



Article Atomistic Simulation Study of Grain Boundary Segregation and Grain Boundary Migration in Ni-Cr Alloys

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Abstract: Using Molecular Dynamics (MD) and Monte Carlo (MC) simulations, we studied the grain boundary (GB) segregation under different temperatures and Cr concentrations in Ni-Cr alloys with two distinct grain-boundary structures, i.e., $\Sigma 5(310)[010]$ and $\Sigma 101(200)[100]$. Temperature plays a minor influence on Cr segregation for $\Sigma 5(310)[010]$ GB, but Cr segregation rapidly diminishes with elevating temperatures for $\Sigma 101(200)[100]$ GB. We also used the synthetic driving force and corresponding identification methods to investigate the effect of Cr solute segregation on grain boundary stability. All Σ 5(310)[010] models have multi-stage grain boundary migration at 800 K. In the first stage, the grain boundary's slow acceleration time is related to solute concentration. The migration temperature can influence this phenomenon. As temperatures rise, the duration of this slow acceleration phase diminishes. No similar phenomenon was observed in the process of the grain boundary movement of $\Sigma 101(200)[100]$. The influence of solute concentration on grain boundary migration is complicated. The segregation concentration at the grain boundary cannot be regarded as the only factor affecting the migration of the grain boundary because the Cr atom on the grain boundary does not move with the grain boundary. This work will also discuss the grain boundary migration's relationship with lattice distortion and grain boundary atom diffusion. The results and findings of this study provide further insights into the segregation-increase GB stabilization of NC Ni-Cr alloys.

Keywords: Ni-Cr alloy; grain boundary segregation; grain boundary migration; atomistic simulation

1. Introduction

Ni-Cr alloys exhibit significant oxidation and corrosion resistance at moderately high temperatures and possess commendable mechanical strength [1–3]. They are widely used in applications related to harsh environments, such as corrosion and oxidation-resistant coatings or turbine disks [4,5]. Notably, Cr can bolster many characteristics of Ni-based alloys, such as oxidation, corrosion resistance, and tensile properties [6,7]. Previous experimental and simulation studies demonstrate that Cr segregation towards the Ni grain boundaries can modify the thermodynamic and kinetic properties of grain boundaries (GB) in nanocrystalline (NC) Ni-Cr alloy [8–10]. Current studies have substantiated that factors, such as GB character and alloy concentration, significantly influence grain size in NC metal materials [11–13]. As is known, the crystallographic texture of polycrystalline solids is intrinsically linked to the characteristics of grain boundaries (GBs), which play a pivotal role in defining the material's physical properties [14,15]. At the same time, the motion of the grain boundaries inevitably causes grain structure changes and the microstructural evolution of NC alloys. Therefore, a deeper understanding of the grain boundary migration is essential in designing advanced Ni-Cr alloys.

It is generally believed that the segregation of solute atoms to the grain boundary can alter the local atomic structure and energy of the grain boundary [16,17]. So, grain



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Copyright: © 2024 by the authors. Licensee MDPI, Basel, Switzerland. This article is an open access article distributed under the terms and conditions of the Creative Commons Attribution (CC BY) license (https:// creativecommons.org/licenses/by/ 4.0/). boundary segregation plays an essential role in the stability of GB [18,19]. The segregation of solute atoms is the result of both physical and chemical energy minimization, which is induced by lattice distortion and atomic bonding, respectively [20]. The high-density dislocation caused by lattice distortion may hinder the grain boundary movement, and the solute may also have a drag effect on the grain boundary movement [21,22]. Additionally, it is crucial to accentuate that the diffusion of pinned segregated states should be fast enough to enable the segregated state aggregates to travel with the grain boundary. Suppose the diffusion of solute atoms is too slow or the grain boundary moves too quickly. In that case, the boundaries will detach from the segregated groups, causing a sudden drop in the resistance of the segregated solute atoms for GB motion [22,23]. For instance, the Mg-segregation morphology depends on the grain boundary types in the Al-Mg alloy. The Mg atoms tend to form clusters in the high-angle tilt GB and segregate into low-angle GBs composed of dislocations. Mg segregation slows down the Al diffusion in high-angle and low-angle GBs due to the significant increase in the activation energy of GB diffusion [24]. Therefore, diffusion-induced grain boundary migration (DIGM) under the influence of solute migration is a common phenomenon in NC alloys [25–27]. Therefore, it is important to reveal the influence of segregation on grain boundary migration in NC alloys.

