



Article

Physical and Numerical Modelling on the Mixing Condition in a 50 t Ladle

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Abstract: The bubbly flow and mixing conditions for gas stirring in a 50t ladle were investigated by using physical modelling and mathematical modelling. In the physical modelling, the effect of the porous plugs' configurations on the tracer homogenization was studied by using a saturated NaCl solution to predict the mixing time and a color dye to show the mixing pattern. In the mathematical modelling, the Euler–Lagrange model and species transport model were used to predict the flow pattern and tracer homogenization, respectively. The results show that, for a ±5% homogenization degree, the mixing time with dual plugs using a radial angle of 180° is shortest. In addition, the mixing time using a radial angle of 135° decreases the most with an increased flow rate. The flow pattern and mixing conditions predicted by mathematical modelling agree well with the result of the physical modelling. For a ±1% homogenization degree, the influence of the tracer's natural convection on its homogenization pattern cannot be neglected. This is especially true for a 'soft bubbling' case using a low gas flow rate. Overall, it is recommended that large radial angles in the range of 135°~180° are chosen for gas stirring in the present study when using dual porous plugs.

Keywords: ladle; gas bubbling; tracer mixing; physical modelling; mathematical modelling

1. Introduction

The homogenization of temperature and alloys are of great importance in metallurgical processes, such as ladle, tundish, and continuous casting. In ladle metallurgy, the mixing pattern has a large influence on the alloying time. Moreover, the inclusion removal and chemical reactions are also closely related to the flow distribution [1,2]. In order to optimize the process, argon bubbling is widely used to enhance the stirring conditions. With gas bubbling, not only the refining time decreases and the production efficiency increases, but also the steel's quality can be greatly improved.

In this research area, a large number of studies were conducted on the flow pattern and mixing conditions in the ladle, using physical and mathematical models. In the physical modelling, the criteria for dynamic similarity [3,4] in gas-stirred ladles were investigated both theoretically and experimentally. For the alloy homogenization in the physical experiment, the mixing time and flow pattern in the ladle was affected by plug numbers, plugs' positions in the radial direction, and dual plugs' angles, and these were studied the most [5–14]. Moreover, the conducting materials are usually used as tracer additions for the electrical conductivity sensors [5,15]. For the mathematical modelling, the Euler–Euler approach or Euler–Lagrange approach is commonly used to calculate the flow pattern and the species transport model, or a user-defined scalar is used to predict the mixing conditions.

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Several studies on the research topic were reviewed and are summarized in Table 1. Joo and Guthrie [5] studied the mixing mechanisms as a function of the porous plug location, tracer injection point, and ladle monitoring point. It was reported that, for single-plug bubbling, the optimal location for a porous plug is at the mid-radius placement. Furthermore, a mid-radius placement of porous plugs was also recommended for diametrically opposed dual-plug bubbling. In Mandal et al.'s [8] work, the mixing time, liquid depth, vessel radius, and gas flow rate with dual porous plugs' stirring were correlated. For a 95% percentage homogenization degree, an empirical expression of mixing time was derived: $\tau_{95pct} = 15Q^{-0.38}L^{-0.5}R^{2.0}$ (where τ , Q, L, and R correspond to the mixing time, gas flow rate, liquid depth, and vessel radius, respectively). Also, Mazumdar et al. [9] analyzed the mixing time and correlation to the flat, tapered cylindrical, step, and funnel-shaped bottoms. The experimental results showed that a flat ladle bottom resulted in both a better mixing and a shorter mixing time compared to a funnel-shaped or a stepped bottom. Ek. et al. [16] studied the optimum gas flow rate for the mixing, inclusion removal, and metal-slag interfacial reactions. The effects of the gas flow rate and the plugs' configurations on the mixing condition were investigated by Geng et al. time with dual-plug bubbling A correction of mixing

$$\tau = 9.448 \times 10^{-5} \times \left(\frac{r}{R}\right)^{2.0} \times \theta^{-8.15} \times \left(\frac{r}{R} + 2.167 \times \theta\right)^{10.195} \times Q^{-0.38}$$
 (where r and θ correspond to the plug's radial

position and radial separation angle, respectively). In Liu et al.'s [18] work, the effects of the gas flow rate and the plug's configuration on the mixing time and open-eye formation were predicted by mathematical modelling. A dual-plug radial angle of 180° at a low flow rate without an open-eye area was recommended to obtain a soft bubbling and good separation of inclusions from the steel. Amaro-Villeda et al. [11] studied the effect of the slag property on the mixing time and energy dissipation. It was shown that a thicker slag layer and a higher slag viscosity decreased the exposed eye area. Furthermore, the mixing time increased in a positive correlation to an increased slag thickness. Luo et al. [19] studied the inclusion behavior and mixing phenomena with different arrangements of tuyeres. Their result showed that a radial position of 0.6R and a radial angle of 135° was the optimal dual configuration to improve the inclusion removal and mixing efficiency. In Tang et al.'s [12] work, the effects of dual-plug separation angles and radial locations on the mixing time were reported. When the flow rates of dual plugs were different, the mixing time was expressed as follows:

$$\tau = 158.8 \times \left(\frac{r}{R}\right)^{0.01525} \times \theta^{0.01258} \times Q^{-0.25866} \times f_{\rm w}^{0.21432} \times f_{\rm s}^{-0.47298} \quad (f_{\rm w} = \frac{Q_{\rm w}}{Q}, \text{ where } Q_{\rm w} \text{ is the weak flow rate, } f_{\rm w} = \frac{Q_{\rm s}}{Q},$$

