

## Article

# Multi-Objective Optimization of Low-Alloy Hot-Rolled Strip Cooling Process Based on Gray Correlation Analysis

Rundong Xue <sup>1,\*</sup> and Aigeng Fei <sup>2</sup>

<sup>1</sup> Institute for Advanced Materials and Technology, University of Science and Technology Beijing, Beijing 100083, China

<sup>2</sup> School of Materials Science and Engineering, University of Science and Technology Beijing, Beijing 100083, China

\* Correspondence: xrd@ustb.edu.cn

**Abstract:** The residual stress in low-alloy hot-rolled strips seriously affects the use and processing of products. Reducing residual stress is important for improving the product quality of hot-rolled strips. In this paper, the changes in grain size and residual stress of hot-rolled strips under different cooling processes were investigated via thermal simulation experiments and electron backscatter diffraction. It was found that the optimum cooling process solution for single-objective optimization of grain size was a final rolling temperature of 875 °C, a laminar cooling speed of 50 °C/s, and a coiling temperature of 550 °C. When single-objective optimization of residual stress was carried out, the optimal cooling process scheme was 900 °C for final rolling temperature, 20 °C/s for laminar cooling speed, and 625 °C for coiling temperature. The significance of the effect of cooling processes on grain size and residual stress was analyzed based on the extreme deviation of the effect of each cooling process on grain size and residual stress in orthogonal experiments. The results show that the coiling temperature was the most influential factor on grain size and residual stress among the cooling process parameters. The difference was that grain size increased with increasing coiling temperature, and residual stress decreased with increasing coiling temperature. Using both grain size and residual stress as evaluation indicators, a multi-objective optimization of the cooling process for hot-rolled strips was carried out via the gray correlation analysis method. The optimized solution was 875 °C final rolling temperature, 30 °C/s laminar cooling speed, and 625 °C coiling temperature. At this time, the grain size was 4.8 μm, and the KAM (Kernel Average Misorientation) was 0.40°. The grain size under the actual production process scheme was 4.4 μm with a KAM of 0.78°. Compared to the actual production process solution, the multi-objective optimization solution showed little change in grain size, with only a 9% increase and a 49% reduction in KAM. The optimization scheme in this paper could significantly reduce the level of residual stresses while ensuring the fine grain size of hot-rolled strips, thus improving the overall quality of hot-rolled strips.



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## 1. Introduction

Hot-rolled strip products are an important support for economic development, occupying an important position in the modern steel industry system; they are widely used in the ship, automobile, bridge, and other industries [1–3]. With continuous social and economic development, the steel industry is becoming more and more competitive, and people have higher and higher quality requirements for hot-rolled strip products. In recent years, quality problems arising from the residual stress within hot-rolled strip have attracted widespread attention [4,5]. Residual stress is an important parameter that will inevitably be formed in the molding process of materials and parts. The existence of residual stress will, on the one hand, lead to deformation, cracking, and other quality defects of hot-rolled strips

in the manufacturing process, and on the other hand, it will be released in the subsequent deep-processing, decreasing the size and shape of the dimensional and shape accuracy of hot-rolled strips, may even be impossible to use [6,7]. Therefore, how to reduce the residual stress in hot-rolled strip has become a key and difficult issue in the steel industry.

The production of hot-rolled strip is a very complex metallurgical process, which is nowadays mainly produced using controlled rolling and cooling technology. Thermal stress and transformation stress generated during the cooling process after rolling are the main sources of residual stresses in hot-rolled strips [8,9]. When the cooling process is changed, the residual stress in the hot-rolled strip is bound to change as well. Previous researchers have optimized the cooling process of hot-rolled strip mainly from the microstructure of the product, ignoring the effect of the cooling process on the residual stress [10,11]. Multi-objective optimization of the cooling process of hot-rolled strip, taking into account the microstructure and residual stress, is extremely important for improving the overall quality of the product. On the basis of existing experimental data, by using appropriate statistical analysis methods to further explore the relationship between process variables and optimization indicators, the processing technology of materials can be effectively optimized [12–17]. Gray correlation analysis is part of gray systems theory, a control theory that applies to small samples and analyzes relationships between systems. Gray correlation analysis can convert multiple evaluation indicators into a single-indicator function, and solve the complex system problem of interrelationships between various factors and indicators by comparing the similarity between the sequences. According to existing research [18], the thickness of the oxide scale on the surface of the strip in actual production also has an impact on the cooling effect. In order to simplify the research, the evolution law of microstructure and residual stress of strip was studied from the perspective of cooling process parameters. In this paper, microstructure and residual stress were simultaneously used as evaluation indexes for multi-objective optimization of the cooling process of the hot-rolled strip based on gray correlation analysis. The research work in this paper could provide guidance for the production of high-quality hot-rolled strips with fine grains and low stress.

## 2. Experimental Procedures

### 2.1. Thermal Simulation Experiments

The test steel used in this paper was an intermediate billet of hot rolled strip produced by a steel mill. Table 1 shows the chemical composition of the test steel.

