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# **CBR Predictive Models for Granular Bases Using Physical and Structural Properties**

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Abstract: The California bearing ratio (CBR) test evaluates the structure of the layers of pavements. Such a test is laborious, time-consuming, and its results are generally affected by sample disturbance and tests conditions. The main objective of this research was to build a numerical model for the prediction of CBR tests that might substitute laboratory tests. The model was based on structural and physical parameters of granular bases. Four different materials from the central region (Querétaro) and north (Mexicali) of Mexico were used for the experimental work. Using the above-mentioned materials, 36 samples were fabricated, and six of them were used for the evaluation of the model presented in this research. Numerical and experimental comparisons demonstrated the adequacy of the model to predict the result of CBR tests from soil parameters.

**Keywords:** CBR; predictive models; granular bases

### 1. Introduction

The pavement is a structure formed by several soil layers designed to provide and maintain a smooth surface for several applications. It requires supporting and distributing the stresses as well as minimizing permanent deformations on it. In general terms, the structure is formed by the main pavement layer, the base, and the sub-base, which are built on a prepared subgrade surface [1,2]. In addition, the pavement structure can be constructed using reinforced concrete or simply asphalt emulsion.

Among the main factors affecting the performance and quality of pavements are the mechanical and hydraulic characteristics of materials employed for each layer, climatic conditions, equipment and technology used in the site, and the skills of workmen involved in the construction. Due to these and other factors, it is complicated to provide quality control schemes in the field of engineering of pavements [3]. Hence, it is important to check and verify certain parameters used in pavements during their construction. Otherwise, the predictions made for the durability and serviceability of pavements will not be realistic, affecting the costs of maintenance and rehabilitation [4]. The design of pavements requires the knowledge of soil mechanics and specifically the behavior of compacted soils. This discipline establishes the laboratory and field tests required to evaluate the quality of compacted layers as well as the needed conditions in terms of durability and serviceability of a pavement subjected to certain loading conditions. In general, field and laboratory tests must meet the following requirements: (a) simple and standardized, (b) swift, (c) easy to interpret, and (d) use inexpensive tools easy to calibrate and use [5].

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It is well-documented in the literature that granular soils are the most common materials used for the construction of bases for pavements [2]. These soils can be mixed with lime, asphalt, or other chemical products to increase its strength and reduce deformations [2]. Then, granular compacted soil layers are stiff, with large hydraulic conductivity, and show low deformations when subjected to cyclic loading [6]. When such materials are not well-compacted, or the strength of aggregates is deficient, fissuring and large permanent deformations occur on the pavement. Because of this and some other reasons, granular materials used on bases and subbases of pavements require a previous and rigorous evaluation. One of the tests employed for this purpose is the California bearing ratio (CBR) test [7]. Although pavements design has evolved in the past fifteen years, and CBR tests have been displaced by cyclic triaxial tests to define the resilient modulus of soil, these last tests are time-consuming and require specialized and expensive equipment. This is one of the reasons why CBR tests are still in use, especially in developing countries [8].

In general, the CBR test is a strength index used for the design of pavements that provides the structural capacity of the different layers of soil employed in the construction of bases, subbases, and subgrades. It can be described as a loading-deformation test that can be performed in the field or laboratory. The results of such a test are used to define the thickness of the different layers of a paved surface, depending on the loading conditions. This value depends on the compaction method and the type of soil. For the supervision of the quality of compacted layers on the field, it is normal to perform these tests on unsaturated soil samples [9,10]. In addition, it is important to mention that the CBR test is frequently time-consuming and burdensome. Its results are affected by soil disturbance and test conditions [5]. Because of this, it is important to implement models that are both reliable and easy to use. If properly generated, the models presented in this research may substitute or complement the CBR tests. Hence, such models are based on correlations between physical and structural properties.

It is well-known that different models have been developed to predict the results of the CBR test. Some models are based on compressibility of the material, the dry lose weight volumetric, and the optimum water content. However, their results are mostly unsatisfactory. Other models use the soil properties, such as the plastic index, gradation, and soil compressibility. The results of such models are complex, presenting low precision because of an inadequate weight on the properties of the soil [11,12].

