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Physically-Based Modeling and Characterization of Hot Flow Behavior in an Interphase-Precipitated Ti-Mo Microalloyed Steel

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Abstract: In this contribution, a series of hot compression tests was conducted on a typical interphase-precipitated Ti-Mo steel at relatively higher strain rates of $0.1\sim 10\text{ s}^{-1}$ and temperatures of $900\sim 1150\text{ }^{\circ}\text{C}$ using a Gleeble-2000 thermo-mechanical simulator. A combination of Bergstrom and Kolmogorov–Johnson–Mehl–Avrami models was first used to accurately predict the whole flow behaviors of Ti-Mo steel involving dynamic recrystallization, under various hot deformation conditions. By comparing the characteristic stresses and material parameters, especially at the higher strain rates studied, the dependence of hot flow behavior on strain rate and deformation temperature was further clarified. The hardening parameter U and peak density ρ_p exhibited an approximately positive linear relationship with the Zener–Hollomon (Z) parameter, while the softening parameter Ω dropped with increasing Z value. The Avrami exponent n_A varied between 1.2 and 2.1 with $\ln Z$, implying two diverse nucleation mechanisms of dynamic recrystallization. The experimental verification was performed as well based on the microstructural evolution and mechanism analysis upon straining. The proposed constitutive models may provide a powerful tool for optimizing the hot working processes of high performance Ti-Mo microalloyed steels with interphase precipitation.

Keywords: Ti-Mo steel; hot deformation; constitutive model; microstructural evolution

1. Introduction

A new generation of advanced high strength steels (AHSSs) with both high/ultrahigh strength and good cold formability is becoming more commonly used in commercial vehicles to meet the continuous demand for better fuel economy and passenger safety [1–3]. However, many of the conventional AHSSs, e.g., dual-phase (DP) steel, have limited the stretch-flangeability during cold stamping in view of the notable difference in hardness between the soft ferrite and the hard martensite [2,3]. As a solution, a ferritic matrix with interphase precipitation has been proposed to improve the stretch-flangeability of AHSSs through optimizing alloy design and thermomechanical processes [4,5].

Funakawa et al. [6] first reported a Ti-Mo ferritic steel strengthened by period arrangement of nanoscale interphase precipitates, which exhibited an ultimate tensile strength (UTS) of $\sim 780\text{ MPa}$ and a hole expansion ratio (HER) of 120%. The basic principle designed for this type of steel was to facilitate the formation of a large fraction of nanoscale precipitates by controlling the coarsening kinetics of (Ti, Mo)C particles [1,4,5,7–10], thus giving rise to a large contribution to the strength of steels. More recently, some research has been carried out with respect to the influence of Mo on the formation of interphase precipitates. It has been demonstrated by atom probe tomography (APT) that the size of (Ti, Mo)C precipitates could be reduced to as fine as 1–3 nm [1].

Additionally, recent research on the hot-compressed Ti-Mo steel [8] revealed that hot deformation promoted segregation of C to grain boundaries and simultaneously reduced the size of precipitates at grain boundaries during the isothermal holding process. Kim et al. [9,10] also pointed out that precipitation hardening exhibited a stronger relation to rolling temperature rather than coiling temperature. However, very few studies have considered the hot flow behaviors of Ti-Mo microalloyed steels, especially at relatively higher strain rates of $0.1\sim 10\text{ s}^{-1}$, which was relevant to the industrial hot rolling processes [11]. A full list of nomenclature for all physical parameters is presented in Table 1.

Table 1. A full list of nomenclature.

Symbols	Parameters
A	Material constant (s^{-1})
AARE	Average absolute relative error
k	Material constant
M	Dislocation strengthening constant
n	Stress exponent
n_A	Avrami's exponent
Q	Activation energy for hot deformation ($\text{kJ}\cdot\text{mol}^{-1}$)
R	Universal gas constant ($\text{J}\cdot\text{K}^{-1}\cdot\text{mol}^{-1}$)
T	Absolute deformation temperature (K)
U	Hardening parameter (m^{-2})
X	Recrystallized volume fraction
Z	Zener–Hollomon parameter (s^{-1})
α	Stress multiplier (MPa^{-1})
γ	Austenite phase
ε	True strain
$\dot{\varepsilon}$	Strain rate (s^{-1})
μ	Shear modulus (GPa)
ρ	Dislocation density (m^{-2})
σ	True stress (MPa)
σ_0	Lattice friction stress (MPa)
σ_p	Peak stress (MPa)
σ_{Rex}	Steady state stress after dynamic recrystallization (MPa)
Ω	Softening parameter

Therefore, the main aim of the present work was to study the hot flow behavior of an interphase-precipitated Ti-Mo microalloyed steel with a typical composition of Fe-0.04C-0.2Si-1.5Mn-0.08Ti-0.22Mo at strain rates of $0.1\sim 10\text{ s}^{-1}$ and a series of deformation temperatures ranging from $900\sim 1150\text{ }^{\circ}\text{C}$. The activation energy for hot deformation and peak stress of both steels were determined, in conjunction with physically-based modeling of hot flow behavior. The experimental verification was performed through microstructural evolution and mechanism analysis during hot deformation.

2. Experimental Procedures

A 30-kg ingot with a typical composition of Fe-0.04C-0.2Si-1.5Mn-0.08Ti-0.22Mo was prepared, followed by heating to $1200\text{ }^{\circ}\text{C}$ for 2 h and hot rolling to $\sim 20\text{ mm}$ in thickness. The calculated austenite to ferrite transformation start temperature A_{r3} by Thermo-calc software is approximately $858.1\text{ }^{\circ}\text{C}$. The as hot-rolled microstructure consisted of ferrite with an average grain size of $\sim 40\text{ }\mu\text{m}$, along with a small amount of pearlite ($\sim 7\%$), as presented in Figure 1. Cylindrical specimens of $\Phi 8 \times 15\text{ mm}$ were machined from the hot-rolled plates, with the axis parallel to the rolling direction.