**Table 1.** Chemical composition of test steel (wt.%).

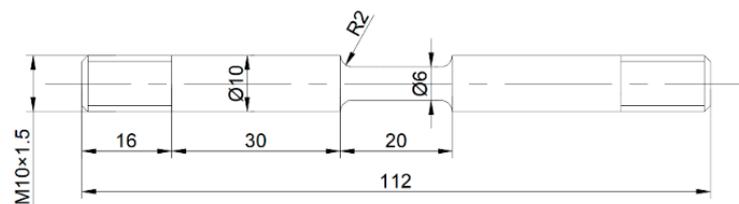
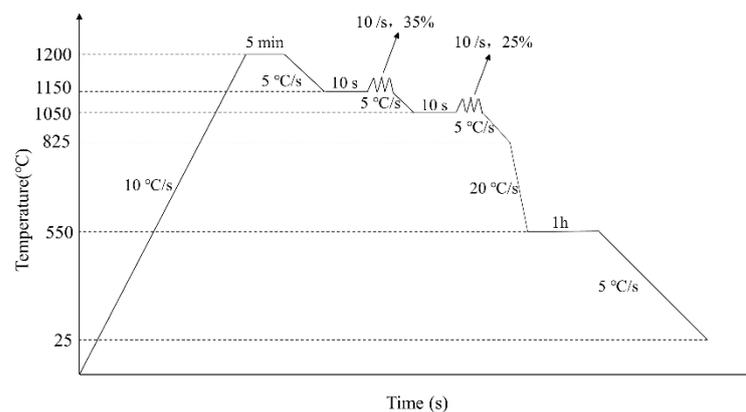
Elements	C	Si	Mn	Al	Nb + V + Ti	Fe
Composition	0.08	0.15	1.25	0.03	0.08	Rest

In the actual production of the hot-rolled strip, the cooling control process is mainly the final rolling temperature, laminar cooling speed, and coiling temperature. Therefore, three process parameters, namely, final rolling temperature, laminar cooling speed, and coiling temperature, were selected as the influencing factors in this paper. Combined with the control window of process parameters in actual production, four levels of each factor were selected. The levels of final rolling temperature were 825 °C, 850 °C, 875 °C, and 900 °C; the levels of laminar cooling speed were 20 °C/s, 30 °C/s, 40 °C/s, and 50 °C/s; and the levels of coiling temperature were 550 °C, 575 °C, 600 °C, and 625 °C. Grain size and residual stress of the test steel were selected as optimization objectives. For ease of description in the subsequent graphs, the three factors of final rolling temperature, laminar cooling speed, and coiling temperature were denoted by A, B, and C, respectively, and the two optimization objectives of grain size and residual stress were denoted by D and E, respectively. The levels corresponding to each factor are shown in Table 2. A three-factor, four-level orthogonal table of  $L_{16}(4^3)$  was used to conduct the experiment in this paper, which required a total of 16 sets of experiments.

**Table 2.** Factors and levels of orthogonal experiments.

Levels	Factors		
	A (°C)	B (°C/s)	C (°C)
1	825	20	550
2	850	30	575
3	875	40	600
4	900	50	625

Hot-rolled production of specimens under different cooling process parameters was simulated with a Gleeble 3500. Figure 1 is the dimensional drawing of the thermal simulation specimen. Figure 2 is the process roadmap of the thermal simulation experiment. Taking a final rolling temperature of 825 °C, laminar cooling speed of 20 °C/s, and coiling temperature of 550 °C as an example, the thermal simulation specimen was first heated from room temperature to 1200 °C and maintained at this temperature for 5 min, then cooled down. Two passes of hot compression deformation at 1150 °C and 1050 °C, respectively, were performed to simulate the rough rolling and finishing rolling processes of the strip. After the hot deformation was completed, the simulation specimen was cooled to the final rolling temperature of 825 °C, and rapid cooling at a cooling speed of 20 °C/s was performed to simulate the laminar cooling process of the strip. When the specimen was rapidly cooled to a coiling temperature of 550 °C, it was maintained at this temperature for 1 h, and then slowly cooled to room temperature to simulate the coiling cooling process of the strip.

**Figure 1.** Thermal simulation specimen size (mm).**Figure 2.** Thermal simulation experiment process roadmap.

After the thermal simulation experiment was completed, the specimen was split along the longitudinal direction, and an area of 6 mm in the longitudinal center was removed to prepare the specimen for EBSD (electron scattering diffraction) using electrolytic polishing. The voltage was 18 V and the electrolysis time was 25 s. The step size of EBSD was 0.3 µm. The KAM (kernel average misorientation) obtained from the EBSD test can be used to analyze the distribution of residual stress in the material; the larger the KAM value, the higher the level of residual stress in the corresponding area. In this paper, KAM was used to characterize the residual stress level under different cooling processes [19–21].

## 2.2. Gray Correlation Analysis

The gray correlation analysis of multiple factors is divided into the following four main steps [22–28]:

### (1) Data preprocessing.

Due to the different physical units of the evaluation indicators in the system, direct calculations and comparisons cannot be made, and standardization of the data for each evaluation indicator is required. Different data preprocessing formulas are required for evaluation indicators with different characteristics.

For the larger and better look-ahead large characteristic index, Equation (1) was used for calculation as follows:

$$x_i^*(k) = \frac{x_i^0(k) - \min x_i^0(k)}{\max x_i^0(k) - \min x_i^0(k)} \quad (1)$$

where  $x_i^*(k)$  is standardized sequences;  $x_i^0(k)$  is original sequences;  $\min x_i^0(k)$  is the minimum value in original sequences; and  $\max x_i^0(k)$  is the maximum value in original sequences.