In this paper, the proposed model had been built from the results of CBR tests performed on four different materials obtained from two cities of Mexico: (1) Querétaro in the central part, and (2) Mexicali on the north. These two different materials were used to verify the applicability of the model for different soils as climatic conditions influence the physical properties of soils [3]. In summary, the main objective of this research was to generate a general, precise, and reliable mathematical model that could simulate the results of the CBR test. First, the gravimetric and volumetric parameters of both materials were obtained. Then, several CBR tests were performed, and the results of them were correlated with the parameters of the soil. Afterward, different models were tested using the proposed correlations. Finally, the results of the different models were compared with the results of real CBR tests, demonstrating the potential benefits of the proposed models. In this sense, the new aspects and contributions of the CBR models presented in this research to the literature remain in the introduction of mathematic expressions that can be used in the pavement engineering area to save time and effort when carrying out the widely-used CBR tests.

## 2. Materials and Methods

Characteristics of Tested Materials

Material 1 was obtained from a quarry in the city of Querétaro, while materials 2, 3, and 4 were obtained from the city of Mexicali. Samples from both cities were extracted according to the recommendations reported in the ASTM D75 Norm [13], and also, the process documented in the norm ASTM C702/C702M-11 was followed [14]. The location and geological characteristics of the above-mentioned materials are summarized in Table 1.

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T ('	Outaver	Coordinate	s UTM (m)	- Origin of Rock	Type of	T	Classification	
Location	Quarry	North		Material	Treatment	USCS		
Querétaro	1	2281062.80	363855.13	Igneous basic extrusive	Basalt	Total crushing and sieving	GW-GM y SM	
	2 36030	3603070.10	629274.95	Sedimentary	Clastic	Partial crushing and sieving	SP	
Mexicali	3	3573429.00	657540.00	Sedimentary	Clastic	Partial crushing and sieving	GW	
-	4	3568274.44	657006.26	Sedimentary	Clastic	Partial crushing	GP	

Table 1. Location and geological characteristics of the rocks, treatment, and classification of the soils.

USCS: unified soil classification system; GW: well-graded gravel; GM: silty gravel; SM: silty sand; SP: poorly graded sand; GP: poorly-graded gravel; GW-GM: well-graded gravel with silt.

In the condition received from the quarry, Table 2 presents some of the main characteristics of the materials studied in this research. The CBR values corresponded to samples compacted at the optimum water content, resulting from the Modified Proctor compaction tests. Besides, for their classification, the following 6 tests were performed: (1) consistency limits according to standard ASTM D4318-05 [15], (2) dry loose volumetric mass according to standard M-MMP-1-08/03 [16], (3) relative density of solids according to standard ASTM C127-12 [17], (4) modified Proctor compaction test according to standard ASTM D1557-09 [18], (5) CBR test according to standard ASTM D1883-07 [19], and (6) water content according to standard ASTM D2216-10 [20].

**Table 2.** Main characteristics of samples from the different quarries.

		Modified Proctor Compaction Test										
Quarry	LL (%)	DI (0/ )	LVW (kg/m³)	SD Ss	Direct V	Direct Values		Corrected Values		CE	CBR (%)	USCS
		PI (%)	v. gr	55	γ <sub>d</sub> (kg/m <sup>3</sup> )	w <sub>opt</sub> (%)	γ <sub>d</sub> (kg/m <sup>3</sup> )	w <sub>opt</sub> (%)	w (%)	(kN*m/m <sup>3</sup> )		
1	27	12	1772	2.75	2240	8.0	2314	6.9	8.3	2692	111	GW-GM
2	-	-	1811	2.63	2230	5.3	2272	4.4	5.3	2642	86	SP
3	-	-	1681	2.63	2162	2.6	2294	1.6	2.6	2642	92	GW
4	-	-	1704	2.64	2304	5.9	2346	4.4	5.9	2645	139	GP

LL: liquid limit; PI: plastic index; LVW: loose volumetric weight; SD: specific density;  $\gamma_d$ : dry specific density;  $w_{opt}$ : optimum water content; w: water content; CE: compaction energy.