where Q_s is the strong flow rate). González-Bernal et al. [7] adopted a new approach for tracer injection at the central bottom of the ladle, to analyze the effects of different numbers and locations of tuyeres on the mixing time. The experimental result showed that an off-centered bubbly stirring with a single plug located at a 0.75R distance resulted in shorter mixing times compared to the other dual-plug systems, due to large, intense circulations. Also, Liu et al. [13] studied the effects of radial locations and separation angles of single and dual plugs on the mixing time. A dual plugs' configuration was recommended at the mid-radius position and diametrically opposite position. Also, the effects of separation angles, radial locations, and slag layer thicknesses on the mixing time were analyzed by Gómez et al. [14]. In an up-to-date study, Duan et al. [20] gave the effects of plugs' radial positions and separation angles on the turbulent dissipation and mixing conditions. The optimal separation angle of dual plugs was found to be 90°, which was attributed to the interaction between recirculation loops.

In most previous studies, the physical modelling or mathematical modelling was employed to analyze the flow patterns and mixing conditions separately. In very few studies [5,12,16], the result predicted by the mathematical modelling was compared directly with results from the physical modelling. Furthermore, the effects of convection and diffusion on the homogenization degree were seldom discussed. Moreover, the recommended values of the plug's radial positions and separation angles were different for ladles of various weights and dependent on the operation conditions.

Table 1. Physical and mathematical modelling of gas-stirred ladles of different weights.

Author	Weight	Scale	Gas Injection Pattern	Plug Position	Plug Radial Angle	Liquid Metal	Gas	Physical Modelling	Mathematical Modelling	Optimal Plug Number and Position
					Water-base	d solution	5			
Liu et al. [13]	45 t	1/3	porous plug	0 <i>R</i> , 0.5 <i>R</i> , 0.56 <i>R</i> , 0.62 <i>R</i> , 0.67 <i>R</i> , 0.73 <i>R</i>	60°, 90°, 120°, 150°, and 180°	water	N ₂	NaCl above the exposed eye	-	N = 2, 0.5R~0.73R-180°
Joo and Guthrie [5]	100 t	1/3	porous plug	0R, 0.33R, 0.5R, 0.67R	45°, 90°, 135°, and 180°	water	air	KCl above the plume	Euler-Euler + species (own code)	$N = 2, 0.5R - 180^{\circ}$
Tang et al. [12]	120 t	1/3	porous plug	0.55 <i>R</i> , 0.64 <i>R</i> , 0.70 <i>R</i>	45°, 90°, 135°, and 180°	water	N_2	KCl above the exposed eye	VOF + species (Fluent)	$N = 2, 0.7R-180^{\circ},$ $0.64R-135^{\circ}, \text{ and } 0.55R-$ 180°
Gómez et al. [14]	120 t	1/8	nozzle	1/3R, 1/2R, and 2/3R	60°, 120°, and 180°	water	air	KCl above the exposed eye	-	$N = 2, 0.67R-60^{\circ}$
González- Bernal et al. [7]	135 t	1/7	Tuyere	1/3R, 2/3R, and 3/4R	60°	water	air	vegetal red colorant at the central bottom	-	N = 1, 3/4R
Mandal et al. [8]	140 t	1/5	tuyere/nozzle	0R, 0.5R	-	water	air/N2	NaCl or H ₂ SO ₄ axis of symmetry	-	$N = 2, 0.5R - 180^{\circ}$
Amaro-Villeda et al. [11]	140 t	1/6	Nozzle	0R, 0.33R, 0.5R, 0.67R, 0.8R	120°, 180°	water	air	NaOH or HCl	-	$N = 2, 0.5R - 180^{\circ}$
Mazumdar et al. [9]	210 t	0.17	Nozzle	0R, 0.5R, and 0.64R	90°, 180°	water	air/N2	NaCl or H ₂ SO ₄ axis of symmetry	-	$N = 2, 0.5R - 180^{\circ}$
Ek. et al. [16]	200 t	1/5	porous plug	0.72 <i>R</i>	-	water	air	NaCl above the plume	Euler-Euler + species (Comsol)	N = 1, 0.72R
This work	50 t	1/5.37	porous plug	0.65R	90°, 135°, and 180°	water	air	NaCl and red dye above the open eye	Euler–Lagrange + species (Fluent)	-
					Steel-based	l solutions	i			
Liu et al. [18]	150 t	-	porous plug	0.687R	90°, 135°, 180°	steel	argon	-	Euler–Lagrange + species (Fluent)	N = 2, 0.687R-180°
Luo et al. [19]	150 t	-	Nozzle	0.3R, 0.4R, 0.5R, 0.6R, 0.7R, 0.8R	45°, 90°, 135°, and 180°	steel	argon	-	Euler-Euler + species (Fluent)	<i>N</i> = 2, 0.6 <i>R</i> –135°
Duan et al. [20]	150 t	-	porous plug	0.34 <i>R</i> , 0.5 <i>R</i> , 0.68 <i>R</i> , 0.75 <i>R</i>	45°, 90°, 135°, and 180°	steel	argon	-	Euler–Lagrange + species (Fluent)	$N = 2, 0.5R - 90^{\circ}$
Geng et al. [17]	295 t	-	Nozzle	0.25 <i>R</i> , 0.33 <i>R</i> , 0.5 <i>R</i> , 0.75 <i>R</i> , and 0.8 <i>R</i>	90°, 120°, 150°, and 180°	steel	argon	-	Euler–Euler +species (CFX)	$N = 2$, $0.75R - 180^{\circ}$

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For this paper, the mixing condition in a 50 t ladle was studied. In the physical modelling, a saturated electrolyte solution and color dye were used to predict the mixing time and to show the flow pattern, respectively. In the mathematical modelling, the flow pattern and alloy homogenization were predicted to enable a comparison with results from physical modelling. Compared to previous works, the optimal radial angle of porous plugs is discussed.

