



Article Shear and Punching Capacity Predictions for One-Way Slabs under Concentrated Loads Considering the Transition between Failure Mechanisms

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Abstract: Reinforced concrete one-way slabs under concentrated loads can develop different shear failure mechanisms: as wide beams in one-way shear, punching shear around the load or a mixed mode between them. Until now, most publications presented recommendations to assess the shear capacity considering only the one-way shear failure mechanism. This study proposed developing recommendations to assess both the one-way shear and punching shear capacity of such slabs. Different codes of practice were addressed, including the current Eurocode and *fib* Model Code 2010 expressions. The recommendations were validated against 143 test results from the literature. Following these recommendations, one-way shear and punching capacities predictions achieved enhanced and almost the same level of accuracy.

Keywords: one-way shear; punching shear; one-way slabs; concentrated loads



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1. Introduction

Reinforced concrete one-way slabs under concentrated loads are commonly found in bridge decks (Figure 1a). In the last decades, this case attracted the increasing attention of the research community because bridges built between the 1960s and 1970s are reaching the end of the design service life [1,2]. To extend the service life of these structures, it is necessary to attest that bridges designed with old codes fulfill the requirements of the current ones. In this context, the expressions to calculate the nominal shear capacity (shear force per unit length) from past codes were replaced by expressions that may be more conservative than those used in the past [2]. In addition, the design trucks became heavier, which increased the design actions. In other words, the same structures must support higher design actions with a lower design resistance. Owing to this, many slab bridges were rated as critical in one-way shear following the traditional design rules applied to assessment.

The traditional approach to verify the one-way shear capacity of such kinds of slabs is the assumption that only a slab strip, of a width equal to the effective shear width (b_{eff}), contributes to the one-way shear capacity (Figure 1b). In practice, this means that the load effect from each loading axle can be distributed over a certain length (the effective shear width) to calculate the total shear stress at the control section (Figure 1b). In assessing existing structures, the actual shear demand v_E is compared to the nominal shear resistance v_R to define if the structure satisfies the requirements of one-way shear resistance. Figure 1b shows the approach frequently named the French load-spreading method resulting in the French effective shear width [3,4], which assumes that the load is spread horizontally from the load back sides with a fixed angle of 45 degrees.

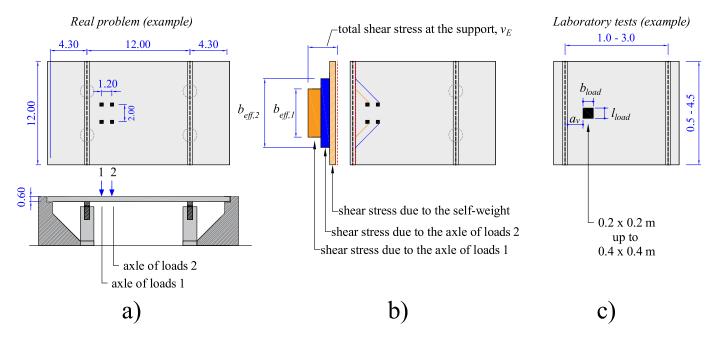


Figure 1. (a) Example of bridge deck slab under the concentrated loads of the European design tandem; (b) example of calculation of the design shear stress v_E at the support combining the actions from the self-weight and the ones from the load axes using the effective shear width definition; (c) example of laboratory test.

Until now, most investigations regarding the accuracy of the approach presented in Figure 1b have been based on reduced-scale laboratory tests (Figure 1c) [5–11]. For such tests, it is more frequent to compare tested and predicted resistances in terms of force (V_{test} for the achieved sectional shear in the test and V_R for the predicted sectional one-way shear capacity). In the last approach, the effective shear width b_{eff} is frequently multiplied by the unitary shear resistance (v_R) in comparing tested and predicted resistances.

In some studies [5,12], different models of the effective shear width were tested with the current Eurocode shear expressions. Between the main results, it was observed that the French effective shear width provides good predictions of one-way shear capacity when the load is placed close to the support $(a_v/d_l \leq 2)$ or when the slabs fail in one-way shear as wide beams [13]. However, this approach presents the shortcoming that the effective shear increases excessively as the distance from the load to the support a_v increases. In practice, this causes the predicted one-way shear capacity to frequently overestimate the tested resistance when the loads are placed far from the support [7,10,13,14]. Until the last years, this has not been considered a significant deficiency because the most critical position of the design tandem for one-way shear was always considered close to the support ($a_v = 2d_l$). In practice, this occurs because arching action improves the shear capacity for a distance $a_v \leq 2d_l$ and because placing the load close to the support increases the shear demand at the support v_E (Figure 2a,b). However, with the advancing understanding of the one-way shear behavior [15–17], this argument is subject to discussion. In fact, increasing the load distance from the support decreases the load effect v_E close to the load (action side). On the other hand, the unitary shear capacity v_R also decreases by increasing a_v due to the higher bending moments around the load (Figure 2c). In summary, the most critical position for one-way shear in Figure 2a can be at the mid-span and not at the support, depending on how the load effect v_E and the shear resistance v_R vary by increasing a_v . Additionally, the approach of checking only one position of the design tandem for one-way shear comes from the use of hand calculations in the past. Nowadays, with the aid of computational tools, it is possible to calculate the load effect for several load positions and for each control section in such a way as to search for the most critical position (resulting in the highest ratio between shear demand v_E and shear capacity v_R). Therefore, a correction in the predicted

effective shear width may be needed to evaluate the one-way shear resistance at different load positions.

Furthermore, most publications frequently address the problem by discussing only the one-way shear failure mechanism, even though some tests reported in the literature failed by punching [6,7,18]. Consequently, recommendations to assess the punching capacity of such slabs are scarce or focused on specific boundary conditions [18–20]. For instance, most publications did not discuss how to consider the influence of the free edges on the effective contribution of the sides of the control perimeter close to them. Moreover, most codes do not discuss the consideration of arching action in a portion of the control perimeter for loads close to the support.

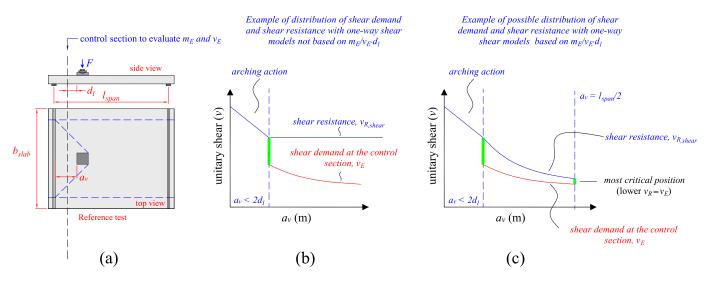


Figure 2. (a) Sketch of the test S35B1-1 from Reißen [14] and position of the control section on which the acting bending moments and shear demand are evaluated with fib Model Code 2010 [21]; (b) example of possible distribution in shear demand v_E and shear resistance v_R using one-way shear models that do not consider the influence of the ratio $m_E/v_E \cdot d_l$ in the unitary shear capacity (note that the most critical position for one-way shear will always be close to the support in this approach); (c) example of possible distribution in shear demand v_E and shear resistance v_R at the control section with the models that consider the lower shear resistance increasing the ratio $m_E/v_E d_l$.

Based on the presented ideas, the following research question was identified: how can the one-way shear and punching shear capacity predictions reach enhanced levels of accuracy by simple and effective enhancements of the current approaches?

This study addresses the research question and proposes a set of recommendations that allow assessing the one-way shear and punching capacity of one-way slabs under concentrated loads with better precision using the European [22] and *fib* Model Code expressions [21]. For this purpose, key parameters influencing the transition between one-way and two-way shear failures for such slabs were addressed and considered in the proposed approaches: (i) the load position, (ii) load size and (iii) the slab width [23,24]. Although simple, accurate predictions of shear and punching shear capacity can be achieved, regardless of the governing failure mechanism of the slabs. In other words, for instance, precise and safe predictions of one-way shear capacity for such slabs can be achieved, even when the test results indicate a punching failure. In practice, the presented approach increases the safety of the global verification since both one-way shear and punching shear capacity predictions will present enhanced levels of accuracy.

2. Literature Review

2.1. Background Calculations for One-Way Shear

The one-way shear capacity of one-way slabs under concentrated loads is commonly calculated by multiplying the unitary shear resistance (shear resistance per unit length) by a given effective shear width:

$$V_{R,predicted} = v_{R,shear} \cdot b_{eff} \tag{1}$$

The expressions to calculate the unitary shear capacity $v_{R,shear}$ according to EN 1992-1-1:2004 [25] are presented below (the legend of each parameter appears in the Notations Section; these expressions use average values for material properties to compare tested and predicted resistances):

$$v_{R,shear,EN} = \max \begin{cases} \begin{bmatrix} C_{R,c}k(100\rho_l f_c)^{1/3} + k_1\sigma_{cp} \end{bmatrix} d_l \\ (v_{\min} + k_1\sigma_{cp})d_l \end{cases}$$
(2)
with d_l in [mm] and f_c in [MPa]

$$v_{\min} = 0.035k^{3/2}f_c^{1/2}$$
 (3)
 $C_{R,c} = 0.18$ (4)

(4)

$$k = 1 + \sqrt{\frac{200}{d_l}} \le 2, \text{ with } d_l \text{ in } [\text{mm}]$$
(5)

The expressions to calculate the unitary shear capacity $v_{R,shear}$ according to fib Model Code 2010 [21] are presented below:

$$v_{R,shear,MC} = k_v \cdot \sqrt{f_c} \cdot z$$
, with f_c in [MPa] (6)

$$k_v = \frac{0.4}{1 + 1500 \cdot \varepsilon_x} \cdot \frac{1300}{1000 + k_{dg} \cdot z}, \text{ with } z \text{ in } [\text{mm}]$$
(7)

$$\varepsilon_x = \frac{1}{2E_s A_s} \left(\frac{m_E}{z} + v_E \right) \tag{8}$$

$$k_{dg} = \frac{32}{16 + d_g} \ge 0.75$$
, with d_g in [mm] (9)

$$z \cong 0.9d_l \tag{10}$$

In the case of the *fib* Model Code 2010 [21], the reader can realize that the unitary shear capacity $v_{R,shear,MC}$ is a function of the applied concentrated load F and, consequently, the unitary bending moments in the control section m_E . In the design or assessment of existing structures, the loads F are generally known, and the solution of $v_{R,shear,MC}$ becomes direct (closed-form solution). However, in the comparison between tested and calculated resistances, the load that causes the failure or the predicted one-way shear capacity is determined iteratively by varying the applied load F(i) until the calculated unitary shear capacity $v_{R(i)}$ is equal to the unitary shear demand $v_{E(i)}$ (Figure 3a). Figure 4 shows a summary of the main calculations in the iterative process to calculate the unitary shear capacity and punching shear capacity with the *fib* Model Code expressions (the punching capacity calculations are discussed in more detail in the next sections).