To truly comprehend what drives this composite behavior, a deeper understanding of how grain boundary alloying and grain boundary segregation influence the grain boundary migration rate is needed. Koju and Mishin investigated the effect of grain boundary segregation on GB diffusion in Cu-Ag and Al-Mg alloys [24,28]. In the Cu-Ag system, they found that the disordering of the GB structure caused by segregation can drastically alter the GB diffusion mechanisms, and the GB diffusivities of the solute (Ag)and solvent (Cu) atoms can exhibit quite different and nontrivial composition and temperature dependencies [28]. For instance, under low concentrations of Ag (around 1% or lower), Ag decelerates the transport. However, when the concentration nears 2%, it can induce a higher migration rate than in non-alloy systems under certain conditions. For Co-Ni alloy [29], at low Co content, solute atoms affect the dislocation movement mainly by regulating lattice mismatch and elastic mismatch, which is consistent with the solid-solution strengthening theory. Solute atoms also affect dislocation movement at high Co content by changing lattice vibration. Therefore, the solute concentration significantly influences the grain boundary deflection diffusion and the grain boundary morphology, which then influences the grain boundary migration.

The temperature dependence of the grain boundary migration rate can be described by the Arrhenius equation [30]: $M(T) = M_0 exp[-Q_M/(k_B T)]$, where k_B is the Boltzmann constant and T is the temperature. The pre-factor M and the activation energy Q_M can be fitting parameters for the temperature-dependent migration rate. A common outcome of various types of molecular dynamics (MD) simulations is that different types of motions may occur depending on the temperature and the size of the force driving the GB, and a critical temperature exists, known as the roughening temperature [14]. Above the roughening temperature, GB consistently exhibits continuous movement, and the GB speed linearly depends on the size of the applied driving force. Below this critical temperature, the type of GB movement depends on the size of the applied driving force. Under high force, continuous or linear GB motion can be enforced. However, GB exhibits discontinuous motion under lower forces. In this case, significant jumps of the entire GB over a specific distance (several atomic layers) can be distinctly separated from the waiting time between individual jumps [14,31]. Additionally, the atomic fraction and distribution of segregated solute atoms at GBs are closely related to the temperature [24]. Therefore, temperature inevitably has a significant effect on the migration behavior of grain boundaries. Therefore, the Ni-Cr alloy must study the influence of Cr concentration and temperature on grain boundary movement.

As mentioned above, a smaller grain size for nanocrystalline nickel-based alloys will increase the grain boundary ratio and the Gibbs free energy. These will reduce the stability of grain boundaries, such as spontaneous grain growth. Solute segregation can effectively stabilize grain boundaries [32–34]. The grain boundary type, temperature, and solute concentration are the key. Therefore, it is necessary to investigate the grain boundary segregation of the solute in the Ni-Cr system and understand the influence of the grain boundary segregation of the solute and temperature on the grain boundary mobility. This paper has carried out a comprehensive atomic computer simulation of the grain boundary segregation, grain boundary atom diffusion, and grain boundary migration in the Ni-Cr system. For segregation, models with more kinds of solute concentrations were selected for segregation simulation, which was rarely seen in previous studies. We chose two iconic grain boundaries. They are high-angle grain boundaries, the symmetric tilt Σ 5(310)[010] GB, consisting of closely spaced structural units, and the low-angle twist grain boundaries $\Sigma 101(200)[100]$, consisting of discrete dislocations. In addition to calculating some key characteristics of the grain boundary segregation in the Ni-Cr system at a specific temperature, we also focus on the influence of Cr concentration, temperature, and different grain boundaries on the diffusion rate and grain boundary migration rate, then discuss the relationship between the grain boundary atom diffusion and grain boundary migration.

2. Methods and Models

2.1. Methods

The 2NN MEAM (Many-Body Embedded Atom Method) interatomic potential developed by Wu et al. describes the Ni-Cr alloy [35]. Molecular statics, molecular dynamics (MD), and Monte Carlo (MC) simulations are conducted using the LAMMPS (Large-scale Atomic/Molecular Massively Parallel Simulator code [36]. Visualization and structural analyses are carried out using OVITO software (https://www.ovito.org/) [37]. The construction of the grain boundary models utilized ATOMSK [38], and these GB models are based on the Coincident Site Lattice (CSL) grain boundary data provided by Olmsted et al. [14], contributing to the acquisition of a stable grain boundary structure.

