



Article Observer-Based Tracking Control for Polysolenoid Linear Motor with Unknown Disturbance Load

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Abstract: Linear motors have been playing a crucial role in mechanical motion systems due to its ability to provide a straight motion directly without mediate mechanical actuators. This paper investigates tracking control problems of Polysolenoid Linear Motor, which is a particular type of permanent magnet linear motor in a tubular structure. In order to deal with unmeasurable velocity, our method proposes a novel observer guaranteed asymptotic convergence of the observer errors. Then, based on observed velocity, our method proposes controllers for position-velocity and current tracking control concerning an unknown disturbance load problem by using Lyapunov direct method. The proposed controllers ensure that the position-velocity tracking error converges to arbitrarily small values by adjusting control parameters. Finally, the validity and effectiveness of our approach are shown in illustrative examples.

Keywords: observer-based control; polysolenoid linear motor; tracking control

1. Introduction

Linear Motor motion systems have been widely applied to fruitful applications in order to provide directed straight motions in which, unnecessary mechanical transmissions are excluded that results in better performance and lost-cost requirement of motion systems [1]. Recently, there has been a great deal of effort devoted to control design for linear motors in various topics including motion control theory [2,3], the planar motion of a nanopositioning platform [4], traction systems for subway [5] and jetting dispenser [6]. As a particular case, polysolenoid linear motor (PLM) belongs to the group of permanent magnet linear motor in tubular structure as shown in Figure 1. The motor has two phases corresponding to two separated windings working differently in 90° of electrical angle. The usage of PLM brings some beneficial properties such as the durable structure, low cost, and reliable operations according to an electromagnetic phenomenon with principles as shown in [7,8]. More recently, various research topics focus on control design for PLM such as model predictive control [9,10] and flatness based control structure [11].

Without the needs of any gearbox for motion transformation, the movement of linear motor systems become sensitive due to external impacts such as frictional force, changed load and non-sine of flux. The disturbance force impacts in both the longitudinal and in the transversal direction, which results in harmful effects to system performance. Over the past few years, there have been several kinds of research spending amounts of effort to deal with position tracking problems of linear motor systems in the presence of external disturbances. A neural network learning adaptive robust controller was designed by [12] to achieve both tracking performance and disturbance rejection. Besides, compensation approaches were proposed in researches [13–15], by which the frictional force and position-dependent disturbance are compensated to guarantee the stability of the overall system. The researches in [16–18] present effective sliding mode control methods for tracking control of the linear motor.

In the progress of disturbances rejection methods, sensorless control problems of a linear permanent-magnet motor have been received a lot of attention from fruitful researches including linear tubular motors [19,20], end-effects [21,22], position sensorless control [23,24]. Generally, for a class of permanent-magnet synchronous motor, almost all researches use back electromotive force (EMF), which are observed via currents and voltages, to estimate the velocity of the linear motor. As a matter of fact, at low and zero speed, the back electromotive force (EMF) voltage magnitude is very small, or zero, and this makes all the techniques based on the back EMF unsuccessful [25,26]. Besides, the main problems of the approach are disturbance impacts in currents and voltages. Furthermore, the variation in inductance parameters due to some main characteristics of the linear motor, such as end effect, may result in considerable estimation error. On the other hand, almost PLMs are packed with at least one position sensor, and Figure 2 describes the typical control scheme of PLM. However, when the sensors are affected by measurement noise, velocity is not obtained accurately by taking derivatives respect to specific interval time.



Figure 1. Structure of polysolenoid linear motor provided by [7,27].

Inspired by the above observations, this paper addresses tracking problems of Polysolenoid Linear Motor under unknown load disturbance effect. In the light of novel observer-based control approach, our research covers a realistic problem arsing when the velocity of PLM can not be measured by using directly position sensor can not be calculated by using data from position sensor. To summarize, our contributions can be highlighted as

- A novel velocity observer has been proposed such that the observer errors exponentially converge by utilizing the available position sensors attached in PLM. To be specific, based on Lyapunov theorem, the exponential convergence of observer errors has been proofed in a rigorous way. Furthermore, conditions for selecting parameters of the observer are provided as well as delay rate of the observer errors.
- From the observer, a position-velocity and current controllers are designed by Lyapunov direct method. Accordingly, the position or velocity tracking error converge to small arbitrary values by adjusting control parameters.