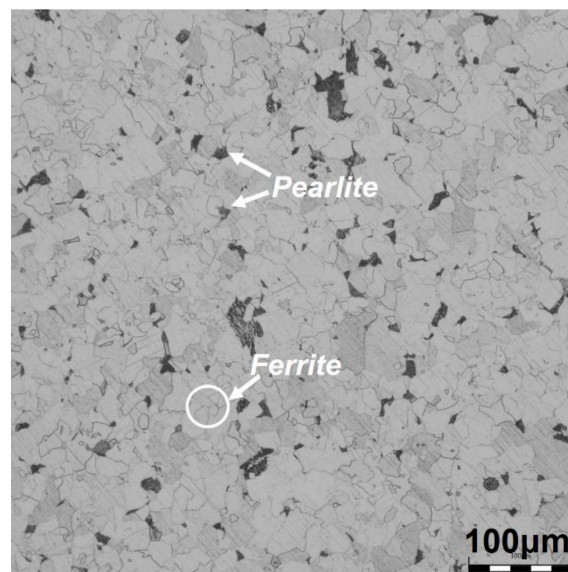


Figure 1. The initial hot rolled microstructure of Ti-Mo steel.

A series of hot compression tests was conducted on a Gleeble-2000 thermo-mechanical simulator. Specimens were reheated at a rate of $10\text{ }^{\circ}\text{C/s}$ to $1200\text{ }^{\circ}\text{C}$ for 3 min for homogenization purposes, followed by cooling at $10\text{ }^{\circ}\text{C/s}$ to diverse deformation temperatures. After soaking for 10 s, they were compressed in a single hit to $\varepsilon = 0.8$ at temperatures of $900\sim 1150\text{ }^{\circ}\text{C}$ and strain rates of $0.1\sim 10\text{ s}^{-1}$, followed by immediate quenching in water. The selection of temperatures considered is based on the following two facts: (1) the austenite was deformed in the single austenitic region; (2) all three common deformation mechanisms appeared on the flow curves in this study.

Microstructural characterization after hot deformation was performed using an optical microscope (OM, OLYMPUS DSX500, Tokyo, Japan) and electron backscattered diffraction (EBSD) in a JEOL JSM-7100F (Jeol, Tokyo, Japan) field emission gun scanning electron microscope. The scanning step size was approximately $0.5\text{ }\mu\text{m}$, and data post-processing was performed using a Tex-SEM Laboratories orientation-imaging microscope (OIM) system. Specimens for EBSD were prepared by standard mechanical grinding and electro-polishing using a perchloric acid-alcohol solution (1:15) at 30 V.

3. Results and Discussion

3.1. Hot Flow Behaviors

Figure 2 shows the representative true stress-strain curves obtained during hot deformation of Fe-0.04C-0.2Si-1.5Mn-0.08Ti-0.22Mo steel at temperatures of $900\sim 1150\text{ }^{\circ}\text{C}$ and strain rates of $0.1\sim 10\text{ s}^{-1}$. As commonly observed, the flow stress level of experimental steel was elevated with increasing strain rate or dropping deformation temperature. In the relatively low strain rate (0.1 s^{-1}), the flow curves were characterized by dynamic recovery (DRV) and dynamic recrystallization (DRX), except at $900\text{ }^{\circ}\text{C}$. Increasing strain rate was found to retard the progress of DRV or DRX, and no DRX phenomenon was observed at the strain rate of 10 s^{-1} , irrespective of deformation temperature. The change in flow stress level with deformation temperature or strain rate was probably due to an increase in the rate of restoration processes and a decrease in the strain hardening rate [12]. The lower strain rate can provide enough time for energy accumulation, and the higher deformation temperature can accelerate the dissolution of precipitates, dislocation movement and grain boundary migration for the formation of DRX nuclei, which in turn lowered the stress level [12,13]. It is worth mentioning that the flow curves exhibited a prominent oscillation at all temperatures for the lowest strain rate of 0.1 s^{-1} , while the oscillations were much slower with increasing strain rate. The oscillation phenomenon could be

mainly attributed to the reduced accuracy and stability of sensors at the lowest strain rate of 0.1 s^{-1} , as well as the competing effect between various deformation mechanisms [13].

