

Communication



# **Back Electro Motive Force Estimation Method for Cascade Proportional Integral Control in Permanent Magnet Synchronous Motors**

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**Abstract:** A cascade proportional integral control method with back-electro motive force compensation has been widely used for permanent magnet synchronous motors. In the permanent magnet synchronous motor control, it is important to accurately know the back-electro motive force constant for torque generation as well as back-electro motive force compensation. In this study, a real-time back-electro motive force constant estimation algorithm is developed to improve the velocity tracking control performance. The proposed method consists of a proportional integral controller and a back-electro motive force constant estimator. The proportional integral controller is designed to reduce the velocity tracking error. The back-electro motive force constant estimator is designed to estimate the back-electro motive force constant. It was verified that the estimated back-electro motive force constant converges to the actual back-electro motive force constant. The estimated back-electro motive force constant is applied to the cascade proportional integral controller. To verify the effectiveness of the proposed method, the performance of the proposed method is validated experimentally.

**Keywords:** back electro motive force constant estimation; proportional integral controller; permanent magnet synchronous motor; velocity control

## 1. Introduction

Permanent magnet synchronous motors (PMSMs) have been widely used in highperformance applications because of their significant advantages, such as high power density, high efficiency, and good dynamic performance [1]. Various control methods have been examined to improve the control performance of PMSMs [2–6]. LPV  $H_{\infty}$  control with disturbance estimation was proposed in [2]. Velocity control for sideband harmonics compensation was developed in [3]. To reduce torque oscillation, a model predictive direct speed control was utilized in [4]. An adaptive second-order sliding-mode observer was used for sensorless control considering the inverter nonlinearity in [5]. A robust speed regulation technique was designed to estimate the disturbances in [6].

Although these methods improve the control performance of PMSMs, they are complex in terms of implementation and gain tuning in industrial applications. Thus, cascade PI control with back-electro motive force (EMF) compensation has been widely used for industrial applications because it is simple to implement [7,8]. In this method, it is important to know the back-EMF constant for back-EMF compensation. Furthermore, the back-EMF constant is also used for torque generation as well as back-EMF compensation. In general, the flux linkage by the back-EMF in the PMSM model is presented as follows [9]:

$$K_E = P\Phi$$

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**Copyright:** © 2021 by the authors. Licensee MDPI, Basel, Switzerland. This article is an open access article distributed under the terms and conditions of the Creative Commons Attribution (CC BY) license (https:// creativecommons.org/licenses/by/ 4.0/). where  $K_E$ , P, and  $\Phi$  are the back-EMF constant, pole pair, and flux linkage, respectively. Unfortunately, the flux linkage may vary according to the variations of temperature, load torque [10-13]. For example, when using a neodymium magnet, NdFeB, the temperature increase reduces the magnetic flux density, which leads to a decrease in the control performance. Furthermore, estimating the nominal value of the model parameters in a static condition has limitations in enhancing the control performance because the flux linkage can change depending on velocity or current [14]. Thus, it is important to design the parameter identification method for the estimation of the back-EMF constant. There are two major approaches for parameter identification: off-line estimation and online estimation. Because the off-line estimation method does not reflect the effect on model parameters that change according to the environment, such as temperature variation and magnetic flux saturation. Various real-time online estimation approaches have been recently utilized in practical applications to determine model parameters. In [15], model reference adaptive PID controller was presented for CNC machine. Novel adaptive control of PMSM was proposed for electric vehicle in [16] A model reference adaptive system was developed for electrical parameter estimation to enhance the tracking performance in [17,18]. Online identification based on an extended Kalman filter was designed for interior PMSMs in [19]. An impedance-model-based multiparameter identification method was developed to identify flux linkage and resistance under various operation conditions in [20]. To estimate the flux linkage, different types of flux observers were designed in [9,14,21,22]. However, in these methods, the performance may degrade due to the load torque injection and/or the variation of the mechanical parameter. Furthermore, the estimation or adaptation methods for the whole back-EMF may result in the lag of the back-EMF estimation.