For the thirty-six different samples, their grain size distribution was obtained. Also, the main volumetric and gravimetric parameters for these samples were obtained, as well as the results of the CBR test. Seven different samples were tested from quarry 1 (samples 1 to 7). These samples were prepared with different grain sizes distributions and water contents. In this way, sample 1 showed the original grain size distribution of the quarry. The grain size distribution for samples 2, 3, and 4 was modified to produce samples with 50% gravel and 50% sand. Samples 5, 6, and 7 only contained sand. Samples with different characteristics were prepared from quarries 2, 3, and 4:10 for quarry 2, 9 for quarry 3, and 10 for quarry 4 (samples 8 to 36). Samples from the same quarry presented similar grain size distributions. Figure 1 shows the grain size distribution for the different samples according to standard ASTM C136-06 [15].

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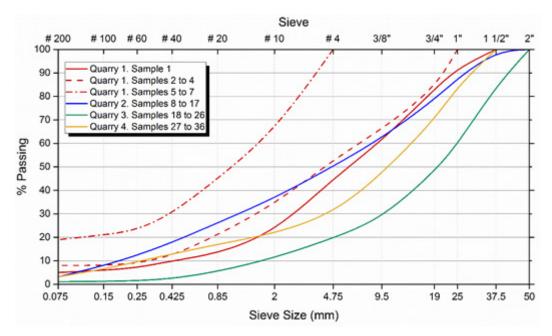


Figure 1. Grain size distribution for the samples.

Some samples were compacted according to the Modified Proctor compaction method and considering different water contents. Other samples were prepared using different compaction energies (CE) with the purpose of analyzing its effect on the CBR results. For such samples, the number of blows was modified. Thus, samples 1 to 4 from quarry 1, samples 8 to 11 from quarry 2, samples 18 to 21 from quarry 3, and samples 27 to 31 from quarry 4 were compacted according to the Modified Proctor compaction method, and the samples 5 to 7 from quarry 1, 12 to 17 from quarry 2, samples 22 to 26 from quarry 3, and samples 32 to 36 from quarry 4 were compacted with the same equipment and procedure but applying a different number of blows. The compaction energy and water content for each sample are summarized in Table 3.

In addition to the main characteristics of the different samples, their volumetric and gravimetric parameters after compaction were obtained according to the procedures established by [21]. Such parameters are shown in Table 3 and include the volumetric weight  $(\gamma_m)$ , the volumetric weight of solids  $(\gamma_s)$ , the specific density of solids  $(s_s)$ , the relative density  $(C_r)$ , the void ratio (e), the porosity (n), the degree of saturation  $(G_w)$ , the degree of concentration of air  $(G_A)$ , the volumetric water content  $(\theta)$ , the degree of compaction with respect to dry volumetric weight from a compaction test  $(G_C)$ .

The low CBR values of some samples from the same quarry were related to their low compaction energy. Therefore, CBR values were influenced by both the grain size distribution and compaction energy.

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**Table 3.** Volumetric and gravimetric parameters of soil samples.