This paper is organized as follows. Section 2 establishes main problems and a mathematical model of the PLM in d - q axis. In Section 3, a novel velocity observer is proposed, and asymptotic

convergence of observer errors are proofed. Section 4 mainly describes position-velocity and current controller design. Section 5 illustrates the simulation results for verification of the proposed method. Finally, conclusions are summarized in Section 6.



Figure 2. Typical control scheme of polysolenoid linear motor.

2. Problem Statement

As mentioned above, the PLM has two separated windings *a*, *b* and is supplied by two AC voltage sources as follow

$$u_a(t) = U\cos(\omega t), \ u_b = U\sin(\omega t). \tag{1}$$

Further, angular electrical position of PLMs inducing in the windings has the relationship with the primary position, and electrical angular frequency can be expressed as

$$\theta(t) = \frac{n_p \pi}{\tau} x(t), \ \omega(t) = \frac{n_p \pi}{\tau} v(t).$$
(2)

By neglecting the friction terms in mechanical equation, let us take into account dynamic model of Polysolenoid Linear Motor (PLM) in d - q frame given in as follow

$$\frac{dx}{dt} = v(t),\tag{3}$$

$$\frac{dv}{dt} = \frac{2\pi\psi_p}{m\tau_p}i_q(t) - \frac{1}{m}f_\ell(t) - \frac{1}{m}f_m(t),\tag{4}$$

$$\frac{di_d}{dt} = -\frac{R_s}{L}i_d(t) + \left(\frac{2\pi}{\tau_p}v(t)\right)i_q(t) + \frac{1}{L}u_d(t),\tag{5}$$

$$\frac{di_q}{dt} = -\frac{R_s}{L}i_q(t) - \left(\frac{2\pi}{\tau_p}v(t)\right)i_d(t) - \left(\frac{2\pi}{\tau_p}v(t)\right)\frac{\psi_p}{L} + \frac{1}{L}u_q(t),\tag{6}$$

where $\tau_p = \frac{\tau}{n_p}$, $i_d(t)$, $i_q(t)$ are the direct and quadrature stator current; v(t), x(t) denote linear velocity and position of rotor; R_s , L represent for phase resistance, and stator inductances; ψ_p , m stand for the flux of the permanent magnet and mass of slider (rotor), respectively. The inputs of system are the direct and quadrature voltage which are denoted as $u_d(t)$, $u_q(t)$. Additionally, $f_\ell(t)$ is disturbance load and $f_m(t)$ represents for a combination of detent force (including cogging and ending force [28]) and the force generated by inductance fluctuation [29].

In what follows, let $x_r(t)$, $v_r(t)$, respectively, are stator's desired position and velocity of the PLM. This note aims to design a position-velocity controller, by which the actual position and velocity can track these references with small errors. It should be noted that the PLM in industrial applications

often does not include a velocity sensor. Unlike rotor rotation motors where velocity sensors can be easily employed by attaching in rotor shape, the velocity sensor equipment for PLM increases enormous additional cost, and it is difficulties in installing and restricted by environmental factors like temperature, humidity and vibration as well. Therefore, the paper develops a novel velocity observer that utilizes the available position sensors in PLM to estimate velocity. Furthermore, the proposed controllers also guarantee robust performance in the presence of unknown disturbance load variations. In views of control performance, the rotor angular position must track a reference trajectory $x_r(t)$. Additionally, to avoid reluctance effects and force ripple, $i_d(t)$ should track a constant direct current reference $i_{dr}(t) = 0$. The following sections present the observer and controller synthesis for position tracking of PLM.

3. Observer Design

To cover more realistic situations in industrial applications, we provide a velocity observer to deal with the velocity sensorless problem. For simplicity's sake, let $f(t) = \frac{1}{m}f_{\ell}(t) + \frac{1}{m}f_{m}(t)$. In this paper, we deal with the continuous disturbance f(t) such that

$$|f(t)| \le \overline{F}, \ |\dot{f}(t)| \le \overline{\delta F},\tag{7}$$

in which \overline{F} and $\overline{\delta F}$ are given positive constants. Let us provide the following observer as