To study the segregation behaviors of Cr on the grain boundaries of Ni-Cr alloys, we employed the Semi-Grand Canonical Monte Carlo (SGCMC) [36] technique. We utilized a hybrid MC/MD algorithm to achieve the desired segregation. Every MC step was followed by 100 MD steps. The MC step completes an atom-type replacement, while the MD step completes relaxation after the atom replacement. At a specific temperature, a pair of Cr and Ni atoms are randomly chosen and exchanged based on the probabilities specified by the Metropolis criterion. Under periodic boundary conditions with zero normal pressure, MD thermal equilibrium is achieved using the NPT ensemble. The entire system is then relaxed at the same temperature. The integration time step is set at 2.5 fs to ensure the system remains fully relaxed. The imposed chemical potential difference ($\Delta \mu$) between Ni and Cr was adjusted to produce the desired chemical composition inside the grains. The simulation temperature varied between 300 K and 1200 K. The chemical potential difference $(\Delta \mu)$ between Ni and Cr changes with the simulation temperature in the SGCMC method. Table 1 presents the selected values of this chemical potential difference in the current study for different temperatures and solute concentrations. These chemical potential differences serve as simulation parameters in the subsequent segregation simulations.

Temperature	Cr Concentration	Δμ
300	5	0.32
	15	0.36
	25	0.38
	5	0.215
600	15	0.287
	25	0.3225
	5	0.115
900	15	0.22
	25	0.275
	5	0.01
1200	15	0.145
	25	0.22

Table 1. Temperature (K), solute atomic concentration (at%), and chemical potential diffe	rence.
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To investigate the impact of grain boundary segregation on the grain boundary motion in Ni-Cr alloys, the comprehensive driving force method proposed by Janssens [26] is employed to achieve grain boundary migration. Under the NPT ensemble (fixed total number of atoms N, fixed temperature T, and zero pressure P), the grain boundary models are relaxed for 20 ps at temperatures of 800 K, 1000 K,1200 K,1400 K, and 1600 K, respectively. Subsequently, an additional synthetic driving force of 0.08 to 0.32 eV/atom was applied at 20 ps. This synthetic driving force (Δe) facilitated the grain boundary migration. The difference in the potential energy (driving force) on both sides of the grain boundary is artificially introduced to make the grain boundary gradually migrate to the non-dominant grains with lower potential energy, to reduce the total free energy of the double crystal system [26]. It is important to note that in all grain boundary migration simulations, the grain boundaries will come close to each other and eventually merge and melt. In addition, grain boundaries are too close to each other to determine the specific position of the grain boundary plane, which is also the reason for the different migration time of the grain boundaries in Section 3.2. We adopt a more efficient grain identification method proposed by Schratt et al. [39], which allows two grains with different grain boundaries and orientations to be imaged by OVITO [37], as shown in Figure 1. Then, the trajectory of grain boundary migration can be obtained. Given the necessity to minimize the driving force at the grain boundary, we matched each model with the minimum suitable force that could facilitate the grain boundary migration. This implies that multiple attempts will be made to apply the minimal grain boundary driving force that permits normal grain boundary migration.

An enhanced understanding of this process can enable more precise control over the microstructural evolution in materials science investigation. At low temperatures (i.e., 800 K), for high-angle grain boundaries $\Sigma 5(310)[010]$, the driving force is up to 0.32 eV/atom due to the substantial hindrance effect of Cr atom segregation on the grain boundary migration, which is significantly higher than those considered in other studies [14,39]. However, during the MD run, the grain boundary extent may vary slightly due to thermal fluctuations. To account for such variations, the instantaneous GB extent was tracked by finding the peak of the potential energy (averaged over a thin layer parallel to the GB plane) as a function of the x-coordinate, normal to the boundary. The potential energy diagram of 300 K is shown in Figure 1. At 300 K, the width δ of the GB was estimated from the width of the peak. Based on these estimates, the GB core region was defined as the layer centered on the peak, with a width $\delta = 0.8$ nm for the high-angle GB ($\Sigma 5(310)[010]$) and a width $\delta = 1.6$ nm for the low-angle GB ($\Sigma 101(200)[100]$). The migration rate (M) was determined using the equation M = V × $\Omega/\Delta e$, where V represents the grain boundary migration velocity, and Ω is the atomic volume [26].



Figure 1. The schematic diagram of our grain boundary migration simulation system, where green atoms belong to grain *a*, blue atoms belong to grain *b*, and white atoms represent grain boundary atoms.