							Gravi	metric					Volu	netric		
Quarry	CE (kN-m/m <sup>3</sup> )	Sample	$\gamma_d$ (kg/m <sup>3</sup> )	CBR (%)		(kg/m <sup>3</sup> )			(0	%)				(%)		
	( ,, ,		J	(70)	$\gamma_{\rm s}$	γd	$\gamma_{m}$	S <sub>s</sub>	w	C <sub>r</sub>	e	n	$G_{w}$	Ga	θ	G <sub>c</sub>
	2692	1	1772	111	2753	2208	2391	2.75	8.3	93	0.25	20	92	7	18.4	95
	2676	2	1759	184	2757	2217	2327	2.76	4.9	83	0.24	20	55	44	10.9	97
	2690	3	1759	178	2757	2241	2394	2.76	6.8	91	0.23	19	81	18	15.2	98
1	2673	4	1759	147	2757	2197	2349	2.76	7.9	82	0.25	20	74	25	15.2	108
	786	5	1616	98	2810	2041	2226	2.81	8.5	100	0.38	27	67	32	18.5	100
	601	6	1616	49	2815	1957	2091	2.81	6.8	80	0.44	30	43	56	13.4	96
	602	7	1616	28	2815	1986	1986	2.81	5.0	87	0.46	32	29	70	9.5	100
		8	2158	72	2634	2158	2248	2.63	4.2	83	0.22	18	50	50	9.0	83
	2642	9	2230	86	2634	2230	2348	2.63	5.3	100	0.18	15	77	23	11.7	100
	2042	10	2192	72	2634	2192	2333	2.63	6.4	91	0.20	17	84	16	14.1	91
		11	2144	43	2634	2144	2326	2.63	8.5	79	0.23	19	98	2	18.2	79
2		12	2090	55	2634	2090	2198	2.63	5.2	83	0.26	21	53	47	10.9	83
		13	2118	53	2634	2118	2243	2.63	5.9	91	0.24	20	64	36	12.6	91
	1179	14	2146	64	2634	2146	2288	2.63	6.6	100	0.23	19	77	23	14.2	100
	1179	15	2122	56	2634	2122	2274	2.63	7.1	93	0.24	19	78	22	15.1	93
		16	2076	41	2634	2076	2257	2.63	8.7	79	0.27	21	85	15	18.1	79
		17	2084	26	2634	2084	2295	2.63	10.2	81	0.26	21	102	-2	21.2	81
		18	2104	72	2627	2104	2132	2.63	1.4	88	0.25	20	14	86	2.8	88
	2642	19	2138	86	2627	2138	2184	2.63	2.1	95	0.23	19	25	75	4.6	95
	2042	20	2162	92	2627	2162	2217	2.63	2.6	100	0.22	18	32	68	5.6	100
2		21	2132	79	2627	2132	2201	2.63	3.2	94	0.23	19	37	63	6.9	94
3		22	2028	47	2627	2028	2046	2.63	0.9	90	0.30	23	8	92	1.9	90
		23	2054	62	2627	2054	2091	2.63	1.8	97	0.28	22	17	83	3.7	97
	1179	24	2062	56	2627	2062	2110	2.63	2.3	99	0.27	22	22	78	4.8	99
		25	2066	59	2627	2066	2137	2.63	3.4	100	0.27	21	33	67	7.0	100
		26	2048	57	2627	2048	2139	2.63	4.5	95	0.28	22	42	58	9.2	95
		27	2196	110	2642	2196	2241	2.64	2.1	82	0.20	17	27	73	4.6	82
		28	2198	93	2642	2198	2277	2.64	3.6	82	0.20	17	47	53	7.9	82
	2645	29	2256	103	2642	2256	2365	2.64	4.8	92	0.17	15	75	25	10.9	92
		30	2304	139	2642	2304	2441	2.64	5.9	100	0.15	13	107	-7	13.6	100
4		31	2294	130	2642	2294	2453	2.64	6.9	98	0.15	13	120	-20	15.8	98
		32	2142	74	2642	2142	2201	2.64	2.7	84	0.23	19	31	69	5.9	84
		33	2132	72	2642	2132	2201	2.64	3.2	82	0.24	19	36	64	6.9	82
	1181	34	2154	89	2642	2154	2243	2.64	4.1	86	0.23	18	48	52	8.9	86
		35	2210	102	2642	2210	2339	2.64	5.8	97	0.20	16	79	21	12.9	97
		36	2226	96	2642	2226	2384	2.64	7.0	100	0.19	16	100	0	15.7	100

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#### 3. Results

In order to define which gravimetric and volumetric parameters have the largest influence on the values of CBR tests, dispersion graphics were used, and a tendency line was plotted for different parameters. This task was performed by plotting the coefficient  $R^2$ , which indicated the reliability or accuracy of the correlation. In other words, the more  $R^2$  coefficient approached unity, the more reliable or accurate was the correlation. Table 4 summarizes the values of coefficient  $R^2$  for each one of the volumetric and gravimetric parameters described in Table 3 with respect to the thirty-four CBR tests.