Against this background, this study proposes a real-time back-EMF constant estimation algorithm to improve the velocity tracking control performance of the PMSM. The performance of the cascade PI control method (where the dual PI controllers are used for both mechanical and electrical subsystems) according to the variation in the back-EMF constant is studied. The back-EMF constant estimator is designed to estimate the back-EMF constant. It is mathematically proven that the estimated back-EMF constant converges to the actual back-EMF constant. In the proposed method, only back-EMF constant is estimated so that the lag of the back-EMF estimation can be avoided. The estimated back-EMF constant is applied to the cascade PI control method for back-EMF compensation and torque generation. The performance of the proposed method was validated experimentally.

The remainder of this paper is organized as follows. Based on PMSM dynamics, the PI controller with back-EMF compensation is described in Section II. Section III introduces the design and analysis of the back-EMF constant estimator. The experimental results to demonstrate the effectiveness of the proposed estimator are provided in Section IV. Section V presents the conclusions.

## 2. Mathematical Modeling and Controller Design

#### 2.1. PMSM Modeling

In this section, we describe the dynamic model of a three-phase synchronous motor with permanent magnets in  $\alpha$ ,  $\beta$ , coordinates as follows [2,3]:

$$\dot{\omega} = \frac{1}{J} \left( -\frac{3}{2} K_E \sin(P\theta) i_{\alpha} + \frac{3}{2} K_E \cos(P\theta) i_{\beta} - B\omega \right)$$
  

$$\dot{i}_{\alpha} = \frac{1}{L} \left( v_{\alpha} - R i_{\alpha} + P \Phi \omega \sin(P\theta) \right)$$
  

$$\dot{i}_{\beta} = \frac{1}{L} \left( v_{\beta} - R i_{\beta} - P \Phi \omega \cos(P\theta) \right)$$
(1)

where  $i_{\alpha}$ ,  $i_{\beta}$  and  $v_{\alpha}$ ,  $v_{\beta}$  are the current [A] and voltage [V] of phases  $\alpha$  and  $\beta$ , respectively. In addition,  $\theta$  is the rotor (angular) position [rad],  $\omega$  is the rotor (angular) velocity [rad/s], *B* is the viscous friction coefficient [N·m·s/rad], *J* is the inertia of the motor [kg·m<sup>2</sup>/rad], *R* is the phase resistance of the phase winding  $[\Omega]$ , and *L* is the phase inductance of the phase winding [H].

In this PMSM model, since the torque can be defined as

$$\tau = -\frac{3}{2}K_E \sin(P\theta)i_{\alpha} + \frac{3}{2}K_E \cos(P\theta)i_{\beta}$$
<sup>(2)</sup>

The back-EMF constant is used to generate the torque as well as back-EMF compensation.

#### 2.2. PI Controller with Back-EMF Compensation

In several industrial applications, the cascade PI control method, where the dual PI controllers are used for both mechanical and electrical subsystems, has been widely applied for PMSM. To design a tracking controller, it is preferable to define the tracking errors as follows:

$$e_{\omega} = \omega_{d} - \omega$$

$$e_{\alpha} = i_{\alpha_{d}} - i_{\alpha}$$

$$e_{\beta} = i_{\beta_{d}} - i_{\beta}$$
(3)

where  $\omega_d$  is the desired velocity,  $i_{\alpha_d}$  and  $i_{\beta_d}$  are the desired currents of phases  $\alpha$  and  $\beta$ , respectively. First, the desired torque  $\tau_d$  for velocity tracking is designed using the PI control as follows:

$$\tau_d = K_{p\omega} e_\omega + K_{i\omega} \int_0^t e_\omega d\tau \tag{4}$$

where  $K_{p\omega}$  and  $K_{i\omega}$  are the proportional and integral gains of velocity controller, respectively. From (2), the desired currents  $i_{\alpha_d}$  and  $i_{\beta_d}$  for generating the desired torque (4) are derived using the commutation scheme as follows:

$$i_{\alpha_d} = -\frac{2}{3} \frac{\sin(P\theta)}{K_E} \tau_d$$

$$i_{\beta_d} = \frac{2}{3} \frac{\cos(P\theta)}{K_E} \tau_d$$
(5)