2.2. Grain Boundaries

To investigate the influence of grain boundary types on segregation behavior, we selected two types of grain boundaries, i.e., high-angle boundaries (HAGB) and lowangle boundaries (LAGB). The high-angle grain boundary (GB) is the symmetric tilt GB Σ 5(310)[010] with a misorientation angle of 36.87°, which [010] indicates the tilt axis, and (310) is the GB plane. The structure of this GB is illustrated in Figure 2a. The grain boundary is composed of structural units with six atoms from two parallel atomic layers, and the structural units are kite-shaped. The $\Sigma 5(310)[010]$ grain boundary in FCC (Face-Centered Cubic) crystals is often the subject of research because of its unique properties and relevance in material science and engineering [40,41]. We utilized the MEAM potential to calculate the grain boundary energy of $\Sigma 5(310)[010]$ and $\Sigma 101(200)[100]$, which were found to be 1.405 J/m² and 0.946 J/m², respectively. Olmsted [14] reported grain boundary energies of 1.218 J/m^2 and 0.701 J/m^2 for these same boundaries. Although there is a discrepancy in the absolute values between our results and theirs, this is primarily due to using different potential functions. The relative differences in the grain boundary energy for the two types of boundaries are similar, indicating that our prediction of the energy trend of these two types of grain boundaries is accurate. The twist grain boundary of $\Sigma 101(200)[100]$ is considered as the low-angle GB, with a misorientation angle of 11.42° which [010] indicates the tilt axis, and (200) is the GB plane. The atomic structures of the $\Sigma 101(200)[100]$ grain boundary equilibrated at 300 K are shown in Figure 3a, characterized by a square network composed of atoms colored gray.

The dimensions of the Σ 5(310)[010] GB block in the x, y, and z directions are 22.26× 5.27 ×11.13 nm³ (comprising 119,400 atoms), while those of the Σ 101(200)[100] GB block are 14.08 × 10.00 × 10.00 nm³ (containing 129,280 atoms). Periodic boundary conditions were applied in all three directions.



Figure 2. A front view of the Σ 5(530)[010] crystalline grain boundary area. The GB plane (530) is perpendicular to the page. (a) The grain boundary is composed of kite-shaped structural units. These structural units are delineated with solid black lines. (b) The description of atomic segregation in the Σ 5(530)[010] grain boundary and its adjacent regions, doped with 5 at%.Cr, at a temperature of 300 K, extending up to a distance of 10 Å from the grain boundary plane. (c) The segregation energy spectrum at a temperature of 300 K within a range of 10 Å from the position of the grain boundary plane.



Figure 3. A right view of the $\Sigma 101(200)[100]$ crystalline grain boundary area. The GB plane (200) is parallel to the page. The perfect-lattice atoms are removed for clarity. (a) The grain boundary structure, represented by gray atoms, forms a net-like configuration. (b) The description of atomic segregation in the $\Sigma 101(200)[100]$ grain boundary at a temperature of 300 K. (c)The segregation energy spectrum at a temperature of 300 K, on the grain boundary at the plane (200).

3. Results and Discussion

3.1. Temperature and Composition-Dependent Cr Segregation at Ni Grain Boundary

In the case of the nickel-chromium alloy with the two types of grain boundaries mentioned above, we performed hybrid MC/MD simulations to reveal the temperature- and composition-dependent segregation behavior of the Cr solute atoms at two GBs. It is found that a different grain boundary morphology will affect the segregation energy and segregation concentration of Cr atoms. In the high-angle grain boundary Σ 5(310)[010], Cr atoms experience segregation, preferring to gather at the low-angle kite head positions within the kite-shaped structural units comprising six atoms (see Figure 2b). The segregation of Cr atoms at the high-angle kite tail positions proves to be energetically unfavorable. Specifically, the segregation energy ranges from -0.617 eV to 0.147 eV, as shown in Figure 2c. For the low-angle grain boundary $\Sigma 101(200)$ [100], the segregation of Cr atoms is more accessible to occur with the segregation energy varying between -1.486 eV and 0.537 eV, which inclines to cluster into the square network structure(see Figure 3b). Although Cr can segregate to both high-angle and low-angle grain boundaries with significantly negative segregation energies, there are more locations for Cr segregation with low segregation energy on the low-angle twisted grain boundary $\Sigma 101(200)$ [100], which is different from the Cr segregation behavior occurring on the high-angle Σ 5(310)[010] tilted grain boundary (see Figures 2c and 3c).