$$\dot{x}(t) = \hat{v}(t) + h_1(x(t) - \hat{x}(t)),
\dot{v}(t) = \frac{2\pi\psi_p}{m\tau_p}i_q(t) + h_2(x(t) - \hat{x}(t)) + K \text{sign}(x(t) - \hat{x}(t)),$$
(8)

where h_1, h_2 , K are real positive constants. By denoting $\tilde{x}(t) = x(t) - \hat{x}(t)$ and $\tilde{v}(t) = v(t) - \hat{v}(t)$, the dynamics of observer errors are given by the combination of (3), (4) and (8):

$$\begin{aligned} \hat{\vec{x}}(t) &= -h_1 \tilde{x}(t) + \tilde{v}(t), \\ \hat{\vec{v}}(t) &= -h_2 \tilde{x}(t) - K \text{sign}(\tilde{x}(t)) - f(t). \end{aligned}$$
(9)

Theorem 1. For a given $\alpha > 0$, let K, h_1 , h_2 are positive constants satisfying

$$\begin{bmatrix} h_1 h_2 & 0 \\ 0 & h_1 \end{bmatrix} \ge 2\alpha \begin{bmatrix} h_2 + \frac{1}{2}h_1^2 & \frac{1}{2}h_1 \\ \frac{1}{2}h_1 & 1 \end{bmatrix},$$
(10)

$$\frac{Kh_1}{2} - \frac{h_1\overline{F}}{2} - \overline{\delta F} \ge 2\alpha(K + \overline{F}).$$
(11)

Then, the system (9) is exponentially stable. Furthermore, there exist β_1 , $\beta_2 > 0$ *such that*

$$|\widetilde{x}(t)| < \beta_1 e^{-\alpha t}, \ |-h_1 \widetilde{x}(t) + \widetilde{v}(t)| < \beta_2 e^{-\alpha t}.$$
(12)

Proof of Theorem 1. Letting $\eta_1(t) = \tilde{x}(t)$, $\eta_2(t) = -h_1\tilde{x}(t) + \tilde{v}(t)$ and $\eta(t) = [\eta_1(t), \eta_2(t)]^T$, then (9) can be rewritten as

$$\dot{\eta}_1(t) = \eta_2(t), \dot{\eta}_2(t) = -h_1 \dot{\tilde{x}}(t) + \dot{\tilde{v}}(t) = -h_1 \eta_2(t) - h_2 \eta_1(t) - K \text{sign}(\eta_1(t)) - f(t).$$
(13)

Consider the following function

$$V_o(t,\eta(t)) = \frac{1}{2}\eta_2(t)^2 + \left(\frac{h_2}{2} + \frac{h_1^2}{4}\right)\eta_1(t)^2 + K|\eta_1(t)| + f(t)\eta_1(t) + \frac{h_1}{2}\eta_1(t)\eta_2(t).$$
(14)

From the fact that $K > \overline{F}$, we have $K|\eta_1(t)| > |f(t)\eta_1(t)|$. Then, $V_o(t, \eta(t))$ is a positive real function, and especially it has $V_o(t, 0) = 0$, $V_o(t, \eta(t)) > 0 \forall \eta(t) \neq 0$, and $V_o(t, \eta(t)) \rightarrow \infty$ as $||\eta(t)|| \rightarrow \infty$. Hence, the time derivative of the Lyapunov function (14) along the solution of (13) is given by

$$\begin{split} \dot{V}_{o}(t,\eta(t)) &= \eta_{2}(t)\dot{\eta}_{2}(t) + \left(h_{2} + \frac{h_{1}^{2}}{2}\right)\eta_{1}(t)\eta_{2}(t) + K\eta_{2}(t)\mathrm{sign}\left(\eta_{1}(t)\right) + f(t)\eta_{2}(t) + \dot{f}(t)\eta_{1}(t) \\ &+ \frac{h_{1}}{2}\eta_{2}(t)^{2} + \frac{h_{1}}{2}\eta_{1}(t)\dot{\eta}_{2}(t) \\ &= -\frac{h_{1}}{2}\eta_{2}(t)^{2} + \dot{f}(t)\eta_{1}(t) + \frac{h_{1}}{2}\eta_{1}(t)\left(-h_{2}\eta_{1}(t) - K\mathrm{sign}\left(\eta_{1}(t)\right) - f(t)\right) \\ &= -\frac{h_{1}}{2}\eta_{2}(t)^{2} - \frac{h_{1}h_{2}}{2}\eta_{1}(t)^{2} + \eta_{1}(t)\left(-\frac{Kh_{1}}{2}\mathrm{sign}\left(\eta_{1}(t)\right) - \frac{h_{1}}{2}f(t) + \dot{f}(t)\right). \end{split}$$
(15)