For the smaller and better look-ahead small characteristic index, Equation (2) was used for calculation as follows:

$$x_i^*(k) = \frac{\max x_i^0(k) - x_i^0(k)}{\max x_i^0(k) - \min x_i^0(k)} \quad (2)$$

### (2) Calculating the gray correlation coefficient.

After the standard post-processing of the original sequence, the gray correlation coefficient  $\zeta$  can be calculated as shown in Equation (3):

$$\zeta(x_0^*(k), x_i^*(k)) = \frac{\min_i \min_k |x_0^*(k) - x_i^*(k)| + \lambda \max_i \max_k |x_0^*(k) - x_i^*(k)|}{|x_0^*(k) - x_i^*(k)| + \lambda \max_i \max_k |x_0^*(k) - x_i^*(k)|} \quad (3)$$

where  $x_0^*(k)$  is reference sequences;  $x_i^*(k)$  is comparison sequences; and  $\lambda$  is deviation factor which is usually taken as 0.5 [29–31].

### (3) Calculating the gray correlation degree.

After obtaining the gray correlation coefficient, the gray correlation degree  $\gamma$  can be calculated, which is shown in Equation (4):

$$\gamma(x_0^*(k), x_i^*(k)) = \frac{1}{n} \sum_{k=1}^n \zeta(x_0^*(k), x_i^*(k)) \quad (4)$$

### (4) Sorting the gray correlation degree.

Finally, the mean of the gray correlation degree at different levels of each factor can be calculated. The higher the mean of the gray correlation degree, the closer the response value under the corresponding process parameter of the factor is to the optimal value of the optimization objective.

## 3. Results and Discussion

### 3.1. Significance Analysis of the Effect of Cooling Process on Grain Size

Table 3 shows the experimental results of the grain size of specimens under different cooling processes. Figure 3 shows the corresponding grain size distribution.

**Table 3.** Orthogonal experimental results of grain size.

Numbers	Factors			Targets
	A (°C)	B (°C/s)	C (°C)	D (µm)
1	825	20	550	4.7
2	825	30	625	6.6
3	825	40	575	4.3
4	825	50	600	5.8
5	850	20	575	5.6
6	850	30	600	4.7
7	850	40	550	4.4
8	850	50	625	7.6
9	875	20	600	5.7
10	875	30	575	4.3
11	875	40	625	8.1
12	875	50	550	4.2
13	900	20	625	9.8
14	900	30	550	4.3
15	900	40	600	5.0
16	900	50	575	4.5

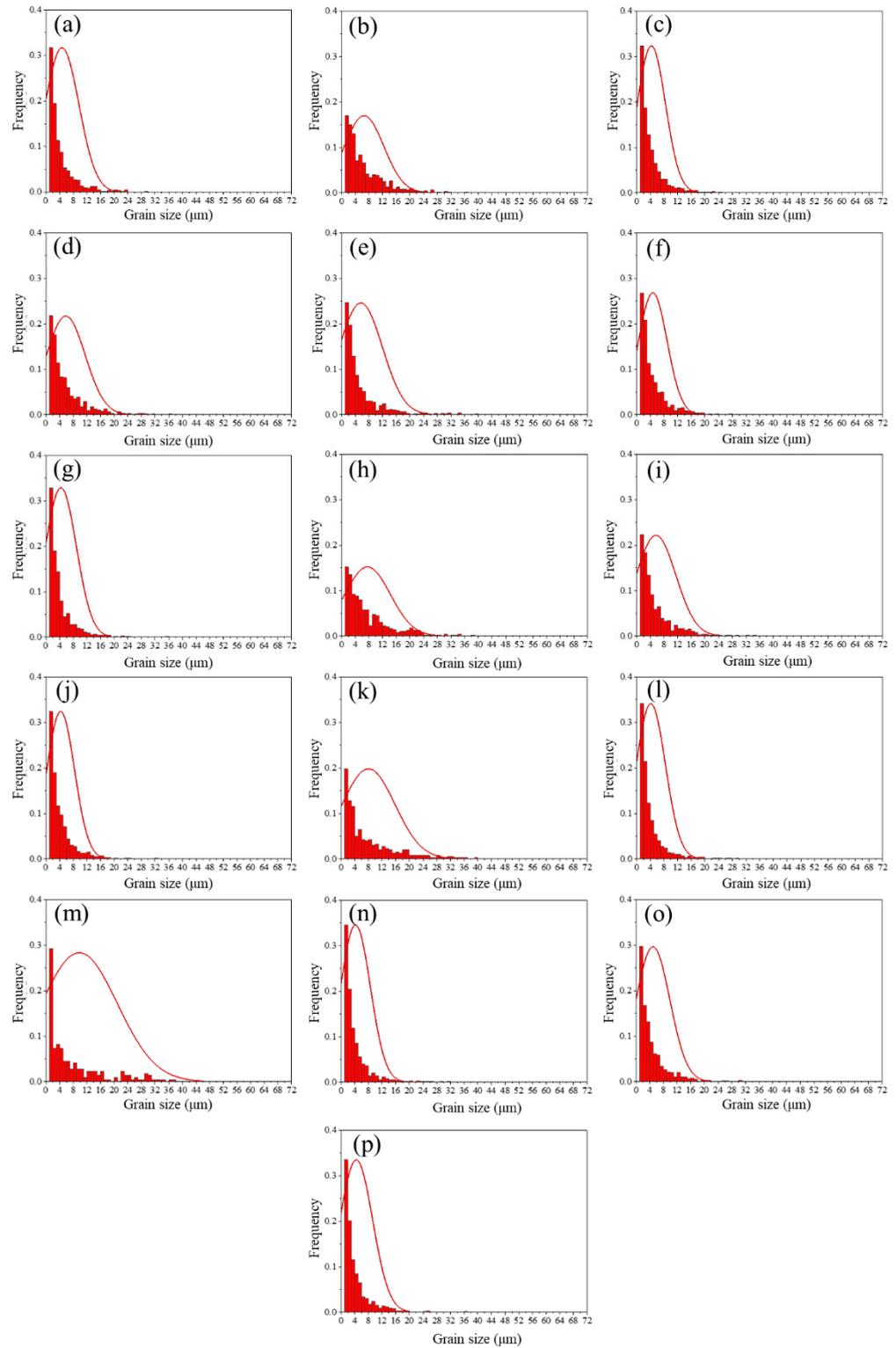
As can be seen from Table 3, the smallest grain size of 4.2 µm was obtained in the 12th group. At this time, the corresponding cooling process was the final rolling temperature of 875 °C, laminar cooling speed of 50 °C/s, and coiling temperature of 550 °C. The grain size of the 13th group was the largest at 9.8 µm, which corresponded to the cooling process for the final rolling temperature of 900 °C, laminar cooling speed of 20 °C/s, and coiling temperature of 625 °C. In correlation studies using the orthogonal experiment method, the range can be used to determine the magnitude of the significance of the effect of each factor on the response target. A higher range means that the factor has a greater impact on the response target; a lower range means that the factor has a lesser impact on the response target. In this paper, the range of the effect of each factor on grain size was calculated and the results are shown in Table 4. According to Table 4, it can be seen that the range of the effect of coiling temperature on grain size was the largest, the range of the effect of final rolling temperature on grain size was the smallest, and the range of the effect of laminar cooling speed on grain size was between the two. Therefore, the order of effect of the cooling process on grain size was coiling temperature > laminar cooling speed > final rolling temperature.