2. Scaling Criterion and Experimental Apparatus

The connection between physical modelling experiments and industrial trials is the scaling criterion. In this study, water and air, at room temperature, were used to represent molten steel and argon, respectively. For the gas injection scaling, the ratio of the inertial and buoyancy forces in the plume was considered to achieve a flow similarity. Using the geometric similarity ($\lambda = \frac{L_{\text{water vessel}}}{L_{\text{specl latel}}}$) and

modified Froude number $Fr_m = \frac{\rho_{gas}^2 Q^2}{\rho_{liquid}^2 gHd_0^4}$ [21], the flow rates in the prototype and water experiment can be correlated as follows:

$$Q_{\text{air}} = \left(\frac{\rho_{\text{argon}} \rho_{\text{water}} d_{\text{water}}^2}{\rho_{\text{air}} \rho_{\text{steel}} d_{\text{steel}}^2} \sqrt{\frac{H_{\text{water}}}{H_{\text{steel}}}}\right) Q_{\text{argon}}'$$
(1)

where d_{water} is the plug diameter in the physical modelling, d_{steel} is the plug diameter in the prototype, ρ_{air} and ρ_{water} are the densities of air and water, ρ_{argon} and ρ_{steel} are the densities of argon and steel, H_{water} is the filled water height, H_{steel} is the filled molten steel height, Q_{air} is the air flow rate in the physical modelling (NL·min⁻¹), and Q'_{argon} is the effective flow rate in the prototype (L·min⁻¹).

In several works [13,15], the effects of temperatures and pressures on the scaling corrections were also studied. The temperature and pressure are taken into consideration by using the ideal gas law pV = nRT and $p_{in} = p_0 + \rho_{steelg}H_{steel}$, respectively. Overall, the scaling criterion is derived as follows:

$$Q_{\text{air}} = \left(\frac{\rho_{\text{argon}}\rho_{\text{water}}d_{\text{water}}^2}{\rho_{\text{air}}\rho_{\text{steel}}d_{\text{steel}}^2}\sqrt{\frac{H_{\text{water}}}{H_{\text{steel}}}}\right) \frac{T_{\text{in}}}{T_0} \cdot \frac{p_0}{p_{\text{in}}} Q_{\text{argon}}$$
(2)

where T_0 is the normal temperature (273 K), T_{in} is the molten steel temperature in the prototype (1873 K), p_0 is the normal pressure (101,325 Pa), p_{in} is the bottom injection pressure in the prototype (Pa), and Q_{argon} is the flow rate under normal conditions in the prototype (NL·min⁻¹).

All parameters in the physical model were linked to the dimensions of a 50 t steel plant by using a ratio of 5.37. The gas bubbling was given by two porous plugs located at the bottom of the reactor, as shown in Figure 1a. The radial position of the porous plugs, corresponding to that in the industrial ladles, was at a distance of 0.65R, where R is the ladle radius. The radial angles of the dual plugs, α , were chosen as 90°, 135°, and 180°, respectively. Moreover, two probes were positioned at $\alpha/2$ and $180 + \alpha/2$. First, the bubble-size distribution was analyzed using a high-speed camera (Motion Blitz Cube 4), which could take 1010 frames per second. The scaled ladle was placed in an acrylic plastic box, which could decrease the effect of light refractions on the size measurement. Moreover, a pipe with a diameter of 8 mm was fixed in a proper position to be used as a reference. A schematic diagram of the experimental apparatus is shown in Figure 1b. In the mixing-time section, the saturated NaCl solution was used as a tracer to represent the alloy in the ladle process. In each case, a volume of 50 mL of NaCl solution was injected through a funnel. The funnel was located above one of the gas injection plumes close to the water's surface. In addition, two conductivity probes were located at two feature points to measure the conductivity in the water. Furthermore, a color dye with a density of around 1100 kg/m³ was added through the funnel, at the same position, to show the flow pattern in the ladle. Because it is difficult to determine whether the color dye's effective diffusion is the same as that of a saturated NaCl solution, the experiments of color dye and saturated NaCl solution were conducted, respectively.

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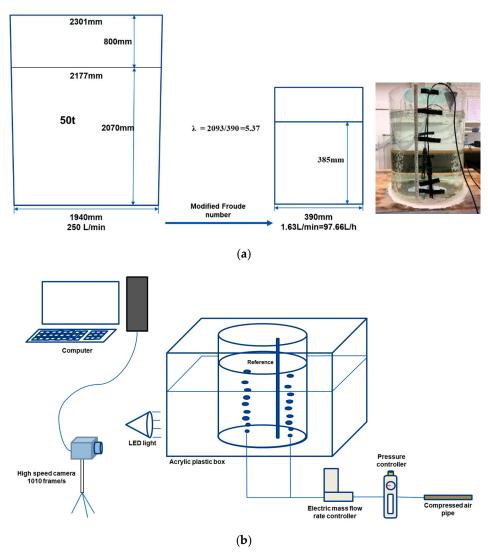


Figure 1. Scaling criterion (a) and experimental apparatus (b).