Recalling *K* in Lemma 1 and (7), it is worth remarking that

$$\frac{Kh_1}{2} > \frac{h_1\overline{F}}{2} + \overline{\delta F} > \left|\frac{h_1}{2}f(t) - \dot{f}(t)\right|.$$
(16)

Using the fact that $\eta_1(t)$ sign $(\eta_1(t)) = |\eta_1(t)|$, and multiplying both sides of (1) by $|\eta_1(t)|$ leads to

$$\frac{Kh_1}{2}\eta_1(t)\operatorname{sign}(\eta_1(t)) \ge \left(\frac{h_1\overline{F}}{2} + \overline{\delta F}\right)|\eta_1(t)| \ge \left|\eta_1(t)\left(\frac{h_1}{2}f(t) - \dot{f}(t)\right)\right|.$$

As a result,

$$\begin{aligned} \eta_1(t) \left(\frac{Kh_1}{2} \text{sign}(\eta_1(t)) - \frac{h_1}{2} f(t) + \dot{f}(t) \right) &\geq \frac{Kh_1}{2} |\eta_1(t)| - \left| \eta_1(t) \left(\frac{h_1}{2} f(t) - \dot{f}(t) \right) \right| \\ &\geq \frac{Kh_1}{2} |\eta_1(t)| - \left(\frac{h_1 \overline{F}}{2} + \overline{\delta F} \right) |\eta_1(t)|. \end{aligned}$$

Therefore, from (15), it follows that

$$\dot{V}_{o}(t,\eta(t)) \leq -\frac{h_{1}}{2}\eta_{2}(t)^{2} - \frac{h_{1}h_{2}}{2}\eta_{1}(t)^{2} - \left(\frac{Kh_{1}}{2} - \frac{h_{1}\overline{F}}{2} - \overline{\delta F}\right)|\eta_{1}(t)|.$$
(17)

On the other hand, it can be derived from (14) that

$$V_o(t,\eta(t)) \le \frac{1}{2}\eta^T(t) \begin{bmatrix} h_2 + \frac{1}{2}h_1^2 & \frac{1}{2}h_1 \\ \frac{1}{2}h_1 & 1 \end{bmatrix} \eta(t) + (K + \overline{F})|\eta_1(t)|.$$
(18)

As the result, from condition (10) and (11), it derived that $\dot{V}_o(t, \eta(t)) \leq -2\alpha V_o(t, \eta(t))$. By using comparison lemma in ([30], Lemma 3.4), we obtain

$$V_o(t,\eta(t)) \le V_o(0,\eta(0))e^{-2\alpha t}.$$
(19)

Accordingly, $\eta_1(t)$ and $\eta_2(t)$ exponentially converge. Further, exist $\beta_1, \beta_2 > 0$ such that $\eta_1^2(t) < \beta_1^2 V_o(t, \eta(t)), \eta_2^2(t) < \beta_2^2 V_o(t, \eta(t))$. Intuitively, the proof of Lemma 1 is completed. \Box

Remark 1. In the case the load disturbance $F_{\ell}(t)$ is excluded ($F_{\ell}(t) \equiv 0$), the switching term in (8) can be removed. In this case, the observer (8) can be reduced as high-gain observer founded in [31]. Hence, our proposed observer can be considered as an extension of high-gain observer to handle the influence of disturbance.

4. Controller Design

In the view of control strategy, the dynamic model (3)–(6) can be separated into two subsystems named as position-velocity and current subsystem. It worth noting that the current subsystem possesses much faster dynamics than that of the position-velocity subsystem. By taking cascade control into account, our method establishes an inner and outer control loop corresponding to the current and position-velocity subsystem.