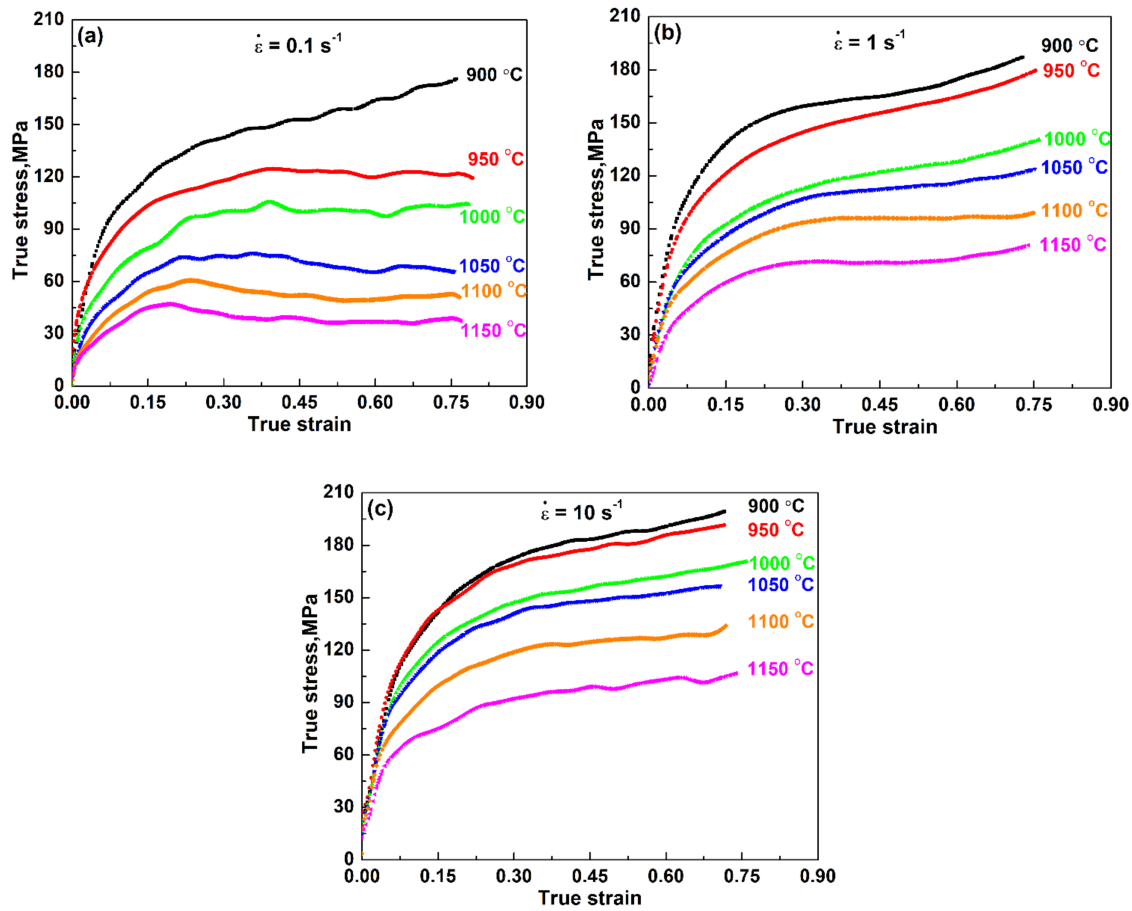


Figure 2. Typical flow curves of Ti-Mo steel obtained under various temperatures in the range of 900–1150 °C and strain rates of (a) 0.1 s^{-1} , (b) 1 s^{-1} and (c) 10 s^{-1} .

3.2. Peak Stress Analysis

In general, the peak stress was one of the most widely-accepted parameter used to find the hot working constants, especially for DRV and DRX types [14–16]. According to the analysis of flow curves, both DRV and DRX behaviors were found to happen in the temperature range from 1000–1150 °C for all strain rates. To elucidate the influence of deformation temperature and strain rate on the peak stress of experimental steel, a peak stress model, which was suitable for a wide range of strain rates and deformation temperatures, was expressed in the hyperbolic sine form [17].

$$\dot{\varepsilon} = A[\sinh(\alpha\sigma_p)]^n \exp(-Q/RT) \quad (1)$$

where σ_p is the peak stress, $\dot{\varepsilon}$ is the strain rate, n is the stress exponent, A is a material constant, α is the stress multiplier, Q is the activation energy for hot deformation, R is the universal gas constant and T is the absolute deformation temperature.

In terms of various stress levels, Equation (1) can be simplified in the power law and exponential law:

$$\dot{\varepsilon} = A_1\sigma_p^{n_1} \exp(-Q/RT) \quad (\alpha\sigma_p < 0.8) \quad (2)$$

$$\dot{\varepsilon} = A_2 \exp(\beta\sigma_p) \exp(-Q/RT) \quad (\alpha\sigma_p > 1.2) \quad (3)$$

where A_1 , A_2 , n_1 , β are material constants. According to the linear regression of experimental data, the values of n_1 and β were determined using plots of $\ln \dot{\epsilon}$ vs. $\ln \sigma_p$ and $\ln \dot{\epsilon}$ vs. σ_p at each deformation temperature [18], as displayed in Figure 3. Thus, the stress multiplier is determined as $\alpha = \beta/n_1 = 0.06653/6.736 = 0.009876$.

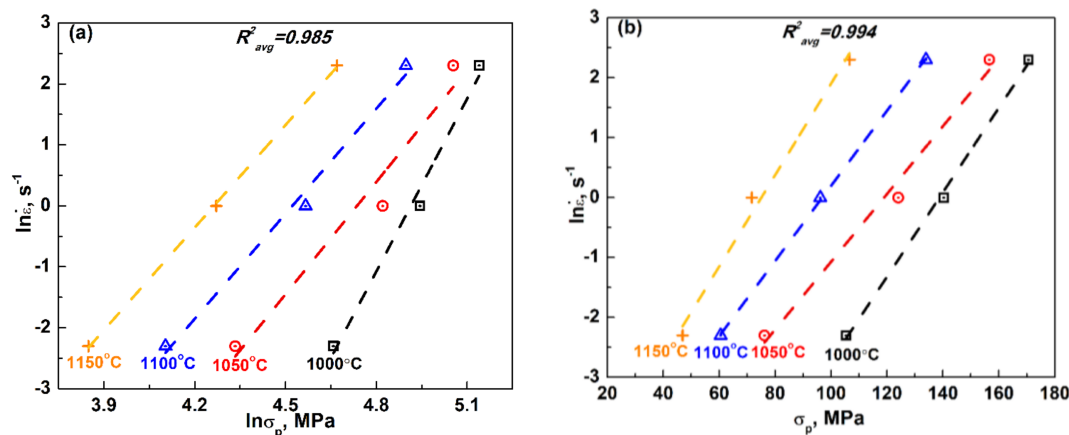


Figure 3. Plots of (a) $\ln \dot{\epsilon}$ vs. $\ln \sigma_p$ and (b) $\ln \dot{\epsilon}$ vs. σ_p at each deformation temperature of 1000–1150 °C for determining material constants, n_1 and β .

