu$ m, the situation is reversed, which implies that when the depth of the textures increases, the diversion effect is disadvantageous because the effect of the increasing gas film thickness is more obvious in a low-pressure environment. When the texture depth

varies from 1 to 11 μ m, the gas film force of the inverted triangle and triangle are close and show the best ranking of the gas film force. However, the leakage rate of the triangle is not as good as that of the inverted triangle, and the difference is more obvious with the greater texture depth. This implies that the mass leakage rate is more sensitive to the divergence and convergence of the texture, and the fully divergent texture type is not conducive to reducing the mass leakage rate.

It can be seen from Figure 9c that as the texture depth increases, the attitude angle increases for different types of texture. The attitude angle of the elliptical texture is always larger than that of others, and the value of the inverted triangle is the smallest. The greater the texture depth, the more obvious the attitude angle difference of different textures is. When $h_c \ge 9 \mu m$, the attitude angle of the diamond-shaped texture exceeds that of the square texture, while the fluctuation of the inverted triangular texture tends to be gentle. It can be seen from Figure 9d that as texture depth increases, the viscous friction force of air film decreases. Compared with the other texture types, the elliptical texture has the largest cross-section and increasing the texture depth can rapidly increase the volume of the micro-pits, thereby considerably increasing the thickness of the gas film in the overall range. Thus, the viscous friction force of the elliptical texture is the most affected by the texture depth, i.e., it is reduced by 38.31%. By contrast, the viscous friction of the triangular texture is the least influence, i.e., it decreases by 16.66%.



Figure 9. (a) Description of force with depth; (b) Description of leakage with depth; (c) Description of attitude angle with depth; (d) Description of friction with depth.

4.3. Analysis of the Dynamic Characteristics

Figure 10a,c show the variation of the direct dynamic coefficients with different rotational speeds. Specifically, k_{xx} of the six texture types is positive and decreases as rotational speed increases, whereas k_{yy} is negative and increases gradually. When the speed varies 10,000 and 20,000 r·min⁻¹, the range of change of direct stiffness coefficient is large, however, it becomes smaller once the speed exceeds 30,000 r·min⁻¹, which indicates that the

direct stiffness coefficient is easily affected by the speed variation in the low-speed range and prone to instability. The changes in the direct damping coefficients have an approximate trend; as the speed increases, c_{xx} and c_{yy} monotonically increases from a negative value to a positive value. Regardless of the texture type, when the speed is less than 30,000 r·min⁻¹, the rate of increase of c_{xx} and c_{yy} is higher. Once this speed is exceeded, the fluctuation of the direct damping gradually becomes smaller; it eventually remains flat, and the magnitude decreases to zero.

As can be seen from Figure 10b,d, the distributions of the cross dynamic characteristic coefficients are mutually symmetrical. As the speed increases, the sum of cross damping of the different texture types has different degrees of convergence, and the value keeps approaching zero, indicating that the cross damping does not need to dissipate more energy; thus, the speed increases to make the sealing system stable. As increasing the rotational speed in the low-speed range significantly improves the dynamic pressure effect, when the rotational speed exceeds a certain value, the dynamic pressure effect decreases, resulting in a larger difference in the cross-damping coefficients when the rotational speed is less than $30,000 \text{ r}\cdot\text{min}^{-1}$.



Figure 10. (a) Description of k_{xx} and k_{yy} with rotational speed; (b) Description of k_{xy} and k_{yx} with rotational speed; (c) Description of c_{xx} and c_{yy} with rotational speed; (d) Description of c_{xy} and c_{yx} with rotational speed.

Figure 11 shows the influence of the texture depth on the dynamic characteristics. Owing to the change in the texture depth, the Couette flow and Poiseuille flows of the gas between the sealing interfaces are changed. The change in the fluid pressure distribution causes the changes in foil deformation; the thickness of the gas film changes accordingly, and the complexity of the flow field is enhanced. Therefore, when the texture depth changes, the dynamic characteristics fluctuate considerably. Figure 11a,b show the relationship between the stiffness coefficient and the texture depth for different texture types; k_{yy} gradually increases with the increase of texture depth, and elliptical, triangular, and inverted triangular textures have the maximum positive k_{xx} at $h_c = 9 \mu m$, after which the value drops sharply. The distributions of k_{xy} and k_{yx} are still symmetrical. Except for the triangular texture, the sum of the cross stiffnesses of the others is basically stable.

From Figure 11b,c, when the texture depth increases, c_{xx} of all textures decreases continuously. It is found by calculation that when the texture depth increases from 1 to 9 µm, the sum of direct damping shows an initially decreasing and subsequently increasing trend. According to the principle of energy, the difference of the cross stiffness has a positive impact on the vortex motion, whereas the sum of direct damping has a negative impact; therefore, the smaller the difference of the cross stiffness, and the greater the sum of the direct damping, the faster the convergence of the vortex motion, and the better the stability of the film. Thus, there is a high probability of instability when the texture depth exceeds 9 µm.



Figure 11. (a) Description of k_{xx} and k_{yy} with depth; (b) Description of k_{xy} and k_{yx} with depth. (c) Description of c_{xx} and c_{yy} with depth; (d) Description of c_{xy} and c_{yx} with depth.

5. Discussion

Compliant foil gas seals are mainly applied under high-speed conditions. The theoretical model in this paper cannot take into account high-speed gas effects such as inertial effect, obstructed flow effect, and turbulent flow effect. Additionally, the coupling of multiple effects on the sealing properties of compliant foil gas seals cannot be characterized by this research. In the future, the above deficiencies need to be improved by revising the theoretical model, which is of great significance for accurately predicting the sealing performance of ultra-high-speed compliant foil gas seals.

6. Conclusions

In this paper, considering the specific structure of the compliant foil gas seal, as well as the stiffness and damping of the bump foil, the micro-scale dynamic lubrication equations of the synchronous circular motion of gas and the rotor in the cylindrical coordinate system are obtained. Then, the finite difference method and the iterative method are used to solve the thickness and deformation equations simultaneously, following which, the static and dynamic sealing characteristics corresponding to different micro-texture shapes are obtained. The analysis results are as follows:

(1) Micro-textures machined on the surface of flat foil create local pressure rise regions within a stable flow field. Owing to the difference in the texture shape characteris-

tics and directionality, the gas film thickness and pressure distribution of different compliant foil gas seals are different.

- (2) As the rotational speed increases, the force and the viscous friction force increase and the attitude angle decreases; however, the effect of the rotational speed on the mass leakage rate is negligible. Thus, the compliant foil gas seal shows good usability under low pressure and high-speed conditions.
- (3) Stiffness coefficients k_{xy} and k_{yx} and cross damping coefficients c_{xy} and c_{yx} are symmetrical. This reflects the circularity and quasi-symmetry of the flow field distribution as well as conform to the structural law of the compliant foil gas seal. Moreover, according to the dynamic parameters, the texture depth can be selected within the range of less than 9 μ m to ensure stability.
- (4) Among the six typical texture shapes, the elliptical texture has the smallest gas film force and the largest mass leakage rate, which is the most unfavorable to the static sealing performance. The gas film force of the triangle and the inverted triangle are basically the same, but the inverted triangular texture can control the mass leakage rate and improve stability, thus showing the best comprehensive sealing performance.

This article selects the optimal shape and depth of micro-textures for compliant foil gas seals, and the results can guide the experimental testings and application of sealing surface modification. Furthermore, the image recognition technology used in this study provides implications for the complex interface design of friction pairs.

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