**Table 4.** Range of effect of cooling process on grain size.

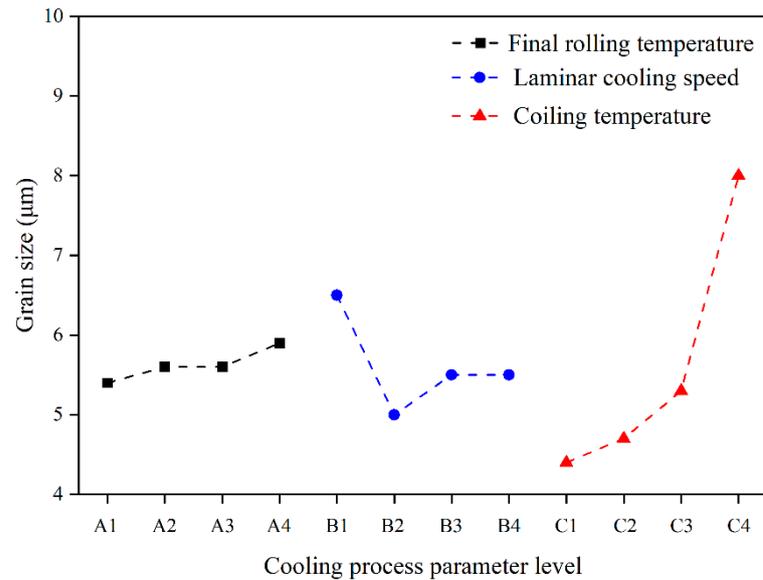
Factors	Mean Grain Size at Different Levels (µm)				Range (µm)	Sort
	1	2	3	4		
A	5.4	5.6	5.6	5.9	0.5	3
B	6.5	5.0	5.5	5.5	1.5	2
C	4.4	4.7	5.3	8.0	3.6	1

Figure 4 shows the trend of grain size variation with the cooling process. When the final rolling temperature increased from level A1 (825 °C) to level A2 (850 °C), the grain size began to increase. When the final rolling temperature increased to level A3 (875 °C), the grain size remained unchanged. When the final rolling temperature increased to level A4 (900 °C), the grain size again showed an increasing trend. When the laminar cooling speed increased from level B1 (20 °C/s) to level B2 (30 °C/s), the grain size decreased significantly. When the laminar cooling speed increased to level B3 (40 °C/s), the grain size began to rise. When the laminar cooling speed increased to level B4 (50 °C/s), no change in grain size occurred. When varying the coiling temperature, the grain size increased with increasing coiling temperature. Especially when the coiling temperature increased from level C3 (600 °C) to level C4 (625 °C), the grain size showed a sharp increase. Fine

grain size is desired in actual production, so when grain size was used as the optimization goal, the optimal combination of cooling processes was A1B2C1 which meant the final rolling temperature was 825 °C, the laminar cooling speed was 30 °C/s, and the coiling temperature was 550 °C.