To derive the value of n in Equation (1), plots of $\ln \dot{\epsilon}$ vs. $\ln [\sinh(\alpha \sigma_p)]$ at each deformation temperature are shown in Figure 4a. By linear fitting, the average value of n was approximately 5.0. Thus, the value of Q was obtained by taking the partial derivative of Equation (1) in the form of the natural logarithm.

$$Q = Rn \left[\frac{\partial \ln(\sinh(\alpha \sigma_p))}{\partial (1/T)} \right]_{\dot{\epsilon}} = RnS \quad (4)$$

where the value of S was determined as 10.31, based on the average slope of plots of $\ln[\sinh(\alpha \sigma_p)] - 1000/T$ at each strain rate (Figure 4b). The Q value of ~428.5 kJ/mol obtained here was much higher than the activation energy for self-diffusion in γ -iron (~280 kJ/mol) [19], indicating that the deformation mechanism at high temperature was not controlled by atomic diffusion.

A widespread parameter, the Zener–Hollomon (Z) parameter [20], was introduced to determine the material constant A , as expressed in Equation (5).

$$Z = \dot{\epsilon} \exp\left(\frac{Q}{RT}\right) \quad (5)$$

By combining Equations (1) and (5), the following natural logarithm form was obtained:

$$\ln Z = \ln A + n \ln [\sinh(\alpha \sigma_p)] \quad (6)$$

According to the plot of $\ln Z$ vs. $\ln [\sinh(\alpha \sigma_p)]$ (Figure 4c), the value of A was determined as $1.69 \times 10^{16} \text{ s}^{-1}$. The detailed fit parameters associated with the peak stress model for both steels are summarized in Table 2. The correlation coefficients (R^2) of all fit parameters were beyond 0.984, implying a desirable fit to experimental data.

Table 2. The fit parameters associated with the peak stress model for Ti–Mo steel.

Sample	Q , kJ/mol	n	A , s^{-1}	α , MPa^{-1}
Ti–Mo	428.5	5.00	1.69×10^{16}	0.009876

Note: Q is the activation energy for hot deformation; n is the stress exponent; A is a material constant; α is the stress multiplier.

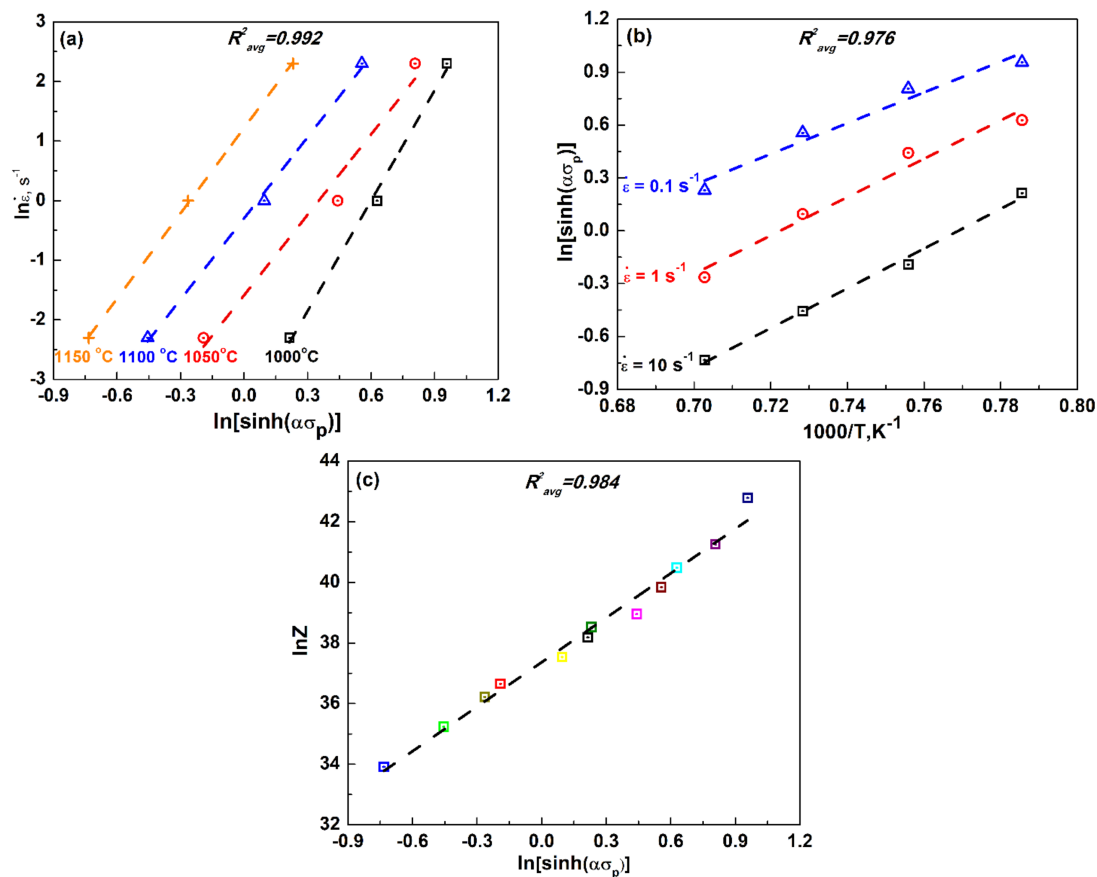


Figure 4. Plots of (a) $\ln[\sinh(\alpha\sigma_p)]$ vs. $1000/T$, (b) $\ln \dot{\epsilon}$ vs. $\ln[\sinh(\alpha\sigma_p)]$ and (c) $\ln Z$ vs. $\ln[\sinh(\alpha\sigma_p)]$ under different experimental conditions for the values of n , S and A .