For the current tracking,  $v_{\alpha}$  and  $v_{\beta}$  are obtained using the PI control and the back-EMF compensation as follows:

$$v_{\alpha} = K_{pi}e_{\alpha} + K_{ii} \int_{0}^{t} e_{\alpha}d\tau - K_{E}\omega\sin(P\theta)$$

$$v_{\beta} = K_{pi}e_{\beta} + K_{ii} \int_{0}^{t} e_{\beta}d\tau + K_{E}\omega\cos(P\theta)$$
(6)

where  $K_{pi}$  and  $K_{ii}$  are the proportional and integral gains of current controller, respectively. The block diagram of the cascade PI control method with the back-EMF compensation is shown in Figure 1.



Figure 1. Block diagram of the cascade PI control method with the back-EMF compensation.

## 3. Design and Analysis of Back-EMF Constant Estimator

3.1. Performance Analysis of Back-EMF Compensation

In this section, we analyze how the back-EMF constant affects the control performance using the following three cases:

Case S.1: Cascade PI control without back-EMF compensation

$$v_{\alpha} = K_{pi}e_{\alpha} + K_{ii}\int_{0}^{t} e_{\alpha}d\tau$$

$$v_{\beta} = K_{pi}e_{\beta} + K_{ii}\int_{0}^{t} e_{\beta}d\tau$$
(7)

Case S.2: Cascade PI control with back-EMF compensation by 50% of the back-EMFs

$$v_{\alpha} = K_{pi}e_{\alpha} + K_{ii} \int_{0}^{t} e_{\alpha}d\tau - K_{EN}\omega\sin(P\theta)$$

$$v_{\beta} = K_{pi}e_{\beta} + K_{ii} \int_{0}^{t} e_{\beta}d\tau + K_{EN}\omega\cos(P\theta)$$
(8)

where  $K_{EN} = 0.5K_E$ 

Case S.3: Cascade PI control with back-EMF compensation

$$v_{\alpha} = K_{pi}e_{\alpha} + K_{ii} \int_{0}^{t} e_{\alpha}d\tau - K_{E}\omega\sin(P\theta)$$

$$v_{\beta} = K_{pi}e_{\beta} + K_{ii} \int_{0}^{t} e_{\beta}d\tau + K_{E}\omega\cos(P\theta)$$
(9)

The simulations were performed using MATLAB/Simulink for the performance analysis. Figure 2 shows the current tracking performance. In Case S.1, the magnitudes of the currents were reduced owing to the back-EMF in the current tracking. In Case S.2, although the 50% of the back-EMFs were rejected, the magnitudes of the currents were reduced because of inaccurate compensation of the back-EMFs. In Case S.3, the current tracking performance was the best among the three cases because the back-EMFs were rejected. These current tracking performances affect the velocity tracking performance, as shown in Figure 3. Similar to the current tracking performances, the velocity tracking performance of Case S.3 was the best among the three cases. From these simulation analyses, we observe that the accurate back-EMF compensation is important for the control performance of the PMSM.



Figure 2. Cont.



Figure 2. Current tracking performance in simulation. (a) Case S.1. (b) Case S.2. (c) Case S.3.