It could be observed that the values of coefficient R<sup>2</sup> showed low values for all volumetric and gravimetric parameters of the soil. This means that not only a single parameter was influencing the CBR values but a combination of them. Also, different parameters affected CBR values, depending on the type of soil. For this reason, different equations were developed, depending on the type of material.

Gravimetric Volumetric Quarry Sample CE C<sub>r</sub>.  $G_{w}$  $G_a$  $G_C$  $\gamma_s$  $\gamma_{\rm m}$ 0.545 0.402 0.096 0.004 0.024 0.197 0.205 0.083 0.083 0.013 0.041 1 - 360.096 0.355

**Table 4.** Values of coefficient R<sup>2</sup> for the thirty-six CBR tests related to different parameters.

Due to the nature of the soils tested, five groups of correlation analyses were performed for the different samples according to their classification: (1) samples with classification GW-GM and GP, (2) samples with classification SP, (3) samples with classification GW, (4) samples with classification GP, and (5) the combination of samples with classification GW or GP. Only these groups were created since the samples tested belong to such soil classifications. In order to develop other correlation analyses of materials with different soil classifications, it is necessary to perform tests on other materials with different graduation than those analyzed in this research.

Table 5 shows the results of coefficient R<sup>2</sup> for the correlations, considering individually each one of the fourteen parameters for each group. Figure 2a–e shows these correlations.

USCS	Gravimetric (g/cm <sup>3</sup> )							Volumetric (%)					
	Υs	$\gamma_d$	γm	S <sub>s</sub>	w	C <sub>r</sub>	e	n	$G_{w}$	Ga	θ	G <sub>C</sub>	CE
GW-GMSM	0.6470	0.8312	0.7758	0.7291	0.9145	0.2552	0.8631	0.8540	0.3929	0.3929	0.0393	0.0159	0.7573
SP		0.7293	0.0634		0.7030	0.4540	0.7293	0.7293	0.2744	0.2744	0.6454	0.4486	0.3166
GW		0.9682	0.7999		0.0037	0.0201	0.9666	0.9675	0.0934	0.0934	0.0118	0.0201	0.8124
GP		0.8556	0.7118		0.3094	0.4461	0.8527	0.8556	0.5442	0.5442	0.3532	0.4455	0.4796
GW and GP	0.4612	0.9317	0.8522	0.4612	0.4315	0.0101	0.9346	0.9384	0.6336	0.6336	0.4814	0.0008	0.3571

**Table 5.** Coefficient R<sup>2</sup> for the correlations of CBR values and soil parameters for different materials.

In general, the parameters presenting the largest correlations with the CBR test are the dry volumetric weight ( $\gamma_d$ ), the water content (w), and the void ratio (e). These correlations could be observed in Figure 2a. For materials GW-GM and SM, a linear relationship with  $\gamma_d$  could be observed with  $R^2 = 0.83$ . For w, a polynomial correlation was observed with  $R^2 = 0.91$ . For e also, a linear relationship was observed with  $R^2 = 0.86$ .

In the case of the materials SP, CBR values correlated linearly with parameters  $\gamma_d$  with  $R^2 = 0.73$ ; w with  $R^2 = 0.7$ ; e and n with  $R^2 = 0.73$ . Also, for materials GW, CBR values correlated linearly with the following four parameters: (1)  $\gamma_d$  with  $R^2 = 0.97$ , (2)  $\gamma_m$  with  $R^2 = 0.79$ , (3) e with  $R^2 = 0.96$ , and (4) n with  $R^2 = 0.96$ . Figure 2c illustrates these correlations. Materials GP showed also linear relationships with the following parameters  $\gamma_d$ , e, and n with  $R^2 = 0.85$  and  $\gamma_m$  with  $R^2 = 0.71$ . These correlations are shown in Figure 2d. The combination of the materials with classification GW and GP showed correlations with parameters  $\gamma_d$  with  $R^2 = 0.93$ ;  $\gamma_m$  with  $R^2 = 0.85$ ; e and n with  $R^2 = 0.93$ . Such correlations are shown in Figure 2d.