While for beams, the relation between F and v_E becomes straightforward, for slabs, most designers recur to using finite element analyses to determine the relation between F(i) and $v_{E(i)}$ and between F(i) and $m_{E(i)}$ in the case of one-way slabs under concentrated loads [10].

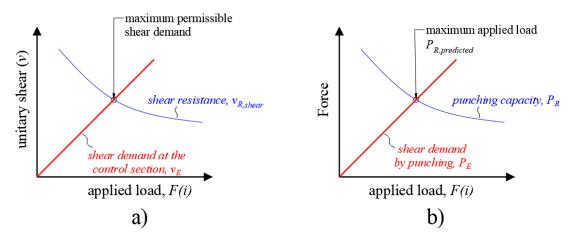


Figure 3. Determination of the (**a**) unitary shear resistance $v_{R,shear}$ and (**b**) punching capacity $P_{R,predicted}$ iteratively for the fib Model Code expressions.

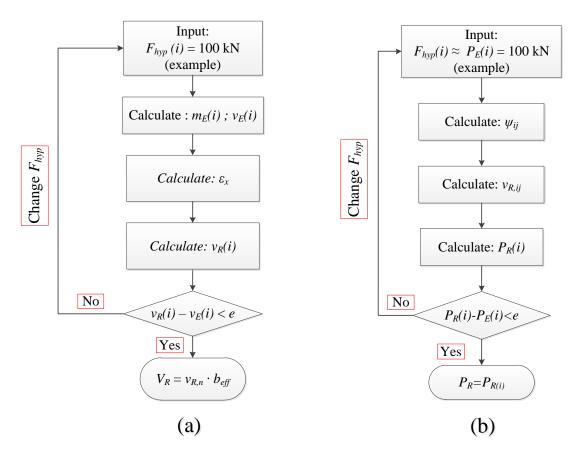


Figure 4. Flowchart of calculations for (**a**) one-way shear resistance predictions and (**b**) punching shear capacity with the *fib* Model Code 2010 expressions in the comparisons between tested and predicted resistances.

In order to allow the evaluation of the acting bending moments and shear forces for one-way slabs under concentrated loads, a simplified approach is proposed (Figure 5): (i) the reference test is transformed into a similar test with a width of 1 m and the bending moments and shear forces are calculated as in a beam loaded over the entire width. After determining iteratively the unitary shear capacity $v_{R,shear,MC}$ and the related concentrated load F(i) for a 1 m slab width, the total shear capacity and concentrated loads are multiplied by the respective effective shear width b_{eff} (Figure 5c). According to the *fib* Model Code 2010, the control section to evaluate the shear force v_E and bending moments m_E is placed at

the distance of $d_l \le a_v/2$ from the load edge for simply supported slabs and at $d_l \le a_v/2$ from the support edge for cantilever slabs. For continuous members, the control section is placed closer to the load or the support, depending on which one leads to the lower shear resistance (typically the section with the higher ratio $m_E/v_E \cdot d_l$).

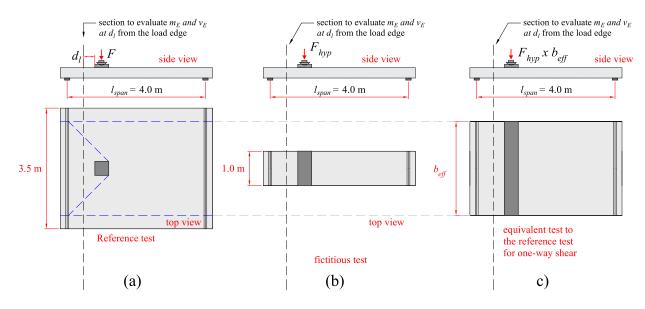


Figure 5. Proposed approach to calculate the relation between the applied concentrated load and the acting shear v_E and bending moments m_E when using the *fib* Model Code 2010 expressions for one-way shear: (a) Sketch of a test to be evaluated; (b) assumption of fictitious a test with 1 m width with equal support conditions to calculate v_E , m_E and, subsequently, the unitary shear capacity v_R ; (c) multiplying of the test sketched in (b) by the respective effective shear width calculated in (a).

For concentrated loads close to the support, the EN 1992-1-1:2004 [25] and *fib* Model Code 2010 [21] allow decreasing the design shear load V_{Ed} for loads placed at $a_v \leq 2d_l$ by considering that a portion of the load is taken directly to the support by strut or arching action. Figure 6 shows the cracking pattern of slender members failing in flexure-shear (here assumed with $a_v/d_l > 2$, Figure 6a) and non-slender members failing in compression-shear (Figure 6b). It can be noted that the flexure-shear crack in Figure 6a disturbs the load transfer in the fictitious strut between the load and the support. On the other hand, when the concentrated loads are placed closer to the support (Figure 6b), the members fail in shear-compression, and direct load transfer between the load and the support can occur by a strut, which is named herein as arching action.

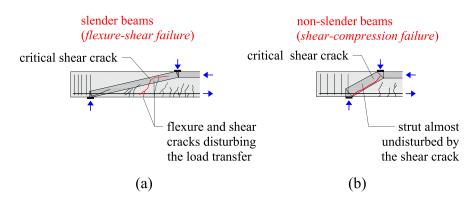


Figure 6. Influence of the shear slenderness (here defined as a_v/d_l) in the cracking pattern and failure mechanism of members loaded over the entire width: (a) slender beams failing in flexure-shear; (b) non-slender beams failing in shear-compression (adapted from Muttoni and Fernandez Ruiz [17]).

In this study, the following reduction factors β can be multiplied by the shear load V_{Fu} caused by the concentrated load F_u (Table 1).

Table 1. Definition of the factor β according to different guidelines.

Code	
EN 1992-1-1:2004 [25]	$eta_{EC} = rac{a_v}{2 \cdot d_l} \left\{ egin{array}{c} \leq 1.00 \ \geq 0.25 \end{array} ight.$
<i>fib</i> Model Code 2010 [21]	$eta_{MC} = rac{a_v}{2 \cdot d_l} \left\{ egin{array}{c} \leq 1.00 \ \geq 0.50 \end{array} ight.$ (12)

Therefore, the shear load (V_E) can be calculated as (considering the effect of the self-weight v_g over the effective shear width assumed):

$$V_E = V_{Fu} \cdot \beta + v_g \cdot b_{eff} \tag{13}$$

Alternatively, one can also consider an enhanced shear capacity due to arching action instead of decreasing the shear demand V_E [11]. In this way, the factor $\mu = 1/\beta$ can be multiplied by the unitary shear resistance v_R , and V_E and V_R become:

$$V_E = V_{Fu} + v_g \cdot b_{eff} \tag{14}$$

$$V_R = (v_R \cdot \mu) \cdot b_{eff} \tag{15}$$

Nowadays, the most widespread approach to defining the effective shear width b_{eff} [3–5,12], also referred to as the French approach, is based on the horizontal load spreading toward the supports from the back sides of the load (Figure 7a). In the French approach, the angle of this horizontal spreading is fixed at 45 degrees. In the *fib* Model Code 2010 [21], the angle of spreading varies as a function of the support conditions (Figure 7b), and the reference line to calculate the effective shear width is placed at min{ d_{1} ; a_v /2} from the support edge.

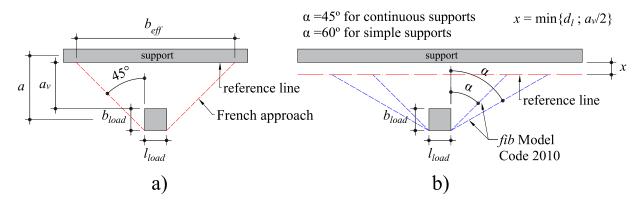
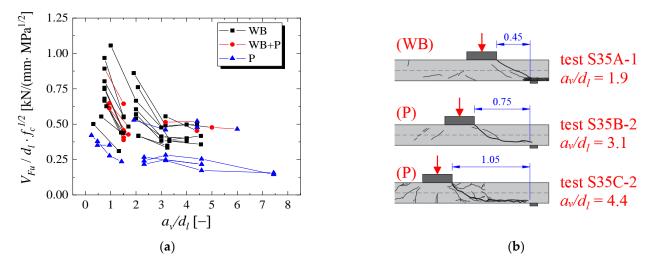


Figure 7. Effective shear width defined according to the (**a**) French guidelines [4]; (**b**) fib Model Code 2010 [21].