## 3.2. Back-EMF Constant Estimator Design

The effect on the back-EMF constant has been investigated in the previous subsection. In this section, we develop the back-EMF constant estimator to avoid the lag of the back-EMF estimation. For the back-EMF constant  $K_E = P\Phi$ , we develop the back-EMF constant estimator as follows: The magnetic flux varies for various reasons such as temperature, current, and velocity conditions. The back-EMF constant is derived as  $K_E = P\Phi$ . The back-EMF constant may vary owing to the temperature changes, but it varies slowly [10]. Thus it is assumed that  $\dot{K}_E \approx 0$ . The estimation algorithm for the back-EMF constant is designed as follows:

$$\begin{aligned} \hat{K}_E &= z + k_a \omega \sin(P\theta) i_{\alpha}^{\mu} \\ \dot{z} &= -k_a \sin(P\theta) \dot{\omega} - k_a P \omega^2 \cos(P\theta) i_{\alpha}^{\mu} \\ &- \frac{k_a \mu}{L} \omega \sin(P\theta) (-Ri_{\alpha} + \hat{K}_E \omega \sin(P\theta) + v_{\alpha}) i_{\alpha}^{\mu-1} \end{aligned}$$
(10)

where  $k_a$  is a positive constant, and  $\mu$  is a positive odd integer. The estimation error  $\tilde{K}_E$  is defined as follows:

$$\tilde{K}_E = K_E - \hat{K}_E. \tag{11}$$



**Figure 3.** Velocity tracking performance in simulation. (**a**) Velocity tracking performance. (**b**) Velocity tracking error.

**Theorem 1.** Suppose that the estimation algorithm of the back-EMF constant (10) is applied to the PMSM (1). Then  $\tilde{K}_E$  locally and asymptotically converges to zero during the PMSM operation.

Proof. The estimation error dynamics are

$$\begin{split} \tilde{K}_E &= -\hat{K}_E \\ &= -\dot{z} - k_a \sin(P\theta)\dot{\omega} - k_a P\omega^2 \cos(P\theta) i_{\alpha}^{\mu} \\ &- \frac{k_a \mu}{L} \omega \sin(P\theta) (-Ri_{\alpha} + K_E \omega \sin(P\theta) + v_{\alpha}) i_{\alpha}^{\mu-1} \\ &= -\frac{k_a \mu}{L} \omega^2 \sin(P\theta)^2 \tilde{K}_E i_{\alpha}^{\mu-1} \end{split}$$
(12)

During PMSM operation,  $\tilde{K}_E$  locally and asymptotically converges to zero.

Therefore, the control inputs can be represented as

$$v_{\alpha} = K_{pi}e_{\alpha} + K_{ii} \int_{0}^{t} e_{\alpha}d\tau - \hat{K}_{E}\omega\sin(P\theta)$$

$$v_{\beta} = K_{pi}e_{\beta} + K_{ii} \int_{0}^{t} e_{\beta}d\tau + \hat{K}_{E}\omega\cos(P\theta)$$
(13)

The block diagram of the proposed method, including the cascade PI controller with back-EMF compensation and the back-EMF constant estimator, is shown in Figure 4.

## 3.3. Tuning Guideline

In this section, we provide the procedure for the estimator gain tuning in order to replicate the proposed method under a different setup, which is as follows:vspace

# Step 1: µ selection

Since operating frequency and electrical parameters are invariable in constant velocity range, estimation performance will be decided by choosing  $\mu$  and  $k_a$ . By (12), homogenous solution of differential equation can be represented as

$$\tilde{K}_E(t) = \exp(\lambda)\tilde{K}_E(0)$$

where *t* goes to infinity.  $\tilde{K}_E(0)$  is initial value of  $\tilde{K}_E$ .  $\lambda = -\frac{k_a \mu \omega^2 \sin(P\theta)^2 i_{\alpha}^{\mu-1}}{L}$ .

If magnitude of  $i_{\alpha}$  is relatively large, then  $i_{\alpha}^{\mu-1}$  is also large. So the convergence rate of  $\tilde{K}_E$  is more faster. And if magnitude of  $i_{\alpha}$  is relatively small, then  $i_{\alpha}^{\mu-1}$  is also small. So the convergence rate of  $\tilde{K}_E$  is more slower. Therefore,  $\mu$  should be determined by the magnitude of the phase currents because there is a tradeoff relationship between  $\mu$  and the phase currents.