Figure 4 shows the Cr segregation distribution depending on alloy components and the temperatures for Σ 5(310)[010] tilted and Σ 101(200)[100] twisted GB. The segregation distribution of Cr is determined by calculating the atomic fraction of Cr in the GB. The calculated model is segmented into thin layers parallel to the GB, and the atomic fraction of Cr in each layer is calculated and averaged over multiple repeat simulations during the thermodynamic equilibrium MD/MC simulation process. As shown in Figure 4, the segregation concentration of Cr can be enhanced at low temperatures, e.g., 300 K. This temperature-dependent segregation behavior was reported in Ni-Bi and Al-Mg polycrystals [24,42], which can be described by Langmuir–McLean's equation [43]. Due to the less negative segregation energy of Cr at the Σ 5(310)[010] tilted grain boundary, Cr has a relatively low segregation atomic fraction (26.2%) at 300 K, compared to the Cr segregation atomic fraction of 32.7% at $\Sigma 101(200)$ [100] GB. Moreover, temperature plays a minor influence on Cr segregation for the $\Sigma 5(310)$ [010] tilted grain boundary. The Cr segregation atomic fraction also remains at 13.80% at 1200 K (see Figure 4a). However, Cr segregation occurring at the $\Sigma 101(200)[100]$ low-angle grain boundary rapidly diminishes with rising temperature. The atomic fraction of Cr at the $\Sigma 101(200)$ [100] GB of Ni-5 at%. Cr alloy can reach 32.7% at 300 K. In comparison, the Cr segregation atomic fraction is only 8.69% at 1200 K (see Figure 4b). This difference in temperature-dependent segregation behavior between tilted Σ 5(310)[010] and twisted Σ 101(200)[100] grain boundaries can be understood by the ability of atomic diffusion at GBs. Generally, the high-angle grain boundaries are densely packed, while low-angle grain boundaries form a network structure. Therefore, high-angle grain boundaries are more easily diffused at the same temperature than lowangle grain boundaries [24]. Additionally, with the increase in total Cr concentration, the ability of Cr segregation will decay, as shown in Figure 4. For instance, the Cr segregation atomic fraction is only about 1.5 times the total Cr concentration for Ni-25 at%. Cr alloy at 300 K, lower than five times the Cr concentration for Ni-5 at%.Cr alloy.

In this part, we discussed the effect of grain boundary types, segregation temperature, and solute concentration on grain boundary segregation. In the following part, we will focus on the significant influence of grain boundary segregation on the mobility of grain boundaries, aiming to unravel how the interplay between these two phenomena impacts the thermodynamic properties and dynamic behavior of grain boundaries in Ni-Cr alloys.



Figure 4. This caption illustrates the distribution of Cr composition bias across various alloy composition models in (a) Σ 5(310)[010] tilt GB and (b) Σ 101(200)[100] twist GB at distinct temperatures.

3.2. Effect of Segregation on Grain Boundary Migration

Based on the above discussion in this study regarding solute atom segregation in Ni-Cr at two different grain boundaries, it is necessary to further elucidate the impact of Cr segregation on grain boundary migration. Therefore, we investigated the behavior of Ni grain boundary migration driven by grain boundary driving force in segregation bicrystal models alloying with various concentrations of Cr. This aims to contribute a deeper understanding of the interactions between solute segregation and grain boundary migration.

Figure 5a,b illustrates the variation in the GB position over time during grain boundary (GB) migration induced by the synthetic driving force for Ni Σ 5(310)[010] GB segregation samples with different Cr concentrations at 800 K and 1200 K. The migration rate is indicated by the slope of the figure. At 800 K, we found that the $\Sigma 5(310)[010]$ grain boundary does not move uniformly within the first few picoseconds after receiving the synthetic driving force, and then it slowly accelerates. A detailed atomic characterization of this can be found in Figure 6. The extent of the grain boundaries gradually widens during this slow acceleration interval. This phenomenon of slowly accelerated motion is due to the discontinuous grain boundary motion, often referred to as roughening [31]. Furthermore, it can be seen that the 5 at%.Cr sample leaves Cr atoms in the initial grain boundary and does not move with the grain boundary. Moreover, the presence of Cr prolongs the roughening period at 800 K. The roughening period of all models with Cr added was extended compared to pure nickel samples (see Figure 5a). The Cr concentrations have a significant influence on the roughening period. The extension time of the Ni-5 at%.Cr and Ni-15 at%.Cr models is more than the Ni-25 at%. Cr model. After applying the driving for a few picoseconds (ca. 6 ps), the grain boundary width almost remains stable, and the grain boundaries start moving steadily. All the $\Sigma 5(310)[010]$ grain boundaries have similar roughening behavior at 800 K. However, a different roughening and accelerating behavior of the Σ 5(310)[010] grain boundary is found at 1200 K, shown in Figure 5b. Compared to the GB motion at 800 K, the roughening period (ca. 2 ps) is relatively shorter, and the uniform migration of the grain boundaries starts earlier. Cr segregation in different Cr concentrations GBs cannot significantly prolong the roughening period of the $\Sigma 5(310)$ [010] grain boundary.