3. Mathematical Modelling and Calculation Methods

In order to predict the flow pattern and mixing condition, a three-dimensional model was established using the commercial software ANSYS FLUENT 19.2 (ANSYS, Canonsburg, PA, USA). The mesh sensitivity was checked by using a method presented in recent publications [22,23]. Meshes with a grid number of approximately 165,000 were used in the simulations. On one side, the Euler–Lagrange model was also used to predict the flow pattern in the same work [22]. On the other side, the mixing condition was calculated by using the species transport model [18,24]. The solution method was also the same as used in previous works [18,22]. The calculations were carried out on a Linux PC, using an Intel E5-2680 CPU with a frequency of 2.50 GHz. The calculations of flow patterns and mixing conditions in each case took approximately two weeks when using a parallel processing mode.

4. Results and Discussion

In the industrial process, the flow rate of the argon injection was in the range of 150~250 NL·min⁻¹. Based on the scaling criterion in Figure 1, the flow rates between the industrial process and water experiments were correlated. In this paper, three conditions of bubbly stirring are linked in Table 2 and later compared to results from physical modelling.

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Tuble 2. Various now rates in the metastral process and scaled varies in the water experiment	Table 2. Various flow rates in the industrial p	process and scaled values in the water experiment.
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Cases	Flo	ow Rate (L·miı	n ⁻¹)
Industrial Process	150	200	250
Water experiment	0.98	1.30	1.63

4.1. Gas Bubbling and Mixing Conditions in the Physical Modelling

In the water experiments, the bubbly flow is mainly affected by the bubble's buoyancy in the fully developed plume zone [25]. The buoyancy, in turn, is closely related to the bubble size, which is not constant in the water experiment; therefore, the bubble-size distribution should be statistically analyzed. The gas injection by porous plugs with various flow rates is shown in Figure 2. According to the size of the reference pipe with a diameter of 8 mm, the gas plume with dispersive bubbles in the middle was chosen, and the bubble size was measured in five figures, under the same flow rate. By using the open-source software ImageJ, the threshold value was adjusted to find the bubble boundaries, and the resulting RGB system figures were converted to binary ones. The post-process of measurement is shown in Figure 3. The maximum, average, and minimum values of bubble sizes are shown in Figure 4. With the flow rate increasing, the minimum bubble size keeps at an around constant value of approximately 2.5 mm, and the maximum and average size only decrease to a small extent. Therefore, the effect of the flow rate on the bubble-size distribution can be neglected in the current cases. Thus, the small effect of the light refraction on the bubble-size measurement was not considered.

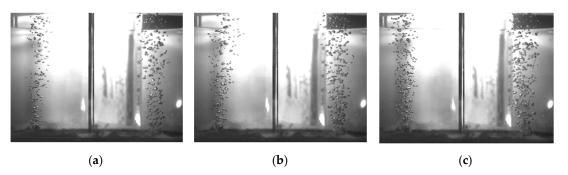


Figure 2. Gas injection using two porous plugs in the physical modelling: (a) $0.98 \text{ L} \cdot \text{min}^{-1}$; (b) $1.30 \text{ L} \cdot \text{min}^{-1}$; and (c) $1.63 \text{ L} \cdot \text{min}^{-1}$.

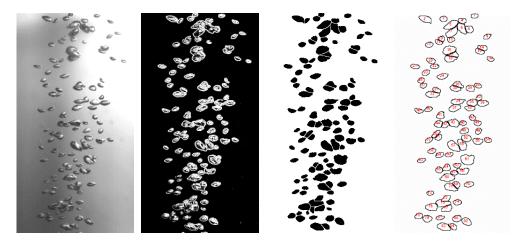


Figure 3. Process of bubble-size statistics in ImageJ, under the condition of 1.30 L·min⁻¹.

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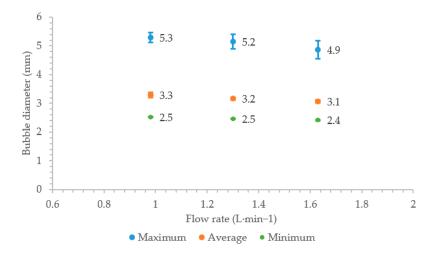


Figure 4. The maximum, average, and minimum values of bubble size in the water experiment.

The configurations of porous plugs and conductivity probes in the mixing experiment are shown in Figure 5. When the flow pattern reached a quasi-steady state, the NaCl solution was uniformly added to the water. The addition was made at a position corresponding to the position of the open eye, where alloys are added into the molten steel during ladle refining. Because of the bubbles' random rising, the plume swung periodically. In order to decrease the error of the random gas stirring on the average mixing time, each case was performed three times. After an experiment, the total normalized conductivity curves for two probes were obtained, as shown in Figure 6a. Moreover, the same conductivity curves with a specified range of 0.9~1.1 are shown in Figure 6b. The solid and dashed lines represent the tracer concentration within ±5% and ±1% of the homogenization degrees' value, respectively. For the ±5% homogenization degree case, the mixing time was determined as the concentration of the tracer, which was continuously within ±5% of a well-mixed bulk value.^[2] The procedure was the same for the case of a ±1% homogenization degree case, but the mixing time corresponded to a ±1% well-mixed bulk value.