**Figure 3.** Grain size distribution of each specimen in orthogonal experiments. (a) 1; (b) 2; (c) 3; (d) 4; (e) 5; (f) 6; (g) 7; (h) 8; (i) 9; (j) 10; (k) 11; (l) 12; (m) 13; (n) 14; (o) 15; (p) 16.



**Figure 4.** Trend plot of grain size variation with cooling process.

### 3.2. Significance Analysis of the Effect of Cooling Process on Residual Stress

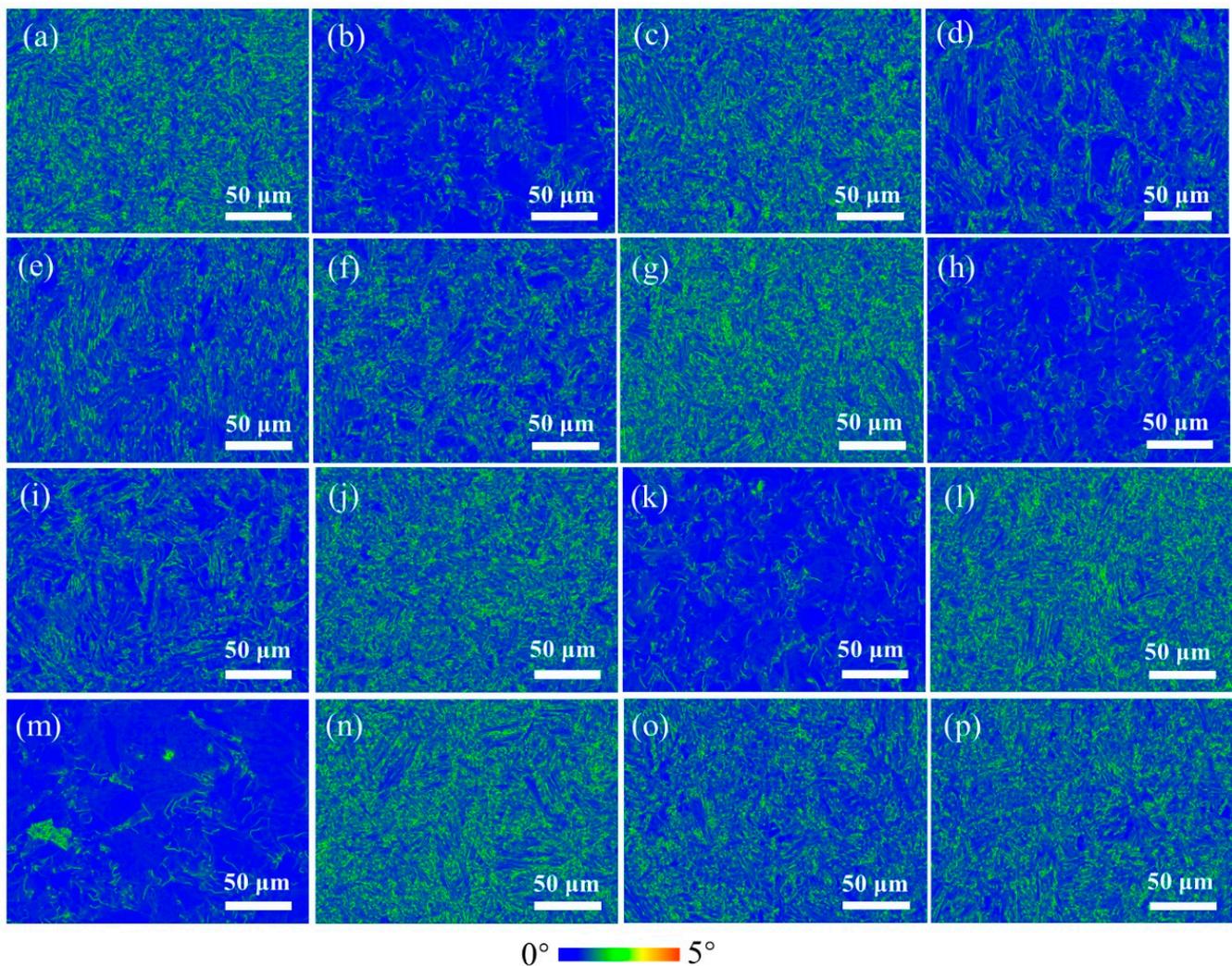
Table 5 shows the experimental results of residual stress of specimens under different cooling processes. Figure 5 shows the corresponding residual stress distribution. As can be seen from Table 5, the smallest KAM of  $0.25^\circ$  was obtained in the 13th group. At this time, the corresponding cooling process was the final rolling temperature of  $900^\circ\text{C}$ , laminar cooling speed of  $20^\circ\text{C/s}$ , and coiling temperature of  $625^\circ\text{C}$ . The grain size of the 14th group was the largest at  $0.73^\circ$ , which corresponded to the cooling process for the final rolling temperature of  $900^\circ\text{C}$ , laminar cooling speed of  $30^\circ\text{C/s}$ , and coiling temperature of  $550^\circ\text{C}$ .