2.2. Insights from the Literature for One-Way Shear

Recently, Sousa, Lantsoght and El Debs [24] evaluated a dataset of 143 one-way slabs under concentrated loads that presented different shear failure mechanisms (shear, punching or a mixed mode between them). Subgroups of tests were organized on which only a specific parameter was varied in the respective references. The sectional shear caused by the concentrated loads achieved in the tests V_{Fu} was normalized by the effective depth d_l and the root of the compressive strength of concrete f_c . Figure 8a shows the normalized shear resistance as a function of the shear slenderness a_v/d_l for 75 test results



and Figure 8b shows the cracking pattern of a set of tests from Reißen et al. [6] that vary only the ratio a_v/d_1 .

Figure 8. (a) Normalized sectional shear achieved in the tests as a function of (a) shear slenderness a_v/d_l and (b) change in the cracking pattern and corresponding failure mechanism as a function of the ratio a_v/d_l (cut views of a set of tests from Reißen et al. [6]). Source: Adapted from Sousa, Lantsoght and El Debs [24]. Note: WB = wide-beam shear failure (one-way shear); P = punching failure; WB + P = mixed failure mode between one-way shear and punching shear.

The results indicated that the tested one-way shear load does not increase by increasing the ratio a_v/d_l , as also demonstrated by other authors [5,7,14]. In fact, the tested shear load decreases markedly until a certain value of $a_v/d_l = 2$ or 3, and after this, it keeps almost the same level. Added to that, it was observed that punching failures become the critical failure mechanism for $a_v/d_l > 4$. In practice, this means that the failure restricts to a narrower length around the load, which could support the definition of a reduced effective shear width when the shear slenderness a_v/d_l increases.

Figure 8b shows how the failure mechanism changes by increasing the ratio a_v/d_l (these figures show the cracking pattern by cut views at the symmetry axis of a set of slabs tested by Reißen et al. [6]). When the load is placed relatively close to the support, arching action and shear compression failure are most likely to occur along a larger slab strip. In such cases, it is frequent that a one-way shear crack is also visible at the slab sides. Increasing the ratio a_v/d_l , the cracking pattern from such tests indicates a punching failure around the load, which naturally is a failure mechanism concentrated around the load. Therefore, the corresponding effective shear width should be decreased compared to that with the load closer to the support.

2.3. Background Calculations for Punching Capacity Predictions

The punching capacity of one-way slabs under concentrated loads is generally less discussed than the respective one-way shear capacity of such slabs. Consequently, enhanced recommendations to assess the punching capacity of such slabs using analytical code expressions are scarce [20]. Until now, most publications showed a large scatter between tested and predicted resistances of one-way slabs under concentrated loads when using punching shear expressions [12,26]. Since such slabs may fail either by one-way shear or two-way shear (punching), this study addressed both shear failure mechanisms.

In both EN 1992-1-1:2004 [25] and *fib* Model Code 2010 [21], the punching capacity can be determined by the following expressions:

$$P_{R,predicted} = v_{R,punch} \cdot b_0 \tag{16}$$

where $v_{R,punch}$ is the unitary punching capacity (punching capacity per unit length) and b_0 is the shear-resisting control perimeter.

The unitary punching capacity according to the Eurocode EN 1992-1-1:2004 [25] is calculated as (using average values for material properties to compare tested and predicted resistances):

$$v_{R,punch,EN} = \max \begin{cases} \left[C_{R,c} k (100\rho_{avg} f_c)^{1/3} + k_1 \sigma_{cp} \right] d_{avg} \\ \left(v_{\min} + k_1 \sigma_{cp} \right) d_{avg} \end{cases}$$
(17)

with d_{avg} in [mm] and f_c in [MPa]

$$\rho_{avg} = \sqrt{\rho_l \cdot \rho_t} \le 0.02 \tag{18}$$

$$d_{avg} = (d_l + d_t)/2 \tag{19}$$

$$v_{\min} = 0.035k^{3/2}f_c^{1/2}$$
 (20)
 $C_{R,c} = 0.18$ (21)

$$C_{R,c} = 0.18$$
 (21)

$$k = 1 + \sqrt{\frac{200}{d_{avg}}} \le 2$$
, with d_{avg} in [mm] and f_{ck} in [MPa] (22)

The unitary punching capacity according to the *fib* Model Code 2010 [21] is calculated as (using average values for material properties to compare tested and predicted resistances):

$$v_{R,punch,MC} = k_{\psi} \cdot \sqrt{f_c} \cdot d_{avg}$$
, with f_{ck} in [MPa] (23)

$$k_{\psi} = \frac{1}{1.5 + 0.9 \cdot \psi \cdot d_{avg} \cdot k_{dg}} \le 0.6, \text{ with } d_{avg} \text{ in [mm]}$$

$$(24)$$

$$k_{dg} = \frac{32}{16 + d_g} \ge 0.75$$
, with d_g in [mm] (25)

For Level of Approximation III:

$$\psi = 1.2 \cdot \frac{r_s}{d_{avg}} \cdot \frac{f_y}{E_s} \cdot \left(\frac{m_E}{m_R}\right)^{3/2} \tag{26}$$

In order to allow the predictions of punching capacity with the fib Model Code 2010 expressions without the use of linear elastic finite element analyses to estimate m_E , some adaptations are needed. The first one is to replace the relation m_E/m_R by $P_{E(i)}/P_{flex}$ in the expression of ψ . In this study, $P_{E(i)}$ is the actual applied concentrated load and P_{flex} is the slab flexural capacity calculated according to yield line analyses. In this way:

$$\psi_{ij} = 1.2 \cdot \frac{r_{s,ij}}{d_{avg}} \cdot \left(\frac{P_{E(i)}}{P_{flex}}\right)^{3/2}, \text{ with } i = \{x, y\}; j = \{1, 2\}$$
(27)

At this point, it is important to note that the punching capacity is determined iteratively until the applied concentrated load $P_{E(i)}$ equals the calculated punching capacity $P_{R,predicted}$ (see Figure 3b).

In Equation (27), $r_{s,ij}$ is generally defined as the length of the loading center to the point of contra-flexure (zero bending moment) in the evaluated direction. In this study, the following values are adopted as a simplification in the absence of results from numerical analyses:

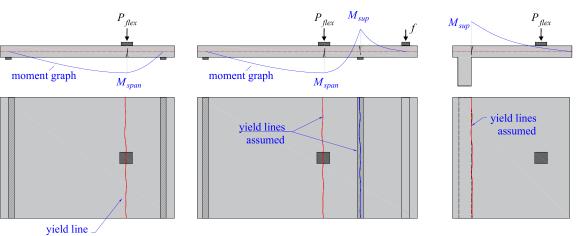
$$r_{s,x1} = a$$

 $r_{s,x2} = l_{span} - a$
 $r_{s,y1} = r_{s,y2} = b_{slab}/2$
(28)

Figure 9 shows the assumed yield line patterns to the flexural assessment of the tests for varying support conditions. For the one-way slabs with continuity on one of the supports, both moments at the support and at the span were checked. The flexural capacity P_{flex} was assumed as the load F that causes M_{span} or M_{sup} to be equal to M_r . The yielding moment M_r was calculated according to the equation (where ρ_l is the reinforcement ratio and b_{slab} the slab width) [17]:

$$M_r = m_r \cdot b_{slab}$$

$$m_r = \rho_l \cdot f_y \cdot b_{slab} \cdot d_l^2 \cdot \left(1 - \frac{\rho_l \cdot f_y}{2 \cdot f_c}\right)$$
(29)



assumed

Figure 9. Yield line pattern for flexural assessment of simply supported, continuous and cantilever slabs.

The shear-resisting control perimeter b_0 is set at the distance $\alpha \cdot d_{avg}$ from the loaded area according to the studied code. The value of α is 2 for the Eurocode [25] and 0.5 for the *fib* Model Code 2010 [21].

Another rule of thumb is that different layouts of the control perimeter can be critical and should be tested (Figure 10). In the case of one-way slabs with a large width, the most traditional control perimeter with four sides for simply supported slabs (Figure 10a) and three sides for cantilever slabs (Figure 10d) are the most critical ones. However, for simply-supported slabs with a reduced slab width compared to the load size, the control perimeter with two sides for simply supported slabs can be the most critical one (Figure 10b). Similarly, for loads close to the free edge, the layout with three sides can provide the lowest length for the control perimeter (Figure 10c).

In the case of cantilever slabs under concentrated loads, another aspect is discussed: the length b_k of the control perimeter (see Figure 10d). For slab–column connections, the length b_k has the following values for both Eurocode [25] and *fib* Model Code 2010 [21]:

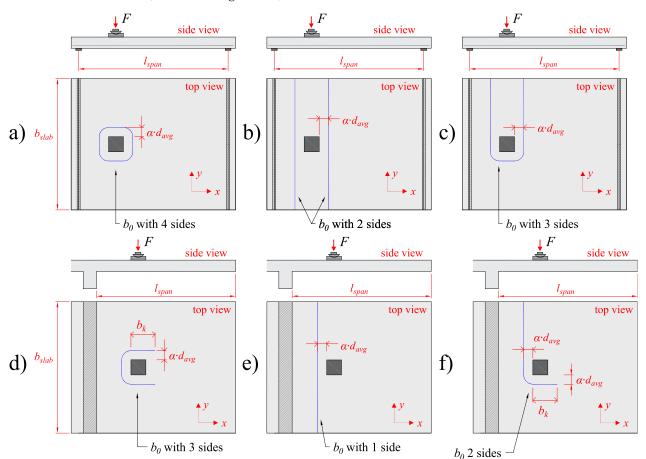
$$b_k = \min\{0.5 \cdot b_{load}; 1.5 \cdot d_{avg}\} \tag{30}$$

However, Vaz Rodrigues et al. [20] suggest using the following value for b_k (used in the following calculations):

$$b_k = b_{load} \tag{31}$$

2.4. Insights from the Literature for Punching Capacity Predictions

Traditionally, one-way slabs under concentrated loads have been investigated in most publications from the perspective of one-way shear failure [6,10]. However, Figure 11a shows that, based on the shear flow characteristics from such slabs, both one-way shear or punching failures may take place: (i) the shear flow close to the support is predominantly linear, which favor one-way shear failures (Detail A in Figure 11a); (ii) on the other hand,



the shear flow in the load vicinity is always radial, which could favor punching failures (Detail B in Figure 11a).