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From the results summarized in Table 5, it could be observed that water content influenced the results of sandy soils (materials SP). The largest correlations of parameters  $\gamma_d$ , e, n, and  $\gamma_m$  were obtained for gravels (materials GW and GP), while the lower for sandy materials. As the parameter w might show seasonal variations during the dry and wet season, also CBR values might be subjected to these seasonal variations.

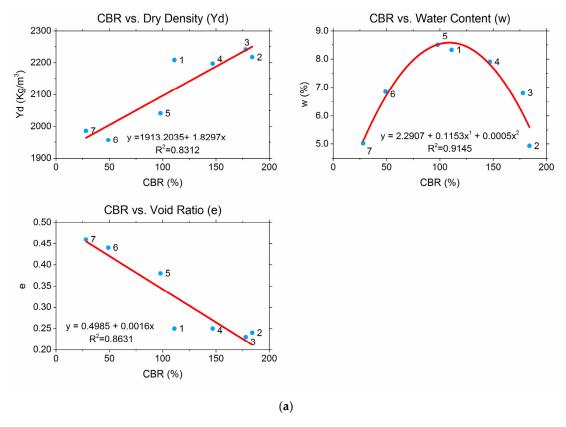
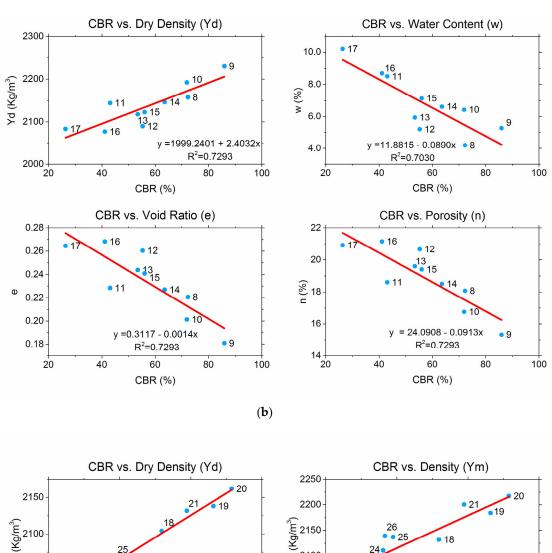


Figure 2. Cont.

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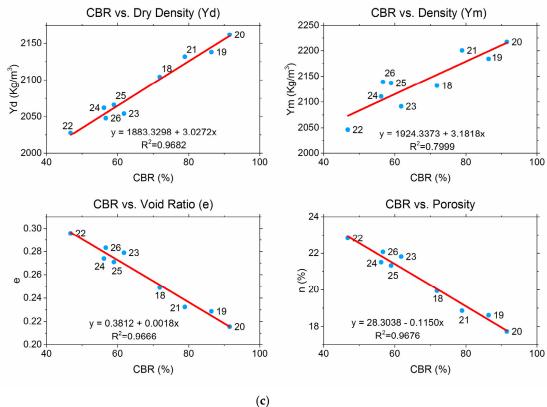
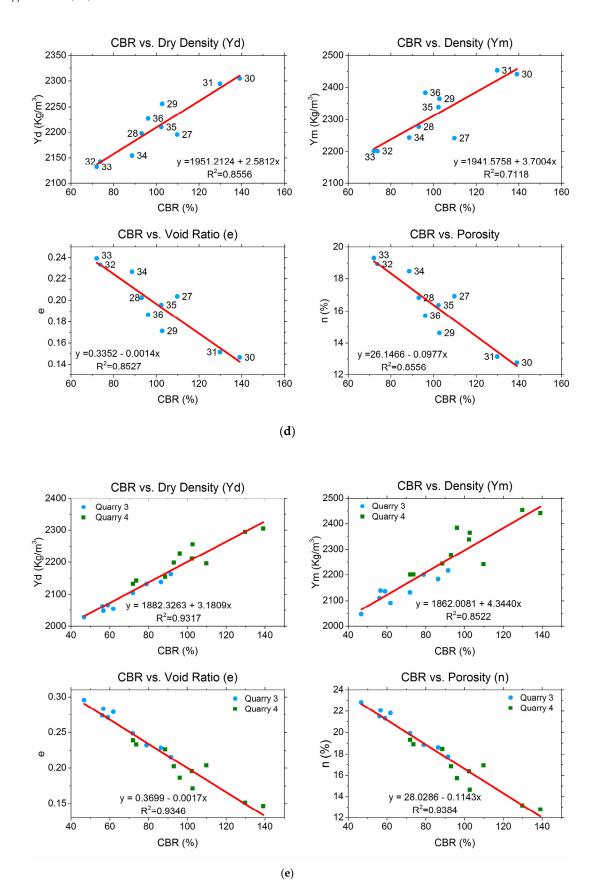