By substituting the fit parameters into Equation (1), the σ_p as a function of deformation temperature and strain rate can be expressed as:

$$\dot{\epsilon} = 1.69 \times 10^{16} (\sinh 0.009876\sigma_p)^5 \exp(-428500/RT) \quad (7)$$

When introducing the Z parameter into Equation (7), the σ_p can be also obtained in the following form.

$$\begin{cases} Z = \dot{\epsilon} \exp\left(\frac{428500}{RT}\right) \\ \sigma_p = \frac{1}{0.009876} \ln \left\{ \left(\frac{Z}{1.69 \times 10^{16}} \right)^{1/5} + \left[\left(\frac{Z}{1.69 \times 10^{16}} \right)^{2/5} + 1 \right]^{1/2} \right\} \end{cases} \quad (8)$$

The experimental peak stresses were compared with those predicted using the constitutive Equation (8) under different deformation conditions, see Figure 5. The validity of the σ_p model was further examined by an average absolute relative error (AARE):

$$\text{AARE} = \frac{1}{N} \sum_{i=1}^N \left| \frac{E_i - P_i}{E_i} \right| \times 100\% \quad (9)$$

where E_i is experimental data, P_i is the predicted value and N is the number of fit data used in this study. The AARE value was about 3.69%, reflecting the accurate estimation of peak stress. The satisfactory agreement between the predicted and experimental data suggests that the constitutive equations we proposed herein gave an accurate prediction of flow stress during hot deformation.

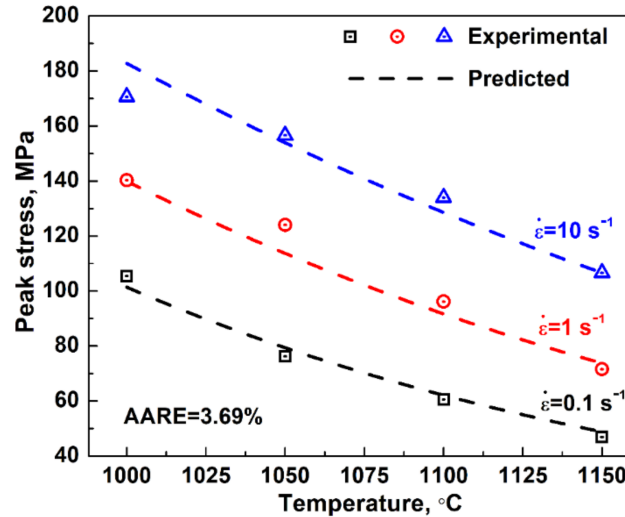


Figure 5. Comparison of the peak stress model and experiment data for Ti-Mo microalloyed steel at different temperatures of 1000–1150 °C and strain rates of 0.1, 1 and 10 s^{−1}. The average absolute relative error was about 3.69%.

3.3. Physically-Based Constitutive Analysis

In general, the dislocation density increased with strain during hot deformation, leading to work hardening (WH) or the DRV phenomenon. Regarding the flow curves of WH and DRV, the dislocation density (ρ)-based flow stress model proposed by Bergstrom [21] was used in this study as follows:

$$\begin{aligned}\sigma &= \sigma_0 + M\mu b\sqrt{\rho} \\ \frac{d\rho}{d\epsilon} &= U - \Omega\rho\end{aligned}\quad (10)$$

where σ_0 is the lattice friction stress, M is a dislocation strengthening constant, μ is the shear modulus, b is the burgers vector, U is the hardening parameter and Ω is the softening parameter. The value of M ranged from 0.88–0.9 [22], and the b value was taken as 2.5×10^{-10} m [6]. The value of μ varied from 43.5–48.4 GPa at temperatures of 900–1150 °C by extrapolating from the experimental data from the literature [23]. Thus, the values of σ_0 , U , Ω could be obtained based on the present experiment data.

After the onset of DRX, the hot flow behavior of Ti-Mo steel was described, based on the Kolmogorov–Johnson–Mehl–Avrami (KJMA) softening model as follows [24,25]:

$$\begin{aligned}\sigma &= \sigma_p - X(\sigma_p - \sigma_{Rex}) \\ X &= 1 - \exp(-kt^{n_A})\end{aligned}\quad (11)$$

where σ_{Rex} is the steady state stress after DRX, X is the recrystallized volume fraction, k is a material constant and n_A is Avrami's exponent. Thus, the flow behavior of Ti-Mo steel involving DRX was modeled by the coupling of the Bergstrom and KJMA's models. The former was used to model the flow stress before reaching peak stress; whereas the later for that after the onset of DRX. All undetermined parameters in Equations (10) and (11) can be obtained based on the MATLAB programing.

To verify the accuracy of the developed models, the predicted and experimental flow curves under different deformation conditions were compared, as plotted in Figure 6. According to Equation (9), the accurate estimation of flow stress using the Bergstrom and KJMA models was about 1.68%, which

reflected a satisfactory agreement between the predicted and experimental data. In contrast, the combined Bergstrom and KJMA models could precisely predict the whole hot deformation behaviors of Ti-Mo steel involving DRX (Figure 6a).