4.1. Position-Velocity Subsystem

As a convenience, we denote desired velocity and acceleration corresponding to $v_r(t) = \dot{x}_r(t)$, $a_r(t) = \dot{v}_r(t)$. Additionally, the following notations are applied

$$\sigma = \frac{2\pi\psi}{m\tau_p}, \ e_x(t) = x(t) - x_r(t), \ e_v(t) = v(t) - v_r(t), \ \hat{e}_v(t) = \hat{v}(t) - v_r(t),$$
(20)

to rewrite position-velocity subsystem in (3)–(4) as

$$\dot{e}_{x}(t) = e_{v}(t),$$

 $\dot{e}_{v}(t) = \sigma i_{a}^{*} - a_{r}(t) - f(t),$
(21)

where the notation " i_q^* " indicates the desired quadrature current which is entrusted to current control loop. In this paper, we assume $i_q(t)$ simultaneously track i_q^* . According, i_q^* replaces $i_q(t)$ in (21). The following theorem provides a controller for

Theorem 2. Let us consider

$$i_{q}^{*} = \frac{1}{\sigma} \left(a_{r}(t) - K_{x} e_{x}(t) - K_{v} \hat{e}_{v}(t) \right),$$
(22)

where K_x , K_v are real positive constants. Then, the system (21) is stable, and $e_x(t)$, $e_v(t)$ converge to a arbitrary small values by choosing large enough control parameters K_x , K_v .

Proof of Theorem 2. Recalling notations in (20), it is obtained that $\hat{e}_v(t) = e_v(t) - \tilde{v}(t)$. Then, (21) can be rearranged as

$$\dot{e}_x(t) = e_v(t),$$

$$\dot{e}_v(t) = -K_x e_x(t) - K_v e_v(t) + K_v \widetilde{v}(t) - f(t).$$
(23)

To analyse stability and control performance of the proposed controller, a Lyapunov function can be chosen from (14) as follows

$$V_x(t) = \frac{1}{2}(K_x + K_v)e_x^2(t) + \frac{1}{2}e_v^2(t) + e_x(t)e_v(t) + V_o(t).$$
(24)

From (23), the time derivative of $V_x(t)$ is given by

$$\dot{V}_{x}(t) = (K_{x} + K_{v})e_{x}(t)e_{v}(t) + e_{v}(t)\dot{e}_{v}(t) + e_{v}^{2}(t) + e_{x}(t)\dot{e}_{v}(t) + \dot{V}_{o}(t)$$

$$= -K_{x}e_{x}^{2}(t) - (K_{v} - 1)e_{v}^{2}(t) + K_{v}\widetilde{v}(t)(e_{x}(t) + e_{v}(t)) - f(t)(e_{x}(t) + e_{v}(t)) + \dot{V}_{o}(t).$$
(25)

As mentioned in (17), it is clear that $\dot{V}_o(t) \leq -\frac{h_1}{8}(h_1\eta_1(t) + \eta_2(t))^2 = -\frac{h_1}{8}\tilde{v}^2(t)$. By using the following inequalities

$$\begin{split} \left| \widetilde{v}(t) \left(e_x(t) + e_v(t) \right) \right| &\leq \epsilon_x e_x^2(t) + \epsilon_v e_v^2(t) + \left(\frac{1}{4\epsilon_x} + \frac{1}{4\epsilon_v} \right) \widetilde{v}^2(t), \\ \left| f(t) \left(e_x(t) + e_v(t) \right) \right| &\leq \frac{\overline{F}^2}{2\epsilon_f} + \epsilon_f \left(e_x^2(t) + e_v^2(t) \right), \end{split}$$

where ϵ_x , ϵ_v , $\epsilon_f > 0$, it can be derived from (25) that

$$\dot{V}_{x}(t) \leq -(K_{x}-\epsilon_{x}-\epsilon_{f})e_{x}^{2}(t) - (K_{v}-\epsilon_{v}-\epsilon_{f}-1)e_{v}^{2}(t) - \left(\frac{h_{1}}{8}-\frac{1}{4\epsilon_{x}}-\frac{1}{4\epsilon_{v}}\right)\tilde{v}^{2}(t) + \frac{\overline{F}^{2}}{2\epsilon_{f}}.$$
 (26)