Figure 10. Different layouts of the control perimeter for simply supported slabs: (**a**) four sides, (**b**) two sides and (**c**) three sides; and for cantilever slabs: (**d**) three sides, (**e**) one side and (**f**) two sides.

According to previous studies [24], one or other failure mechanisms may occur as a function of the load position (or the ratio a_v/d_l) and slab width (or the ratio b_{slab}/l_{load}). At this point, it is important to note that the shear flow through the sides of the control perimeter close to the free edges is higher or lower as a function of the slab width (Figure 11a). Therefore, for punching capacity predictions, the effective contribution of these sides should be considered as a function of the slab width.

In other words, a possible way to improve the predictions of punching capacity for one-way slabs under concentrated loads would be to consider different contributions for each side of the control perimeter as a function of the load position and slab width (Figure 11b). At this point, Regan [19] was one of the first that propose to consider the influence of arching action for punching expressions. However, the effect of the slab width was not considered in this original approach.

Figure 11c shows the normalized failure load by the average effective depth and root of the compressive strength of the concrete for a set of 20 test results organized by Sousa, Lantsoght and El Debs [24]. In this subset of test results, the only parameter that varied among the tests connected by lines was the slab width and, consequently, the ratio b_{slab}/l_{load} . The reader can realize that by increasing the ratio b_{slab}/l_{load} , the normalized failure load increases almost linearly for each series of tests until reaching a plateau on which the governing failure mechanism starts to be punching. Before reaching such a plateau, the governing failure mechanism of such slabs is most likely one-way shear as a wide beam.

Figure 11d shows how the cracking pattern and, consequently, the governing failure mechanism changes by changing the slab width. In the test S15B-2 from Reiβen et al. [6],

the shear crack that crosses the compression chord arises from flexural cracks and reaches the load almost horizontally, typical of flexural-shear failures as wide beams. Additionally, such cracks extend over the whole slab width. On the other hand, in the tests with a slab width of 2.5 or 3.5 m, the shear crack at the cut view reaches the load with a crack inclined at around 45 degrees. Moreover, such cracking is not visible at the free sides of the slab, as is typical of punching failures.

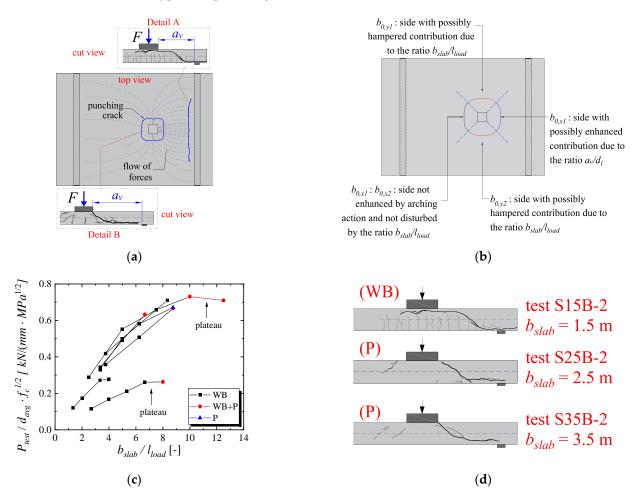


Figure 11. (a) Shear flow and possible shear failure mechanisms for the slab: one-way shear as wide beams, punching shear around the load and a mixed-failure mode; (b) sides enhanced or disturbed due to the ratio a_v/d_l and b_{slab}/l_{load} for a simply supported slab; (c) influence of the slab width to load size ratio b_{slab}/l_{load} on the failure load of slabs under concentrated loads (adapted from [24]); (d) influence of the slab width on the cracking pattern and consequently on the failure mechanism of the tests (adapted from Reißen et al. [6]). Note: WB = wide-beam shear failure (one-way shear); P = punching failure; WB + P = mixed failure mode between one-way shear and punching shear.

3. Proposed Approach

3.1. Proposed Approach for One-Way Shear

In this study, it is assumed that the one-way shear capacity increases for loads close to the support due to arching action benefitting the direct load transfer [27,28]. Therefore, the unitary shear capacity can be multiplied by the following factor:

$$\mu_{shear,1} = 1/\beta_{EC} \tag{32}$$

Herein, the factor β_{EC} is suggested for both shear codes (Eurocode and *fib* Model Code) since it correlated better with test results for loads close to the support.

The French effective shear width (Figure 7a) has been demonstrated to be adequate mainly to check the one-way shear capacity of slabs that failed in one-way shear or that are influenced by arching action [5,13]. The higher spreading angle of the *fib* Model Code 2010 for simply supported slabs overestimates the shear capacity of such slabs in comparisons between tested and predicted resistances of laboratory tests [14]. Because of this, the reference effective shear width is assumed as the French effective shear width.

In order to consider that the ultimate capacity of one-way slabs under concentrated loads does not increase by increasing the shear slenderness a_v/d_l [6,11] (see Figure 8a) and to avoid unsafe predictions of one-way shear capacity for $a_v/d_l > 3$ [10] (as shown in the following sections), a correction in the predicted effective shear width is proposed. In practice, this correction allows considering that the failure occurs along a narrower region in front of the load, mainly by punching, by increasing the shear slenderness a_v/d_l (Figure 12b). To this effect, a factor $\mu_{shear,2}$ is multiplied by the effective shear width calculated according to the French approach, $b_{eff,french}$. Consequently, the predicted effective shear width decreases as a_v/d_l increases (see Figure 12a).

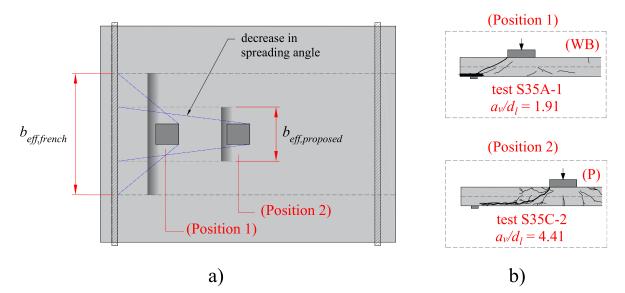


Figure 12. (a) Effective shear width corrected as a function of the shear slenderness a_v/d_l (the proposed effective shear width decreases as the shear slenderness increases) and (b) failure mechanism varying from one-way shear as wide-beam (WB) to punching shear (P) increasing a_v/d_l for the tests from Reißen et al. [6].

The correction factor for each code and support condition was derived by statistical regression analyses (Figure 13). In this approach, a comparison between the tested and predicted resistances was performed with the following set of assumptions: (i) the enhanced shear capacity for loads close to the support was considered by $\mu_{shear,1}$; (ii) the French effective shear width was used for both codes to estimated $V_{R,predicted}$; (iii) a linear fitting function was assumed for simplicity. In this study, the calibration of the factors according to the support condition was based on the different coefficients observed for the fitting functions. In practice, this method can be justified mainly due to the different shear flow that occurs for cantilever members (one line support) and simply supported or continuous members (two line supports).

In this way, the proposed effective shear width for any one-way shear model is calculated as:

$$b_{eff,proposed} = b_{eff,french} \cdot \mu_{shear,2}, \text{ with } b_{eff,proposed} \begin{cases} \leq b_{slab} \\ \geq 4 \cdot d_l \end{cases}$$
(33)

Table 2 describes the detailed expressions of $\mu_{shear,2}$ calibrated for each shear code provision. These factors were derived based on linear regression analyses observing the functions that fitted the ratio $V_{test}/V_{R,predicted}$ for each code (see Figure 13). For each code ($V_{R,predicted}$), the French effective shear width model and the factor $\mu_{shear,1}$ were applied.

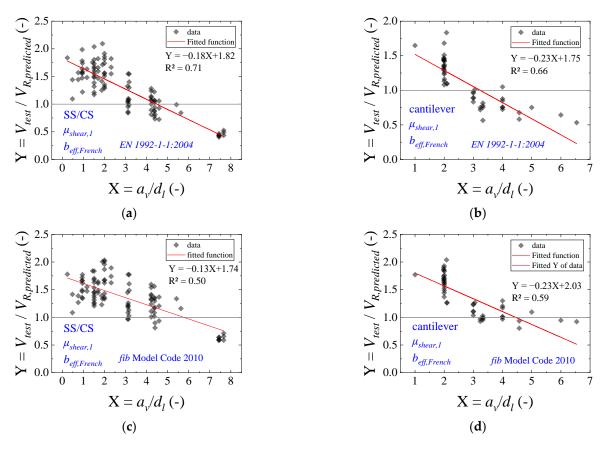


Figure 13. Calibration of $\mu_{shear,2}$ for (**a**) simply supported and continuous slabs using the current Eurocode expressions; (**b**) cantilever slabs using the current Eurocode expressions; (**c**) simply supported and continuous slabs using the *fib* Model Code 2010 expressions; (**d**) cantilever slabs using the fib Model Code 2010 expressions. Note: SS = simple support (hinged support); CS = continuous support; CT = cantilever slab.