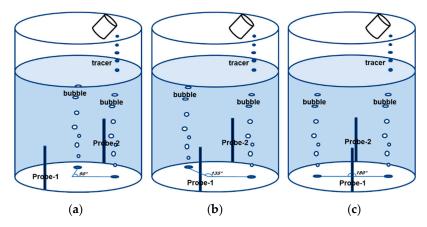


Figure 5. Schematic diagram of the porous plugs and conductivity probes' configurations at radial angles of (a) 90°; (b) 135°; and (c) 180°.

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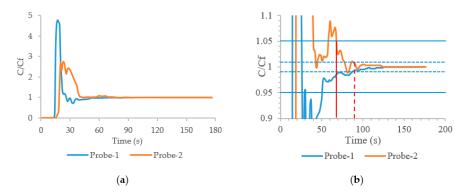


Figure 6. Normalized conductivity curves for two probes for a flow rate of 1.30 L·min⁻¹, using a 135° plug angle. (a) Normalized value with whole range. (b) Normalized value between 0.9 and 1.1.

The mixing times under various flow rates are shown in Figure 7. As the flow rate increases, both the times for $\pm 5\%$ and $\pm 1\%$ homogenization degrees decrease by 7% to 32%. Actually, in terms of the precision of the water experiments, the $\pm 5\%$ homogenization degree was mainly chosen to evaluate the mixing time. For the $\pm 5\%$ homogenization degree, using various configurations in Figure 7d, the averaged mixing time with a radial angle of 180° is always 0% to 7% shorter than that with a radial angle of 90°. Furthermore, the mixing time with a radial angle of 135° decreases the most with an increased flow rate. Nevertheless, under various flow rates, the tendency for the mixing condition for a $\pm 1\%$ homogenization degree is different from that of a $\pm 5\%$ homogenization degree. The reasons for this are discussed in Section 4.3.

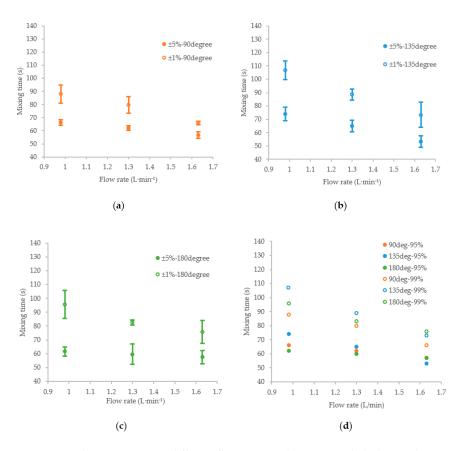
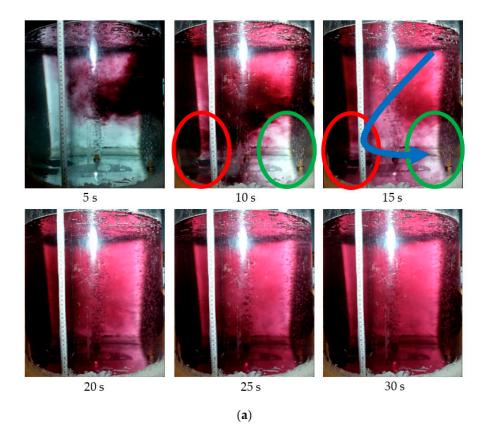


Figure 7. Measured mixing times at different flow rates with various radial-plug angles: (a) 90°; (b) 135°; (c) 180°; and (d) total.

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For the color-dye experiment, each case was performed once. In the color-dye experiments, the tracer path for a flow rate of 1.63 L·min⁻¹ is shown in Figure 8. In the figures, the color dye's concentration at the bottom corner is marked distinctly using red and green circles. The red and green circles correspond to the conditions with high and low concentration, respectively. Moreover, the blue vectors show the tracer's circulation behavior.



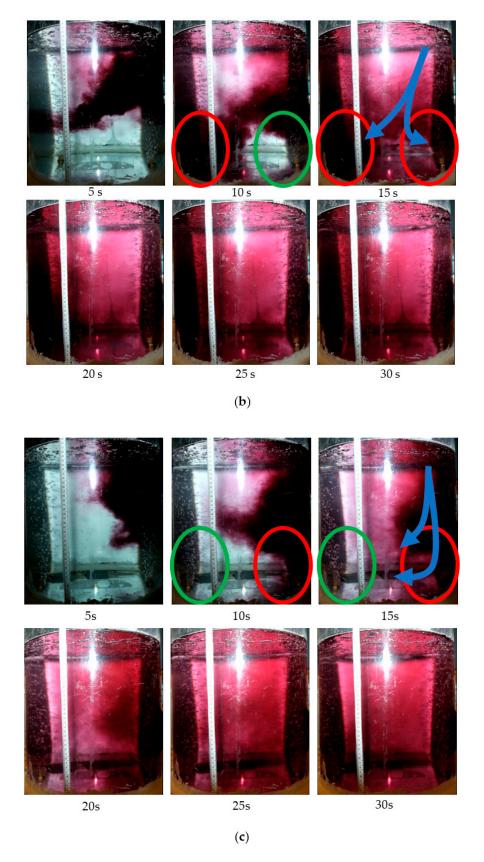


Figure 8. Color dye path for a 1.63 L·min⁻¹ flow rate when using various radial-plug angles: (a) 90° ; (b) 135° ; and (c) 180° .