Figure 5. Plot of grain boundary position and time after the influence of a combined driving force. (**a**,**b**), respectively, depict the variation of the grain boundary position over time for samples with varying alloy concentrations at the Σ 5(310)[010] temperatures of 800 K and 1200 K, (**c**,**d**), respectively, depict the variation of the grain boundary position over time for samples with varying alloy concentrations at the Σ 101(200)[100] grain boundary at temperatures of (**a**) 800 K and (**b**) 1200 K.

From Figure 5c,d, it can be seen that all the $\Sigma 101(200)[100]$ grain boundaries with or without Cr segregation migrate at an approximately constant velocity after applying a driving force. The phenomenon that occurs here is what we need to discuss. It has been mentioned before that the Cr atom segregated on the grain boundary may impact the microstructure and energy of the grain boundary and the diffusion rate. The excessive migration speed of the grain boundary may cause the segregated atoms on the grain boundary to not move with the grain boundary and stay in the original position, which has been observed in all migration processes.

In addition, the factors affecting grain boundary migration may change in the Ni-Cr alloy with a higher Cr concentration, which also contains more Cr in the bulk, because not all Cr can be segregated into the grain boundary, as can be verified from Figure 4. Therefore, the concentration of Cr in the bulk increases with the total concentration due to chromium's weaker segregation tendency. Then, we simulated the migration of all samples at more temperatures, as shown in Figure 7. For example, at 1200 K, the pure Ni Σ 5(310)[010] grain boundary system has a grain boundary mobility of M = 9.39×10^{-8} m⁴/Js, while grain boundary mobility is 6.10×10^{-8} m⁴/Js at 800 K. A slightly fast mobility of pure Ni Σ 101(200)[100] GB is found, and the grain boundary mobility is 2.43 \times 10⁻⁷ m⁴/Js at 800 K and 2.89×10^{-7} m4/Js at 1200 K. Our results are consistent with the findings of the study of the grain boundary mobility in Ni by Olmsted and Simonnin et al. in order of magnitude [14,44]. Figure 7 provides a more comprehensive comparison of the grain boundary mobility at various temperatures for each model of the two kinds of grain boundary alongside their respective Arrhenius fitting curves. Each sample demonstrates pronounced Arrhenius behavior with significantly different activation energies, as indicated by the Arrhenius plots' slopes.



Figure 6. Growth mechanism of the Σ 5(310)[010]GB shown for the pure-Ni sample (**a**–**d**) and Ni-5 at %.Cr sample (**e**–**h**) at 800 K. (**a**,**e**) show the initial configuration, (**b**,**f**) show the configuration was slowly moved, (**c**,**d**) GB migrated at a constant rate, at the same time, leaving clusters on the migration path. (**g**,**h**) GB migrates constantly, and Cr atoms do not move with grain boundaries. The initial GB position is marked by a dashed line. The atomic size of nickel in bulk is reduced.



Figure 7. (a) The mobility of the $\Sigma 5(310)[010]$ grain boundary for alloy systems with varying concentrations at different temperatures in the context of tilted grain boundaries. (b) The mobility of the $\Sigma 101(200)[100]$ grain boundary at various temperatures for alloy systems with different concentrations within the framework of twisted grain boundaries.

The temperature dependence of the GB mobility can be described by an Arrhenius equation: $M(T) = M_0 exp\left(-\frac{Q_M}{k_BT}\right)$ [27]. The pre-exponential factor (M_0) and the energy for activated GB migration (Q_M) can be obtained as fit parameters from the temperature-dependent mobility. In Figure 7, comparing the slopes affords an evaluation of the relative activation energy magnitudes. Figure 5a,b illustrate the Arrhenius plots corresponding to the high-angle and low-angle grain boundaries. The mobility of low-angle grain boundaries

is faster than that of high-angle grain boundaries at all temperatures. Table 2 summarizes the activation energy Q_M and pre-exponential factor M_0 obtained by fitting the Arrhenius equation to the simulation data.