Table 2. Factors $\mu_{shear,2}$ to correct the predicted effective shear width with the French approach when using different codes and support conditions. Note: Sup. Cond = support condition close to the load; SS = simple support (hinged support); CS = continuous support; CT = cantilever slab.

Code	Sup. Cond.	Factors
EN 1992-1-1:2004 [25]	SS, CS	$\mu_{shear,2} = -0.144 \cdot a_v / d_l + 1.456 \begin{cases} \geq 0 \\ \leq 1.50 \end{cases} $ (34)
EN 1992-1-1:2004 [25]	СТ	$\mu_{shear,2} = 0 - 0.184 \cdot a_v / d_l + 1.400 \begin{cases} \ge 0\\ \le 1.50 \end{cases} $ (35)
<i>fib</i> Model Code 2010 [21]	SS, CS	$\mu_{shear,2} = -0.104 \cdot a_v / d_l + 1.392 \begin{cases} \geq 0 \\ \leq 1.50 \end{cases} $ (36)
<i>fib</i> Model Code 2010 [21]	СТ	$\mu_{shear,2} = -0.184 \cdot a_v / d_l + 1.624 \begin{cases} \geq 0 \\ \leq 1.50 \end{cases} $ (37)

Therefore, the following expression can be applied to determine the predicted one-way shear capacity $V_{R,predicted}$:

$$V_{R,predicted} = \left(v_{R,shear,any} \cdot \mu_{shear,1}\right) \cdot b_{eff,proposed}$$
(38)

3.2. Proposed Approach for Punching Shear Capacity Predictions

In the literature, a large scatter between tested and predicted resistances is commonly reported for punching capacity predictions of one-way slabs under concentrated loads [12,26]. In practice, this occurs mainly due to two reasons: (i) most design codes do not discuss how the enhanced shear capacity for loads close to the support could be considered in punching capacity predictions; and (ii) the effect of the free edges disturbing the contribution of the control perimeter lateral sides is not considered in the calculations (Figure 2c). Consequently, the predictions of punching capacity may be overly conservative if the arching action is not considered for loads close to the support, or even the predictions may be unsafe for slabs with a reduced slab width compared to the load size [24].

The first step in order to improve the predictions of punching capacity with current design expressions, as suggested by Regan [19], is to consider that the different sides of the control perimeter develop different contributions to the punching capacity. In this study, the partition of the control perimeter, such as that shown in Figure 14a, addresses this need. However, the intersection of the control perimeter with the support for loads close to the support needs attention. Using the rounded corners for the control perimeter of the Eurocode, one may assume $b_{0x,1}$ as the length covered by the dashed blue lines (Figure 14b) or the straight length that intercepts the support (Figure 14c). However, such approaches would lead to very small values of $b_{0x,1}$ when the load is placed at $a_v = 0$ or when $a_v = 2d_{avg}$, respectively. Because of this, we concluded that the most consistent approach would consider $b_{0x,1}$ as the length between the middle points of the rounded corners (Figure 14d). Alternatively, and most simply for the Eurocode control perimeter, one can also use a squared control perimeter at $1.5d_{avg}$ (Figure 14e), which simplifies the calculations for the partitions of the control perimeter, as suggested by Regan [19]. In this way, the length $b_{0x,1}$ would not vary as a function of a_v (Figure 14f), and the total control perimeter b_0 would be very similar to that using rounded corners.

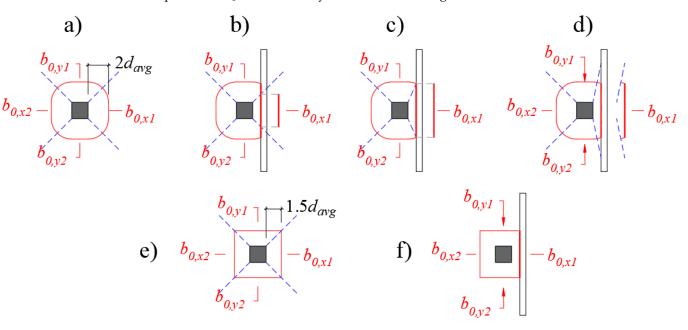


Figure 14. Possible partitions of the shear-resisting control perimeter for simply supported slabs and EN 1992-1-1:2004: (**a**–**d**) using the rounded corners; (**e**,**f**) using the squared control perimeter.

In the following sections, we compare the results using the partitions of Figure 14d,e for the Eurocode. In the case of the *fib* Model Code 2010 expressions, using the control perimeter with rounded and square corners at $0.5d_{avg}$ provides similar results (this is demonstrated in the next sections).

After defining the partitions of the control perimeter, the proposed approach is grounded on two main aspects: (i) the consideration of the enhanced shear capacity of the portion of the control perimeter close to the support ($b_{0x,1}$) when $a_v/d_l \le 2$; (ii) the reductions in the capacity for the lateral sides $b_{0,y1}$ and $b_{0,y2}$ as a function of the slab width.

The enhanced shear capacity for the portion $b_{0x,1}$ is achieved by multiplying the unitary shear capacity on this side by the factor $\mu_{punch,1}$, which is equal to that for one-way shear.

$$\mu_{punch,1} = 1/\beta_{EC}, \text{ with } \beta_{EC} = \frac{a_v}{2 \cdot d_l} \begin{cases} \ge 0.25\\ \le 1 \end{cases}$$
(39)

The impaired contribution of the sides $b_{0,y1}$ and $b_{0,y2}$ to the punching capacity of slabs with reduced width b_{slab} is considered by multiplying these sides by a correction factor $\mu_{punch,2}$ (Table 3). In this study, the same factors were proposed for both codes.

Table 3. Factor $\mu_{punch,2}$	for EN 1992-1-1:2004 and fib Model Code 2010.	

Code	Parameter	Factor $\mu_{punch,2}$
Eurocode EN 1992-1-1:2004	$t = \left(b_{slab} - l_{load} - 4 \cdot d_{avg}\right) / d_{avg}$	$\mu_{punch,2} = 0.2 \cdot t \left\{ \begin{array}{c} \ge 0\\ \le 1 \end{array} \right. \tag{40}$
fib Model Code 2010	$t = (b_{slab} - l_{load} - d_{avg}) / d_{avg}$	$\mu_{punch,2} = 0.2 \cdot t \left\{ \begin{array}{c} \ge 0\\ \le 1 \end{array} \right. \tag{41}$

Figure 15 shows how the factor $\mu_{punch,2}$ was calibrated. A comparison between tested and predicted resistances with the punching capacity expressions from Eurocode was performed (Figure 15a). This comparison demonstrated sensitivity in the predictions with the value of *t* and, consequently, the slab width. In this way, the function of $\mu_{punch,2}$ (assumed linear) was modified until removing this sensitivity (Figure 15b). As only the simply supported and continuous slabs varied the parameter *t* more extensively in the database than the respective cantilever slabs, the derivation of such parameters was based only on the results of simply supported and continuous slabs (97 test results).

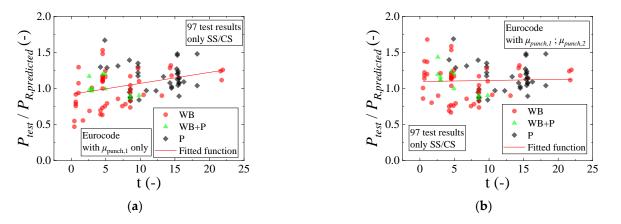


Figure 15. Comparison between tested and predicted resistances using the punching capacity expressions from Eurocode according to the parameter *t* (related to the slab width) for the dataset of simply supported and continuous slabs (97 tests results): (a) using only the factor $\mu_{punch,1}$ and (b) using both factors $\mu_{punch,1}$ and $\mu_{punch,2}$.

For cantilever slabs under concentrated loads, the predictions of punching capacity with the Eurocode were quite conservative for shear slenderness values of $a_v/d_l \approx 2$ (see Figure 16a). Since the effect of arching action by $\mu_{punch,1}$ was considered only until $a_v/d_l = 2$, this could indicate that a different factor should be used for cantilever slabs. However, even extending the length of influence until $a_v/d_l = 3$ did not significantly change the results. Because of this, another explanation was needed for such results. A possible explanation for these results was that observing the cracking pattern of the tests from Henze et al. [7], the failure mechanism for loads closer to the support of cantilever slabs would be more influenced by the longitudinal reinforcement at the top side of the slabs (Figure 16c,d). In other words, considering the predicted resistance as a function of the bottom reinforcement of cantilever slabs would lead to overly conservative predictions since such reinforcement ratios are significantly lower than the ones used at the top side of the slab. At this point, it is important to note that the bending moments for cantilever slabs are slightly different from cantilever beams since we always have sagging bending moments and hogging bending moments for cantilever slabs (see Figure $16e_{f}$). In order to keep the core of the expressions for the punching capacity of cantilever slabs by considering the bottom reinforcement in the expressions, an alternative is to consider another load position parameter in the expressions, such as the ratio a/l_{span} (Figure 16b). Consequently, it would be possible to consider some enhancements in the punching capacity as a function of the load position on the cantilever slab not related to arching action.