It is shown that, for a 90° angle, the tracer goes to the bottom corner opposite to the tracer injection side at 10 s in Figure 8a. This is because of an intense deflected rotation. Therefore, the tracer returns to the injection side along the bottom of the vessel at 15 s. Moreover, for the 135° angle, the off-centered rotation is weaker compared to that for a 90° angle. Some of the tracer is dispersed to the central bottom position at 10 s in Figure 8b, and the remaining tracer is transported to the bottom corner at the injection side at 15 s. However, the condition for a 180° angle is largely different from those of the two other conditions. Because the flow pattern is ideally symmetric when using a 180° angle, the tracer is first mixed at the injection side at 10 and 15 s in Figure 8c. Then, it gradually diffuses and is directed toward the other side of the vessel.

4.2. Calculated Gas Bubbling and Mixing Conditions Using Mathematical Modelling

From previous mathematical modelling, it is clear that the bubble size has some influence on the multiphase interface forces and flow pattern [22]. However, according to the results from the physical modelling, the effect of the flow rate on the size distribution of bubbles injected by the porous plug could be ignored. The bubble-size distribution is within the range of 2.5~5.5 mm, and the average bubble size is 3.5 mm. In the mathematical modelling, the Rosin–Rammler algorithm [24] was used to set up the bubble-size distribution. The bubble injection for various flow rates is shown in Figure 9.

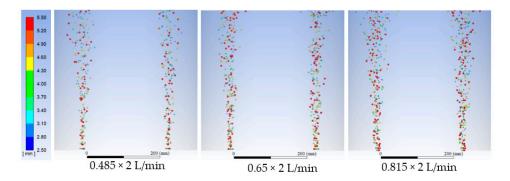


Figure 9. Color-dye path for a 1.63 L·min⁻¹ flow rate when using various radial-plug angles.

The mixing condition in the ladle is predicted using the species transport model. Several feature points are chosen to monitor the mass fraction of tracers in each zone. For example, the locations of points corresponding to a radial angle of 135° are shown in Figure 10. Also, the normalized curves of the mass fraction at each point are shown in Figure 11. The method to post-process the calculation data was the same as that for the experimental results. The solid and dashed lines correspond to the normalized mass fractions of tracers within the ±5% and ±1% homogenization degrees, respectively.

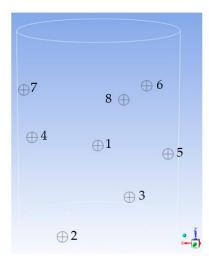


Figure 10. Monitoring point in the mathematical modelling. Ponit1 (0, 0, and 200 mm), Ponit2 (70.8, 170.9, and 20 mm), Ponit3 (-70.8, -170.9, and 20 mm), Ponit4 (170.9, -70.8, and 200 mm), Ponit5 (-170.9, 70.8, and 200 mm), Ponit6 (-117, 0, and 350 mm), Ponit7 (170.9, 70.8, and 350 mm), Ponit8 (-70.8, 170.9, and 350 mm).

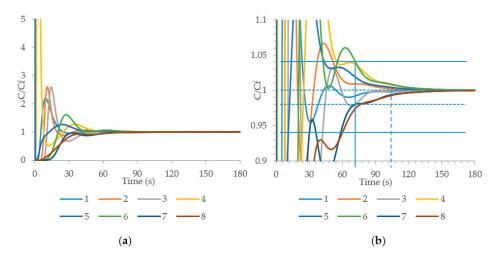


Figure 11. Normalized mass fraction curves when using a flow rate of 1.30 L⋅min⁻¹ and a 135° plug angle. (a) Normalized value in whole range. (b) Normalized value between 0.9 and 1.1.

In the mathematical modelling, the momentum model coupled with the multiphase model is used to calculate the flow pattern. Thereafter, using a fixed flow pattern, the species model is employed to predict the tracer homogenization. Therefore, the flow pattern is the main driver for the tracer diffusion and convection. However, the influence of the tracer's natural convection, such as the tracer density and temperature, on the mixing condition are not properly considered. The mixing time under various flow rates for ±5% and ±1% homogenization degrees are shown in Figure 12. As can be seen, an increased flow rate results in a large decrease of the mixing time. For the ±5% homogenization degree case and a lower flow rate of 0.98L·min⁻¹, the mixing time with a radial angle of 180° is approximately 15% shorter compared to a case when using a radial angle of 135°. For a higher flow rate of 1.63 L·min⁻¹, the mixing time for a radial angle of 180° is 27% shorter compared to a case using a radial angle of 90°. Moreover, the reduction of the mixing time is approximately 53% larger for a radial angle of 135°. The results from the mathematical modelling are consistent with those from the physical modelling. When using various radial angles, the variation of mixing times

in the $\pm 1\%$ homogenization degree experiments are the same as those in the $\pm 5\%$ homogenization degree experiments. For the $\pm 1\%$ homogenization degree, the smallest and largest variations are approximately 24% and 46% for radial angles of 90° and 135°, respectively.

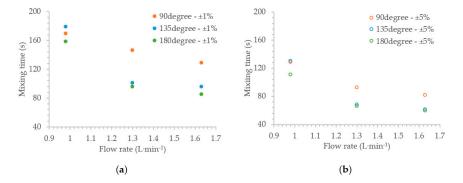
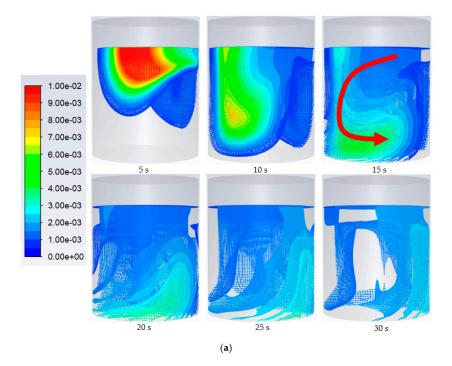


Figure 12. Measured mixing time with various radial-plug angles in the experiment: (a) $\pm 5\%$ homogenization and (b) $\pm 1\%$ homogenization.