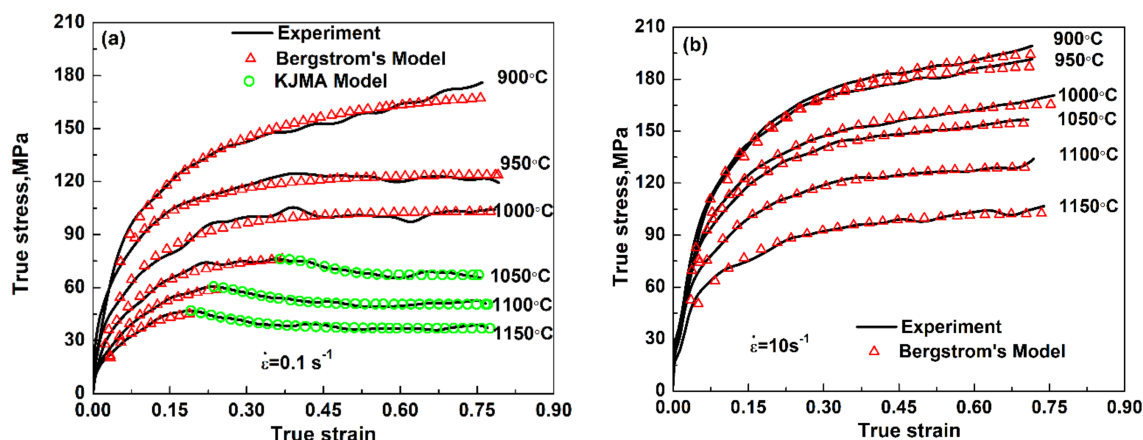


Figure 6. The typical predicted and experimental flow curves of Ti-Mo microalloyed steel at temperatures of 900–1150 °C and different strain rates: (a) $\dot{\epsilon} = 0.1 \text{ s}^{-1}$; (b) $\dot{\epsilon} = 10 \text{ s}^{-1}$.

Meanwhile, several important parameters such as U , Ω and n_A were utilized to compare the variations in hot deformation behavior of Ti-Mo steel as a function of the Z parameter. From Figure 7, the U value was found to exhibit an approximately positive linear relationship with $\ln Z$ (Figure 7a). An increase in the Z value corresponded to the larger strain rate or the lower deformation temperature, implying more effective work hardening. On the contrary, the Ω value dropped with increasing Z value (Figure 7b). Furthermore, the peak dislocation density (ρ_p) exhibited a similar tendency with the U (Figure 7c), due to the proportional relationship between these two parameters.

Additionally, the values of the Avrami exponent, n_A , were found to vary between 1.2 and 2.1 with $\ln Z$, as presented in Figure 7d, which was comparable with those values reported in previous studies [11,26]. The variation in n_A indicated different mechanisms of DRX. In the lower Z region, the n_A value was close to one, suggesting a larger probability of nucleation sites on the interfacial surface of grain and twin boundaries. In the larger Z region, however, the n_A value reached ~ 2 , implying that nucleation of DRX happened on the grain and twin edges [27].

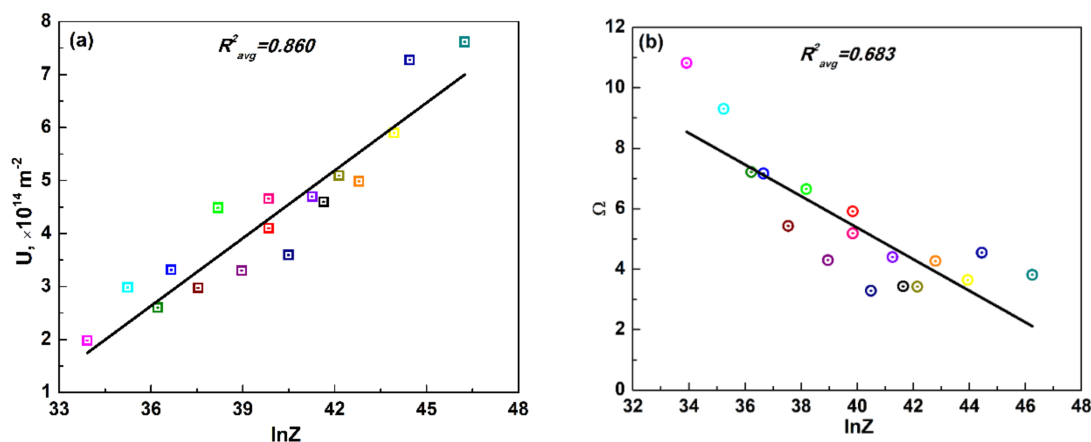


Figure 7. Cont.

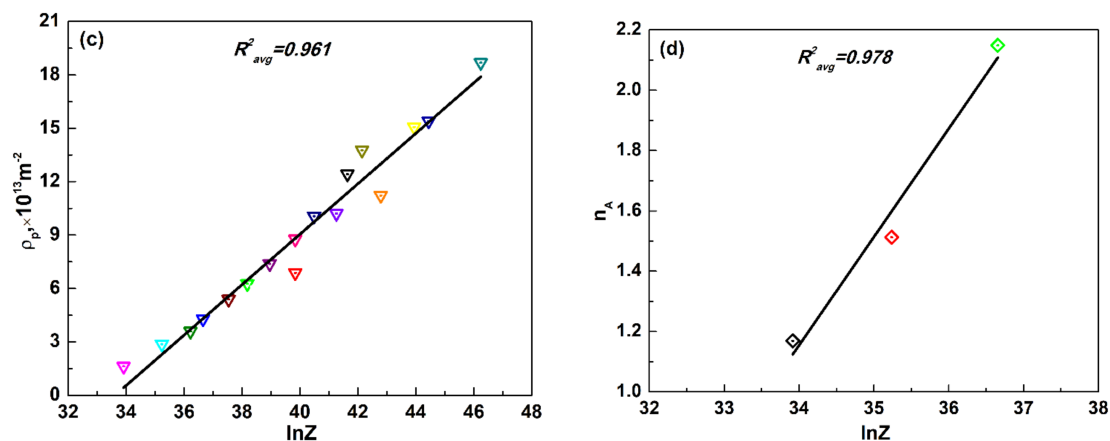


Figure 7. The relationship between typical parameters for physical models and the Z parameter. (a) Hardening parameter, U ; (b) softening parameter, Ω ; (c) Avrami's parameter, n_A ; (d) peak dislocation density, ρ_p .