	0 at%.Cr (Pure)	5 at%.Cr	15 at%.Cr	25 at%.Cr
		$\Sigma 5(310)[010]$		
Q _M (meV)	64.76	61.26	49.86	42.43
$M_0(10^{-7} \text{ m}^4/\text{Js})$	1.91	1.90	1.80	1.76
C(at%.)	0	4.03	13.96	24.11
		Σ101(200)[100]		
Q _M (meV)	43.53	55.18	59.58	65.36
$M_0(10^{-7} \text{ m}^4/\text{Js})$	4.43	4.92	5.09	5.96
C(at%.)	0	3.02	12.06	21.80

Table 2. The activation energy Q_M , the concentration of chromium in the bulk C, and pre-exponential factor M_0 for GB Mobility in 0 at%.Cr (pure Ni), 5 at%.Cr alloy, 15 at%.Cr alloy, and 25 at%.Cr alloy.

In all temperatures except 800 K, the migration rate of the model doped with 25 at%. Cr is the fastest in both HAGB and low-angle grain boundaries LAGB. The migration rate of HAGB is approximately half that of LAGB. Due to the non-uniform movement phase present in HAGB, it is necessary to fit the uniform phase of grain boundary migration for both types of grain boundaries, leading to new fit parameters, as shown in Table 2. The migration activation energy of pure nickel HAGB is nearly 1.5 times that of LAGB, while the pre-exponential factor M_0 is close to half that of LAGB. For HAGB, the grain boundary migration barrier decreases with increasing Cr concentration in the bulk; for LAGB, it does not fit Arrhenius well, and the grain boundary migration barrier increases with the rise in Cr concentration in the bulk. Both show a strong correlation with the Cr concentration doped in the bulk.

Interestingly, within the same grain boundary model, the pre-exponential factor M_0 increases with the increase in Q_M . The impact of solute doping on activation energy is controlled by various factors, such as the differences in grain boundary microstructure, grain boundary energy, segregation energy, etc. Between the two types of grain boundaries, solute concentration may have opposite effects on grain boundary migration activation energy [45,46]. This variability in the influence of the solute on the activation energy even extends to different effects within the grain boundary and bulk. The solute concentration in the bulk also affects the grain boundary mobility and is complex. The migration activation energy (Q_m) and pre-exponential factor (M_0) increase and decrease with the increase in the solute concentration in the high-angle grain boundaries. Moreover, the behavior of the two kinds of grain boundary is opposite.

As mentioned, there is already a significant slow migration phase in the absence of Cr doping and segregation in the high-angle grain boundaries. Chromium segregation to the grain boundary can prolong the coarsening phase of grain boundary migration, with an optimal level of 5 at%. This is because a limited number of sites on the grain boundaries can segregate, so higher Cr doping concentrations will increase the Cr concentrations in the grain boundaries and bulk regions. However, a higher concentration of Cr doping will increase the concentration in the grain boundary and bulk regions. Excessive Cr makes the high-angle grain boundary relatively easy to migrate, so the plateau period for the 25 at% Cr sample is shorter than at 5%. The higher the Cr content doped in the bulk, the faster the grain boundary migration rate. These findings indicate that the influence of solute doping on activation energy is complex.

3.3. Analyzing the Effects of Grain Boundary Atom Diffusion and Lattice Distortion on Grain Boundary Migration

Given that the impact of the grain boundary solute segregation differences on grain boundary migration behavior appears to still have areas of uncertainty, we have calculated the Radial Distribution Function (RDF) at various temperatures and used the full width at half maximum (FWHM) of the first nearest neighbor peak from RDF to represent lattice distortion [47]. Additionally, to better understand the mechanism of grain boundary migration and the influence that segregation brings to this mechanism, we calculated atomic diffusion at the grain boundary under the solid-liquid temperatures.

Upon the examination of Figure 8a–d, it is evident that the concentration of the segregation on the grain boundaries and the width of the first nearest neighbor peak increase with the rise in Cr concentration, indicating an increase in lattice distortion. Due to Cr segregation typically replacing the original nickel atoms of the FCC lattice, Cr atoms segregate onto the nickel grain boundaries. This results in a higher relative density of Cr and a lower relative density of nickel in the grain boundary region, altering the g(r) function plot. However, the ordering of nickel on the grain boundaries remains largely unchanged under the influence of Cr segregation. The ordering of nickel is primarily determined by the morphology of the grain boundaries, with nickel atoms in the grain boundary maintaining a distribution pattern akin to that of pure nickel bicrystals.



Figure 8. Radial distribution function $g(\mathbf{r})$ over interatomic distance r at different temperatures for (a) pure Ni grain boundary samples, (b) 5 at%.Cr samples, (c) 15 at%.Crsamples, and (d) 25 at%.Cr samples. The FWHM of (e) Σ 5(310)[010] grain boundaries and (f) Σ 101(200)[100] grain boundaries as a function of homology temperature (normalized by the melting temperature T_{Melt}).