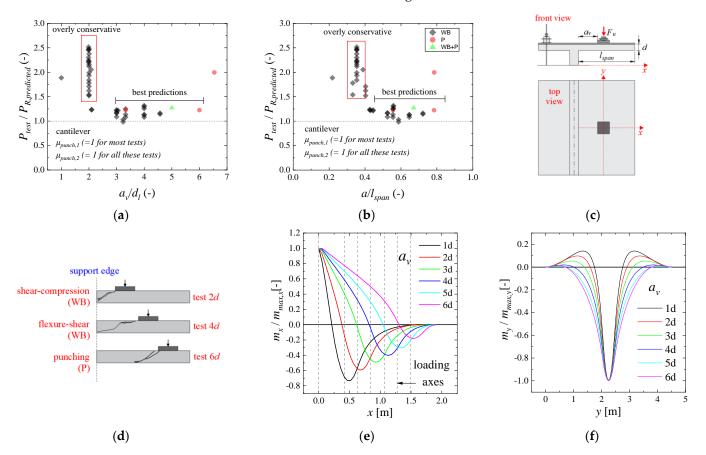


Figure 16. (a) Comparison between tested and predicted resistances with the punching capacity expressions from the Eurocode for cantilever slabs as function of the shear slenderness a_v/d_l ; and (b) as function of the ratio a/l_{span} ; (c) sketch of the tests performed by Henze et al. [7] on cantilever slabs; (d) cracking pattern of the tests performed by Henze et al. [7] (cut views); (e) distribution in the bending moments in the axis of symmetry of the slabs (axis *x*); (f) distribution in the bending moments in the transverse direction of the slabs (axis *y*).

In this study, the same tendency was not observed when using the *fib* Model Code expressions. At this point, it is important to note that the expressions of punching capacity $(v_{R,punch})$ with the *fib* Model Code 2010 [21] expressions already lead to enhanced resistances for loads close to the support by considering that the flexural capacity of the slabs P_{flex} is enhanced in such regions and, hence, smaller slab rotations ψ around the load occur for these regions. In the end, this effect is combined with the one expected from arching action, which leads to significant enhancements in resistance. In the expressions from Eurocode [25], on the other hand, the unitary shear capacity predicted is not influenced by the load position and can be enhanced only as a function of the arching action.

As a result, a third factor was considered in the expressions of punching capacity when using the Eurocode expressions $\mu_{punch,3}$ (Table 4).

Table 4. Factor	$(\mu_{punch,3})$) related	to the	ratio a/	l _{span} .
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Code	Factor $\mu_{punch,2}$	
Eurocode EN 1992-1-1:2004	$\mu_{punch,3} = 0.672 \cdot (a/l_{span})^{-0.76} \begin{cases} \geq 0.80 \\ \leq 2.15 \end{cases}$ (42)	
fib Model Code 2010	$\mu_{punch,3} = 1 (43)$	

Neglecting the influence of the shear demand from the self-weight in the control perimeter, the punching capacity can be determined for any of the codes by the following calculations (for cantilever slabs, the term $b_{0,x2} = 0$):

$$P_{R,proposed} = \begin{bmatrix} \left(v_{R,punch} \cdot b_{0,x1} \cdot \mu_{punch,1} \right) + \left(v_{R,punch} \cdot b_{0,x2} \right) \\ + \left(v_{R,punch} \cdot b_{0,y1} \cdot \mu_{punch,2} \right) + \left(v_{R,punch} \cdot b_{0,y2} \cdot \mu_{punch,2} \right) \end{bmatrix} \cdot \mu_{punch,3}$$
(44)

4. Database

The database used for validation of the proposed recommendations was organized by the authors and was published in the public domain [29]. This dataset includes 143 test results. The following references are included in this database: Bui et al. [30], Carvalho [31], Coin and Thonier [3], Damasceno [32], Ferreira [33], Lantsoght [34], Natário et al. [11,35], Reißen [14], Regan [19], Regan and Rezai-Jarobi [18], Rombach and Latte [36,37], Rombach and Henze [38], Vaz Rodrigues [39] and Vida and Halvonik [40].

In terms of support conditions: (i) 77 tests were conducted with the concentrated load applied closer to the simple support (SS: hinged support without continuity of the slab in the spanning direction); (ii) 20 tests were conducted with the concentrated load applied closer to the support with continuity of the slab in the spanning direction (CS); and (iii) 46 tests were conducted with the concentrated load applied on a cantilever slab (CT).

In terms of the governing failure mechanism in shear of the slabs: (i) 40 tests were classified as failing by punching (P: with predominant radial and circumferential cracks at the slab tensile side, occasionally with a visible conical crack at the bottom side, and without the arising of inclined shear cracks at the slab sides); (ii) 91 tests were classified as failing as wide beams in shear (WB = shear cracks similar to those of beams that failed in shear are visible at the slab sides and most cracks at the tension side of the slabs are parallel to the line support); (iii) 12 tests were classified as presenting a mixed mode between wide-beam shear and punching shear (WB + P = combines characteristics from both failure mechanisms).

Table 5 shows the ranges of parameters in the database. All experiments were conducted on thicknesses less than 0.60 m. Hence, such tests do not include the size effect that may occur for actual solid slab bridges. In addition, all tests selected have a relation between the member width and effective depth higher than 5 and, therefore, are representative of slabs according to the Eurocode. The shear slenderness tested varied between 0.24 and 7.66. Therefore, the database includes tests both influenced and not influenced by arching action.

Parameter	Minimum	Maximum
<i>h</i> (m)	0.10	0.30
b _{slab} (m)	0.60	4.50
$\mathbf{t} = (b_{slab} - l_{load} - 4d_{avg})/d_{avg}$	0.45	27.21
l _{span} (m)	0.90	4.00
b _{slab} /l _{load} (-)	1.67	23.08
b_{slab}/d_l (-)	5.66	29.41
a_v/d_l (-)	0.24	7.66
f _c (MPa)	19.20	77.74
<i>ρl</i> (%)	0.602	2.150
$ ho_t$ (%)	0.132	1.526

Table 5. Ranges of parameters in the database.

5. Results

In this section, the results are presented separately according to the design code expressions applied and show the tendencies as a function of the governing failure mechanism of the tests. In this way, the benefits of the proposed recommendations can be distinguished more closely.

5.1. Results with the European Code Expressions

Figure 17 shows the ratio between tested and predicted resistances for one-way shear $(V_{test}/V_{R,predicted})$ and punching shear $(P_{test}/P_{R,predicted})$ considering two cases: (i) without the use of any correction factor μ_{shear} or $\mu_{punching}$; (ii) with the use of the correction factors μ_{shear} or $\mu_{punching}$.

Figure 17a shows that the predictions of one-way shear capacity are conservative in the range $a_v/d_l < 2$, even using β_{EC} to decrease the sectional shear V_{test} ($V_{test,red}/V_{R,predicted} > 1$). On the other hand, the predictions of one-way shear capacity for the tests with $a_v/d_l > 5$ may become quite unsafe ($V_{test}/V_{R,predicted} < 0.6$). In Figure 17a, this occurs because the effective shear width predicted with the French approach increases excessively by increasing the shear slenderness a_v/d_l . Figure 17d shows that the accuracy and precision of the predictions improved notably by using the proposed correction factors to consider the arching action and the reduced effective shear width for large shear slenderness a_v/d_l . The average ratio $V_{test}/V_{R,predicted}$ changed from 1.22 to 1.25 and the coefficient of variation decreased from 33.1% to 17.2%.

Figure 17b shows the predictions of punching capacity with the EN 1992-1-1:2004 as a function of the ratio between the slab width and load size in the transverse direction b_{slab}/l_{load} and without the use of any correction factor ($\mu_{punching,1}$ and $\mu_{punching,2}$). Figure 17b shows that the predictions may become quite unsafe for the tests that failed as wide beams in one-way shear, mainly for ratios $b_{slab}/l_{load} < 7.5$ (see Detail 1 in Figure 17b). This occurs because the contribution of the sides of the control perimeter parallel to the slab-free edges was overestimated with the traditional approach (which is rarely discussed in most publications). In the same way, the predictions of punching capacity with the European code expressions may become overly conservative if arching action is not considered in the portion of the control perimeter close to the line support when $a_v/d_l < 2$ (see Detail 2 in Figure 17b). On the other hand, Figure 17e shows that the proposed recommendations significantly improve the predictions of punching capacity. Comparing Figure 17b,e, the average ratio between tested and predicted resistances changes from 1.44 to 1.17 and the coefficient of variation decreases from 40.1% to 22.1%.

Figure 17c,f also shows the relation $P_{test}/P_{R,predicted}$, with and without the corrections factors for punching, respectively, but using a square control perimeter such as suggested by Regan [19] and sketched in Figure 14e,f. As can be seen, the results using a square control perimeter is similar to that achieved with the round control perimeter but slightly more conservative (see Figure 17c,f).

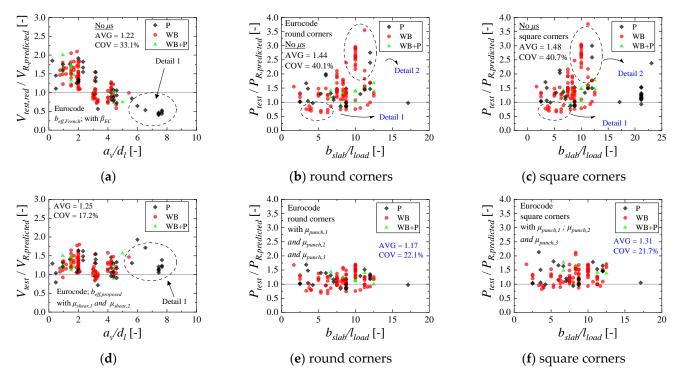


Figure 17. Comparison between tested and predicted resistances the European code expressions for: (a) one-way shear and without the correction factors μ ; (b) punching shear, without the correction factors μ , and using round corners for the control perimeter; (c) punching shear, without the correction factors μ , and using square corners for the control perimeter; (d) one-way shear with the correction factor μ ; (e) punching shear expressions, with the correction factors, and using round corners for the control perimeter; (f) punching shear expressions, with the correction factors μ s, and using square corners for the control perimeter; (b) punching shear expressions, with the correction factors μ s, and using square corners for the control perimeter; (f) punching shear expressions, with the correction factors μ s, and using square corners for the control perimeter. Note: P = punching failure; WB = wide-beam shear failure in one-way shear; WB + P = mixed mode between one-way shear and punching.