3.4. Experimental Verification and Mechanism Analysis

To analyze the influence of hot deformation on the microstructural features of Ti-Mo steel, both OM and EBSD were employed to study the deformed specimens. When the specimen was deformed at 900 °C to a strain of 0.8 at 0.1 s^{-1} , the severely pancaked prior austenitic grains were observed (Figure 8a), implying that WH was the dominant deformation mechanism. Furthermore, the fresh ferrite formed at the prior grain boundaries (inset of Figure 8a), which suggests that the strain-induced ferrite (SIF) occurred due to the lower deformation temperature, just above the A_{r3} temperature ($\sim 858.1 \text{ }^\circ\text{C}$). With increasing deformation temperature to 1150 °C at 0.1 s^{-1} , the fully-equiaxed grains were observed (see the black lines in Figure 8b), indicating that the hot deformation of Ti-Mo steel was mainly controlled by DRX. This was in agreement with the continuous softening mechanism observed on the flow curves in Figure 2a. Accordingly, the formation of new equiaxed grains was mainly associated with the rearrangement or annihilation of dislocations [28,29]. Meanwhile, further straining was accompanied by an acceleration of the transformation of low to high angle grain boundaries resulting from the recovery-assisted absorption of dislocations in the existing sub-boundaries. The whole microstructural evolution upon straining at 1150 °C and 0.1 s^{-1} is schematically illustrated in Figure 8d as well.

However, at the higher strain rate of 10 s^{-1} and deformation temperature of 1150 °C, some deformation bands and substructures were still observed in the large pancaked prior austenite grains (Figure 8c). This suggests that DRV played an important role during hot compression in the high strain rate domain (e.g., 10 s^{-1}) at higher temperatures, which was also in accordance with the steady flow stress with strain in Figure 2c. As schematically displayed in Figure 8d, the new grain evolution involved the development of strain-induced HAGBs resulting from an increase in the misorientations of individual LAGBs and progressive subgrain rotation [30,31] upon further straining.

The change in boundary misorientation angle as a function of deformation temperature and strain rate is displayed in Figure 9. In EBSD analysis, the number of high angle austenitic/martensitic boundaries was distinguished, in view of the variation between their crystal orientations. When deformation was performed at 900 °C and 0.1 s^{-1} , a large number of low-angle subgrain boundaries of $2\text{--}5^\circ$ ($>40\%$) was observed inside the deformed grains (Figure 9a). As the deformation temperature increased to 1150 °C at the same strain rate of 0.1 s^{-1} , the fraction of LAGBs of $2\text{--}5^\circ$ dramatically dropped by $\sim 33.6\%$ with a number of high angle austenitic grain boundaries ($\sim 46.2\%$), implying the occurrence of a pronounced DRX [32]. Consequently, the DRX was accelerated, and the flow stress was greatly reduced due to the decreased density dislocation, which corresponded to Figures 2a and 8b. Having deformed at higher strain rates (e.g., 10 s^{-1}) and 1150 °C, the fraction of high angle austenitic

grain boundaries was reduced to $\sim 29.7\%$ with a higher fraction of LAGBs of $2\text{--}5^\circ$ ($\sim 37.5\%$), implying that the DRX process was impeded and that the flow stress increased, owing to the accumulating strain and hardening substructure, which correspond to the flow curves in Figures 2c and 8c.

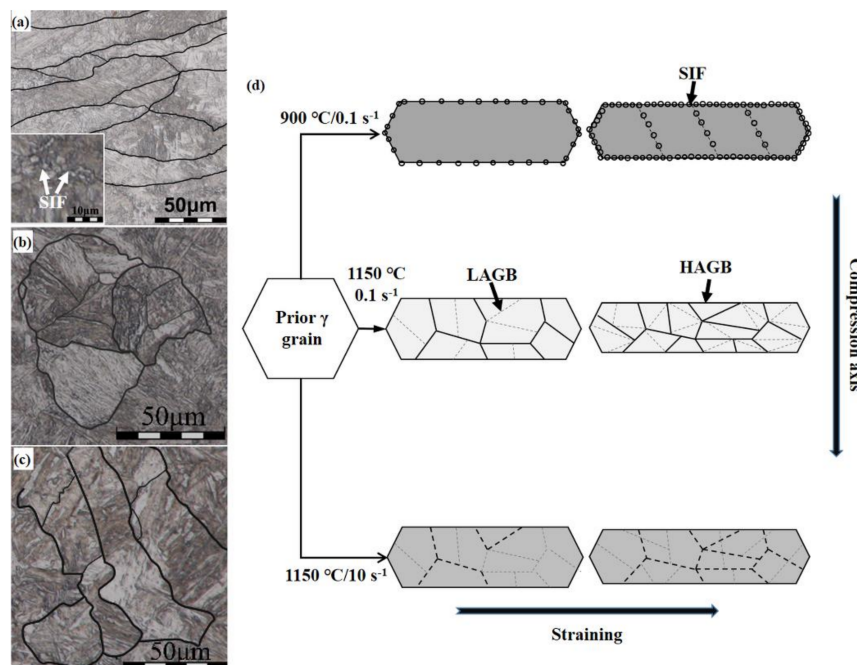


Figure 8. Microstructural evolution of a Ti-Mo microalloyed steel during hot compression at different temperatures and strain rates: (a) $900\text{ }^\circ\text{C}/0.1\text{ s}^{-1}$, (b) $1150\text{ }^\circ\text{C}/0.1\text{ s}^{-1}$ and (c) $1150\text{ }^\circ\text{C}/10\text{ s}^{-1}$; as well as the corresponding schematic diagrams (d). LAGBs and HAGBs indicate the low/high angle grain boundaries. The background colors represent the low/high density of dislocations, respectively. SIF, strain-induced ferrite.