Furthermore, with increasing temperature, atoms vibrating near their equilibrium positions broaden the peaks of g(r) as thermal vibrations and intrinsic lattice distortions overlap. Similar behavior can be observed in $\Sigma 101(200)[100]$ samples. As interfacial regions,

grain boundaries possess unique structural and energetic characteristics that may impact the distribution of Cr and Ni atoms. Lattice distortions at grain boundaries are generally believed to reduce grain growth [21]. By comparison of Figure 8e,f, it is hard to observe significant differences in lattice distortion between two kinds of grain boundary with the same Cr doping concentration at different temperatures. This proves from the side that the effect of lattice distortion is small.

The mean-square displacements at 1600 K were calculated to further explore the relationship between GB atom diffusion coefficients and temperature. The GB atom diffusion coefficients were all obtained from Einstein's relations: $Dx = (x^2)/2\delta t$, $Dy = (y^2)/2\delta t$, and $Dz = (z^2)/2\delta t$. Due to our modeling method and grain boundary diffusion method, the mean azimuth shift in the X-axis direction is more representative. Figure 9 illustrates plots from selected representative 5 at%. Cr models at a temperature of 1600 K, displaying the relationship between $\langle x^2 \rangle$ and time. The slopes of these plots can be utilized to compute the grain boundary (GB) atom diffusion coefficients. As anticipated from the Einstein relation, these plots exhibit a high degree of linearity. The slope of the curve shows that the GB atom diffusion coefficient of nickel in the pure nickel model is larger than that in the 5 at%.Cr model. This trend is consistent across all temperatures studied for high-angle GB. Also, the diffusion rate is higher in high-angle GB than in low-angle GB. The segregation of Cr in high-angle grain boundaries can decelerate the diffusion rate of Ni at the grain boundaries while in low-angle grain boundaries. Moreover, the diffusion rates of those above three are roughly equivalent. This suggests that the effect of grain boundary segregation on the grain boundaries is primarily concerned with the diffusion rate of the atoms on the grain boundaries due to the variance in types of grain boundaries. The Cr atoms segregated on the high-angel grain boundaries lower the diffusion rate of the Ni atoms and cause a roughening phenomenon.



Figure 9. Mean-square atomic displacements perpendicular to the tilt axis in (**a**) Σ 5(310)[010] grain boundaries and (**b**) Σ 101(200)[100] grain boundaries versus time at 1600 k. The lines represent GB atom diffusion in pure Ni and GB diffusion of Ni and Cr in the Ni-5 at%.Cr alloy.

4. Conclusions

To investigate the effect of solute segregation on the grain boundary stability of Ni-Cr alloys with different Cr concentrations two typical grain boundaries are chosen as models using MD/ MC methods to simulate the solute segregation of Cr with different concentrations, then using the synthetic driving force method to simulate the (spontaneous) motion of grain boundaries. The key conclusions drawn from this investigation are summarized as follows:

1. Grain boundary segregation increases at decreased temperatures, with a more substantial segregation of Cr to the grain boundaries at lower temperatures. However, not all Cr segregates to the grain boundaries due to the high mutual solubility of Cr in the Ni-base, leading to a smaller tendency towards Cr segregation. This effect is more significant for LAGB.

- 2. For the $\Sigma 5(310)[010]$ grain boundary, at a low temperature (800 K), the roughing period of the grain boundary migration is longer, and the grain boundary undergoes a long slow acceleration movement. Compared with pure nickel, all alloys have a longer roughing time, but this increase decreases with the upper Cr concentration of the alloy. At a higher temperature (1200 K), the coarsening period is shorter, the grain boundary migration starts earlier, and the influence of solute concentration is small. For all $\Sigma 101(200)[100]$ GB models, the roughening process of grain boundary mobility and is complex. And the behavior of the two kinds of grain boundaries is opposite.
- 3. For $\Sigma 5(310)[010]$ grain boundary, Cr segregation can decrease Ni self-propagation to impede grain boundary movement, while there is no such phenomenon at small angle grain boundaries. The distribution of segregated Cr atoms on grain boundaries is relatively uniform, and the lattice distortion increases with the total Cr concentration in the system.

To summarize, grain boundary segregation of Cr has a complex effect on grain boundary migration. The mechanism of grain boundary migration can be understood more carefully and comprehensively by considering factors such as solute concentration, grain boundary type, and temperature. Thus, our results revealed some important factors in the segregation-increased GB stabilization of NC Ni-Cr alloys.

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