# Step 2: k<sub>a</sub> selection

In many industrial applications, it is common for measurement noise to be present in the signal measured from the sensor. Suppose that the measured angular velocity can be rewritten as

$$\omega = \omega_f + \omega_n$$

where  $\omega_f$  and  $\omega_n$  are fundamental frequency and noise frequency obtained from the sensor, respectively. By this definition, the convergence rate,  $\lambda$  is redefined as

$$\lambda = -\frac{\mu \sin(P\theta)^2 i_{\alpha}^{\mu-1}}{L} (\omega_f^2 + \omega_f \omega_s + \omega_n^2) k_{\alpha}$$

It means that high  $k_a$  results in amplification of the measurement noise. Therefore,  $k_a$  should be determined within a range that does not amplify the frequency of the measurement noise.

From the aforementioned procedure, we can analytically determine the back-EMF constant estimator gains  $\mu$  and  $k_a$ .



Figure 4. Control block diagram of the proposed PI controller with the back-EMF constant estimator.

## 4. Experimental Results

Experiments were tested to validate the performance of the proposed method. Figure 5 shows the hardware configuration of the PMSM driver set. Experiments were performed using ControlDesk software, two RapidPro, and a SCALEXIO real-time system. We generated a real-time control code in MATLAB/Simulink to apply ControlDesk. SCALEXIO supported a sample rate of 40 kHz. Each RapidPro unit consisted of three half-bridge power stage modules. The two switches of each half-bridge were driven by complementary signals with dead time to prevent feed-through faults. Surface mounted PMSM (APM-SB03ADK-9, Kwapil & Co, Wien, Austria) was directly connected to an encoder (2500 pulses per revolution). The parameters used in the experiments and simulations were determined by referring to the data sheet. Powder brake was used to generate load torque. A personal computer was used to implement the control program in C language, compile the program, and upload executable output code to the SCALEXIO real-time system. The switching frequency was set to be 20 kHz. To evaluate the performance of the proposed estimator, we

assume there is a control situation in which the nominal value of the back-EMF constant is not accurately known. Two cases were tested as follows:

- Case 1: PI controller with  $K_E = 0.105$  (70% of nominal back-emf constant),
- Case 2: PI controller with  $\hat{K}_E$  (proposed back-EMF estimator).

The experimental setup parameters for PMSM and gains are listed in Table 1. For fair comparison, we use same control gains for two cases. The different three cases with two desired velocities (30 rad/s and 80 rad/s) were examined in the experiments.

Table 1. PMSM parameters and gains.

PMSM Parameters, Control Gains, and Estimator Gains		
PMSM parameters	В	$3.7  imes 10^{-3}$ [N·m·s/rad]
	J	$4.675  imes 10^{-4}  [ ext{kg} \cdot  ext{m}^2/ ext{rad}]$
	R	80.2 [Ω]
	L	$0.4 imes10^{-3}$ [H]
	$K_E$	0.15 [V/rad/s]
Controller gains	$K_{pw}$	2000
	$K_{iw}$	40
	$K_{pi}$	5
	$\dot{K_{ii}}$	10
Estimator gains	μ	1
	$k_a$	$2.5 imes10^{-6}$



Figure 5. PMSM experiments setup.

## 4.1. 30 rad/s Operation

Figure 6 shows the desired velocity for 30 rad/s operation. Figure 7 shows the back-EMF constant estimation performance in Case 2. In the constant velocity region, the estimated back-EMF constant tracked the nominal back-EMF constant (=0.15) well. Figure 8 shows the velocity tracking performance for both cases. In Figure 8b, the velocity tracking error of Case 2 was relatively smaller than that of Case 1 because the back-EMF constant was accurately estimated by the proposed back-EMF estimator as shown in Figure 7.