**Table 5.** Orthogonal experimental results of KAM.

Numbers	Factors			Targets
	A ( $^\circ\text{C}$ )	B ( $^\circ\text{C/s}$ )	C ( $^\circ\text{C}$ )	E ( $^\circ$ )
1	825	20	550	0.67
2	825	30	625	0.31
3	825	40	575	0.63
4	825	50	600	0.40
5	850	20	575	0.47
6	850	30	600	0.49
7	850	40	550	0.72
8	850	50	625	0.29
9	875	20	600	0.41
10	875	30	575	0.66
11	875	40	625	0.28
12	875	50	550	0.70
13	900	20	625	0.25
14	900	30	550	0.73
15	900	40	600	0.57
16	900	50	575	0.63

In order to analyze the significance of the effect of cooling process on KAM, the range of KAM under different cooling processes was counted and the results are shown in Table 6. According to Table 6, it can be seen that the range of the effect of coiling temperature on the KAM was the largest, the range of the effect of final rolling temperature on the KAM was the smallest, and the range of the effect of laminar cooling speed on the KAM was between the two. Therefore, the order of effect of the cooling process on KAM was coiling

temperature > laminar cooling speed > final rolling temperature. This order was consistent with the effect of the cooling process on grain size.



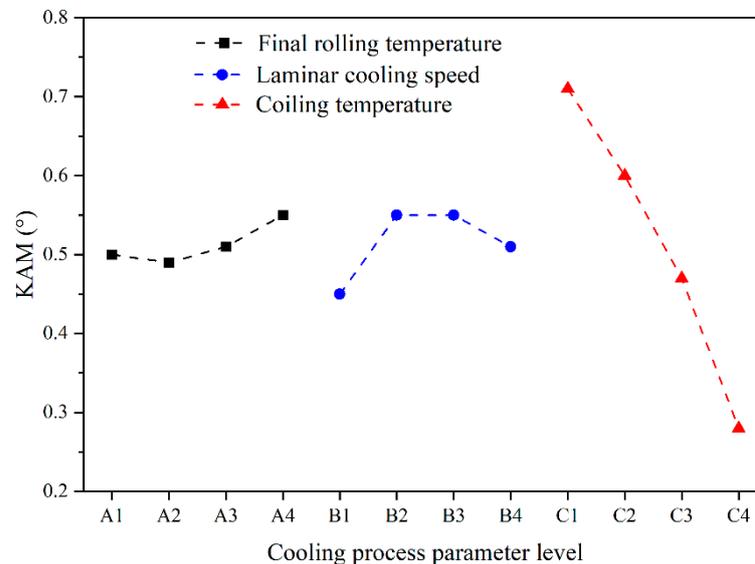
**Figure 5.** KAM distribution of each specimen in orthogonal experiments. (a) 1; (b) 2; (c) 3; (d) 4; (e) 5; (f) 6; (g) 7; (h) 8; (i) 9; (j) 10; (k) 11; (l) 12; (m) 13; (n) 14; (o) 15; (p) 16.

**Table 6.** Range of effect of cooling process on KAM.

Factors	Mean KAM at Different Levels (°)				Range (°)	Sort
	1	2	3	4		
A	0.50	0.49	0.51	0.55	0.06	3
B	0.45	0.55	0.55	0.51	0.10	2
C	0.71	0.60	0.47	0.28	0.43	1

Figure 6 shows the trend of KAM variation with the cooling process. When the final rolling temperature increased from level A1 (825 °C) to level A2 (850 °C), the KAM showed a decreasing trend. When continuing to increase the final rolling temperature, the KAM began to show a continuous upward trend. When the laminar cooling speed increased from level B1 (20 °C/s) to level B2 (30 °C/s), the KAM showed an upward trend. When the laminar cooling speed increased from level B2 (30 °C/s) to level B3 (40 °C/s), the KAM did not change. When the laminar cooling speed increased to level B4 (50 °C/s), the KAM showed a decreasing trend. Observing the change curve of the KAM with cooling temperature, it was found that the KAM maintained a negative correlation with cooling

temperature, and the higher the coiling temperature, the smaller was the KAM. The lower the level of residual stress in hot-rolled strip, the better the product quality. This means that the smaller the KAM, the better the product quality. When residual stress was used as the optimization goal, the optimal combination of cooling processes was A2B1C4 which meant the final rolling temperature was 850 °C, the laminar cooling speed was 20 °C/s and the coiling temperature was 625 °C.



**Figure 6.** Trend plot of KAM variation with cooling process.

In summary, the optimal process combinations obtained from single-objective cooling process optimization by selecting grain size and residual stress, respectively, were not the same. Among the factors of the cooling process, the effect of coiling temperature on both grain size and residual stress was the largest. In contrast to the increase in grain size with increasing coiling temperature, the residual stress decreased with increasing coiling temperature. The optimal combination of cooling processes obtained by taking any single index of grain size and residual stress as the optimization goal would inevitably lead to the deterioration of the other index, thus affecting the overall quality of hot-rolled strips. Therefore, it was necessary to carry out a multi-objective simultaneous optimization study of the cooling process with respect to the grain size and residual stress of hot-rolled strips.

### 3.3. Calculation Results of Gray Correlation Analysis

For hot-rolled strip, grain size and residual stress both belong to the smaller and better look-ahead small characteristic index. In this paper, Equation (2) was used to normalize the experimental results of grain size and KAM, and the results are shown in Table 7.