In addition, the species transport results are also used to show the bubbly flow pattern in Figure 13. The red vectors correspond to the tracer's mixing patterns. For a radial angle of 90°, the species transport is controlled by a large circulation, as shown in Figure 13a. This is due to the intense deflected flow. The tracer rotates directly to the side away from the injection side, along with the gasliquid interface, and thereafter recirculates along the wall. Compared to the results for a radial angle of 90°, the flow pattern changes into two rotation flows for a radial angle of 135°, as shown in Figure 13b. Therefore, the tracer is also divided into two parts, and it gradually diffuses at the same time. For a radial angle of 180°, the flow pattern in the ladle is symmetric. Most of the tracer rotates at the injection side and gradually diffuses to the other side, as shown in Figure 13c. Comparing the conditions under various flow rates, the flow pattern predicted by the mathematical modelling agrees well with the results from the physical modelling.



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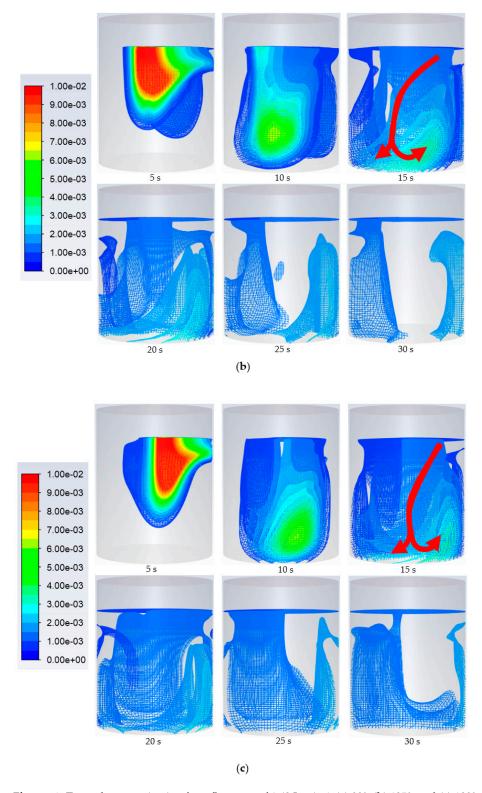


Figure 13. Tracer homogenization for a flow rate of 1.63 $L \cdot min^{-1}$: (a) 90°; (b) 135°; and (c) 180°.

The mixing times in the physical and mathematical modelling are collected in Table 3. Due to the comparison, the mixing time predicted by the mathematical modelling in each condition is always less than that predicted by the physical modelling. Therefore, some parameters in the Euler–Lagrange approach, such as drag coefficient, need to be modified further. Moreover, the main errors between

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physical modelling results and mathematical modelling results exist under the conditions of the low flow rate and the separation angle of 90 degrees. The discussion of the error is in the next section.

Table 3. Com	parison of th	e tracer hom	ogenization in t	the physica	al and mathema	tical modelling.
			0			

	_	Mixing Time (s)									
-	Flow Rate	90 degree			135 degree			180 degree			
	(L·min⁻¹)	Physical	Numerical	Error	Physical	Numerical	Error	Physical	Numerical	Error	
	0.98	66	129.3	96%	74	130.5	76%	62	111	79%	
±5%	1.3	62	92.3	49%	65	68.7	6%	60	66.2	10%	
	1.63	57	82	44%	53	61	15%	57	60	5%	
	0.98	88	169	92%	107	179	67%	96	158	64%	
±1%	1.3	80	146	83%	89	101	13%	83	96	16%	
	1.63	66	129	95%	73	85	16%	76	85	12%	

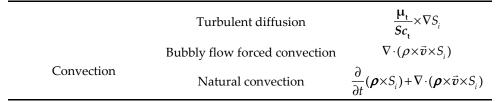
Bold terms are in the large error ratio between the physical modelling and mathematical modelling.