5.2. Results with the Fib Model Code 2010 Code Expressions

Figure 18a,d evaluates the relation between tested and predicted resistances for oneway shear with the fib Model Code expressions. The results shown in Figure 18a do not include any correction factor $\mu_{shear,1}$ or $\mu_{shear,2}$. At this point, however, it is important to note that the *fib* Model Code 2010 adopts the factor β_{MC} , to consider the arching action (having a similar effect to the proposed $\mu_{shear,1}$). Figure 18d shows the results, including the proposed correction factors $\mu_{shear,1}$ or $\mu_{shear,2}$.

In summary, similar results compared to that presented for the Eurocode expressions are observed (Figure 17). The predictions of one-way shear capacity were conservative in the range $a_v/d_l < 2$. On the other hand, these predictions were quite unsafe for $a_v/d_l > 5$ (Figure 18a). Using the correction factors $\mu_{shear,1}$ and $\mu_{shear,2}$, these shortcomings are corrected (Figure 18d). The average ratio $V_{test}/V_{Rpredicted}$ reduced from 1.44 to 1.26 and the coefficient of variation decreased from 31.9% to 18.2%, comparing Figure 18a,d.

Evaluating the predictions with the punching capacity expressions from *fib* Model Code 2010 (Figure 18b,e), the results differ more from those observed with the Eurocode expressions (Figure 17b,e). Figure 18b shows that, in general, the predictions of punching capacity without the correction factors $\mu_{punching}$ already reached enhanced levels of accuracy (coefficient of variation lower than 20%, for instance, and the average ratio $P_{test}/P_{R,predicted}$

between 1.0 and 1.20). Using the proposed correction factors to consider the disturbed contribution as a function of the slab width, the predictions on this range were slightly enhanced (Figure 18e). Comparing Figure 18b,e, the average ratio $P_{test}/P_{R,predicted}$ decreased slightly from 1.14 to 1.09 and the coefficient of variation varied from 17.0% to 15.6%.

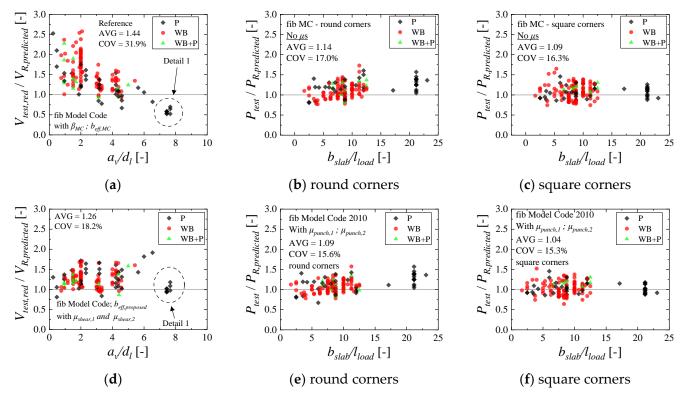


Figure 18. Comparison between tested and predicted resistances the *fib* Model Code 2010 expressions for: (**a**) one-way shear and without the correction factors μ ; (**b**) punching shear, without the correction factors μ , and using round corners for the control perimeter; (**c**) punching shear, without the correction factors μ , and using square corners for the control perimeter; (**d**) one-way shear, with the correction factors μ ; (**e**) punching shear expressions, with the correction factors, and using round corners for the control perimeter; (**f**) punching shear expressions, with the correction factors, and using square corners for the control perimeter; WB = wide-beam shear failure in one-way shear; WB + P = mixed mode between one-way shear and punching.

These results indicate that the presented approach, without the correction factors, already takes into consideration some important aspects of the problem. For instance, the critical shear crack theory (CSCT) expressions of punching already take into account the part of the enhanced shear capacity for loads close to the support due to the smaller slab rotations in such regions.

Comparing the predictions of punching capacity using round corners (Figure 18b,e) and square corners (Figure 18c,f), the results are quite similar. This occurs because placing the control perimeter at $0.5d_{avg}$ makes the total length of the control perimeter more similar, even with the different shapes.

6. Discussion

In the literature, most evaluations of the shear capacity of one-way slabs under concentrated loads focus on the predictions of the one-way shear capacity [6,7,10]. Consequently, most recommendations until now have focused on improving the definitions of the effective shear width [5,10] or improving the evaluation of the shear demand by the concentrated loads [7,41,42]. Therefore, these studies contributed to evaluating the problem from a narrower perspective since, in practice, these slabs may fail either by one-way shear or punching shear, even for loads close to the support (Detail 1 in Figure 17a, for instance).

In addition, in most studies in which the one-way shear capacity was evaluated, the proposed recommendations were frequently validated only to a specific support condition (such as cantilever slabs, [10]). Consequently, this study brings a more comprehensive contribution since it discusses both one-way shear and two-way shear failure mechanisms and is validated to a dataset of slabs with varied support conditions and load layouts. At this point, the following aspects of the problem are highlighted: (i) For either cantilever slabs, simply supported slabs and continuous slabs, a decrease in the effective shear width as a function of the shear slenderness is justified, regardless of the code expressions. In the end, despite being based on very different expressions, both Eurocode and *fib* Model Code expressions reached similar levels of accuracy. (ii) The level of accuracy for the punching expressions from different codes varies more significantly. In practice, it is more difficult to reach enhanced predictions of punching capacity with the Eurocode expressions for cantilever slabs since the reinforcement considered for punching is different from that considered for one-way shear and because the punching resistance expressions are not sensitive to the load position. As a consequence, the failure load predicted with the punching expressions can be overly conservative if the slabs fail as wide beams in one-way shear. On the other hand, as the *fib* Model Code expressions take into consideration the load position in the determination of the punching capacity through the slab rotations, the predictions of punching capacity are more accurate, even when the slabs failed in one-way shear and despite considering the bottom reinforcement for cantilever slabs.

By evaluating the governing failure mechanism of the tests, it is interesting to note that both one-way shear and punching shear failures may occur for loads close to the support $(a_v/d_l < 2)$ (Figure 17a, for instance). Additionally, it can be seen that the ultimate loads were enhanced for $a_v/d_l < 2$ regardless of the governing failure mechanism being one-way shear or punching shear (Figure 17a). Therefore, these results indicate a close relation between one-way shear mechanisms and two-way shear mechanisms for loads close to the support in one-way slabs.

It is also interesting to note that the predictions of one-way shear capacity with the *fib* Model Code 2010 expressions follow the same tendency observed with the European code expressions: conservative results for shear slenderness $a_v/d_l \le 2$ and unsafe predictions for large values of a_v/d_l . Since the shear expressions of the *fib* Model Code 2010 already take into account the beneficial effect of short shear spans and the detrimental effect of the large shear spans through the calculations of m_E and v_E , this result draws attention. In practice, this occurs because the influence of the arching action is more significant than the effect of smaller m_E for $a_v/d_l < 2$ [15]. In the same way, the effect of larger bending moments m_E for $a_v/d_l > 5$ (which decreases the unitary shear capacity $v_{R,shear,MC}$) does not compensate for the increase in the effective shear width when the load is placed so far from the support with the current French approach $b_{eff,French}$ or *fib* Model Code rules to determine the effective shear width. Therefore, the predictions of one-way shear capacity for large shear slenderness can be safe only if the effect of a reduced effective shear width is considered in the expressions, as proposed in this paper.

Notably, the predictions of the punching capacity with the *fib* Model Code expressions did not change significantly by using the proposed factors compared to the Eurocode expressions. The reasons for this are: (i) the shear-resisting control perimeter with the *fib* Model Code is less sensitive to the slab width, as the control perimeter is set at the distance of $0.5d_{avg}$ from the loaded area, and (ii) because the expressions of the *fib* Model Code 2010 already take into account the influence of a reduced shear span in the expressions by calculating the slab rotations. Moreover, the unitary punching capacity is greater than the corresponding unitary shear capacity in one-way shear [43], as the failure for the first always occurs around the load, which is enhanced by significant confinement stresses [44]. In this way, the enhanced punching capacity for loads close to the support is already partially considered without a factor $\mu_{punching,1}$ through the (i) enhanced unitary punching capacity compared to the one-way shear capacity and (ii) the calculations of the slab rotations around the load.

In summary, this study shows that arching action is a key parameter for loads close to the support, mainly for the one-way shear expressions. Additionally, this study shows that considering a reduced shear demand V_E by the factor β or improved shear capacity V_R by $\mu_{shear,1}$ leads to similar results for the tests with $a_v/d_l < 2$. Concerning the effective shear width, this study demonstrates with different one-way code expressions that a simple correction in the French effective shear width by the factor $\mu_{shear,2}$ allows for improving the accuracy of the one-way shear expressions for loads far from the support. In this way, the factor $\mu_{shear,2}$ allows consideration that a possible one-way shear failure or punching failure will develop under a narrower slab strip.

For the punching shear expressions, however, different results were observed. For the Eurocode expressions, consideration of arching action, slab width and the position a/l_{span} plays a key role in enhancing the predictions of punching capacity, mainly when the slabs may fail as wide beams and for cantilever slabs. On the other hand, the *fib* Model Code expressions are less dependent on such factors to reach enhanced levels of accuracy. In practice, this occurs mainly because the arching action is indirectly considered for the punching shear expressions through the calculations of the slab rotations, which decrease for loads close to the support, and also because the unitary punching strength in the *fib* Model Code is larger than the corresponding unitary one-way shear strength.