Accordingly, by letting

$$K_x - \epsilon_x - \epsilon_f = 1, \tag{27}$$

$$K_v - \epsilon_v - \epsilon_f - 1 = 1, \tag{28}$$

$$\frac{h_1}{8} - \frac{1}{4\epsilon_x} - \frac{1}{4\epsilon_v} > 0, \tag{29}$$

 $\dot{V}_x(t) < 0$ for all $(e_v(t), e_x(t)) \notin \mathcal{E} \triangleq \left\{ (e_x, e_v) \in \mathbb{R}^2 : e_x^2 + e_v^2 \leq \frac{\overline{F}^2}{2\epsilon_f} \right\}$. As a result, $(e_v(t), e_x(t))$ converges to \mathcal{E} in finite time. By choosing ϵ_f large enough, the region \mathcal{E} can be arbitrary small. Obviously, the proof of Theorem 2 is completed. \Box

4.2. Current Subsystem

In this part, due to much faster dynamics of current loop control, the desired quadrature current i_q^* can be considered as a constant in current control process. Further, fluctuations in inductance due to end-effect phenomenon can be ignored. In what follows, let us denote

$$e_{iq}(t) = i_q(t) - i_q^*, \ e_{id}(t) = i_d(t) - i_{dr}(t).$$
(30)

For the current subsystem, let us consider controllers which are a combination of PI controller and decoupler based on the observed velocity as

$$u_d(t) = R_s i_d^* - K_d e_{id}(t) - K_{id} \int_0^t e_{id}(\tau) d\tau - \frac{2\pi L}{\tau_p} i_q(t) \vartheta(t),$$
(31)

$$u_{q}(t) = R_{s}i_{q}^{*} - K_{q}e_{iq}(t) - K_{ip}\int_{0}^{t} e_{iq}(\tau)d\tau + \left(\frac{2\pi L}{\tau_{p}}i_{d}(t) + \frac{2\pi\psi_{p}}{\tau_{p}}\right)\hat{v}(t).$$
(32)

where K_d, K_p, K_{id}, K_{iq} are positive constants. As a result, the closed-loop of current subsystem is derived

$$\dot{e}_{id}(t) = -\frac{K_d + R_s}{L} e_{id}(t) - \frac{K_{id}}{L} \int_0^t e_{id}(\tau) d\tau + \frac{2\pi}{\tau_p} i_q(t) \widetilde{v}(t),$$
(33)

$$\dot{e}_{iq}(t) = -\frac{K_q + R_s}{L} e_{iq}(t) - \frac{K_{iq}}{L} \int_0^t e_{iq}(\tau) d\tau - \left(\frac{2\pi}{\tau_p} i_d(t) + \frac{2\pi\psi_p}{\tau_p L}\right) \widetilde{v}(t).$$
(34)

In the same manner as subsection 4.1, by using the following Lyapunov candidate function

$$V_{I}(t) = V_{o}(t) + \frac{1}{2}e_{id}^{2}(t) + \frac{1}{2}e_{iq}^{2}(t) + \frac{K_{id}}{2L}\left(\int_{0}^{t}e_{id}(\tau)d\tau\right)^{2} + \frac{K_{iq}}{2L}\left(\int_{0}^{t}e_{iq}(\tau)d\tau\right)^{2},$$
(35)

we can point out that current tracking errors converge to zero. It should be noted that the current control parameters K_d , K_{id} , K_q , K_{iq} are chosen such that the time response of current control loop is considerably smaller than that of position-velocity loop. For further theoretical studies, we can apply the backstepping technique provided by [32] to analyze the stability of the whole system, and the work in [33] can be used to design an observer in the presence of nonlinear uncertainties. Finally, the overall control scheme are shown in Figure 3.



Figure 3. The proposed control scheme of polysolenoid linear motor.

5. Numerical Simulation

The Polysolenoid Linear Motor's parameters use in this simulation are listed in Table 1. The parameters are selected from LinMot industrial PLM (P01-23x80/80x140). This motor is packed with two position sensors which release $sin(\theta)$ and $cos(\theta)$ for flux oriented control (FOC). To verify the effectiveness of the proposed method, the simulation includes two scenarios. The first one demonstrates the performance of the proposed controllers and observer in the case where measurement noises are excluded. While the other one focuses on the impacts of measurement noise in the position feedback signal. Both of them share the same controller, observer, and disturbance load.

Table 1. Parameters of the Polysolenoid Linear Motor (PLM).