Figure 2. Cont.

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**Figure 2.** Parameters influencing California bearing ratio (CBR) values: (a) materials GW with  $\gamma_d$ , w, and e; (b) materials SP with  $\gamma_d$ , w, e and n; (c) materials GW with  $\gamma_d$ ,  $\gamma_m$ , e, and n; (d) materials GP with  $\gamma_d$ ,  $\gamma_m$ , e and n; (e) combination of materials GW and GP with  $\gamma_d$ ,  $\gamma_m$ , e and n.

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#### 3.1. Regression Analysis

Regression analysis is a statistical method used to identify the relationship between dependent and independent variables. It provided the coefficients of the best fitting relationship between dependent and independent variables. In this case, CBR values represented the dependent variable, while soil parameters  $\gamma_d$ ,  $\gamma_m$ , w, and e represented the independent variables.

## 3.2. CBR Predictive Model

Table 6 shows the coefficients of the CBR predictive models for each type of soil obtained from the multi-linear regression analysis. For this technique, how the coefficient R<sup>2</sup> was obtained had no relevance, since this parameter was used to determine the level of influence on the CBR, so, it was valid to use multilinear regression analysis even though the coefficient R<sup>2</sup> of w was obtained by means of a polynomial function. Also, the linear multiple regression analysis yielded values for coefficients that made up equations whose variables are of degree 1 (linear). It could be observed that the standard deviation for material GP was larger when compared with the combination of models for GP and GW. For this reason, a model was proposed for both materials.

USCS	$\gamma_d(x_1)$	$\gamma_m (x_2)$	w	e	n	Constant	$\mathbb{R}^2$	Error	Standard Deviation
GW-GM SM	-0.6231		-9.5447	-1319.1924		1924.9925	0.9052	26.3470	3.7380
SP	1.6064		-5.3303	2462.2411	0	-3913.2472	0.9559	4.4894	1.7746
GW	0.5979	0.0024		469.4978	0	-1307.6738	0.9686	3.4216	2.4894
GP	13.9330	0.0667		4816.3003	292.0012	-36564.5609	0.8938	9.4288	2.4352
GW and GP	0.1856	-0.0551		-346.259	0	-113.4502	0.9256	6.8143	6.0547

**Table 6.** Coefficients of the predictive models for each type of soil.

In Table 6, it could be noticed that the predicted CBR values for gravels were closer to experimental results when the soil was clean with no traces of plastic soil. Therefore, four models had been established for the materials analyzed in this research. The four models (Equation (4)) could be used in materials GW or GP, but it was decided to apply only in GP materials since model 3 (Equation (3)) had greater reliability when applied to GW materials. Besides,  $\gamma_d$  was replaced by its equivalence (Equation (5)), where  $\gamma_0$  is the specific weight of distilled water (equal to 1 or an entire power of 10); n was eliminated; hence it is related to Equation (6).