In this paper, the minimum values of grain size and KAM obtained from orthogonal experiments were selected as reference sequences. According to Table 7, the minimum values of grain size and KAM experimental data were 4.2  $\mu\text{m}$  and 0.25°, respectively. After normalization, the minimum values of both grain size and KAM experimental data were converted to a dimensionless “1”. Thus, the reference sequence in this paper was  $x_0^*(k) = \{1,1\}$ . The gray correlation coefficients for the 16 groups of experiments were calculated using Equation (3), and then the gray correlation degree was calculated using Equation (4). Table 8 shows the results of calculating the gray correlation coefficient and gray correlation degree. The gray correlation degree of the 3rd set of experiments was the highest, at 0.676. This indicated that among the 16 sets of orthogonal experiments conducted in this paper, the combined evaluation index of the 3rd set of experiments was closest to the reference sequence.

**Table 7.** Normalization results for response objectives in gray correlation optimization schemes.

Numbers	Experimental Data		Normalized Data	
	D ( $\mu\text{m}$ )	E ( $^{\circ}$ )	D	E
1	4.7	0.67	0.911	0.125
2	6.6	0.31	0.571	0.875
3	4.3	0.63	0.982	0.208
4	5.8	0.40	0.714	0.688
5	5.6	0.47	0.750	0.542
6	4.7	0.49	0.911	0.500
7	4.4	0.72	0.964	0.021
8	7.6	0.29	0.393	0.917
9	5.7	0.41	0.732	0.667
10	4.3	0.66	0.982	0.146
11	8.1	0.28	0.304	0.938
12	4.2	0.70	1.000	0.063
13	9.8	0.25	0.000	1.000
14	4.3	0.73	0.982	0.000
15	5.0	0.57	0.857	0.333
16	4.5	0.63	0.946	0.208

**Table 8.** Calculation results of gray correlation coefficient and gray correlation degree.

Numbers	Gray Correlation Coefficient		Gray Correlation Degree
	D	E	
1	0.848	0.364	0.606
2	0.538	0.800	0.669
3	0.966	0.387	0.676
4	0.636	0.615	0.626
5	0.667	0.522	0.594
6	0.848	0.500	0.674
7	0.933	0.338	0.636
8	0.452	0.857	0.654
9	0.651	0.600	0.626
10	0.966	0.369	0.667
11	0.418	0.889	0.653
12	1.000	0.348	0.674
13	0.333	1.000	0.667
14	0.966	0.333	0.649
15	0.778	0.429	0.603
16	0.903	0.387	0.645

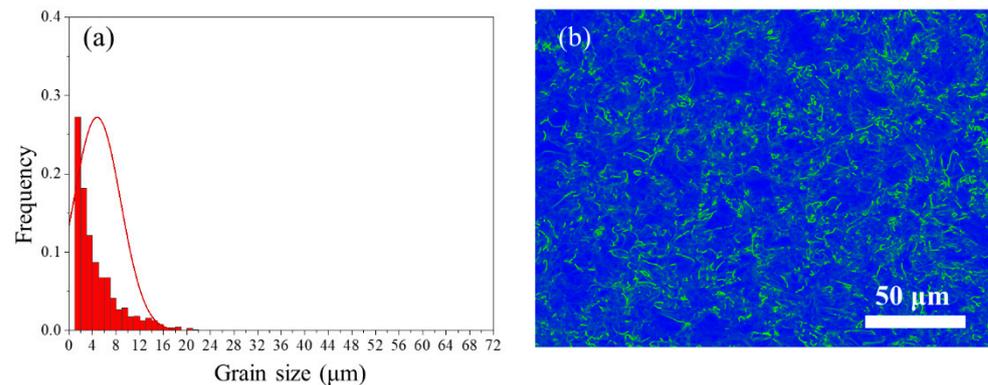
In order to further analyze the effect law of each factor on the comprehensive evaluation index, and get the best combination of process parameters of each factor, this paper calculated the mean gray correlation degree of each factor at different levels, and the results are shown in Table 9. For final rolling temperature, the mean gray correlation degree was largest at the A3 level; for laminar cooling speed, the mean gray correlation degree was largest at the B2 level; and for coiling temperature, the mean gray correlation degree was largest at the C4 level. When using gray correlation analysis for multi-objective optimization, the greater the mean gray correlation degree of a factor level, the closer the comprehensive evaluation index obtained under that factor level is to the optimal solution. Therefore, the optimal process combination for the multi-objective optimization of cooling process obtained in this paper based on gray correlation analysis was A3B2C4 which meant the final rolling temperature was 875  $^{\circ}\text{C}$ , the laminar cooling speed was 30  $^{\circ}\text{C}/\text{s}$  and the coiling temperature was 625  $^{\circ}\text{C}$ .