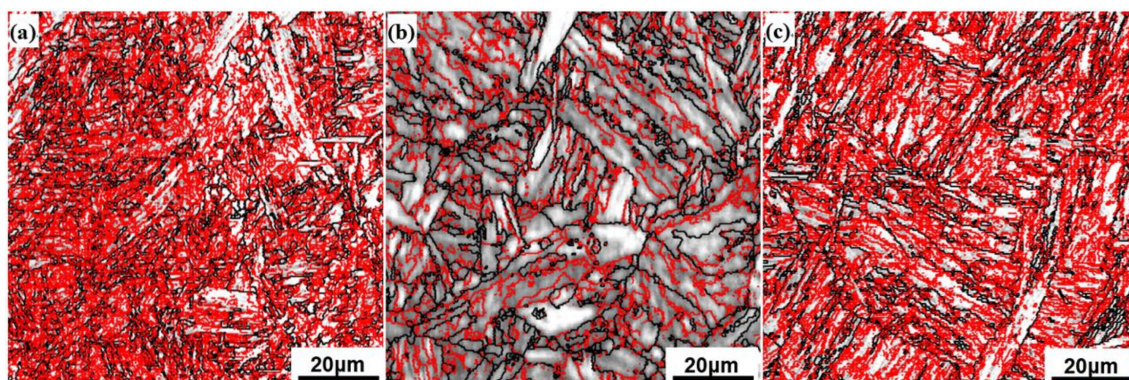


Figure 9. Electron backscattered diffraction (EBSD) maps of Ti-Mo microalloyed steel under different deformation conditions: (a) $900\text{ }^\circ\text{C}/0.1\text{ s}^{-1}$, (b) $1150\text{ }^\circ\text{C}/0.1\text{ s}^{-1}$ and (c) $1150\text{ }^\circ\text{C}/10\text{ s}^{-1}$. The red and black solid lines represent the low-angle grain boundaries (LAGBs) of $2\text{--}15^\circ$ and high-angle grain boundaries (HAGBs) of above 15° . The plane of EBSD observation was parallel to the compression axis.

The present study demonstrates that a combination of Bergstrom and KJMA models, which we proposed herein, could be used to predict the whole flow behaviors of the interphase-precipitated microalloyed steels under various hot deformation conditions, involving DRX. By comparing the characteristic stresses and material parameters over all deformation conditions, especially at the higher strain rates studied, the dependence of hot flow behavior on strain rate and deformation temperature

was further clarified. Therefore, the constitutive model may provide a powerful tool for optimizing the hot working processes of high performance Ti-Mo steels with interphase precipitation.

4. Conclusions

The hot flow behaviors of an interphase-precipitated Ti-Mo steel were investigated by conducting a series of hot compression tests at higher strain rates of $0.1\sim 10\text{ s}^{-1}$ and temperatures of $900\sim 1150\text{ }^{\circ}\text{C}$ on a Gleeble-2000 thermo-mechanical simulator. The main conclusions involved:

- (1) The peak stress as a function of deformation temperature and strain rate was determined as:

$$\dot{\varepsilon} = 1.69 \times 10^{16} (\sinh 0.009876 \sigma_p)^5 \exp(-428500/RT) \quad (12)$$

- (2) Under conditions where DRV or WH was dominant, the hot flow behavior could be modeled using the Bergstrom equation; once DRX was initiated, the coupling of the Bergstrom and KJMA's models was capable of predicting the flow behaviors in the whole hot deformation.
- (3) The values of U and ρ_p exhibited an approximately positive linear relationship with the $\ln Z$ parameter, while the Ω dropped with increasing Z value. Meanwhile, the n_A value varied between 1.2 and 2.1 with $\ln Z$, indicating the variation in the mechanisms of DRX with deformation conditions.
- (4) After the microstructure deformed at $900\text{ }^{\circ}\text{C}$ and 0.1 s^{-1} , the severely pancaked prior austenitic grains remained; with increasing deformation temperature above $950\text{ }^{\circ}\text{C}$ and 0.1 s^{-1} , the fully-equiaxed DRX grains formed through rearrangement or annihilation of dislocations. However, as the strain rate increased to 10 s^{-1} for different deformation temperatures, WH and DRV were dominant, resulting in some deformation bands and substructures in the large pancaked prior austenite grains.
- (5) With increasing the temperature from $900\sim 1150\text{ }^{\circ}\text{C}$ at 0.1 s^{-1} , the fraction of LAGBs of $2\sim 5^{\circ}$ dropped by $\sim 33.6\%$, with greatly increased high angle austenitic grain boundaries ($\sim 46.2\%$) due to a pronounced DRX phenomenon. With increasing strain rate to 10 s^{-1} at $1150\text{ }^{\circ}\text{C}$, the fraction of LAGBs of $2\sim 5^{\circ}$ increased to $\sim 37.5\%$, which was associated with inhibition of DRX.

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Author Contributions: Chuanfeng Wu and Peiru Yang performed the physically-based modeling and microstructural characterization. Junhua Su and Xiaopeng Guo designed the experimental procedures and carried out the hot compression tests. Minghui Cai was responsible for the discussion, plotting figures and paper writing.

Conflicts of Interest: The authors declare no conflict of interest.

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