**Figure 6.** Desired velocity ( $\omega_{d. \max} = 30 \text{ rad/s}$ ).



**Figure 7.** Back-EMF estimation performance ( $\omega_{d. \max} = 30 \text{ rad/s}$ ).



**Figure 8.** Velocity tracking performance ( $\omega_{d. \max} = 30 \text{ rad/s}$ ). (a) Velocity tracking performance. (b) Velocity tracking errors.

Figure 9 shows the current tracking performance and current tracking errors for both cases. In Figure 9a,b, even the phase delays of both methods are almost same, and the tracking performance of Case 2 is more close to the desired phase current compared to





**Figure 9.** Current tracking performances (30 rad/s Operation). (**a**) Current tracking performance (Case 1). (**b**) Current tracking performance (Case 2). (**c**) Current tracking errors.

# 4.2. 80 rad/s Operation

We conducted another experiment with 80 rad/s operation to evaluate the performance based on the presence of a load torque. Figure 10 shows the desired velocity for the 80 rad/s operation. A step load torque (=0.45 Nm) was injected after 16 s, as shown in Figure 11. Because the rated torque of the PMSM is 1.9 Nm, the injected load torque is approximately 23% of the rated torque.

Figure 12 shows the back-EMF constant estimation performance for Case 3. When the load torque was injected at 16 s, the estimated back-EMF constant was changed from 0.15 to 0.155. As mentioned in the introduction, the estimated back-EMF constant depends on the variation in the flux linkage. We can also observe fluctuations with a low frequency of the estimated back-EMF constant caused by structural vibration, such as the alignment of the mechanical coupler between the PMSM and the powder brake.



Figure 10. Desired velocity (80 rad/s Operation).



Figure 11. Injected load torque (80 rad/s Operation).



Figure 12. Back-EMF estimation performance (80 rad/s Operation).

Figure 13 shows the velocity tracking performance for all cases. Before the load torque was injected, the velocity tracking errors of Case 2 were smaller than those of Case 1. After the load torque was applied, the velocity tracking error increased in both cases; however, it can be seen that the difference in velocity tracking error between Case 1 and Case 2 is relatively larger than before load torque application. In Case 2, the back-EMF constant according to the change in the experimental environment was well estimated, whereas the same back-EMF constant was still applied to the control input in Case 1; hence, this difference occurred after the load torque was injected. In contrast, the velocity tracking error of Case 2 was smaller than that of Case 2 after the load torque was injected at 16 s. After the load torque was injected, even if the flux linkage and the back-EMF constant were changed, the changed back-EMF constant was well estimated by the proposed estimator.

Figure 14 shows the current tracking performance and current tracking errors for both cases, respectively. Similar phase delay are observed in both cases, while the phase current well tracked the desired phase current in case 2. After the load torque injection, the peak of the current tracking error in case 2 was decreased by about 15 % from 1.95 A to 1.66 A compared with that of case 1, because current tracking performance was improved by designing the back-EMF constant estimator in case 2.



**Figure 13.** Velocity tracking performance (80 rad/s Operation). (**a**) Velocity tracking performance. (**b**) Velocity tracking errors.



Figure 14. Cont.



**Figure 14.** Current tracking performance after load torque injection (80 rad/s Operation). (**a**) Current tracking performance (Case 1). (**b**) Current tracking performance (Case 2). (**c**) Current tracking errors.

# 4.3. Step Response

In this subsection, we conducted experiment with existing method [23] using step function as the desired velocity. Step time and final value of step function are 1 second and 40 rad/s, respectively. For fair comparison, the PI controller gains were determined with same gains used in the proposed method.

The velocity tracking performances are shown in Figure 15. Both methods have similar rising time (=0.065 s), whereas settling time of case 2 is faster than that of case 3. We can observe that the velocity tracking error of case 2 is smaller even though the same control gains were used in steady-state response. The velocity tracking errors were not zero, because an objective is not to optimize control performance in this paper.