Parameter	Notation	Value	Unit
Phase resistance	R_s	10.3	ohm
Slider (rotor) mass	т	0.171	kg
Phase inductance	L_a, L_b	1.4	mĤ
Pairs of poles	n_p	1	
Pole pitch	τ	10	mm
Flux	ψ_p	0.035	Wb

MATLAB/Simulink models of the observer-based tracking control for PLM drive system are built with sampling time 10^{-5} s. The disturbance load used in the simulations is chosen as: $f_{\ell}(t) =$

 $3 + \frac{16}{\pi}\sin(20t) + \frac{16}{3\pi}\sin(60t) + \frac{16}{5\pi}\sin(100t)$. Practically, it should be noted that $f_m(t)$ is very small in comparison with $f_{\ell}(t)$. As a result, we select $\overline{F} = 60$, $\overline{\delta F} = 2000$. From (10) and (11), parameters of observer (8) are give by K = 100, $h_1 = 10^3$, $h_2 = 2.10^4$, $\alpha = 30$, $\gamma = 0.1$. In addition, (27), (28) and (29) result in the position and current controller parameters: $K_p = 10^5$, $K_v = 2.10^3$, $K_d = K_p = 10$, $K_{id} = K_{iq} = 10^4$.

5.1. Simulation Results in Case of None Measurement Noise

In this scenario, we assume that the position sensor is accurate, the initial observer errors are selected as $\tilde{x}(0) = 0$ and $\tilde{v}(0) = 0.1$. As can be seen in Figure 4, position, and velocity of PLM track the reference signals. Besides, there are fluctuations in position and velocity error in Figure 4c,d due to the transition of observer error. According to Figure 5c, despite the disturbance load shown in Figure 5d, the observer error still converges to zero in approximately in 0.1 s. During this interval, the motor does not move, which shows our advantage in velocity observer in comparison with other techniques based on EMF. Therefore, the statement in Theorem 1 is verified. Further, the position can be maintained under the impact of disturbance load. The Figure 5c shows that $i_q(t)$ tracks the reference signal i_q^* by current controllers in Section 4.2. The simulated results verify that the PLM observer-based control system under the disturbance load has a high precision and response position.



Figure 4. Time response of (a) position tracking; (b) velocity tracking; (c) position error; (d) velocity error.



Figure 5. Time behavior of (**a**) quadrature current; (**b**) quadrature voltage; (**c**) velocity observer error; (**d**) disturbance load.

5.2. Simulation Results in Presence of Measurement Noise

To verify our algorithm, we assume that the position feedback signal is affected by measurement noise as following

$$x_{meas}(t) = x(t) + n(t) \tag{36}$$

where $x_{meas}(t)$ is the position feedback signal and n(t) is a white noise process. In this case, the conventional approaches based on measurement of speed using a position sensor fails to estimate the actual velocity. Due to the measurement noise, the initial observer position $\hat{x}(0)$ can not match to initial actual position x(0). Accordingly, observer errors are selected as $\tilde{x}(0) = 5.10^{-3}$, $\tilde{v}(0) = 0.1$ in the simulation. Figure 6a shows the measurement and actual position. With this measurement signal, the conventional approach which uses low-pass filter and derivatives can not estimated velocity. Overall, our control method still has merits in position tracking control, as presented in Figure 6c,d. As can be seen in Figure 7c,d, the observer errors remain small values after 0.1 s.



Figure 6. Effects of noise measurement in time response of (a) position tracking; (b) velocity tracking; (c) position error; (d) velocity error.



Figure 7. Effects of noise measurement in time behavior of (**a**) quadrature current, (**b**) quadrature voltage, (**c**) velocity observer error and (**d**) position observer error.

6. Conclusions

This paper has addressed tracking control problems of PLM with velocity sensorless and unknown disturbance force. The key success in our approach has laid on a novel observer, which guarantees asymptotic convergence of the observer errors. Further, the observer can provide estate estimation in the presence of unknown disturbance, and also deal with measurement noises. In cooperation

with observed velocity, the position-velocity and current tracking controllers have been designed by using the Lyapunov direct method, such that the tracking error converges to arbitrarily small values by adjusting control parameters. Accordingly, the stability analysis has been presented religiously to enhance the reliability of our results. As a result, this study has possibly proposed a method to overcomes some drawbacks of existed studies on velocity-sensorless control. Our future works will focus on a problem of lack of current sensors, with the aim of no further sensor required in the control of PLM.

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