Soils GW-GM and SM (plastic):

$$CBR = -0.6231 \frac{S_S}{1 + \omega S_S} \gamma_O - 9.5447w - 1319.1924e + 1924.9925 \tag{1}$$

For soils SP with no traces of plastic soils:

$$CBR = 1.6064\gamma_d - 5.3303w + 2462.2411e - 3913.2472$$
 (2)

For clean GW soils with no traces of plastic soils:

$$CBR = 0.5979 \frac{S_S}{1 + \omega S_S} \gamma_O + 0.0024 \gamma_m + 469.4978e - 1307.6738 \tag{3}$$

For soils GP with no traces of plastic soil:

$$CBR = 0.1856 \frac{S_S}{1 + \omega S_S} \gamma_O - 0.0551 \gamma_m - 346.259e - 113.4502 \tag{4}$$

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$$\frac{S_S}{1 + \omega S_S} \gamma_O \tag{5}$$

$$n = \frac{e}{1 + e} \tag{6}$$

The above-mentioned models were selected, depending on the soil classification, according to USCS. Hence, they required volumetric weight, void ratio, and water content of the compacted material according to the Modified Proctor test [18].

As previously mentioned, the precision of such models had been tested using six samples (37 to 42) of compacted material obtained from three different quarries. Samples 37 and 38 came from different quarries and were tested at the optimum water content, whereas samples 39 to 42 were compacted at a water content different from the optimum. For sample 41, the CBR test was performed at the maximum dry volumetric weight. Table 7 shows the CBR values obtained in the laboratory and those obtained with the corresponding predictive model according to the soil classification and the consistency limits.

Samples 39 and 42 showed the largest deviation from the experimental CBR value. This might suggest that Equation (1) was more accurate when it was applied to soils compacted at the maximum dry density. This was so because the model was built from samples compacted at the optimum level. In addition, the model applied to sample 38 showed a difference of 24, which was reasonable, considering the differences in materials coming from different quarries.

It is important to mention that the CBR predictive models could be applied to materials showing the same geologic conditions, mechanical parameters, and consistency limits. Thus, due to this important limitation, it is necessary to develop more models of prediction of CBR, particularly applicable to materials with different classifications than those analyzed in this research. In addition to the classification of soils, consideration should be given to the plasticity of the material.

Quarry	Sample	USCS	Consistency	Origin of Rock	Type	Model	CBF	R (%)	Difference
Quarry	Sample	USCS	Limits	Origin of Rock	туре	Model	Expl	Num	Difference
5	37	GW	Plastic	Igneous extrusive basic	Crushed	Equation (1)	160	164	4
6	38	GP	Non plastic	Igneous extrusive acid	Sieved	Equation (4)	110	104	4
	39	GW	Plastic			Equation (1)	111	174	63
7	40	GW	Plastic	- Igneous	Crushed	Equation (1)	175	180	5
/	41	GW	Plastic	extrusive basic	Crusnea	Equation (1)	170	180	10
	42	GW	Plastic	_		Equation (1)	124	176	52

**Table 7.** The precision of CBR predictive models.

#### 4. Discussion

The adequacy in developing CBR predictive models comes from the fact that laboratory tests need to be quick, easy, with no interference of the operator. The use of an analytical model to predict the result of CBR tests from simpler and current laboratory tests may yield in time-saving while keeping the same precision. In addition, it must be considered that the CBR values for a similar soil may be very diverse; such a variation depends on the number of combinations of the factors that define soil resistance. However, once results are obtained, certain correlations can be established to estimate the CBR value for a particular type of soil. Finally, it is important to mention that the CBR models presented in this paper might be restricted, in a certain way, to the physical conditions of the selected soil samples.

## 5. Conclusions

Based on the results presented in this paper, the following conclusions could be stated.

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• The predictive models for CBR tests were applied according to the classification of the considered soil. Four different CBR predictive models were obtained: for gravel and sand with some plasticity (GW-GM and SM); for sands (SP); for clean gravel (GW); and clean gravel well or poorly graded (GW or GP).

- For the development of the regression models, 14 parameters of the soil were considered.
- The more influencing parameters on the results of CBR tests were:  $\gamma_m$ ,  $\gamma_d$ , e, n, and w. The last parameter presented an important influence on plastic materials.
- The precision of the models presented in this research was tested using compacted samples from different quarries to those initially employed for the development of the models. In this sense, it was observed that Equation (1) was more precise for samples compacted at the optimum level. On the other hand, Equation (4) presented important differences to experimental results, which might come from the origin of the parent rock.

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