4.3. Convection and Diffusion

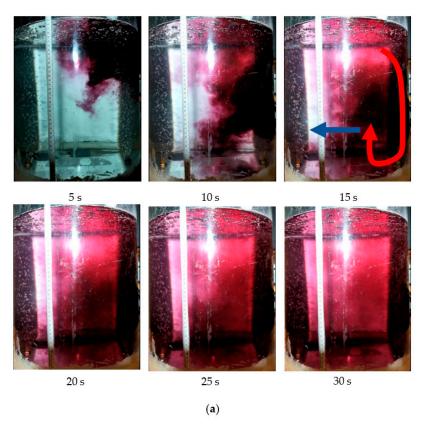
For the tracer mixing in the water experiment, the convection and diffusion of tracers took place at the same time. Because the experiment was conducted at room temperature, the effect of temperature on the diffusion rate does not need to be taken into consideration. In the mathematical modelling, the tracer homogenization was controlled by several factors, as shown in Table 4. Compared to the laminar diffusion rate, the turbulent diffusion rate is much higher [26]. Therefore, there are three factors, namely the bubbly flow forced convection, natural convection, and turbulent diffusion, which determine the homogenization degree in the ladle. Under high flow rates, the bubbly flow forced convection is the foremost cause of the tracer's mixing compared to the contributions from natural convection and turbulent diffusion. However, for low flow rates, the natural convection and turbulent diffusion also influence the homogenization of the tracers. Both for the mathematical modelling and physical modelling results, an increased flow rate resulted in a decreased mixing time for a radial angle of 135°. This is because two stirring rotations can increase the surface of the tracer diffusion. In most of the previous works [5,8,9,12-14,16], NaCl or KCl solutions were used as the tracers to determine the mixing time by monitoring the conductivity in the physical modelling trials. Nevertheless, the tracer's density is larger than that of normal water. Concerning the effect of the tracer's density on its homogenization pattern, the conditions with and without fixed flow pattern were compared in the mathematical modelling, as shown in Figure 14. The red and blue vectors correspond to the convection pattern and the diffusion pattern, respectively. In comparison to the species transport with and without fixed flow patterns, the latter agrees better with the physical modelling results. Here, the effect of the tracer's density on its mixing pattern is considered. The result shows that the influence of the alloy's natural convection on its homogenization pattern cannot be neglected, especially for 'soft bubbling' conditions, using low flow rates. In terms of the physical modelling, it is complicated to relate the tracer's density to the alloy's density used in the industrial process; therefore, it could be more accurate if the mathematical modelling is validated with data from the physical modelling and thereafter is used to predict the industrial conditions, instead of using physical modelling to predict industrial conditions. Furthermore, in the ladles with different volumes, the contributions of convection and turbulent diffusion on the mixing pattern should be analyzed in more detail in the future.

Table 4. Factors that affect the tracer homogenization in the mathematical modelling.

Species Transport	Factor	Expression
Mass diffusion	Laminar diffusion	$ ho{ imes}D_{ ext{lam}}{ imes} abla S_i$



Bold terms are the controlling parameters of each term in mathematical modelling.



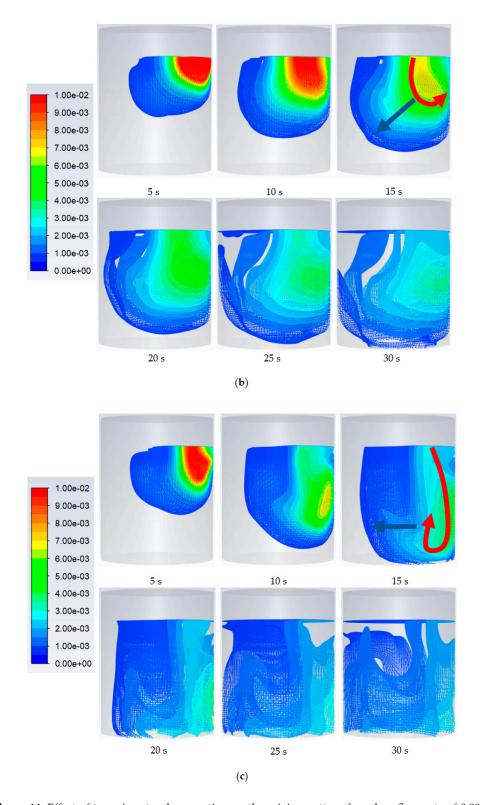


Figure 14. Effect of tracer's natural convection on the mixing pattern for a low flow rate of 0.98 L· \min^{-1} : (a) color dye experiment; (b) modelling with a fixed flow pattern; and (c) modelling without a fixed flow pattern.

Moreover, for the ladles with various weights, the optimal radial positions and separation angles of the plugs were collected in previous works [5,7–9,11–14,16,19,20], as shown in Figure 15. In terms

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of the mixing condition, an optimal range of plug's radial location is mainly off-centered for a single plug injection at values ranging from 0.72R to 0.75R. For dual-plug injections, a separation angle between the plugs of approximately 160° is mostly recommended, and the optimal dual-plug radial position is around 0.65R. Overall, larger radial angles in the range of 135~180° are recommended to reach a bubbly stirring condition when using dual porous plugs.

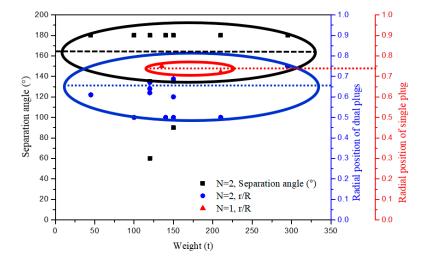


Figure 15. Collection of optimal radial position and separation angle of plugs in ladles with various weights. (Points with black color, blue color, and red color represent the data of dual plugs' separation angles, radial positions of dual plugs, and radial positions of single plug, respectively. The color of point is same as that of the axis.)

5. Conclusions

The bubbly flow and tracer mixing in a 50t ladle were studied based on physical and mathematical modelling. The effects of tracer convention and diffusion on the mixing pattern were discussed. For a ±5% homogenization degree, the effect of convection on the mixing pattern is most important. Also, the mixing time using dual plugs positioned at a radial angle of 180° is shortest. In addition, the mixing time when using dual plugs positioned with a radial angle of 135° decreased most with an increasing flow rate, among the various conditions. In addition, a comparison of the conditions for various flow rates shows that the flow pattern predicted by the mathematical modelling agrees well with the physical modelling results. For a ±1% homogenization degree, the influence of the alloy's natural convection on its homogenization pattern cannot be neglected, especially for a 'soft bubbling' condition using a low flow rate. Furthermore, in the ladles with different weights, the effect of convection and diffusion on the mixing should be studied in more detail. In comparison to the previous works, it is recommended that a larger radial angle in the range of 135°~180° is chosen to obtain bubbly stirring conditions when using dual porous plugs.

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