**Table 9.** Mean gray correlation degree at different levels of each factor.

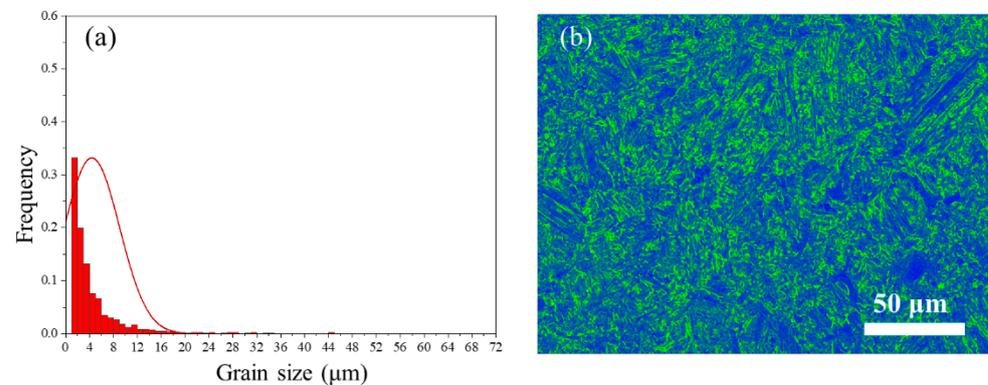
Factors	Mean Gray Correlation Degree at Different Levels			
	1	2	3	4
A	0.644	0.640	0.655	0.641
B	0.623	0.665	0.642	0.650
C	0.641	0.646	0.632	0.661

### 3.4. Validation of Optimization Results

Since the process combinations obtained via gray correlation analysis optimization were not among the 16 sets of orthogonal experiments, it was impossible to judge the specific optimization effect; therefore, it was necessary to carry out the experiment of the corresponding scheme to obtain the evaluation indexes under the optimization scheme. The actual production cooling process corresponding to the test steel was the final rolling temperature of 890 °C, the laminar cooling speed of 19 °C/s, and the coiling temperature of 568 °C. In this paper, the process combination optimized via gray correlation analysis and the actual production process scheme were used as the process parameters for the thermal simulation experiments seen in Figure 2. Subsequently, EBSD characterization was performed to obtain the grain size and KAM under different schemes. Figures 7 and 8 show the distribution of grain size and KAM for the optimized scheme of gray correlation analysis, and the actual production process scheme, respectively.



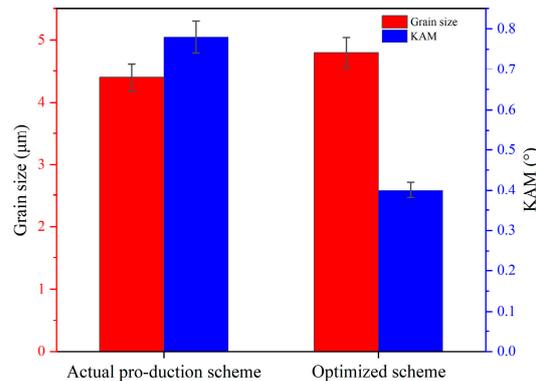
**Figure 7.** Evaluation indicators of gray correlation analysis optimization scheme. (a) Grain size distribution; (b) KAM distribution.



**Figure 8.** Evaluation indicators of practical production process scheme. (a) Grain size distribution; (b) KAM distribution.

The grain size of the optimized scheme of gray correlation analysis was 4.8  $\mu\text{m}$  with a KAM of 0.40°, and the actual production process scheme had a grain size of 4.4  $\mu\text{m}$  with a KAM of 0.78°. The grain size and KAM of the gray correlation analysis optimization

scheme were compared with the actual production process scheme and the results are shown in Figure 9. It can be seen that the grain size of the optimized scheme had increased by 9% and the KAM had decreased by 49% compared to the actual production process scheme. This indicated that the multi-objective optimized cooling process obtained in this paper based on gray correlation analysis was able to significantly reduce the residual stress level while ensuring fine grain size. This research work could provide guidance for the production of high-quality hot-rolled strip with fine grains and low stress.



**Figure 9.** Comparison of evaluation indicators between optimized and actual production process scheme.

#### 4. Conclusions

- (1) When the cooling process was a final rolling temperature of 875 °C, laminar cooling speed of 50 °C/s, and coiling temperature of 550 °C, the grain size was the smallest, 4.2 µm; when the cooling process was a final rolling temperature of 900 °C, laminar cooling speed of 20 °C/s, and coiling temperature of 625 °C, the grain size was the largest, 9.8 µm. By comparing the range of the effect of each factor on the grain size, the order of the effect of the cooling process on the grain size was obtained as coiling temperature > laminar cooling speed > final rolling temperature.
- (2) When the cooling process was a final rolling temperature of 900 °C, laminar cooling speed of 20 °C/s, and coiling temperature of 625 °C, the KAM was the smallest, 0.25°; when the cooling process was a final rolling temperature of 900 °C, laminar cooling speed of 30 °C/s, and coiling temperature of 550 °C, the KAM was the largest, 0.73°. By comparing the range of the effect of each factor on the KAM, the order of the effect of the cooling process on the KAM was obtained as coiling temperature > laminar cooling speed > final rolling temperature.
- (3) The gray correlation coefficient and gray correlation degree of the orthogonal experiment results were calculated by using gray correlation analysis, with grain size and KAM as reference sequences. By calculating the mean gray correlation degree of each factor at different levels, the optimal cooling process combination was obtained as follows: a final rolling temperature of 875 °C, laminar cooling speed of 30 °C/s, and coiling temperature of 625 °C. Compared to the actual production process scheme, the gray correlation analysis optimized scheme increased the grain size by only 9%, while the residual stress level decreased by 49%. This optimized scheme significantly reduced the residual stress level while maintaining a fine grain size.

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