Figure 16 shows the back-emf estimation performance. In the existing technique [23], since a nominal back-EMF signal,  $K_M \omega \sin(P\theta)$ , was estimated,  $\hat{K}_M \omega \sin(P\theta)$  was estimated in both methods. The phase of the nominal back-EMF signal and the estimated back-EMF signal in case 2 are almost in-phase, whereas the phase delay was observed in case 3. This back-EMF estimation performance can affect the velocity tracking performance because the control input was designed by using the estimated back-EMF constant.

Figure 17 shows the current tracking performance. The estimated back-EMF constant,  $\hat{K}_E$ , was used in denominator of the desired phase current, magnitude of the desired current in case 3 is larger than that in case 2. However, we can observe that the both methods have different current tracking performance due to the difference in the back-EMF estimation performance. Therefore, the peak of the current tracking error in case 2 was smaller than that of case 3.



Figure 15. Cont.



Figure 15. Velocity tracking performance (Step response). (a) Velocity tracking performance.(b) Velocity tracking errors in transient region. (c) Velocity tracking errors in steady-state region.



Figure 16. Back-EMF estimation performance (Step response). (a) Case 2. (b) Case 3.



**Figure 17.** Current tracking performance (Step response). (**a**) Current tracking performance (Case 2). (**b**) Current tracking performance (Case 3). (**c**) Current tracking errors.

# 5. Conclusions

In this paper, a real-time back-EMF constant estimation algorithm is proposed to enhance the velocity tracking control performance. The PI controller with the back-EMF constant estimator was designed to reduce the velocity tracking error. Using inaccurate back-EMF constants, an analysis was performed to find how the back-EMF constant affects the control performance. The back-EMF constant estimator is designed to estimate the back-EMF constant. Through experimental validation, it was observed that the back-EMF constant can be changed by the operating conditions such as the velocity, current, and load torque. The back-EMF constant was well estimated by the proposed real-time estimation algorithm under various operating conditions. We intend to estimate the back-EMF constant considering operating conditions such as the temperature and 3-phase unbalanced current in the future.

**Author Contributions:** J.G. and W.K. designed the algorithm and developed the simulation; S.Y. and Y.L. provided guidance in designing the algorithm; W.K. and Y.L. verified the simulation model and results; and all authors reviewed and approved the manuscript. All authors have read and agreed to the published version of the manuscript.

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#### Abbreviations

PI	Proportional integral
PID	Proportional integral differential
EMF	Electro motive force
PMSMs	Permanent magnet synchronous motors
LPV	Linear parameter varying
Nomenclature	1 2 0
θ	Rotor angular position [rad]
ω	Rotor angular velocity [rad/s]
τ	Mechanical torque [N·m]
$i_{\alpha}$	Current of phase $\alpha$ [A]
$i_{\beta}$	Current of phase $\beta$ [A]
$v_{\alpha}$	Voltage of phase $\alpha$ [V]
$v_{\beta}$	Voltage of phase $\beta$ [V]
$\dot{\omega}_d$	Desired rotor angular velocity [rad/s]
$i_{\alpha_d}$	Desired current of phase $\alpha$ [A]
$i_{\beta_d}$	Desired current of phase $\beta$ [A]
$\tau_d$	Desired mechanical torque [N· m]
$K_E$	Back-EMF constant [V·s/rad]
Р	Pole pair
Φ	Flux linkage [Wb]
В	viscous friction of the motor [N·m·s/rad]
J	Inertia of the motor [kg·m <sup>2</sup> /rad]
R	Resistance of the phase winding $[\Omega]$
L	Inductance of the phase winding [H]
$\tilde{K}_E$	Estimation error of back-EMF constant [V·s/rad]
$\hat{K}_E$	Estimation state of back-EMF constant [V·s/rad]
$K_{p\omega}$	Proportional gain of velocity control loop
$K_{i\omega}$	Integral gain of velocity control loop
$K_{pi}$	Proportional gain of current control loop
K <sub>ii</sub>	Integral gain of current control loop
$\mu$ , $k_a$	Estimator gains

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