For future studies, however, it seems essential to validate such insights for the combination of concentrated loads representing the whole design truck or tandem. At this point, it is important to note that the number of tests with a combination of concentrated loads is very limited compared to that with single concentrated loads. Since testing such loading combinations is challenging, using numerical models may be a good alternative [23,45,46].

7. Conclusions

This study evaluated one-way slabs under concentrated loads that failed in different shear failure mechanisms. Both one-way shear and punching shear resistance predictions were discussed according to the current Eurocode [25] and *fib* Model Code 2010 expressions [21]. From the results observed with and without the proposed recommendations, the following conclusions can be drawn:

- The ultimate capacity of one-way slabs under concentrated loads increases significantly when the loads are placed close to the support at distances $a_v/d_l \leq 2$, due to arching action, regardless of the slabs failing in one-way shear as wide-beam (WB) or punching shear (P). In this study, the enhancement factor $\mu_{shear,1}$ and $\mu_{punch,1}$ are applied for both one-way shear and punching shear expressions to consider this mechanism. Comparatively, the ultimate resistance of the slabs decreases significantly when the loads are placed at distances $a_v/d_l \geq 3$. At such positions, most slabs from the database failed by punching, which is a failure mechanism concentrated around the load. Therefore, a reduced effective shear width should be employed if the one-way shear resistance needs to be checked at such positions. In this study, the factor $\mu_{shear,2}$ allows for decreasing the effective shear width for larger distances from the load to the support.
- In the punching shear resistance predictions, however, the slab width may also play a significant role. For slabs with a reduced slab width compared to the effective depth, for instance, t < 5 with $t = (b_{slab} l_{load} 4d_{avg})/d_{avg}$, the contribution of the sides of the control perimeter parallel to the free edges is reduced due to the small shear flow going through these sides. In this study, it is proposed to multiply the contribution of these sides by $\mu_{punch,2}$ to consider this effect. In the case of cantilever slabs, and particularly with the Eurocode expressions, another aspect considerably influences the predictions of punching capacity. The punching capacity expressions use the bottom reinforcement of the slab in the calculations, and many of these slabs fail in one-way shear, presenting higher demand on the top reinforcement of the slabs. Consequently, the predictions of punching capacity can become overly conservative

for loads placed at distances a_v/d_l close to 2. Because of this, a third factor was needed to reach enhanced predictions for cantilever slabs using the Eurocode expressions.

- The one-way shear capacity predictions are significantly enhanced by considering the arching action for loads close to the support by a factor $\mu_{shear,1}$. Furthermore, the transition from one-way shear failures as wide-beam (WB) to punching failures (P) by increasing the shear slenderness a_v/d_l can be considered in a simplified way by multiplying the predicted effective shear width $b_{eff,french}$ by the factor $\mu_{shear,2}\mu_{shear,2}$. In this way, enhanced predictions of one-way shear capacity can be achieved for the tests, even when they fail by punching. In practice, these observations were valid for both codes (Eurocode and *fib* Model Code).
- The predictions of punching capacity with the Eurocode expressions are significantly enhanced considering the factors related to arching action and to the slab width in the proposed approach. In the case of the *fib* Model Code 2010 expression, these enhancements were less pronounced since the results without the proposed factors already led to relatively enhanced predictions. In other words, the proposed recommendations to calculate the slab rotations and respective shear capacity on each portion of the control perimeter (without the use of numerical models) have already led to good levels of accuracy.
- In general, the one-way shear and punching shear predictions led to similar levels of accuracy when using the proposed recommendations. In the case of the current Eurocode, the average ratio $V_{test}/V_{R,predicted}$ was 1.25 with a coefficient of variation of 17.2%, while the average ratio $P_{test}/P_{R,predicted}$ was 1.17 with a coefficient of variation of 22.1%. In the case of the *fib* Model Code 2010, the average ratio $V_{test}/P_{R,predicted}$ was 1.26 with a coefficient of variation of 18.2% and the average ratio $P_{test}/P_{R,predicted}$ was 1.09 with a coefficient of variation of 15.6%. Therefore, both one-way shear and punching shear predictions may lead to close estimations of the ultimate capacity, regardless of the governing failure mechanism of the slabs, when the parameters that influence the transition from one failure mechanism to another are embedded in the calculations.

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Notation

а	shear span: distance between the center of the support and the center of the load
a_v	clear shear span: distance between face of support and face of load
b_0	total length of the shear-resisting control perimeter
$b_{0,x1}$	side of the control perimeter in the spanning direction between the load and the
1.	closer support
$b_{0,x2}$	side of the control perimeter in the spanning direction between the load and the
Ь	far support
b _{0,y1}	side of the control perimeter in the transverse direction close to the free edge 1 side of the control perimeter in the transverse direction close to the free edge 2
b _{0,y2}	effective shear width
b _{eff}	proposed effective shear width
b _{eff,proposed}	French effective shear width
b _{eff,french}	slab width
b _{slab} b.	size of the concentrated load in the slab width direction (transverse direction)
b _{load} d	average effective depth of the flexural reinforcement
$d_{avg} \\ d_1$	effective depth towards longitudinal steel
d_t	effective depth towards transverse steel
d_g	maximum aggregate size
d_{g0}	reference aggregate size (=16 mm in fib Model Code 2010)
d_{dg}	parameter that considerers the crack roughness
и _{dg} fc	average compressive strength measured on cylinder specimens
· .	steel yielding stress in the evaluated direction (<i>x</i> = longitudinal direction and
f_{yi}	y = transverse direction)
h _{slab}	slab thickness
k k	constant accounting for size effect in one-way shear for EN 1992-1-1:2004
k_1	factor accounting for axial forces in one-way shear for EN 1992-1-1:2004
k_{dg}	coefficient for aggregate size $(=32/(16 \text{ mm} + dg) \text{ in } fib \text{ Model Code 2010})$
k_v	factor accounting for strain effect and member size in <i>fib</i> Model Code 2010
k_{ψ}	factor accounting for effect of crack widths and roughness of cracks on shear strength
÷Ψ	in <i>fib</i> Model Code 2010
l _{span}	span length
l _{load}	size of the concentrated load in the span direction
ls	is the length of the sides with one-way shear behavior
$m_{R,i}$	yielding moment per unit length in the evaluated direction
m _{max}	maximum bending moment at the control section for a given applied load
$m_{s,ij}$	averaged acting bending moment at the loading plate edge ij within the width b_s
m_{Ed}	design bending moment at the control section
r _s	distance between the center of the concentrated load and the line of contraflexure
	of moments (subscripts x, y refers to the direction considered)
r _{s,ij}	distance between the center of the concentrated load and the point of contraflexure
	in the evaluated direction
υ	shear force per unit length (nominal shear force)
v_E	shear force at the control section
v_{Ed}	design shear force at the control section
v_{min}	minimum one-way shear resistance per unit length in EN 1992-1-1:2004
$v_{R,shear}$	unitary one-way shear resistance
v_g	shear forcer per unit length in the control section placed at $a/2$ due to the self-weight
w _{cr}	width of the critical shear crack
z	effective shear depth in <i>fib</i> Model Code 2010
A_s	cross-sectional area of flexural reinforcement
$C_{R,c}$	calibration factor in the shear and punching expressions of EN 1992-1-1:2004
E_c	modulus of elasticity of concrete
E_s	steel modulus of elasticity
F	applied concentrated load

Г	
F _{Ed}	design concentrated load
F _{predicted}	predicted load that causes a one-way shear failure or two-way shear failure
F_u	applied concentrated load at failure
F_{hyp}	arbitrary concentrated load
L	span length
V _{control}	total shear force going through the evaluated direction along the slab width
V_{Ed}	design shear action
V_{Fu}	shear force due to the concentrated load F_u
V _{test}	measured one-way shear force at failure in the tests for a section at $a/2$.
V_R	one-way shear capacity
$V_{R,predicted}$	predicted one-way shear resistance
V_{Rd}	design one-way shear capacity
$V_{R,CSCT}$	predicted one-way shear resistance with the CSCT expressions
$V_{R,ij}$	punching shear strength corresponding to $b_{0,ij}$
P_{test}	maximum applied concentrated load at failure
P_{Ed}	design concentrated loads
P_{Rd}	design punching capacities
P _{predicted}	predicted punching resistance
P_{flex}	concentrated load associated with the slab flexural capacity
P _{R,punching}	total shear force resisted by punching
β_{shear}	enhancement factor to account for arching action
$ ho_{avg}$	average flexural reinforcement ratio considering both directions
ρ_l	flexural reinforcement ratios in longitudinal direction
ρ_t	flexural reinforcement ratio in transverse direction
ψ	rotations around the loaded area
ψ_{ij}	rotations in each side of the control perimeter
ε_x	strain in the control depth for one-way shear analyses
ε _y	is the flexural reinforcement yield strain
γ	concrete specific weight (assumed = 24 kN/m^3 in this study)
γ _c	partial safety factor of concrete factor accounting for arching action in one-way shear analyses
$\mu_{shear,1}$	
$\mu_{shear,2}$	factor accounting for reduced b_{eff} for loads far away from the support factor accounting for arching action in punching shear analyses
$\mu_{punch,1}$	factor accounting for the influence of the slab width in the effective contribution of
$\mu_{punching,2}$	the sides $b_{0,\nu/2}$ and $b_{0,\nu/2}$ to the punching capacity
11	correction factor related to the load position in cantilever slabs for punching
$\mu_{punching,3}$	capacity predictions
AVG	average
COV	coefficient of variation
P	observed failure mode is punching failure
SS	test was performed with the load closer to the simple support
CS	tests was performed with the concentrated loads close to a continuous support
CT	test was performed with the concentrated load applied on a cantilever slab
WB	observed failure mode is wide-beam shear failure
WB + P	the observed failure mode combines characteristics of WB and P

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